## **Alexander Hiller**

# Non-Homogeneous Differential Equations Practice

**Undetermined Coefficients** Problems, Ch3 of 'Differential Equations...' by Boyce (10 Ed.)
Section 3.5

### Problem 2:

$$\begin{split} & \textit{In[e]} := \text{DSolve}[\{y''[t] + 2\,y'[t] + 5\,y[t] == 3\,\text{Sin}[2\,t]\}\,,\,\,y[t]\,,\,\,t] \\ & \textit{Out[e]} = \Big\{ \Big\{ y[t] \rightarrow e^{-t}\,C[2]\,\,\text{Cos}[2\,t] + e^{-t}\,C[1]\,\,\text{Sin}[2\,t] - \frac{3}{68}\,\,\Big(17\,\,\text{Cos}[2\,t] - \text{Cos}[2\,t]\,\,\text{Cos}[4\,t] + 4\,\,\text{Cos}[4\,t]\,\,\text{Sin}[2\,t] - 4\,\,\text{Cos}[2\,t]\,\,\text{Sin}[4\,t] - \text{Sin}[2\,t]\,\,\text{Sin}[4\,t] \Big) \Big\} \Big\} \end{split}$$

Taking only that which is from the particular solution:

### Problem 5:

$$In[*]:= DSolve[{y''[t] - 2y'[t] - 3y[t] == -3t*Exp[-t]}, y[t], t]$$

$$\{\{y[t] \rightarrow \frac{3}{64} e^{-t} (1 + 4t + 8t^2) + e^{-t} C[1] + e^{3t} C[2]\}\}$$

#### Problem 10:

Taking only that which is from the particular solution:

$$\begin{aligned} & \text{Simplify} \Big[ \frac{1}{18} \left( -9 \, \text{t} \, \text{Cos}[\text{t}]^2 + 3 \, \text{t} \, \text{Cos}[\text{t}] \, \text{Cos}[3 \, \text{t}] - 36 \, \text{Cos}[\text{t}] \, \text{Sin}[\text{t}] - 8 \, \text{Cos}[3 \, \text{t}] \, \text{Sin}[\text{t}] + 9 \, \text{t} \, \text{Sin}[\text{t}]^2 + 8 \, \text{Cos}[\text{t}] \, \text{Sin}[3 \, \text{t}] + 3 \, \text{t} \, \text{Sin}[\text{t}] \, \text{Sin}[3 \, \text{t}] \Big) \Big] \Big] \\ & \textit{Out}[*]_{=} \, - \frac{1}{3} \, \text{t} \, \text{Cos}[2 \, \text{t}] - \frac{5}{9} \, \text{Sin}[2 \, \text{t}] \end{aligned}$$

### Variation of Parameters Problems, Ch3 of 'Differential Equations...' by Boyce (10 Ed.) Section 3.6

### Problem 1:

$$\begin{aligned} & & \text{In[*]:= DSolve} \Big[ \Big\{ y \, ' \, ' \, [t] \, - \, 5 \, y \, ' \, [t] \, + \, 6 \, y \, [t] \, = \, 2 \, E^t \Big\} \,, \, \, y \, [t] \,, \, \, t \Big] \\ & & \text{Out[*]:= } \Big\{ \Big\{ y \, [\, t\, ] \, \rightarrow \, \mathbb{e}^t \, + \, \mathbb{e}^{2 \, t} \, C \, [\, 1\, ] \, + \, \mathbb{e}^{3 \, t} \, C \, [\, 2\, ] \, \Big\} \Big\} \end{aligned}$$

#### Problem 2:

$$\begin{aligned} & & \text{In[*]:= DSolve} \Big[ \Big\{ y \, ' \, ' \, [t] \, - y \, ' \, [t] \, - 2 \, y [t] \, = 2 \, E^{-t} \Big\}, \ y [t], \ t \Big] \\ & & \text{Out[*]= } \Big\{ \Big\{ y \, [t] \, \to \, -\frac{2}{9} \, e^{-t} \, \Big( 1 + 3 \, t \Big) \, + e^{-t} \, C \, [1] \, + e^{2 \, t} \, C \, [2] \, \Big\} \Big\} \end{aligned}$$

### Problem 3:

$$\begin{aligned} & & \text{In[$\circ$]$:= } \mathsf{DSolve}\Big[\Big\{y''[t] + 2\,y'[t] + y[t] == 3\,E^{-t}\Big\}, \ y[t], \ t\Big] \\ & & \text{Out[$\circ$]$:= } \Big\{\Big\{y[t] \to \frac{3}{2}\,\,\mathbb{e}^{-t}\,t^2 + \mathbb{e}^{-t}\,C[1] + \mathbb{e}^{-t}\,t\,C[2]\,\Big\}\Big\} \end{aligned}$$

### Problem 4:

$$\label{eq:local_$$