

Probability Exercise Lecture 2 I

1. $P(\text{Sat}) = 0.25$, $P(\text{Sun}) = 0.25$

$$\begin{aligned} P(\text{Sat} \cup \text{Sun}) &= P(\text{Sat}) + P(\text{Sun}) - P(\text{Sat} \cap \text{Sun}) \\ &= P(\text{Sat}) + P(\text{Sun}) - P(\text{Sat}) \times P(\text{Sun}) \\ &= \frac{1}{4} + \frac{1}{4} - \frac{1}{4} \times \frac{1}{4} = \frac{7}{16} < 0.5 \end{aligned}$$

2. (i) $\frac{5}{11} > \frac{3}{7}$, choose black

(ii) $\frac{6}{9} > \frac{9}{14}$, choose black

(iii) $\frac{11}{11+9} < \frac{12}{21}$, choose white

Simpson's paradox

$$\begin{array}{cccccc} 5 & 10 & 10 & 5 & 1 & \\ \binom{5}{1} + \binom{5}{2} + \binom{5}{3} + \binom{5}{4} + \binom{5}{5} & = & 2^5 - 1 & = & 31 & \\ \hline + \binom{5}{0} & & & & & \end{array}$$