$$\begin{array}{lll} & \emptyset \text{ a. } \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 0 & 3 \end{pmatrix} \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix} \Rightarrow \begin{pmatrix} \alpha \\ \beta \\ \gamma \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} & \text{ XI-A} \\ & \text{ Ax=} \lambda \chi \\ & \lambda 1 - A \\ & \lambda 1 - A \end{pmatrix} = \begin{vmatrix} \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} = \begin{pmatrix} \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ 0 \\ 1 \end{vmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_{-1} \end{pmatrix} \Rightarrow \begin{pmatrix} \lambda_{-1} \\ \lambda_$$

3.3.3 $\overrightarrow{A}\overrightarrow{v} = \lambda \overrightarrow{v} \Rightarrow (\lambda I - A)\overrightarrow{v} = \overrightarrow{o}$, when $\lambda = 0$, $|\lambda I - A| = (1)|A| = 0 \Rightarrow |A| = 0 \Rightarrow A$ not inv 3.3.19 \overrightarrow{a} , $\overrightarrow{A} = \begin{pmatrix} a_{11} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix}$, $\overrightarrow{v} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$, $\overrightarrow{A}\overrightarrow{v} = \begin{pmatrix} a_{11}v_1 + a_{12}v_2 + a_{13}v_3 \\ a_{21}v_1 + a_{22}v_2 + a_{23}v_3 \\ a_{31}v_1 + a_{32}v_2 + a_{33}v_3 \end{pmatrix} = \begin{pmatrix} \lambda v_1 \\ \lambda v_2 \\ \lambda v_3 \end{pmatrix}$

When $\vec{v} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$, $A\vec{v} = \begin{pmatrix} a_{11} + a_{12} + a_{13} \\ a_{21} + a_{22} + a_{23} \\ a_{31} + a_{32} + a_{33} \end{pmatrix} = \begin{pmatrix} 5 \\ 5 \\ 5 \end{pmatrix} = 5 \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = 5\vec{v}$, 5 is an eigenvalue. \checkmark

b. $A^{T} = \begin{pmatrix} a_{11} & a_{21} & a_{31} \\ a_{12} & a_{22} & a_{32} \\ a_{13} & a_{23} & a_{33} \end{pmatrix}$, $A^{T} V = \begin{pmatrix} a_{11} V_{1} + a_{21} V_{2} + a_{31} V_{3} \\ a_{12} V_{1} + a_{22} V_{2} + a_{32} V_{3} \end{pmatrix} = \begin{pmatrix} \lambda V_{1} \\ \lambda V_{2} \\ \lambda V_{3} \end{pmatrix}$

when $\vec{V} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$, $A^TV = \begin{pmatrix} a_{11} + a_{21} + a_{31} \\ a_{12} + a_{22} + a_{32} \end{pmatrix} = \begin{pmatrix} 5 \\ 5 \\ 5 \end{pmatrix} = 5 \begin{pmatrix} 1 \\ 1 \end{pmatrix} = 5\vec{v}$, S is an eigenvalue of A^T , also of A^T

3.3.21 a. $A\vec{x} = \lambda \vec{x} = \lambda A\vec{x} = \lambda A\vec{x} = \lambda \lambda \vec{x} = \lambda^2 \vec{x}$ an eigenvalue of $A^2 \checkmark$