Survival Analysis Lecture 8

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Outline

Regression models

PH regression

Coding Covariates

Partial Likelihoods

Tests

Breast cancer data

Ties

Example





The objective

- We are studying survival data
- Time to an event plus status variable
- We have discussed ways of estimating survival curves, hazards
- We have discussed the problem of testing whether two (or more) survival curves are equal (log-rank test)
- We would like to quantify the effect of covariates on survival
 - ► We would like to have an effect size, not only a P-value, when comparing two survival curves
 - We would like to study the effect of continuous covariates, like age
 - We would like to look at several covariates at the same time.



Regression in general

The basic problem

$$Z_1, Z_2, \ldots, Z_p \Rightarrow Y$$

- ▶ Interest in the relation between $Z_1, Z_2, ..., Z_p$ and Y
- $ightharpoonup Z_1, Z_2, \dots, Z_p$:
 - Predictors
 - Explanatory variables
 - "Independent" variables
 - Covariates
 - Prognostic factors
- Y:
 - Response variable
 - Dependent variable
 - Outcome variable





Regression models

Statistical relationship

- ▶ The statistical relationship between $Z_1, ..., Z_p$ and Y can be studied by means of a regression model
- ► The type of regression model depends on the type of the distribution of Y given the Z's
 - Y continuous (approximately normal): linear regression
 - ▶ Y dichotomous: logistic regression model
 - Y Poisson (count): Poisson regression model





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Regression models for survival data

- Y survival data: cannot use linear regression or logistic regression
- Special regression models for survival data
 - Accelerated failure time model
 - Poisson regression
 - Cox's proportional hazards model
 - The last one is by far the most popular

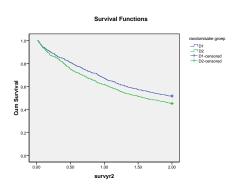




Motivation

Recall the D1/D2 study

Two survival curves







Question

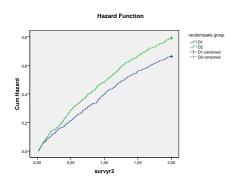
- We have already tested equality of these survival curves
- We tested equality at 2 years, which gave P=0.038
- Now we would like to quantify how much better D1 is than D2





A look at the hazards

The two cumulative hazards







Proportional hazards

- \blacktriangleright $h_1(t)$: the hazard rate of D1
- ▶ h₂(t): the hazard rate of
- ► $HR(t) = \frac{h_2(t)}{h_1(t)}$ is the ratio of these hazards, the hazard ratio
- Since both h₁(t) and h₂(t) depend on time, in principle HR(t) depends on time

Proportional hazards assumption

► HR(t) does not depend on time, but is a constant HR

$$\frac{h_2(t)}{h_1(t)} = HR$$





Other notation

Same story

- Z: covariate, treatment
 - ightharpoonup Z = 0 corresponds to D1-dissection
 - ightharpoonup Z = 1 corresponds to D2-dissection
 - ▶ D1 is called *reference category*
- h₀(t): hazard rate corresponding to reference category
 (Z = 0), also called baseline hazard
- Model:

$$h(t | Z) = h_0(t) \exp(\beta Z)$$





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What does it mean?

Proportional hazards model

$$h(t | Z) = h_0(t) \exp(\beta Z)$$

- ightharpoonup Z = 0: $h(t | Z = 0) = h_0(t) \exp(\beta \cdot 0) = h_0(t)$
- ightharpoonup Z = 1: $h(t | Z = 1) = h_0(t) \exp(\beta \cdot 1) = h_0(t) \exp(\beta)$
- ► Hazard rate of D1-dissection (Z = 0): $h_0(t)$ (previously called $h_1(t)$
- ► Hazard rate of D2-dissection (Z = 1): $h_0(t) \exp(\beta)$ (previously called $h_2(t)$





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► The ratio of these hazards, the hazard ratio is given by

$$\frac{h(t \,|\, Z=1)}{h(t \,|\, Z=0)} = \frac{h_0(t) \exp(\beta)}{h_0(t)} = \exp(\beta)$$

• $\exp(\beta)$ is the hazard ratio (does not depend on time), β is the log-hazard ratio





D1/D2 trial

Table with estimates

- Recall:
 - ightharpoonup Z = 0: D1-dissection
 - ightharpoonup Z = 1: D2-dissection

Variables in the Equation

							95,0% CI for Exp(B)	
	В	SE	Wald	df	Sig.	Exp(B)	Lower	Upper
randgr	.187	.085	4.863	1	.027	1.206	1.021	1.425





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The Cox model in general

- ▶ It has become the most used procedure for modeling the relationship of covariates to a survival or other censored outcome
- X: time to some event
- ► Z_j: vector of covariates (risk factors) for the jth individual at time t which may affect the survival distribution of X; covariates can be fixed or vary over time (ex repeated laboratory test); in the latter case the notation is Z_j(t)
- ▶ data consist of $(T_j, \delta_j, \mathbf{Z}_j(t))$





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The Cox model in general

► The Cox model specifies the hazard $h(t|\mathbf{Z})$ for individual i as

$$h(t|\mathbf{Z}) = h_0(t) \exp(\boldsymbol{\beta}^{\top} \mathbf{Z}) = h_0(t) \exp(\sum_{k=1}^{p} \beta_k Z_k)$$

- h₀: baseline hazard rate; β: parameter vector of coefficients
- It is a semi-parametric model
 - A parametric form is assumed for the covariate effect
 - ▶ The baseline hazard is non-parametric
- ▶ Event rate $h(t|\mathbf{Z})$ must be positive
 - $\exp(\boldsymbol{\beta}^{\top}\mathbf{Z})$ ensures that $h(t|\mathbf{Z})$ is positive (as long as $h_0(t)$ is)



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Proportional hazards

The hazard ratio for two subjects with fixed covariates vectors \mathbf{Z}_i and \mathbf{Z}_i

$$\frac{h(t|\mathbf{Z}_i)}{h(t|\mathbf{Z}_j)} = \frac{h_0(t) \exp(\sum_{k=1}^p \beta_k \mathbf{Z}_{ik})}{h_0(t) \exp(\sum_{k=1}^p \beta_k \mathbf{Z}_{jk})}$$

- Is constant over time
- The hazards are proportional





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Relation between covariate and hazard

$$h(t | Z) = h_0(t) \exp(\beta Z)$$

Relation between covariate and cumulative hazard

$$H(t \mid Z) = H_0(t) \exp(\beta Z)$$

Relation between covariate and survival function

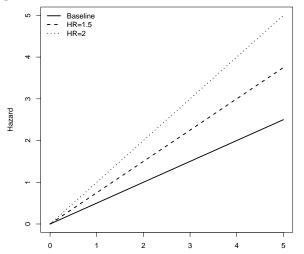
$$S(t \mid Z) = \exp(-H(t \mid Z)) = \exp(-H_0(t) \exp(\beta Z))$$
$$= S_0(t)^{\exp(\beta Z)}$$





Relation illustrated (Weibull(2,2))

Hazards

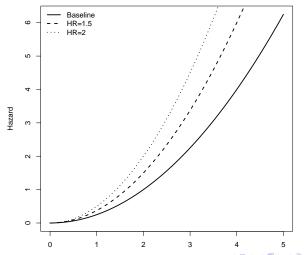




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Relation illustrated (Weibull(2,2)

Cumulative hazards

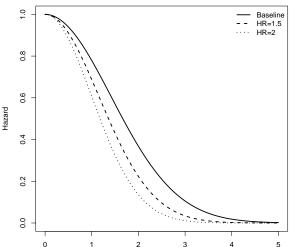




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Relation illustrated (Weibull(2,2)

Survival functions





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Coding Covariates

- Numerical (quantitative) or categorical (qualitative) covariates (explanatory variables)
- Numerical
 - Blood pressure, blood glucose levels, age or waiting time until a transplant
- Categorical
 - Gender, smoking behavior, stage of disease, presence/absence of something, treatment yes/no
- Categorical variables in regression analysis: care needs to be taken in the coding and interpretation
- Different ways of coding categorical variables





Coding Covariates

- ▶ Dichotomous (for instance gender): obvious way is to code one of the genders as 0, the other as 1
- Coding is arbitrary
- Interpretation of the results will depend on the way the coding is done





Data Section 1.5

```
> data(btrial)
> head(btrial)

time death im
1    19    1    1
2    25    1    1
3    30     1    1
4    34    1    1
5    37    1    1
6    46    1    1
```

- Cox model with immunoperoxidase status (im) as single covariate
- ► Coded as 1=negative, 2=positive

```
> table(btrial$im)
1 2
```



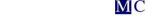


36

Define

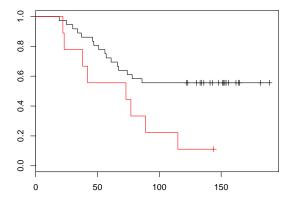
$$Z_1 = \begin{cases} 1 & \text{if immunoperoxidase positive (im+)} \\ 0 & \text{if immunoperoxidase negative (im-)} \end{cases}$$





A plot

> plot(survfit(Surv(time, death) ~ im, data=btrial), col=1:2)







Model

► The Cox model specifies

$$h(t \mid Z_1) = h_0(t) \exp(\beta Z_1)$$

• $\exp(\beta)$: hazard ratio of patient being im+ relative to the patient being im-





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Software

Function coxph from the survival package

> c1 <- coxph(Surv(time, death) ~ z1, data=btrial)

- ► Hazard ratio for an im+ patient relative to an im- patient is exp(0.98) = 2.67
- Patient who is im+ has 2.67 times higher risk of dying than ⊥ ∪ an im- patient
 MC



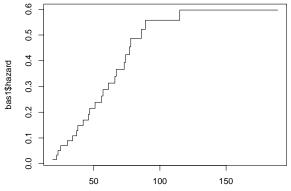
More detail with summary()

```
> summarv(c1)
Call:
coxph(formula = Surv(time, death) ~ z1, data = btrial)
 n=45, number of events= 24
   coef exp(coef) se(coef) z Pr(>|z|)
z1 0.9802 2.6650 0.4349 2.254 0.0242 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
  exp(coef) exp(-coef) lower .95 upper .95
z1 2.665 0.3752 1.136 6.25
Rsquare= 0.094 (max possible= 0.976)
Likelihood ratio test= 4.45 on 1 df, p=0.03498
Wald test = 5.08 on 1 df, p=0.0242
Score (logrank) test = 5.49 on 1 df, p=0.01908
```



The cumulative baseline hazard

- > bas1 <- basehaz(c1, centered=FALSE)
- > plot(bas1\$time, bas1\$hazard, type="s")



bas1\$time



Reversing reference category

- Let's use a different coding of immunoperoxidase status
- ► $Z_2 = 0$: im+
- ▶ $Z_2 = 1$: im-

$$h(t \mid Z_2) = \tilde{h}_0(t) \exp(\tilde{\beta} Z_2)$$

- ► $h(t | Z_2 = 0) = \tilde{h}_0(t)$
- Since $Z_2 = 0$ is the same as $Z_1 = 1$, we have $\tilde{h}_0(t) = h_0(t) \exp(\beta)$
- $h(t \mid Z_2 = 1) = \tilde{h}_0(t) \exp(\tilde{\beta})$
- Since $Z_2 = 1$ is the same as $Z_1 = 0$, we have $\tilde{h}_0(t) \exp(\tilde{\beta}) = h_0(t)$, so $\tilde{h}_0(t) = h_0(t) \exp(-\tilde{\beta})$
- $\exp(\tilde{\beta}) = \exp(-\beta) = \frac{1}{\exp(\beta)}; \tilde{\beta} = -\beta$



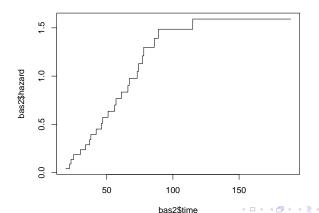


Cox with z2

```
> btrial$z2 <- ifelse(btrial$im==1,1,0)
> table(btrial$z2,btrial$im)
 1 36 0
> coxph(Surv(time, death) ~ z2, data=btrial)
Call:
coxph(formula = Surv(time, death) ~ z2, data = btrial)
   coef exp(coef) se(coef) z
z2 -0.98 0.375 0.435 -2.25 0.024
Likelihood ratio test=4.45 on 1 df, p=0.035 n= 45, number of events=
```

The cumulative baseline hazard

- > bas2 <- basehaz(c2, centered=FALSE)
- > plot(bas2\$time, bas2\$hazard, type="s")





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With factors in R

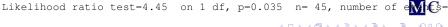
```
> btrial$im12 <- factor(btrial$im,levels=1:2,labels=c("neg","pos"))
> table(btrial$im12)
neg pos
36    9
> btrial$im21 <- factor(btrial$im,levels=2:1,labels=c("pos","neg"))
> table(btrial$im21)
pos neg
9    36
```





Cox with these factors

```
> coxph(Surv(time,death) ~ im12, data=btrial)
Call:
coxph(formula = Surv(time, death) ~ im12, data = btrial)
      coef exp(coef) se(coef) z p
im12pos 0.98 2.66 0.435 2.25 0.024
Likelihood ratio test=4.45 on 1 df, p=0.035 n= 45, number of events=
> coxph(Surv(time,death) ~ im21, data=btrial)
Call:
coxph(formula = Surv(time, death) ~ im21, data = btrial)
        coef exp(coef) se(coef) z p
```



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im21neg -0.98 0.375 0.435 -2.25 0.024

The design matrix

```
> btrial[35:38,1
   time death im im12 im21 z1 z2
35
    182
                       nea
                  nea
36
  189
                  neg
                       neg
37
   2.2
            1 2
                  pos
                       pos 1 0
  23
3.8
                  pos
                       Rog
> mm1 <- model.matrix(coxph(Surv(time, death) ~ im12, data=btrial))
> mm1[35:38,,drop=FALSE]
   im12pos
35
36
37
38
> mm2 <- model.matrix(coxph(Surv(time,death) ~ im21, data=btrial))
> mm2[35:38,,drop=FALSE]
   im21neg
35
36
```



37

More than two categories

Data Section 1.8 (used for the trend test last time)

```
> data <- larynx
> head(data)
  stage time age diagyr delta
       0.6
              77
                     76
              5.3
                    71
      1 2.4
             4.5
                 71
     1 2.5
                 78
5
      1 3.2
             58
                    74
        3.2 51
                    77
```

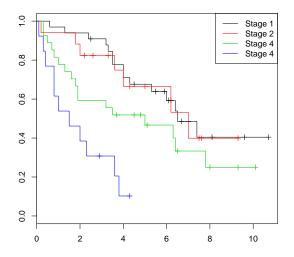
> table(data\$stage)

```
1 2 3 4
```





- > plot(survfit(Surv(time,delta) ~ stage, data=larynx), col=1:4)
- > legend("topright",c("Stage 1","Stage 2","Stage 4","Stage 4"),
- + lwd=1,col=1:4)





- Coding of the variable stage of disease
- Fit a proportional hazards regression with only stage as covariate in the model
- Stage has four levels
- Construct the dummy (or indicator) variables
- $ightharpoonup Z_1 = 1$: if the patient is in stage II, 0 otherwise
- $ightharpoonup Z_2 = 1$: if the patient is in stage III, 0 otherwise
- $ightharpoonup Z_3 = 1$: if the patient is in stage IV, 0 otherwise
- ▶ Patient with stage I cancer is the referent group $(Z_1 = Z_2 = Z_3 = 0)$
- Model

$$h(t \mid Z) = h_0(t) \exp{\{\beta_1 Z_1 + \beta_2 Z_2 + \beta_3 Z_3\}}$$





We have to declare covariate stage as categorical

```
> larynx$stage <- factor(larynx$stage)
> table(larynx$stage)
1 2 3 4
33 17 27 13
```

R-code coxph to fit the model

Likelihood ratio test=16.5 on 3 df, p=0.000902 n= 90, number c^{M} ver

Interpretation

- ► Estimated HR of death for Stage II disease with respect to Stage I disease: exp(0.0648) = 1.07
- ► Estimated HR of death for Stage III disease with respect to Stage I disease: exp(0.6148) = 1.85
- Estimated HR of death for Stage IV disease with respect to Stage I disease: exp(1.7349) = 5.67
- ► HR of death for Stage IV with respect to stage III exp(1.7349 – 0.6148) = 3.065





Continuous covariates

- ▶ Code the variable as a single covariate: Z = age (in years)
- ► Hazard ratio of an event for an individual of age x years compared to an individual of age x - 1 years
- ► Hazard ratio of the event for an individual 10 years older than another individual: $\exp(10 \cdot \beta)$
- Model for larynx data with risk factors stage of the disease and age

$$h(t | \mathbf{Z}) = h_0(t) \exp(\beta_1 Z_1 + \beta_2 Z_2 + \beta_3 Z_3 + \beta_4 Z_4)$$





► The model fitted with coxph

 stage3
 0.6424
 1.90
 0.3561
 1.804
 7.1e-02

 stage4
 1.7060
 5.51
 0.4219
 4.043
 5.3e-05

 age
 0.0190
 1.02
 0.0143
 1.335
 1.8e-01

> res <- coxph(Surv(time, delta) ~ stage + age, data = larynx)

Likelihood ratio test=18.3 on 4 df, p=0.00107 n= 90, number of event





Interpretation

- ▶ the relative risk for a 50-year-old patient compared to a 40-year-old (with the same disease stage) is $\exp(10 \cdot \beta_4) = \exp(10 \cdot 0.0190) = 1.21$
- Or: a 50-year-old patient has a 1.21 times greater risk of dying than a 40-year-old patient with the same disease stage





The design matrix

```
> larynx[c(1,34,51,78),]
   stage time age diagyr delta
         0.6
               77
                      76
34
       2 0.2 86
                   74
      3 0.3
51
             49
                   72
       4 0.1
78
             6.5
                      72.
> model.matrix(res)[c(1,34,51,78),]
   stage2 stage3 stage4 age
                         77
34
                        86
51
                        49
78
                         6.5
```





Interactions

- When there are interactions, the coding of the covariates becomes even more important
- Computer exercise this afternoon





Partial Likelihoods for Distinct-Event Time Data

- $t_1 < t_2 < \ldots < t_D$: ordered event times
- Z_{(i)k}: k-th covariate associated with the individual whose failure time is t_i
- ► R(t_i): risk set at time t_i, (set of all individuals who are still under study at a time just prior to t_i
- Partial likelihood based on the hazard function is given by

$$L(\beta) = \prod_{i=1}^{D} \frac{\exp(\sum_{k=1}^{p} \beta_k Z_{(i)k})}{\sum_{i \in R(t_i)} \exp(\sum_{k=1}^{p} \beta_k Z_{jk})}$$

▶ (Make computations how to derive $L(\beta)$ on the blackboard)



Log partial likelihood

$$LL(\beta) = \log \left(\prod_{i=1}^{D} \frac{\exp(\sum_{k=1}^{p} \beta_k Z_{(i)k})}{\sum_{j \in R(t_i)} \exp(\sum_{k=1}^{p} \beta_k Z_{jk})} \right)$$

We can also write it as

$$LL(\beta) = \sum_{i=1}^{D} \sum_{k=1}^{p} \beta_k Z_{(i)k} - \sum_{i=1}^{D} \log \left[\sum_{j \in R(t_i)} \exp \left(\sum_{k=1}^{p} \beta_k Z_{jk} \right) \right]$$

- Estimate the parameters β by maximizing the partial likelihood or the log-likelihood
- ▶ Score equations: $U_h(\beta) = \partial LL(\beta)/\partial \beta_h$, h = 1, ..., p
- ▶ Information matrix $\mathcal{I}(\beta) = [\mathcal{I}_{gh}(\beta)]_{p \times p}$
- ▶ Show how to derive $U_h(\beta)$ and $\mathcal{I}(\beta)$



12....

- ► The (partial) maximum likelihood estimates $\hat{\beta}_1, \dots \hat{\beta}_p$ are found by solving the set of p nonlinear equations $U_h(\beta) = 0$
- ► The log-likelihood does **not** depend on the baseline hazard rate $h_0(t)$, inference may be made on the effects of the explanatory variables without knowing $h_0(t)$





Tests for the regression parameters

- $\hat{\beta} = (\hat{\beta}_1, \dots \hat{\beta}_p)$: partial MLE of β ;
- $\triangleright \mathcal{I}(\beta)$: $p \times p$ information matrix evaluated at β
- ▶ test of the global hypothesis: $H_0: \beta = \beta_0$

Wald's test

▶ Based on the asymptotic normality of the (partial) maximum likelihood estimates: $\hat{\beta} \sim N(\beta, \mathcal{I}^{-1}(\hat{\beta}))$

$$X_W^2 = (\hat{\boldsymbol{\beta}} - \boldsymbol{\beta}_0)^{\top} \mathcal{I}(\hat{\boldsymbol{\beta}}) (\hat{\boldsymbol{\beta}} - \boldsymbol{\beta}_0) \sim \chi_D^2$$





Tests for the regression parameters

Likelihood ratio test (LRT) test

$$X_{LR}^2 = 2[LL(\hat{\boldsymbol{\beta}}) - LL(\boldsymbol{\beta}_0)] \sim \chi_p^2$$

Score test

▶ Based on the efficient scores (first derivative of the log partial likelihood) $\mathbf{U}(\beta) = (U_1(\beta), \dots, U_p(\beta))^{\top}$

$$X_{SC}^2 = \mathbf{U}(\boldsymbol{\beta}_0)^{\top} \mathcal{I}^{-1}(\boldsymbol{\beta}_0) \mathbf{U}(\boldsymbol{\beta}_0) \sim \chi_D^2$$





Breast cancer data Section 1.5 (recall)

```
> data(btrial)
> head(btrial)
  time death im
  19 1 1
 25
 30 1 1
 34 1 1
5 37
6 46
> res <- coxph(Surv(time, death)~im, data=btrial)
> res
Call:
coxph(formula = Surv(time, death) ~ im, data = btrial)
  coef exp(coef) se(coef) z
im 0.98 2.66 0.435 2.25 0.024
Likelihood ratio test=4.45 on 1 df, p=0.035 n= 45
```





Software

Wald's test and score test can be found with summary

```
> summary(res)
Call:
coxph(formula = Surv(time, death) ~ im, data = btrial)
 n= 45, number of events= 24
    coef exp(coef) se(coef) z Pr(>|z|)
im 0.9802 2.6650 0.4349 2.254 0.0242 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
  exp(coef) exp(-coef) lower .95 upper .95
      2.665 0.3752 1.136
                               6.25
im
Rsquare= 0.094 (max possible= 0.976)
Likelihood ratio test= 4.45 on 1 df, p=0.03498
Wald test = 5.08 on 1 df, p=0.0242
Score (logrank) test = 5.49 on 1 df, p=0.01908
```



Software

► Test the hypothesis H_0 : $\beta = 0$ by using the three tests seen

Check the computations by using the anova function





Software

- ▶ From anova we obtain $LL(\hat{\beta})$ and $LL(\beta_0)$
- ► LRT:

$$X_{LR}^2 = 2[LL(\hat{\beta}) - LL(\beta_0)] = 2(-81.521 - (-83.744)) = 4.446$$

```
> 1-pchisq(4.446,1)
[1] 0.0349831
```





Partial likelihoods when ties are present

- ► The partial likelihood for the Cox model is developed under the assumption of continuous data
- Real data sets often contain tied event times
- $ightharpoonup t_1, \ldots, t_D$: *D* distinct, ordered, event times
- d_i: number of deaths at t_i;
- D_i: set of all individuals who die at time t_i
- ▶ $\mathbf{s}_i = \sum_{j \in D_i} \mathbf{Z}_j$ (sum of the vectors \mathbf{Z}_j over all individuals who die at t_i)
- R_i: set of all individuals at risk just prior to t_i
- Three different algorithms are commonly used to address this problem



Partial Likelihoods When Ties Are Present

Breslow approximation

- Simplest to write down, easiest to program
 - Default method in most packages (but not in survival package!!)
 - Solution is the least accurate but the method is fast (see (8.4.1) in your book)

Efron approximation

- Quite accurate unless the proportion of ties relative to the size of the risk set is extremely large;
- As fast as the Breslow'method; default option in survival package (see (8.4.2))





Exact partial likelihood

- Exact method involves exhaustive enumeration of all possible risk sets at each tied death time
 - Can require a prohibitive amount of computation time
 - It computes the exact partial likelihood (method="exact" in coxph)
- Use data Section 1.4 to compare estimates obtained with different approximation

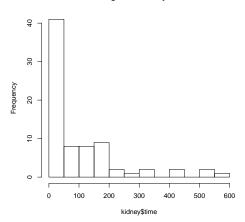
```
> data(kidney)
> names(kidney)
[1] "time" "delta" "type"
> table(kidney$type)

1  2
43  76
> hist(kidney$time)
```





Histogram of kidney\$time







> coxph(formula = Surv(time, delta) ~ type, data = kidney,

Likelihood ratio test=2.45 on 1 df, p=0.118 n= 119

Example

Call:

method = "efron")

```
coxph(formula = Surv(time, delta) ~ type, data = kidney,
method = "efron")
      coef exp(coef) se(coef) z p
type -0.613 0.542 0.398 -1.54 0.12
Likelihood ratio test=2.41 on 1 df, p=0.121 n= 119
> coxph(formula = Surv(time, delta) ~ type, data = kidney,
method = "breslow")
Call:
coxph(formula = Surv(time, delta) ~ type, data = kidney, method = "bre
      coef exp(coef) se(coef) z p
type -0.618 0.539 0.398 -1.55 0.12
```

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Example

```
> coxph(formula = Surv(time, delta) ~ type, data = kidney,
method = "exact")
```

Could not estimate the model, the software is stuck!!!



