

# Feasibility Study of Real Time Path Tracing

*Or: How Much Noise Is Too Much?*

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by

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# Abstract

This study aims to investigate the viability of a physically-based technique called **path tracing** in lieu of or in corporation with classical techniques in interactive media such as video games and visual effects tools.

Real time path tracing has been prohibitively expensive in regards to computational complexity. However, modern GPUs and even CPUs have finally gotten fast enough for real time path tracing to become a viable alternative to traditional real time approaches to rendering. Based on that assumption, this thesis presents the idea, algorithm and complexity behind path tracing in the first part and extrapolates feasibility and suitability of real time path tracing on consumer hardware according to the current state of technology and trends in the second part.

As part of the research, the author has implemented a path tracing 3D engine in modern C++ in order to empirically test the assumptions made in this thesis. The study found path tracing to be a viable rendering technique for average commodity hardware in approximately 4 years.

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*We all make choices in life, but in the end, our choices make us.*

*Andrew Ryan*

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# Acronyms

**AABB** axis-aligned bounding box

**AO** ambient occlusion

**BRDF** bidirectional reflection distribution function

**BVH** bounding volume hierarchy

**BSP** binary space partitioning

**CPU** central processing unit

**CSG** constructive solid geometry

**FPS** frames per second

**GI** global illumination

**GPU** graphics processing unit

**PSNR** Peak signal-to-noise ratio

**HDR** high dynamic range

**GFLOPS** billions of floating point operations per second

**MLT** Metropolis light transport

**PBR** physically based rendering

**RT** real time

**RGB** red-green-blue

**SIMD** single instruction multiple data

**SPP** samples per pixel

**SSAO** screen-space ambient occlusion

# 1 Introduction

As part of the quest for ever-improving game graphics, researchers, graphics hardware developers and video game developers alike have been coming up with more and more convoluted and technically challenging ways of improving the graphics in interactive media such as games and visualizations in order to give users a deeper sense of immersion or to provide special effects artists with faster feedback.

While rendering techniques are currently shifting from the traditional fixed pipeline approach towards the new, fully programmable approach that lets developers implement deferred renderers that can more closely mimic reality by using multiple combined shading and lighting algorithms and rendering the scene multiple times for different buffers, the fundamental concept of rasterization-based rendering has largely remained the same.

The real world photon-collecting approach that actual cameras use has so far not been adopted for interactive media by the industry in any capacity because the computational cost has historically been prohibitively expensive. It is, however, used extensively (and has been in use since decades) for offline, non-interactive rendering of computer-generated movies and visualizations of scientific simulations.

This study assumes that the next logical step for the industry will be to adopt this method for real time media as well. For the purpose of this thesis, a renderer is considered *real time* when it manages to render a frame within  $16.67ms$  since that equals 60 frames per second (FPS) which is the current de facto standard refresh rate for most available computer screens. Conversely, a renderer is called *offline* when it is not designed for interactive rendering which usually means that it will render an image or a batch of images over the course of a few days. The differences of real time and offline path tracing renderers will be explained in the next chapter.

The focus of this research is, first and foremost, interactivity. Therefore, whenever a trade-off between interactivity and image quality is considered, we will always prefer rendering speed if the target of 60 FPS would otherwise not be reached anymore.

## 1.1 Motivation

Real time path tracing (and physically based rendering in general) offers many benefits over traditional real time rendering methods such as better visuals and simpler

implementation but also allows for completely new types of graphics such as realistic caustics [1] and even light dispersion [2] (using a prism, for instance) since path tracers might simulate wavelengths instead of plain red-green-blue (RGB) colors. Modern video games tend to rely on a growing number of tricks to keep them visually appealing as the consumer grows more demanding. They're called *tricks* in this study because they merely trick the beholder into seeing something that appears to be physically accurate when it is, in fact, not the result of a physically-based calculation and as such this study aims to keep tricks and emergent phenomena separated by language. Some notable tricks include screen-space ambient occlusion (SSAO) [3], motion blur [4], lens flares [5], chromatic aberration [6], depth of field [7] and light mapping [8].

## 1.2 Leading Questions and Goals

The primary research objective of this thesis is finding out when real time path tracing will be a viable alternative to rasterization on commodity hardware. This question is explored by looking at theoretical indicators (such as Moore's Law) and practical indicators (by implementing a real time path tracer and benchmarking it) about its performance and the current state of the industry.

## 2 Real Time Path Tracing Explained

This chapter will explain the concepts, mathematics, physics and algorithms behind path tracing, how real time path tracing differs from offline path tracing and the trade-offs made to achieve acceptable performance. It will also explain how path tracing differs from rasterization and other global illumination (GI) techniques.

### 2.1 Physically Based Approach

In our physical world, we see pictures because our eyes collect photons emitted by light sources which then bounce around various surfaces until they eventually hit our eyes' photoreceptor cells. On every bounce, a bit of light is absorbed which is why light loses intensity when it bounces. Some surfaces absorb a particular band of wavelengths of the light when it bounces which we perceive as a change in the light's color. Cameras work exactly like this as far as collection of photons is concerned.

This physical approach would be extremely wasteful and computationally complex to simulate, however, since most photons never reach an observer. Consider, for instance, that only an extremely small percentage of all the photons sent by the Sun actually reach Earth and an even smaller percentage of those are ever observed (although photons don't have to be observed to have a physical effect, of course). Since we only care for photons that are relevant to the image that we are trying to render, it makes more sense to use *backwards ray tracing* in which rays (which simulate streams of photons) are shot from the observer into the scene for every sensor. It is called *backwards* because the rays go the reverse direction compared to their physical counterparts.

This is efficient since we usually only care about a single observer (the scene camera) for which we will trace every single ray that it can possibly perceive. In computer graphics terms, we will trace a ray for every pixel of the camera (and for now we will assume that the viewport is exactly the same resolution as the camera simplicity's sake). For every ray, we check for intersections with geometry and then either bounce a few more times or shoot directly towards a light. We might do this multiple times per pixel and integrate all resulting values to improve image quality. This type of sampling is called *Monte Carlo integration*. The more iterations we spend on sampling, the better the quality of our image becomes. This is called *converging*. There are many approaches that

improve this completely random approach to sampling. While the most straightforward approach is given by uniform sampling, other methods such as stratified sampling [9] and importance sampling [9] will usually provide a clear advantage in terms of time to convergence. Other, more complicated approaches are bidirectional path tracing [10] and the Metropolis light transport (MLT) [11] which shoot rays from both the light and the camera and then connect all the intersection points in order to form a light path.

## 2.2 Theoretical Basis

### 2.2.1 The Rendering Equation

The fundamental problem solved by path tracing is the *rendering equation* originally described by James Kajiya [12]. This thesis uses the form from Wikipedia [13] since the author considers it easier to read:

$$L_o(\mathbf{x}, \omega_o, \lambda, t) = L_e(\mathbf{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o, \lambda, t) L_i(\mathbf{x}, \omega_i, \lambda, t) (\omega_i \cdot \mathbf{n}) d\omega_i$$

For our purposes, this can be simplified by removing the time and wavelength components which we will not make use of:

$$L_o(\mathbf{x}, \omega_o) = L_e(\mathbf{x}, \omega_o) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o) L_i(\mathbf{x}, \omega_i) (\omega_i \cdot \mathbf{n}) d\omega_i$$

This equation can be broken down into its individual parts to make it easier to explain and understand:

$$L_o(\mathbf{x}, \omega_o) = L_e(\mathbf{x}, \omega_o) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o) L_i(\mathbf{x}, \omega_i) (\omega_i \cdot \mathbf{n}) d\omega_i$$

$L_o(\mathbf{x}, \omega_o)$  is the **outgoing light** with  $\mathbf{x}$  being a point on a surface from which the light is reflected from into direction  $\omega_o$ .

$L_e(\mathbf{x}, \omega_o)$  is the **emitted light** from point  $\mathbf{x}$ . Usually surfaces don't emit light themselves unless they are area lights.

$\int_{\Omega} \dots d\omega_i$  is the integral over  $\Omega$  which is the hemisphere at  $\mathbf{x}$  (and thusly centered around  $\mathbf{n}$ ). All possible values for  $\omega_i$  are therefore contained in  $\Omega$ .

$f_r(\mathbf{x}, \omega_i, \omega_o)$  is the **bidirectional reflection distribution function (BRDF)** which determines how much light is reflected from  $\omega_i$  to  $\omega_o$  at  $\mathbf{x}$ .

$L_i(\mathbf{x}, \omega_i)$  is the **incoming light** at  $\mathbf{x}$  from  $\omega_o$ . It is not necessarily *direct light*. The rendering equation also considers *indirect light* which is light that has already been

reflected.

$(\omega_i \cdot \mathbf{n})$  is the **normal attenuation** at  $\mathbf{x}$ . The incoming light  $\omega_i$  is weakened depending on the cosine of the angle between  $\omega_i$  and the surface normal  $\mathbf{n}$ .

Path tracing offers a numerical solution to the integral found in this equation. For every pixel, every bounce and every sample of the camera, the rendering equation is solved. It becomes apparent why this is an expensive algorithm to run. For practical reasons, not every possible value for  $\Omega$  is sampled since this would take a vast amount of time to calculate at physical photon density. Instead, only a few possible values for  $\Omega$  are calculated each bounce. Depending on the exact algorithm used, usually only a low number of samples (approximately 20) is required for the image to converge to an acceptable level of quality.

### 2.2.2 Algorithm

The general naive algorithm for path tracing in Python-like pseudocode for diffuse and emissive materials can be written as follows:

```
1 max_depth = 5
2
3 def trace_ray(ray, depth):
4     if depth >= max_depth:
5         # Return black since we haven't hit anything but we're
6         # at our limit for bounces
7         return RGB(0, 0, 0)
8
9     collision = ray.check_collision()
10    if not collision:
11        # If we haven't hit anything, we can't bounce again so
12        # we return black
13        return RGB(0, 0, 0)
14
15    material = collision.material;
16    emittance = material.emittance
17
18    # shoot a ray into random direction and recurse
19    next_ray = Ray()
20    next_ray.origin = collision.position
```

```

21     next_ray.direction = random_vector_on_hemisphere(collision.normal)
22
23     reflectance_theta = dot(next_ray.direction, collision.normal)
24     brdf = 2 * material.reflectance * reflectance_theta
25     reflected = trace_ray(next_ray, depth + 1)
26
27     return emittance + (brdf * reflecte)
28
29 for sample in range(samples):
30     for pixel in pixels:
31         trace_path(ray_from_pixel(pixel), 0)

```

Listing 1: Naive path tracing algorithm

The algorithmic complexity of this algorithm is not immediately obvious because of its pseudocode character and a few methods whose implementations are not provided. It is known, however, that the output image  $O$  will be a 2D matrix with dimensions given by width  $w$  and height  $h$ . Additionally, for every pixel, multiple samples  $s$  are required in order for the algorithm to converge to an image of acceptable quality. Every ray has a certain maximum depth  $d$ .

So far, this lets us determine the total worst number of rays required per image. In the worst case, no ray exits early. The resulting formula is:

$$O_w \times O_h \times s \times d$$

Running this for a single pixel with 30 samples and a ray depth of 5 would require

$$30 \times 5 = 150$$

rays per pixel.

For example, an image with a resolution of  $1920 \times 1080$  would have

$$1920 \times 1080 \times 30 \times 5 \approx 300\,000\,000$$

rays per frame.

This does still not yield the algorithmic complexity, however, since there is no input size  $n$  in it. We will assume the lookup time for every ray to be  $O(\log n)$  in a suitable data structure. Hence, the formula becomes:

$$O_w \times O_h \times s \times d \times \log n$$

The result of this formula yields the number of total lookups per image. Continuing the example from above given a scene with 2 million triangles thus results in

$$1920 \times 1080 \times 30 \times 5 \times \log 2\,000\,000 \approx 2\,000\,000\,000$$

lookups per frame.

In the context of this thesis, a goal was set to reach 60 FPS which means that

$$1920 \times 1080 \times 30 \times 5 \times \log 2\,000\,000 \times 60 \approx 120\,000\,000\,000$$

lookups per second.

Thankfully, the whole formula can be reduced to just the lookup time  $O(\log n)$  because the other formula elements are covariants.

### 2.2.3 Acceleration Data Structures

The data structure used for the underlying scene is the principal factor for the performance of the path tracing algorithm. The most commonly used naive data structure for path tracing is a simple list of shapes. Upon scene lookup, a ray is tested for intersection with every shape. The complexity in this case is  $O(n)$  where  $n$  is the number of shapes which is comparable to rasterization but a lot worse than it could be with a proper acceleration data structure.

Assuming a flat list of shapes as the current data structure, the next logical step to improve scene look up time is to add axis-aligned bounding boxes (AABBs) around clusters of smaller shapes. For instance, an AABB might surround an icosahedron shape that is made up of hundreds of triangles. This way, the triangles inside the AABB are only tested for ray intersections if the ray intersects the AABB that surrounds the shape. The complexity is now  $O(mn)$  where  $m$  is the number of shapes (which is equal to the number of AABBs) and  $n$  is the number of triangles. This might seem like a worse complexity class compared to before but in practice the number of comparisons is a lot lower.

The next iteration on top of simple AABBs is provided by tree-based acceleration data structures. The most commonly used ones are the bounding volume hierarchy (BVH) and the kd-tree. By using these data structures, scene lookup performance per ray could be drastically improved to  $O(\log n)$  at the cost of a tree rebuild once per frame. This is usually a good trade-off since a scene is looked up millions of times per frame but the

tree only has to be rebuilt once. While there are multiple ways to build a BVH, most of them have a complexity close to  $O(n(\log n)^2)$  while building a kd-tree can be done in  $O(n \log n)$ .

## 2.3 Properties of Path Tracing

This section summarises the general properties of path tracing.

### 2.3.1 Computational Cost

Even though path tracing has a high initial cost, the lookup time for ray collisions is in  $O(\log n)$  which means that as scenes increase in complexity, the time spent on doing the lookups is fairly small. The initial cost of path tracing heavily depends upon screen resolution and desired quality. Due to the high initial cost, path tracing is generally considered slow and it made real time path tracing infeasible up until recent years.

### 2.3.2 Dynamic Scenes

Path tracing is well suited for dynamic scenes since it doesn't depend on pre-computations. This makes it viable for use in interactive applications. The scene data structure must allow for dynamic scenes in this case, though.

### 2.3.3 Global Illumination

Commonly global illumination (GI) means that every object's illumination affects every other object and that the renderer doesn't make a distinction between reflected light and light sources.

### 2.3.4 Problems

Due to the unbiased and random way rays are reflected from surfaces, it takes a long time for classic path tracing to produce sharp caustics as rays tend to very rarely hit objects with caustic properties. This makes it especially difficult for real time path tracing to produce sharp caustics. This can be alleviated by using bidirectional path tracing or by using an additional photon map.

Another problem is that subsurface scattering and can't be addressed by classic Monte Carlo path tracers. This can be addressed by using *volumetric path tracing*. [14] [15] Since path tracers do not simulate light wavelengths, natural phenomena caused by chromatic aberration, fluorescence and iridescence can not be realistically simulated. A

fairly new improvement to path tracing called *spectral path tracing* with realistic lenses can produce physically accurate images in those cases. [16] [17] [18] [19]

### 2.3.5 Comparison to Traditional Ray Tracing

Ray tracing is the fundamental algorithm behind path tracing. The only difference is that when a ray hits an object, it doesn't keep bouncing but instead fires off one ray to every light source directly. This subtle difference means that ray tracing can only calculate direct lighting as opposed to GI.

### 2.3.6 Comparison to Rasterization

Rasterization is widely implemented in the industry and most interactive 3D applications use it to render their scene. Its fundamental algorithm has a complexity of  $O(n)$  and is therefore theoretically slower than path tracing. However, a wide array of algorithmic improvements such as back-face culling exist and additionally its initial cost is very low. Unlike path tracing, it does not automatically simulate a wide range of physical phenomena. Physical effects such as shadows, global illumination and caustics have to be calculated separately in other algorithms and then be composited on top of the rasterized scene. This makes rasterization complicated to use for when many physical effects are desired.

### 2.3.7 Comparison to Other Global Illumination Algorithms

This section compares some of the more popular GI algorithms beside ray tracing and path tracing. In general, GI is considered to be a group of algorithms that calculate direct light as well as indirect light for computer graphics scenes. However, not all algorithms that fulfill this purpose are in fact physically accurate. We will therefore take a look at how some of these algorithms compare to path tracing.

The algorithms that are compared to path tracing in this section are: *photon mapping*, *radiosity* and *ambient occlusion*. These were chosen due to their widespread use and their varied approaches. Other GI algorithms include: Lightcuts (and its variants), Point Based Global Illumination and Spherical harmonic lighting.

To note: This thesis considers path tracing at the current state of research which means that path tracing, bidirectional path tracing and the MLT are shortened to just *path tracing* and will therefore not be individually compared.

## Photon Mapping

Photon mapping is a two-step process that was developed in 1996 by Henrik Wann Jensen [20] as an approximate way to simulate charged particles (*photons*) traversing the scene.

In the first step, every photon carries a *charge* and is traced through the scene. On every collision with scene geometry, it is stored to the *photon map* at that location. Afterwards, the photon is either reflected, refracted, scattered or absorbed depending on the material and loses a bit of its charge. The photon map serves as a cache for the second step in which a ray tracing-like process is used to calculate the radiance of the resulting image.

Compared to path tracing, photon mapping has a few advantages and a few disadvantages. In particular, photon mapping can simulate subsurface scattering and volume caustics which path tracing can't accurately calculate. On the other hand, photon mapping is unsuitable for real time applications with dynamic scenes since the photon map can only be used as long as the scene geometry or light position doesn't change. In the case the scene geometry changes, the cache is invalidated and a new photon map has to be calculated which is a slow process.

## Radiosity

Made originally for simulating heat transfer in 1984 by Goral et al.[21], radiosity is one of the oldest algorithms for calculating GI. It outputs a light value for every patch (a smaller part of a surface) on a cache or map. It is a physically accurate way of simulating light transfer but cannot simulate volume scattering, fog, caustics, transparent objects or mirrors. These limitations make it unsuitable to use in complex modern scenes. Additionally, the cache is invalidated whenever the scene changes and therefore it is also usually not usable for dynamic scenes.

## Ambient Occlusion

The idea for ambient occlusion (AO) was first presented by Gavin Miller in 1994 [22]. It is meant as an algorithm to calculate realistic occlusion of every point in a scene and cannot generate an accurate image on its own. It is usually used with a classic rasterization renderer whose output image is multiplied with the result of the AO and its resulting image is multiplied. The output of this algorithm is sometimes called the *ambient occlusion map* which serves as a cache. As such, rendering is extremely fast once the cache has been calculated. However, this cache is invalidated once the scene changes and is the algorithm is therefore unsuitable for dynamic scenes.

For real time applications, a variant of AO called screen-space ambient occlusion (SSAO) is usually used. While SSAO is inaccurate from a physical point of view, it results in some very fast and acceptable approximations that are suitable for real time applications.

## 2.4 History of Path Tracing

As with so many things in computer science and science in general, the modern idea of physically based rendering using path tracing builds upon many important past discoveries and algorithms such as ray tracing and ray casting. Arthur Appel is generally credited as being the father of *ray casting* as he was the first to describe the algorithm in a 1968 paper [23].

Ray casting is an important idea needed for *ray tracing* which was first published in a paper in 1980 by Turner Whitted [24].



Figure 2.1: Turner Whitted's original 1980 [24] image showing off the usage of ray tracing for reflection, refraction and shadows.

Building upon ray tracing, an improved algorithm was published in 1986 by James T. Kajiya which used ray tracing combined with a Monte Carlo algorithm in order to create a new algorithm that was called *Monte Carlo ray tracing* [12]. Nowadays, Monte Carlo ray tracing is better known as *path tracing*.

It took another decade for path tracing to become the physically based rendering approach that it is known for today. In 1996, Eric Lafortune improved the algorithm by suggesting the usage of bidirectional path tracing [10] and finally the MLT was suggested

in 1997 by Eric Veach and Leonidas J. Guibas [11] to improve performance in complex scenes.

This was the last notable improvement to the algorithm, though many micro optimizations have since been published. All of these achievements and improvements are generally collapsed into the term *path tracing* since they do not diverge from the general algorithm but instead improve upon it.

It took longer still for the industry to become interested in path tracing. The early interest in ray tracing was of mostly academical and recreational nature. One of the most notable creations of the early days of ray tracing is The Juggler created and published by Eric Graham in 1986 [25] on an Amiga 1000. It was a pre-rendered animation using ray tracing. Eric Graham stated that it took the Amiga 1 hour to render each frame [25].



Figure 2.2: Eric Graham's Juggler

While the animation seems very primitive compared to the animations of today, it was exceptional at the time. Ernie Wright's statement about The Juggler provides some contemporary context:

Turner Whitted's paper (1980) is widely regarded as the first modern description of ray tracing methods in computer graphics. This paper's famous image of balls floating above a checkerboard floor took 74 minutes to render on a DEC VAX 11/780 mainframe, a \$400,000 computer. The Juggler would appear a mere six years later, created and displayed on a \$2000 Amiga. ([25])

The first feature-length computer-animated film, *Toy Story*, released in 1995 [26], is sometimes miscredited as being the first film using a ray tracing-like algorithm. However,

it actually used traditional scanline rendering. The first feature-length film using ray tracing, *Cars*, was released much later, in 2006 [27] [28] and started a wave of interest in the movie industry.

The first example of *real time* path tracing was likely produced by the demo scene [29] which was quick to adopt it [30] for the purpose of producing complex graphics rendered and generated on the fly. One notable example of this is the WebGL Path Tracing by Evan Wallace made in 2010 [31] which runs in most modern web browsers, making path tracing very accessible.

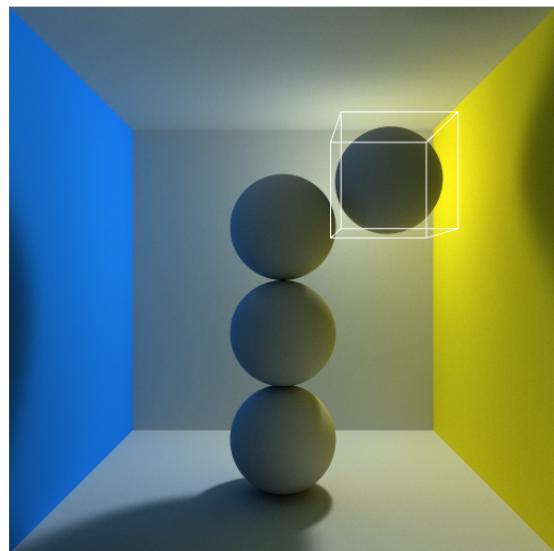


Figure 2.3: WebGL Path Tracer by Evan Wallace

Another example is the demo *5 faces* by Fairlight from 2013 [32] which uses a real time ray tracer running on the GPU to render a complex scene at 30 FPS.

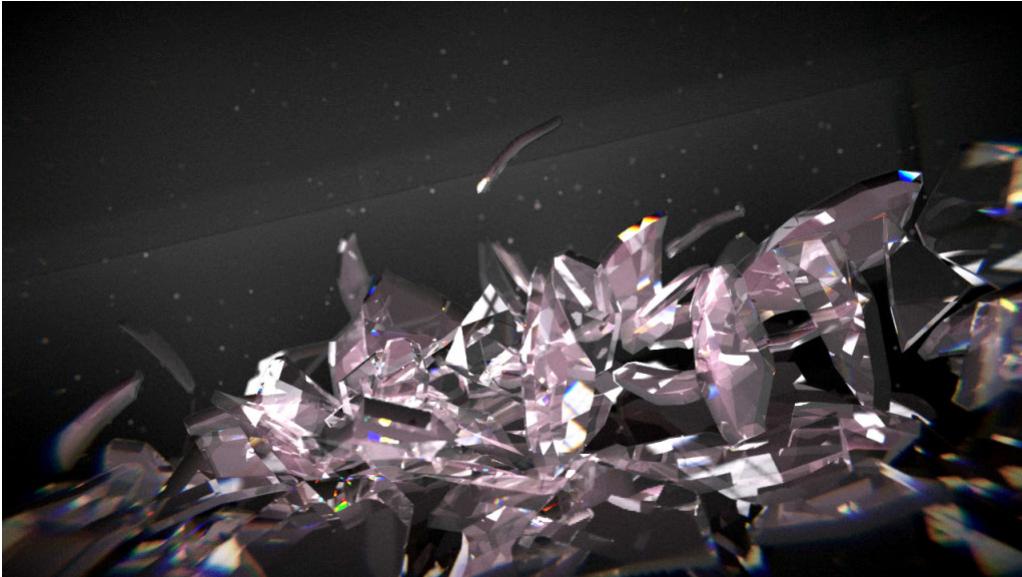


Figure 2.4: 5 faces by Fairlight

In the past, some critics have offered critical insights about why it might not be a viable alternative to rasterization on consumer hardware in the short term [33] [34]. Even John Carmack of id Software was sceptical of real time ray tracing in games in 2012 in a comment on Ars Technica [35].

## 2.5 Current State of Technology

Recently the interested in real time path tracing seems to be at peak levels. The most notable example of this is Jacco Bikker's and Jeroen van Schijndel's *Brigade Renderer* [36] [37]. This renderer is aimed at game developers and is meant to run on commodity hardware in real time. Its company, OTOY, is also developing a cloud-based rendering solution called Octane Render [38] for animation professionals.

Microsoft's DirectX 12 [39] is receiving *Hybrid Ray-Traced Shadows*, a technology that combines real time ray tracing with rasterization to create fast high quality shadows. A video game using actual real time path tracing and physics called *Sfera* was created by David Bucciarelli [40] in 2011. It uses OpenCL for calculating the paths and OpenGL to render them to the screen.

It's important to keep in mind that while the real time graphics industry has mostly been driven by video games, the most important hardware currently exist in game con-

soles which generally evolve at a much slower pace than desktop computers in terms of hardware power and their graphics hardware especially is usually non-upgradeable. This means that it wouldn't be economically viable to develop a real time path tracing renderer that only ran on current generation desktop computers because most consumers would not be able to benefit from the technology.

# 3 Research

The entirety of the research in this thesis was done with a Monte Carlo path tracer called *trac0r*. An effort was made to find an existing open source implementation of a path tracer focused on real time applications but none seem to exist as of this writing. The most likely cause for that is the enormous hardware cost currently still associated with doing real time path tracing.

## 3.1 Implementation

Alongside this thesis, a Monte Carlo Path path tracer called *trac0r* was implemented in C++. It can optionally make use of OpenCL or OpenMP in order to speed up computation. A conscious decision was made to only implement triangles for geometric primitives due to two reasons. Firstly, since every other geometric shape can be expressed easily using an amount of triangles, it seems unnecessary to add additional complexity (although using triangles to approximate other shapes will be less efficient from a performance perspective). Secondly, real world applications very rarely make use of perfect mathematical shapes such as spheres, boxes and tori when rendering. Most modern mesh modeling approximates these shapes using triangles. Since this renderer is supposed to be used for real world application such as games and interactive visualizations, it didn't seem necessary to implement anything in addition to what mesh modeling tools will export.

Additionally to triangles, AABBs were implemented with the aim to speed up rendering. While *trac0r* does not implement any advanced acceleration structures (such as BVHs or kd-trees), it uses AABBs to dramatically decrease the number of triangle intersection tests. Every ray first tests for intersections with every AABB in the scene and upon a hit tests every triangle enclosed by the AABB. The fast Möller–Trumbore intersection algorithm [41] is used for triangle intersection tests.

The program does not currently support importing of externally defined scenes or meshes. Scenes are defined in-code. Utilities for generating planes, boxes and icosahedra out of triangles are provided. A properly sized AABB is built around every shape. It uses classic reverse path tracing and implements four basic materials.

### 3.1.1 Materials

The materials implemented are as follows:

1. Emitter: Arguably the most important material as it is the one providing the light to a scene. This simulates a black body heated to a certain temperature and as such serves as an area light when applied to geometry. Any ray hitting geometry using the emitter material is terminated. A scene without any geometry using emitter material will be utterly dark.
2. Diffuse: A matte material that scatters light to a random location on the hemisphere around the normal of the intersected geometry.
3. Glass: A material that will choose between reflection and refraction depending on the Fresnel coefficients [42]. It is the only material capable of handling intersections within an object.
4. Glossy: A metal-like material that will reflect a ray towards a cone centered around the direction of the outgoing light  $\omega_o$ . A roughness parameter determines the opening angle of that cone. A roughness of 0 will result in a perfect mirror while a roughness of 1 will produce a cone with an angle of  $\pi$ .

```
1  struct Material {  
2      /**  
3      * @brief Used to determine the material type used.  
4      * Refer to the table below:  
5      *      m_type = 1: Emissive  
6      *      m_type = 2: Diffuse  
7      *      m_type = 3: Glass  
8      *      m_type = 4: Glossy  
9      */  
10     uint8_t m_type = 1;  
11  
12     /**  
13     * @brief Used as the basic color for most materials.  
14     */  
15     glm::vec3 m_color = {0.9f, 0.5f, 0.1f};  
16  
17     /**  
18     * @brief Used to determine the ratio between reflection and diffusion
```

```

19 * for some materials. Value must be between 0.0 and 1.0.
20 */
21 float m_roughness = 0.f;
22
23 /**
24 * @brief Index of refraction (IOR) is used to determine how
25 * strongly light is bent inside a glass material.
26 */
27 float m_ior = 1.f;
28
29 /**
30 * @brief Luminous emittance provides the strength of emissive
31 * material. Values can be larger than 1.0.
32 */
33 float m_emittance = 0.f;
34 };

```

Listing 2: Material struct in trac0r. Depending on the `m_type` set, different attributes of this material are used.

### 3.1.2 Sampling

trac0r provides a few different methods for geometric sampling.

```

1 /**
2 * @brief Selects a random point on a sphere with uniform distribution.
3 * point on a uniform.
4 *
5 * @return A random point on the surface of a sphere
6 */
7 inline glm::vec3 uniform_sample_sphere() {
8     glm::vec3 rand_vec =
9         glm::vec3(rand_range(-1.f, 1.f),
10                  rand_range(-1.f, 1.f),
11                  rand_range(-1.f, 1.f));
12     return glm::normalize(rand_vec);
13 }

```

Listing 3: Function to sample random points on the surface of a sphere implemented from [43]

```

1  /**
2   * @brief Given a direction vector, this will return a random uniform
3   * point on a sphere on the hemisphere around dir.
4   *
5   * @param dir A vector that represents the hemisphere's center
6   *
7   * @return A random point the on the hemisphere
8   */
9  inline glm::vec3 oriented_uniform_hemisphere_sample(glm::vec3 dir) {
10     glm::vec3 v = uniform_sample_sphere();
11     return v * glm::sign(glm::dot(v, dir));
12 }
```

Listing 4: Function to sample uniform points on a hemisphere given by `dir`

```

1  /**
2   * @brief Selects a random point on a sphere with uniform or
3   * cosine-weighted distribution.
4   *
5   * @param dir A vector around which the hemisphere will be centered
6   * @param power 0.f means uniform distribution while 1.f means
7   * cosine-weighted
8   * @param angle When a full hemisphere is desired, use pi/2.
9   * 0 equals perfect reflection. The value
10  * should therefore be between 0 and pi/2. This angle is equal
11  * to half the cone width.
12  *
13  * @return A random point on the surface of a sphere
14  */
15 inline glm::vec3 sample_hemisphere(glm::vec3 dir, float power, float angle) {
16     // Code adapted from Mikael Hvidtfeldt Christensen's resource
17     // at http://blog.hvidtfeldts.net/index.php/2015/01/path-tracing-3d-fractals/
18     // Thanks!
19
20     glm::vec3 o1 = glm::normalize(ortho(dir));
```

```

21     glm::vec3 o2 = glm::normalize(glm::cross(dir, o1));
22     glm::vec2 r = glm::vec2{rand_range(0.f, 1.f),
23                             rand_range(glm::cos(angle), 1.f)};
24     r.x = r.x * glm::two_pi<float>();
25     r.y = glm::pow(r.y, 1.f / (power + 1.f));
26     float oneminus = glm::sqrt(1.f - r.y * r.y);
27     return glm::cos(r.x) * oneminus * o1 +
28           glm::sin(r.x) * oneminus * o2 + r.y * dir;
29 }
```

Listing 5: Function to sample cosine-weighted points on a hemisphere given by `dir`. `power` is used to determine whether to generate uniform samples or cosine-weighted ones. If `power` is `0.f`, uniform samples are generated. If it's `1.f`, cosine-weighted samples are generated. `angle` provides the opening angle of the cone that rays will be generated inside of.

```

1 /**
2  * @brief Given a direction vector, this will return a random
3  * cosine-weighted point on a sphere on the hemisphere around dir.
4  *
5  * @param dir A vector that represents the hemisphere's center
6  *
7  * @return A random point the on the hemisphere
8 */
9 inline glm::vec3 oriented_cosine_weighted_hemisphere_sample(glm::vec3 dir) {
10     return sample_hemisphere(dir, 1.f, glm::half_pi<float>());
11 }
```

Listing 6: Helper function to get samples from an entire hemisphere making use of 5

```

1 /**
2  * @brief Selects a random point on a cone with cosine-weighted
3  * distribution.
4  *
5  * @param dir Direction in which the cone is oriented
6  * @param angle Angle of the cone in radians
7  *
8  * @return A random point on the surface of a cone
9 */
```

```

9  */
10 inline glm::vec3 oriented_cosine_weighted_cone_sample(glm::vec3 dir, float angle) {
11     return sample_hemisphere(dir, 1.f, angle);
12 }
```

Listing 7: Helper function to get samples from a partial hemisphere making use of the code in listing 5

Russian roulette is used as a ray terminator with

$$\text{continuation\_probability} = 1 - \frac{1}{\text{max\_depth} - \text{depth}}.$$

Rays are randomly offset within a pixel which results in anti-aliasing. For generating random numbers, it uses `xorshift*` generators.

A secondary program was implemented additionally to the renderer called `tracer_viewer` which allows for interactive scene navigation.

## 3.2 Results

### 3.2.1 Visual Results

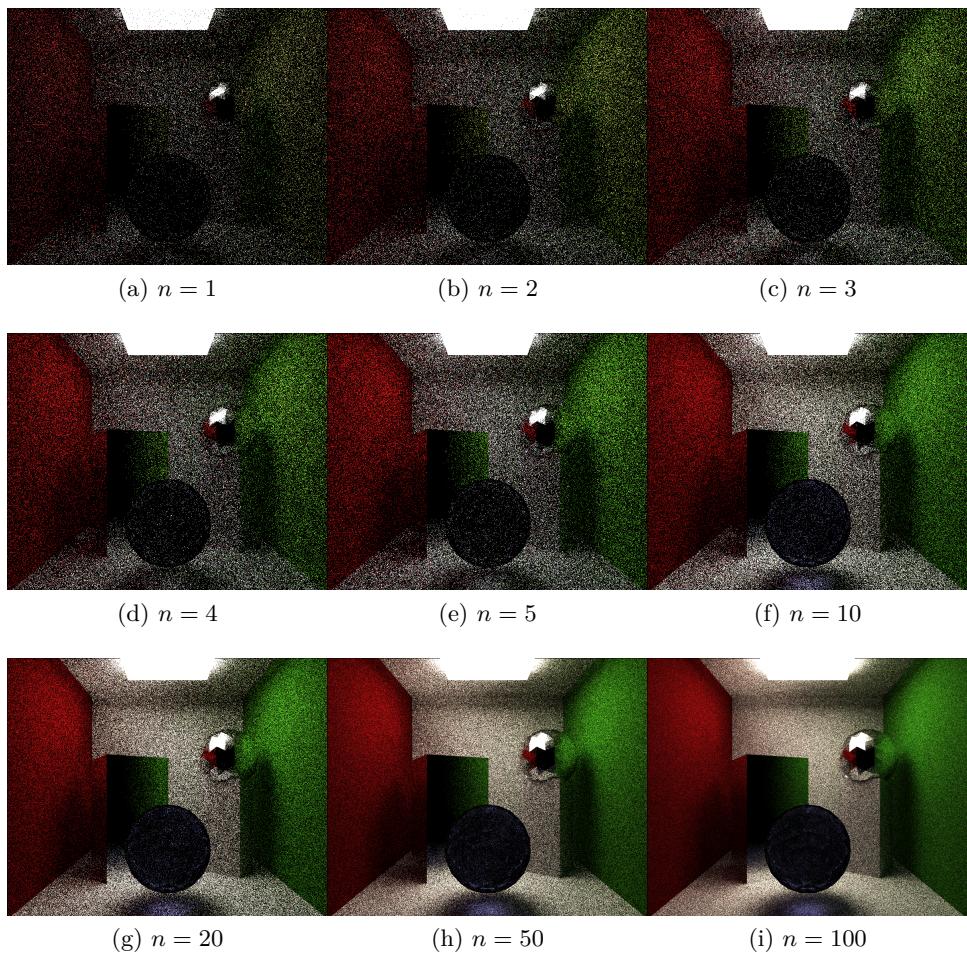


Figure 3.1: trac0r\_viewer viewport after integrating  $n$  frames

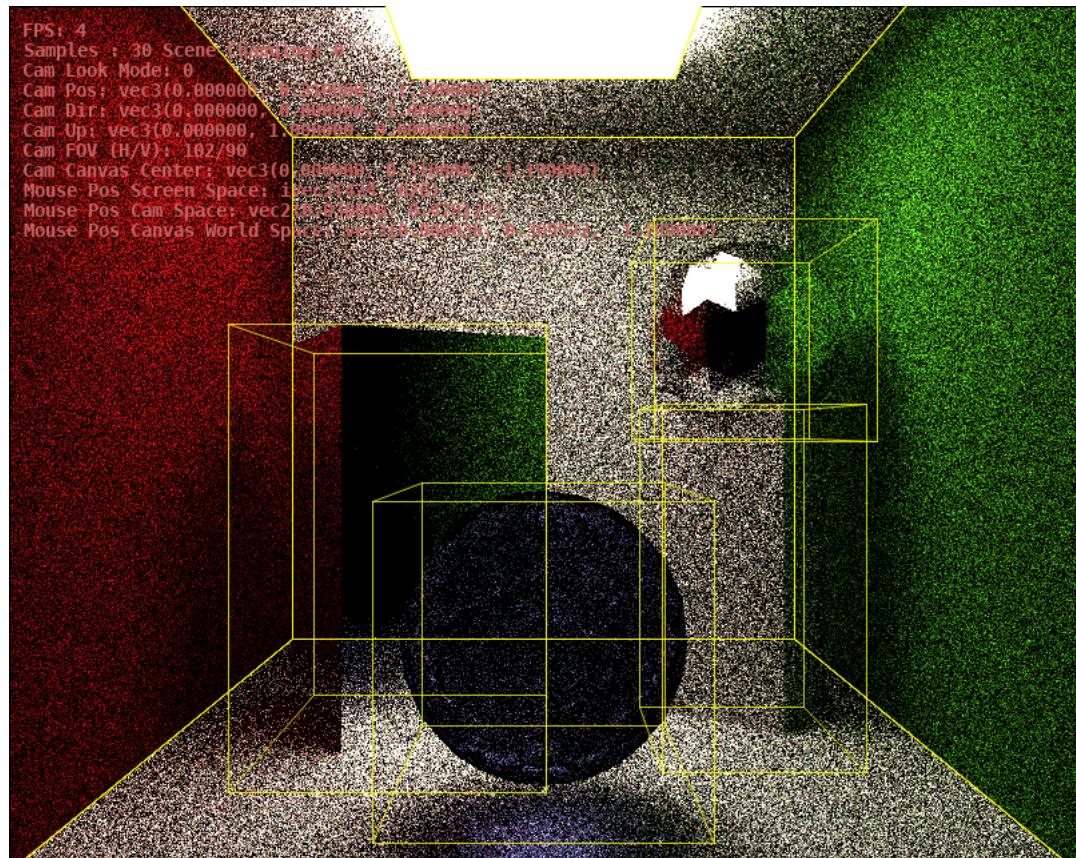


Figure 3.2: trac0r\_viewer debug view

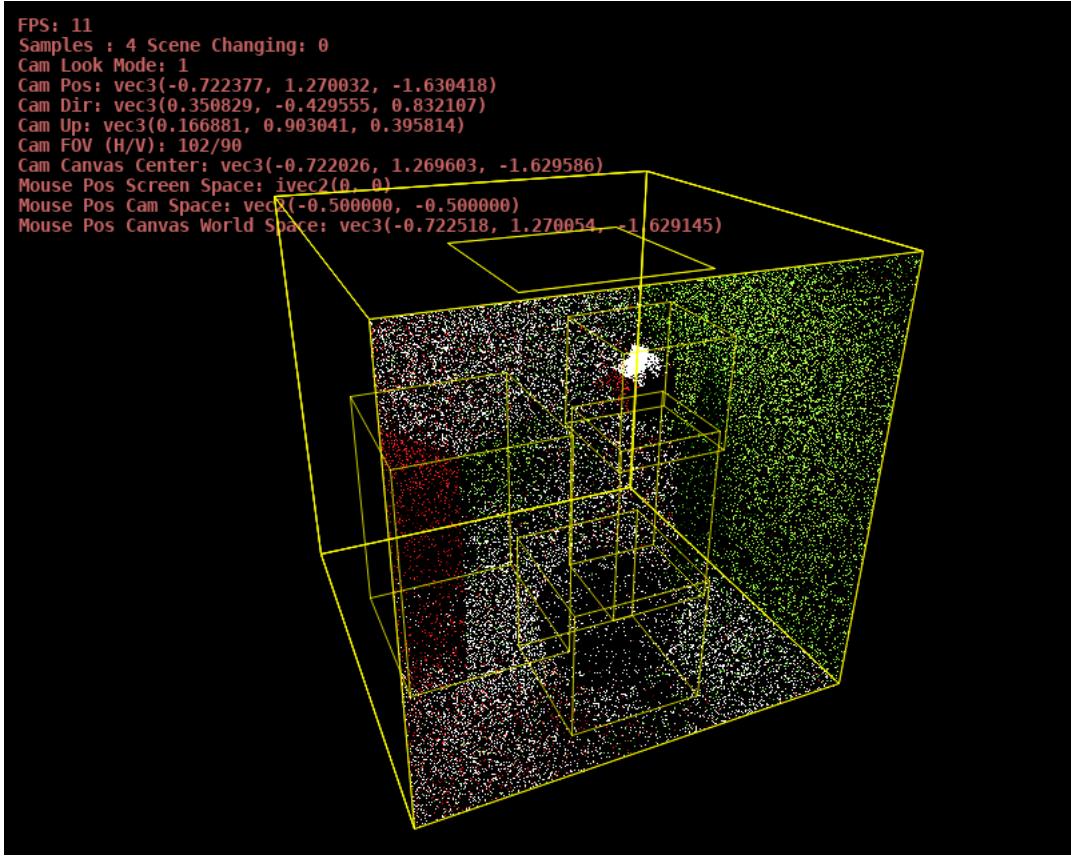


Figure 3.3: trac0r\_viewer debug view while interactively navigating the scene

### 3.2.2 Performance Results

Comparing FPS is not a particularly good criterion between different path tracing since usually FPS doesn't correlate to rate of convergence. That is, one path tracer might be able to iterate at 60 FPS but takes three seconds to converge while a different path tracer may only be able to do 10 FPS but takes only 2 seconds to converge. This might seem unintuitive at first but remember that path tracing is a very different algorithm compared to rasterization. In rasterization, once a frame is rendered, the image is "done", it won't improve by rendering the same scene a second time. In path tracing, particularly Monte Carlo path tracing, an image will be improved with every new frame that is rendered using the same parameters due to how Monte Carlo integration works.

In spite of that, this thesis uses FPS as the primary criterion for two reasons. Firstly,

we are not comparing different path tracers to the one made as part of the thesis. We only compare it against itself in different scene and hardware configurations. Secondly, FPS is much easier to work with and compare than image quality. One might use Peak signal-to-noise ratio (PSNR) to do the latter but that still leaves open the question of when to measure the image as even a single frame might take longer than a second to render under specific circumstances.

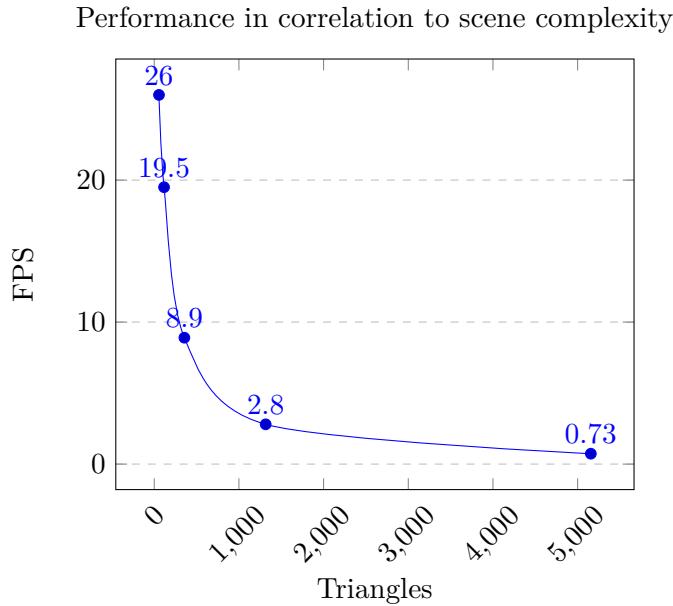
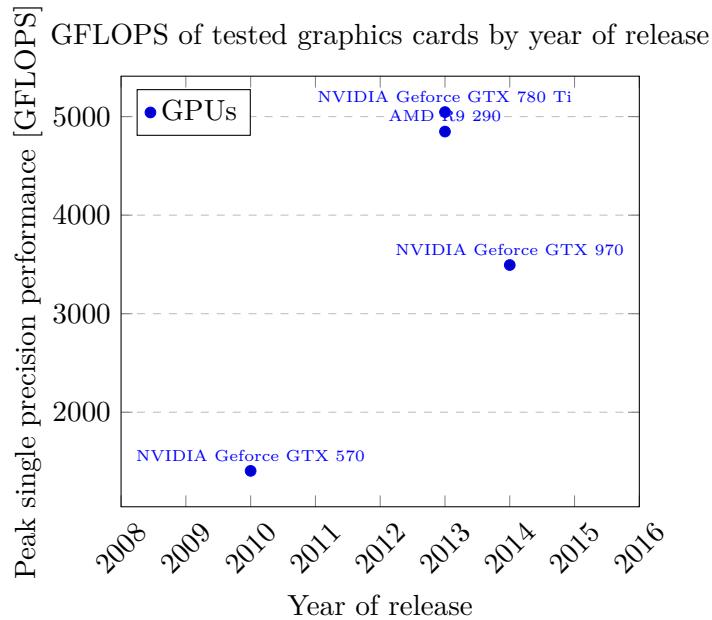


Figure 3.4: Scene complexity benchmark on an NVIDIA Geforce GTX 570

lol 3.4

### 3.3 Evaluation

In order to properly rate the results seen above, they need to be put into perspective. Performance of central processing units (CPUs) and graphics processing units (GPUs) varies enormously depending on their year of release due to technical progress.



All billions of floating point operations per second (GFLOPS) numbers are taken from the chip designers' official sites.

It should be noted that while GFLOPS isn't the only relevant criterion to estimating the performance of a GPU, it's likely the most important one.

# 4 Conclusion

## 4.1 Outlook

Scene lookup performance could be drastically improved by employing an acceleration structure such as BVH or kd-trees.

Convergence performance could be best improved by making use of bidirectional path tracing and better sampling techniques such as *Multiple Importance Sampling*.

The implementation's usage of memory architectures is likely far from optimal and could be improved.

Lastly, overall image quality could be improved by running an image filter over the rendered image before displaying it to the user. A suitable image filtering algorithm should be non-linear and edge-preserving as well as energy-preserving so that it won't lower the quality of the resulting image. A notable filter fulfilling those requirements is the *bilateral filter*. Popular but unsuitable algorithms include the *box filter* and the *gaussian filter*.

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## **Eidesstattliche Erklärung**

„Hiermit versichere ich an Eides statt, dass ich die vorliegende Arbeit im Studiengang Informatik selbstständig verfasst und keine anderen als die angegebenen Hilfsmittel – insbesondere keine im Quellenverzeichnis nicht benannten Internet-Quellen – benutzt habe. Alle Stellen, die wörtlich oder sinngemäß aus Veröffentlichungen entnommen wurden, sind als solche kenntlich gemacht. Ich versichere weiterhin, dass ich die Arbeit vorher nicht in einem anderen Prüfungsverfahren eingereicht habe und die eingereichte schriftliche Fassung der auf dem elektronischen Speichermedium entspricht.“