## Exercises for Lecture 7

#### Statistical Computing with R, 2023-24

### Exercise 1

- 1. Create an RStudio project and link it to the folder where you have saved all your files from Lecture 7
- 2. Create an R Markdown document where you will write your solutions to this assignment. Save the document in the project folder. Make sure to use section (#) and subsection (##) headers to clearly structure your solutions
- 3. Compile the RMarkdown document by "knitting it" to a pdf output. If you have issues compiling to pdf, ask for help from the TAs. They might be able to help you solving the problem. If the problem persists, compile your solutions as html file

#### Exercise 2

Write a function that takes a dataframe as input and does the following:

- Check if the dataframe contains any numeric, character or factor variables. If not, return the message "This dataframe contains no numeric, character or factor values".
- If the dataframe contains at least one numeric, character or factor variable, then:
  - for each numeric variable, create a **histogram** that displays its distribution. Make sure that the axes' labels and chart title are informative and meaningful.
  - for each categorical or factor variable, create a barplot that displays its frequency distribution. Make sure that the axes' labels and chart title are informative and meaningful.

Apply the function you created to the gala and to the amlxray datasets available in the faraway package. Does the function yield the desired outputs?

## Exercise 3

The state.x77 matrix from the MASS package contains (outdated) information on the 50 US states. To get it, load the MASS library:

```
library(MASS)
?state # check the help page out!
```

## starting httpd help server ... done

#### head(state.x77)

##		${\tt Population}$	Income	Illiteracy	Life Exp	Murder	HS Grad	Frost	Area
##	Alabama	3615	3624	2.1	69.05	15.1	41.3	20	50708
##	Alaska	365	6315	1.5	69.31	11.3	66.7	152	566432
##	Arizona	2212	4530	1.8	70.55	7.8	58.1	15	113417
##	Arkansas	2110	3378	1.9	70.66	10.1	39.9	65	51945
##	${\tt California}$	21198	5114	1.1	71.71	10.3	62.6	20	156361
##	Colorado	2541	4884	0.7	72.06	6.8	63.9	166	103766

- 1. Compute the mean, median, standard deviation and skewness of each of the numeric variables in the data frame. Store the results in a data frame where each row corresponds to a variable, and each column to a summary statistics
- 2. Draw a histogram or a density plot for each variable. Make sure the name of each variable is included in the title of the chart
- 3. Compare the plots to the summary variables: which variables appear to be symmetric? Which ones are positively skewed, and which ones negatively skewed?
- 4. Make a scatter plot of Illiteracy versus Life Exp. Do you notice any trend?
- 5. Use the function cor.test() to evaluate the correlation between Illiteracy and Life Exp. Can you think of a plausible explanation for this correlation?

#### Exercise 4

Execute the following code:

```
c1 = c(0, 1)
c2 = expand.grid(c1, c1)
c2s = rowSums(c2)
```

- 1. Create a chart to visualize the frequency distribution of c2s. Inspect c2, c2s, and the chart. What are the dimensions of c2? What do you think expand.grid() and rowSums() do? (Check out the documentation of the two functions to double-check your answer)
- 2. Create the equivalent of c2 and c2s, but repeating c1 5 times. Call the outcomes c5 en c5s respectively. Create a chart to visualize the frequency distribution of c5s Can you notice something happening to the distribution of c5s? What are the dimensions of c5?
- 3. Now use expand.grid(replicate(15, c, simplify = F)) to create c15, and use c15 to create c15s. Again, visualize the frequency distribution of c15s. Can you predict and/or calculate the dimensions of c15?
- 4. Calculate and save the range, mean, and standard deviation of c15s. Are these numbers surprising? If so, how could you verify if these numbers are correct? (Hint: think about what you've learnt in the Probability course!)
- 5. Use the rnorm() function to draw  $n = 10^3$  random numbers from a normal distribution with mean mean(c15s) and standard deviation sd(c15s). Create a histogram of your

- draws (set the parameter breaks = 16). What are your conclusions?
- 6. Compare the histogram of c15s to the density of a normal distribution with mean  $\mu = \text{mean(c15s)} 0.5$  and standard deviation  $\sigma = \text{sd(c15s)}$ ; combine the histogram and the density curve in the same chart. What are your conclusions? (Hints: 1. for the histogram, use prob = T; 2. to add the normal curve, use dnorm(x, mean, sd) and add = T)

## Exercise 5

How many elements in the Fibonacci sequence do you need to sum, before the sum of such elements reaches 22000?

# Exercise 6 (extra exercise)

Note: this exercise is not material for the exam; it goes beyond the scope of the material you covered so far. It is a fun one, so if you want to, give it a go!

## Part 1: manipulating images in R

Download the file academiegebouw.jpg from https://github.com/mirkosignorelli/Teaching/tree/main/SCwR\_course:



This image contains 666 x 1000 pixels. In this exercise, we will manipulate this image in R. An image has 3 channels Red, Green and Blue (RGB). Those values range from 0 to 255. Install the jpeg package and see ?readJPEG.

#### install.packages("jpeg")

- 1. Import the image in R, and assign it to an object called my\_image. What type of object is it? (Tip: use is(my\_image) to verify that). Do the dimensions of my\_image make sense?
- 2. Black and white images are 2 dimensional arrays, typically obtained by computing the average of the 3 color channels. Convert the image to black and white, and export it as .jpg file using the writeJPEG() function.
- 3. Create a function to convert the 3D array to a data.frame with 5 variables: column, row, red, blue and green. The resulting data frame should have 666 x 1000 = 666000 rows (to wit, one row for each pixel). You may find useful the function expand.grid(). See ?expand.grid. Notice that a the 3D array is a 2D array in 3 different channels. In R you can get all the values from one of the channels with my\_image[ , , channel\_number]. The latter is a 2D array.
- 4. Check how many different colors exist in the your data.frame. Remember that a color is the combination of red, green and blue.

### Part 2: compressing an image using the k-means method

NB: the remainder of this exercise is a bit more advanced than usual, so don't worry if you have troubles understanding it or implementing it!

K-means is a simple clustering algorithm that can be shortly summarized as follows:

- 1. Choose randomly k starting points as centroids.
- 2. While not converged (no movement in the centroids):
  - 1. Assign each point to the nearest centroid.
  - 2. Update the centroid with the mean of all the points under that cluster.

In the context of image compression, the idea is that the k-means algorithm can be used to summarize the original image using less memory (the stronger the compression and memory saving, the smaller the number of unique colors). To apply the k-means algorithm, you can use the function kmeans() (see ?kmeans()).

- 5. Apply kmeans() function to the red, green and blue colors of our data.frame. Use 40 centroids. Store the clustered values, and check the value of the centroids. Those are your new colors!
- 6. Use the new centroids as the value for your colors in each pixel. The pertenence of each row in the data.frame to each cluster is given by the function. Substitute the values of each row for the values of its cluster. Notice that kmeans() returns the value of each center and a vector with cluster label of each row.

7.	Convert the new data.frame to a 3D array, save it to a happens if you reduce the number of centroids?	.jpg file and visualize it. Wha	ıt