

ATE/risk difference:  $E(Y(1)) - E(Y(0))$ , risk ratio:  $E(Y(1))/E(Y(0))$ , odds ratio:  $\frac{E(Y(1))}{1-E(Y(1))} / \frac{E(Y(0))}{1-E(Y(0))}$

Assumptions: Consistency: well defined exposure (no differ in exposure) and no interference (subjects' outcomes are independent), Exchangeability:  $X \perp Y$ ,  $E(Y(x)|X = 1) = E(Y(x)|X = 0) = E(Y(x))$ , Positivity:  $P(X = x) > 0$

Assumption	Eligibility Criteria	Exposure Definition	Assignment Procedures	Follow- up Period	Outcome Definition	Causal contrast	Analysis Plan
Consistency (Well defined exposure)	✓	✓					
Consistency (No interference)		✓	✓		✓		✓
Positivity	✓		✓				✓
Exchangeability	✓		✓	✓			✓

Study design: randomized trials vs target trials (observational studies)

Observational studies: Cohort

studies/Prospective/ $X \rightarrow Y$  vs Outcome based

sampling/ case-control studies/Retrospective/ $Y \rightarrow X$

Key elements in protocol: eligibility criteria, exposure definition (intervention&control), assignment procedures, follow-up period, outcome definition, contrast of interest, analysis plan

PS aims: overlap between exposure groups, balance the data

Propensity score:  $P(X = 1|C = c)$ , package function: svydesign, svyglm

d-separation: path  $p$  is d-separated by  $\{Z\} \Leftrightarrow$  chain in  $\{Z\}$ /fork in  $\{Z\}$ /collider and descendants not in  $\{Z\}$

Backdoor criterion: adjustment set  $\{Z\}$  to  $X$  on  $Y$  satisfies: descendants of  $X$  not in  $\{Z\}$ ,  $\{Z\}$  d-separates (blocks) all paths between  $X$  and  $Y$  that contain an arrow into  $X$  (backdoor paths). Distribution of PS in groups should overlap, no PS values close to 1 or 0.

G-computation: ① Model  $E(Y|C, X)$  ② Calculate for each individual:  $\hat{E}(Y_i|C = c_i, X = x)$  ③ Estimate  $E_C E(Y|C, X = x)$

$E(Y(1)) = E(Y|\text{do}(X = 1)) = E(Y|C = 0, X = 1)P(C = 0) + E(Y|C = 1, X = 1)P(C = 1)$ ,  $ATE = E(Y(1)) - E(Y(0))$

$E(Y(0)) = E(Y|\text{do}(X = 0)) = E(Y|C = 0, X = 0)P(C = 0) + E(Y|C = 1, X = 0)P(C = 1)$ ,  $ATT = E(Y(1)|X = 1) - E(Y(0)|X = 1)$

$E(Y(1)|X = 1) = E(Y|X = 1, \text{do}(X = 1)) = E(Y|X = 1, C = 0)P(C = 0|X = 1) + E(Y|X = 1, C = 1)P(C = 1|X = 1)$

$E(Y(0)|X = 1) = E(Y|X = 1, \text{do}(X = 0)) = E(Y|X = 0, C = 0)P(C = 0|X = 1) + E(Y|X = 0, C = 1)P(C = 1|X = 1)$

Variables: outReg: confounders, var only  $\sim Y$ , no mediators, no var only  $\sim X$ , PSM: confounders, var only  $\sim Y$ , no var only  $\sim X$

Weights: ATE:  $1/P(X = 1|C_i)$  if exposed,  $1/P(X = 0|C_i)$  if unexposed; ATT: 1 if exposed,  $P(X = 1|C_i)/P(X = 0|C_i)$  if unexposed

MCAR:  $P(M = 1|Y_{\text{obs}}, Y_{\text{mis}}) = P(M = 1)$ , estimates consistent, se larger, imputation valid (consider only for efficiency gain)

MAR:  $P(M = 1|Y_{\text{obs}}, Y_{\text{mis}}) = P(M = 1|Y_{\text{obs}})$ , estimates consistent, se larger, imputation valid

MNAR:  $P(M = 1|Y_{\text{obs}}, Y_{\text{mis}})$ ,  $P(M = 1|Y_{\text{mis}})$ , estimates inconsistent, se larger, imputation invalid

MAR/MNAR but not dependent on outcome: complete cases may still be unbiased for some analyses, consider multiple imputation for efficiency gain

MAR with dependency on outcome: multiple imputation; MNAR with dependency on outcome: sensitivity analysis