

Quantifying Explainability with Multi-Scale Gaussian Mixture Models

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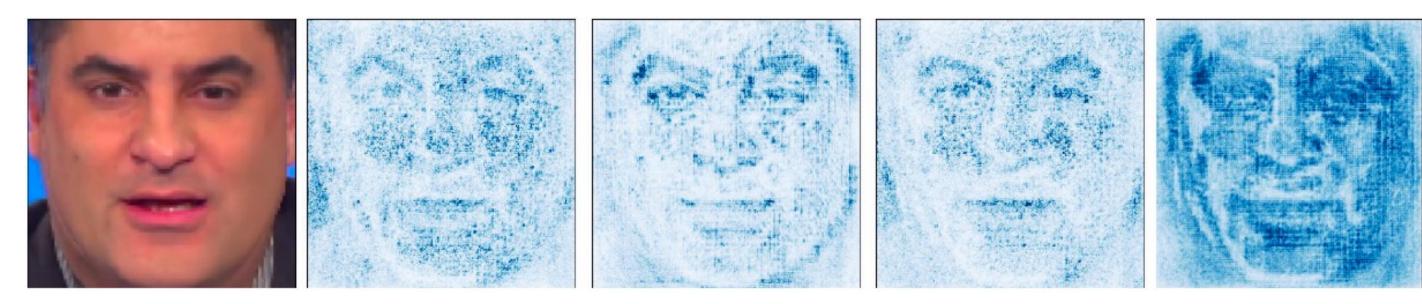
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Motivation

Which represents the best saliency?

Saliency maps significantly vary between different XAI methods, different evaluated detectors, and different data distributions.



❖ How to systematically compare and evaluate saliency map quality?

Traditional metrics cannot capture the multi-level information embedded in a saliency map; whereas model-dependent approaches limit comparisons across models, datasets, and domains with costly inference per input manipulation.

Image Space	Distribution Space	Input Space	
SSIM, IoU, RMSE	KL, EMD	IC, AD, ADD, I/D AuC	
Sensitive to noise, pixel, and spatial changes	Not hierarchical, spatial structure is lost	Model-dependent, heavy-inference time	

XMGD

We introduce a novel explainability comparison metric, eXplainable Multi-Scale GMM Distance (**XMGD**). XMGD provides a principled probabilistic algorithm for analyzing and quantifying any model or dataset similarity through the lens of explainability. Through experimental results, we demonstrate several critical advantages of XMGD over alternative saliency comparison metrics:

- * XMGD is more robust against individual input/pixel saliency.
- * XMGD is not sensitive to dataset size so it does not suffer from poor convergence properties due to small datasets.
- * XMGD operates directly on the saliency images, without the need for input or model manipulation.
- * XMGD can enhance explainability across a large number of diverse use cases, including saliency comparisons for individual images, entire datasets, or outputs of different models.

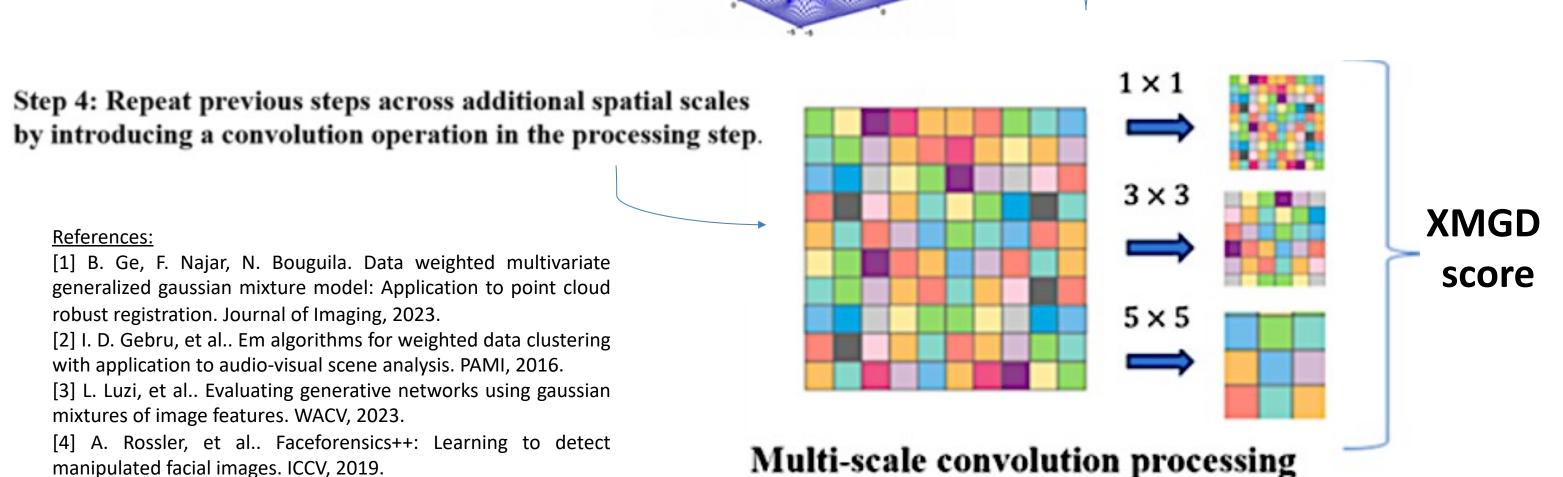
Method

Given two input saliency maps (or two aggregations over saliency maps) representing different models or datasets, XMGD proceeds as:

- 1. Saliency maps are extracted and projected onto the 2D unit grid.
- 2. A Weighted-Data GMM (WD-GMM) [1] is fit to each of the saliency maps.
- 3. Mixed 2-Wasserstein distance is calculated between the WD- GMMs.
- 4. Steps (1-3) are repeated across spatial scales by a convolution operation.
- 5. Final XMGD score is computed as a weighted sum of multi-scale distances.

WD-GMM is solved using expectation maximization over a duplicated point GMM [2], by a tunable binning parameter b over saliency maps on the unit grid. The distance between GMMs is computed using discrete optimal transport as in [3]. Then we repeat it across l scales using l-l 2D convolutions of sizes w. $\{l, w, b, g\}$ can be adjusted per domain, dataset, model, map size.

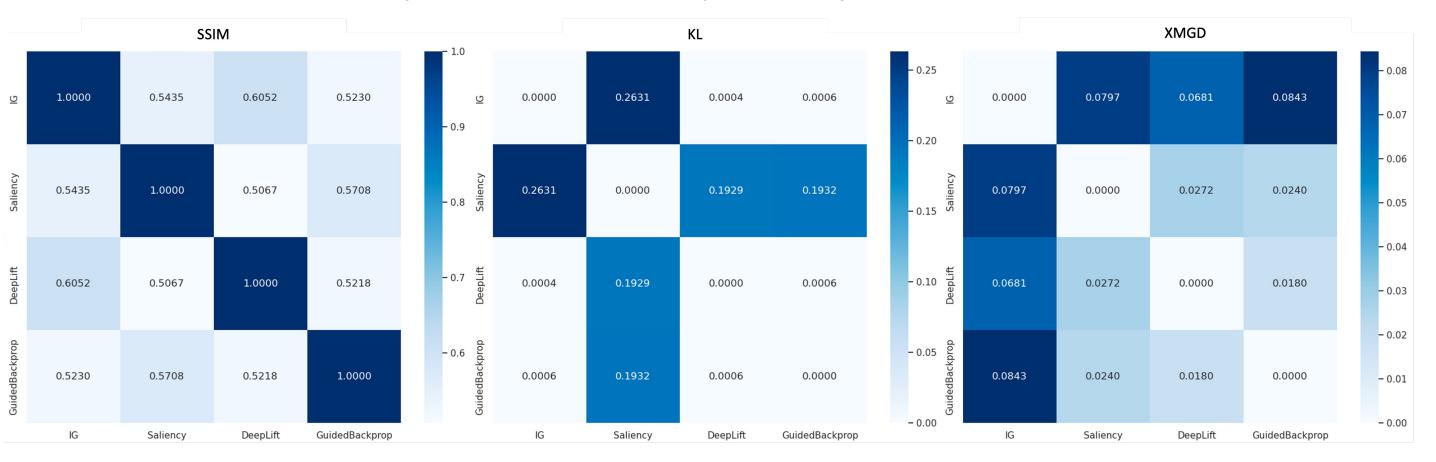
Step 1: Process saliency maps, project to unit grid. Step 2: Fit a Weighted-Data GMM (WD-GMM) to each of the processed saliency maps/ sets of saliency maps. $P = \sum_{i=1}^{K_0} \pi_i v_i \text{ and } Q = \sum_{i=1}^{K_1} \alpha_i \mu_i \\ \forall i \in \{1, \dots, K_0\}, \forall j \in \{1, \dots, K_1\}$ Saliency Model B \vdots Saliency Model A $\downarrow 0.1] \times [0.1] \times [0.1]$ Step 3: Calculate the 2-Wasserstein distance between the WD-GMMs. $MW^2(P,Q) = \min_{y} \sum_{\ell,j} y_{\ell,j} W_2^2(v_{\ell},\mu_j)$ $W_2^2(N(\mu_1, \Sigma_1), N(\mu_2, \Sigma_2)) = ||\mu_1 - \mu_2||_2^2 + Tr(\Sigma_1) + Tr(\Sigma_2) - 2Tr\left(\frac{1}{\Sigma_1^2} \sum_{\ell=1}^2 \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{j=1}^{N_2} \sum_{\ell=1}^{N_2} \sum_{$



Experiments

Diversity of distances

Experimental results for generated saliencies are aggregated over seven detectors, then their pairwise similarity is compared across four XAI methods.



When compared to KL Divergence and SSIM, XMGD demonstrates the most differentiated levels of distances between distributions.

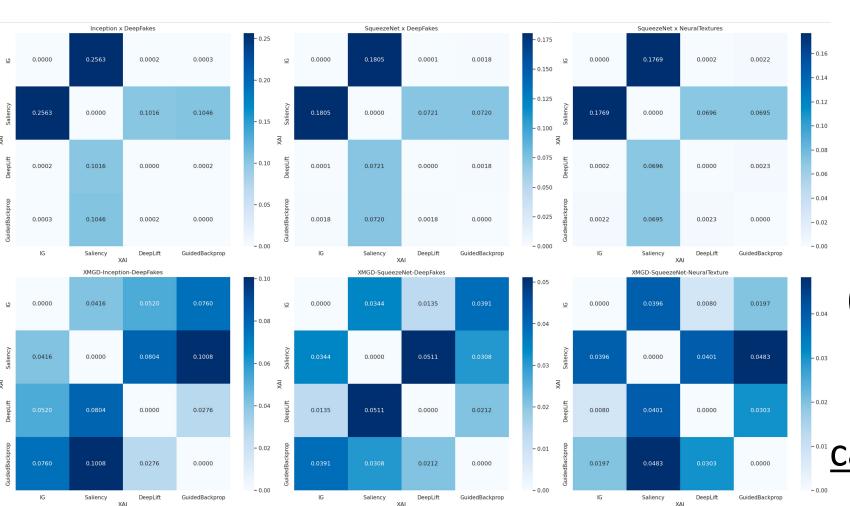
Relevance to model-based metrics

On FaceForensics[4] with five generators, using the same seven detectors, we compute model-dependent metrics IIC, AD, and ADD as for four XAI

Metric	IG	Saliency	DeepLift	GuidedBl
IIC个	0.612	0.358	0.561	0.518
AD↓	-0.082	0.344	0.289	0.229
ADD 个	1.064	-0.070	0.201	-0.120

methods. IG performs the best on all. In Tab. 1 and Fig. 3, IG is preferred by both XMGD and model-based metrics, demonstrating that <u>XMGD can capture</u> model-based insights without input manipulation and additional inference.

Preserved correlations between detectors and generators



Assuming that same detector/
generator comparisons to
surface as high correlations,
DF+SQ (mid) vs. DF+Inc (left)
yields 0.813, DF+SQ vs. NT+SQ
(right) gives 0.810, but the pair
without common components
yields only 0.742. XMGD
captures underlying similarities.