

$$4.1 \text{ b. } E(Y|C=0, X=0) = \frac{0 \times 80 + 1 \times 20}{80+20} = 0.2$$

$$E(Y|C=1, X=0) = \frac{0 \times 20 + 1 \times 10}{20+10} = 0.33$$

$$E(Y|C=0, X=1) = \frac{0 \times 80 + 1 \times 20}{80+20} = 0.2$$

$$E(Y|C=1, X=1) = \frac{0 \times 80 + 1 \times 40}{80+40} = 0.33$$

$$P(C=1) = \frac{20+10+80+40}{350} = 0.43$$

$$P(C=0) = \frac{20+10+80+40}{350} = 0.57$$

$$\begin{aligned} E(Y(1)) &= E(Y|do(X=1)) = E(Y|C=0, X=1) \cdot P(C=0) + E(Y|C=1, X=1) \cdot P(C=1) \\ &= 0.2 \times 0.57 + 0.33 \times 0.43 = 0.26 \end{aligned}$$

$$\begin{aligned} E(Y(0)) &= E(Y|do(X=0)) = E(Y|C=0, X=0) \cdot P(C=0) + E(Y|C=1, X=0) \cdot P(C=1) \\ &= 0.2 \times 0.57 + 0.33 \times 0.43 = 0.26 \end{aligned}$$

$$ATE = E(Y(1)) - E(Y(0)) = 0$$

$$\begin{aligned} E(Y(1)|X=1) &= E(Y|X=1, do(X=1)) \\ &= E(Y|C=0, X=1) \cdot P(C=0|X=1) + E(Y|C=1, X=1) \cdot P(C=1|X=1) \\ &= 0.2 \times 0.45 + 0.33 \times 0.55 = 0.27 \end{aligned}$$

$$\begin{aligned} E(Y(0)|X=1) &= E(Y|X=1, do(X=0)) \\ &= E(Y|C=0, X=0) \cdot P(C=0|X=1) + E(Y|C=1, X=0) \cdot P(C=1|X=1) \\ &= 0.2 \times 0.45 + 0.33 \times 0.55 = 0.27 \end{aligned}$$

$$ATT = E(Y(1)|X=1) - E(Y(0)|X=1) = 0$$