Power Circuit Theory - Lab Report 3 $\,$

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Y-Neutral/Y-Neutral Transformer

DC Resistance of the Windings

1++1

Explain the reasons for your position of the ammeter and the voltmeter.

The voltmeter comes after the resistor bank so that we both limit the current to safe levels as well as measure the primary voltage.

The ammeter is placed before the branching of the conductor into each phase of the transformer. This gives us $3I_0$ or 3 times the current in each phase of the transformer. Measuring when the current is larger allows the error of the instrument to be reduced in comparison to one phase was being measured.

$$V_1 = 0.6 \tag{1}$$

$$I_1 = V_2 = 0.28 (2)$$

$$I_2 = 1.016 (3)$$

$$R_1 = 0.48$$
 (4)

$$R_2 = 0.27$$
 (5)

Measured Voltage and Current on the Primary Side of the Transformer

Primary Voltage:

$$|V^{'}| = 4.53V$$
 (6)

$$|I^{'}| = 5.7A \tag{7}$$

Calculate the Transformer's Parameters

$$Z_b = \frac{(V_{base})^2}{S_{base}} = \frac{(\sqrt{3} \times 240)^2}{4500} = 38.400\Omega$$
 (8)

$$R_0 = \frac{4.53}{5.70} \frac{1}{38.4} = 0.02070 \ (p.u.) \tag{9}$$

$$|Z_0| = \frac{|V_0|}{|I_0|} = \frac{|V'|}{\left|\frac{I'}{3}\right|} = \frac{2.3842}{Z_b} = 0.0621 \ (p.u.)$$
(10)

$$X_0 = \sqrt{|Z_0|^2 - R_0^2} = 0.05855 \ (p.u.) \tag{11}$$

Measure the secondary neutral current with the Fluke clamp meter

$$|I^{"}| = 10.02 \ A \ (rms)$$
 (12)

Measure the voltage between the neutral points with DMM

$$|V_{Nn}| = 3.9V \tag{13}$$

This measurement was oscillating a lot.

Draw the zero sequence equivalent circuit of the transformer



Explain:

The impedance of the transformer directly impedes the current on the secondary side.

Y-Neutral to Y Transformer

If |I'| = 5.4 A, then

Predict $|I_s|$

$$|I_s| = \frac{N_p}{N_s} |I_p| = \frac{2}{1} (5.4) = 10.8 \text{ A}$$
 (14)

Explain:

Current through an ideal transformer is related through the turns ratio as seen in the equation above.

If $|I^{'}| = 5.4A$, expectations are that:

 $V^{'}$ to be: Larger

 Z_0 to be: Magnetising/Leakage ++;

The current in each primary winding to be: The same.

Give explanations using Faraday's Law, Ampere's Law and the magnetic equivalent circuit.

1++1

Measure voltage, current and power one the primary side of the transformer

Primary Voltage:

$$|V^{'}| = 16.95 \text{ V (rms)}$$
 (15)

Primary Current:

$$|I'| = \frac{5.53}{3} = 1.843 \text{ A (rms)}$$
 (16)

Primary Power:

$$P' = 21 \text{ W}$$
 (17)

Secondary Winding Current:

$$|I_s| = 0.4 \text{ A (rms)}$$
 (18)

Calculate the transformer's parameters (referred to the primary)

$$\frac{1}{3}R_0 = \frac{P'}{|I'|^2} = 6.186 \ \Omega \ \Rightarrow 0.161 \ (\text{p.u.})$$
 (19)

$$R_0 = 0.161 \times 3 = 0.483 \text{ (p.u.)}$$
 (20)

Comparing R_0 with that measured in part 1: Much higher.

$$|Z_0| = \frac{|V_0|}{|I_0|} = \frac{|V'|}{\left|\frac{I'}{3}\right|} = 27.591 \Rightarrow 0.71851 \text{ (p.u.)}$$
 (21)

$$X_0 = \sqrt{|Z_0|^2 - R_0^2} = 0.53195 \text{ (p.u.)}$$
 (22)

Draw the zero sequence equivalent circuit of the transformer



Explain

1++;

Clamp meter measurements of each primary winding

$$|I_A^{'}| = 1.70 \text{ A}$$
 (23)

$$|I_{B}^{'}| = 1.74 \text{ A}$$
 (24)

$$|I_C^{'}| = 1.59 \text{ A}$$
 (25)

The measurements are slightly unequal, this could be because of any of the following:

- Imbalance of heat amongst the inductors in each phase.
- Differences in absolute impedance, independent of temperature.
- Faulty measurement equipment.
- Tolerances in the measurement equipment.
- Experimental error.

With secondary terminals open-circuited and |I'| = 5.4 A

Primary voltage measured was:

$$|V^{'}| = 16.94 \text{ V (rms)}$$
 (26)

Calculated zero sequence impedance is:

$$|Z_0| = \frac{16.94}{5.4} \frac{1}{Z_b} = 0.081694 \text{ (p.u.)}$$
 (27)

Draw the zero sequence equivalent circuit of the transformer



Explain

Comparing the calculated transformer's parameters with the zero sequence impedance $\,$

;++;

Y-Neutral to Delta Transformer

Measured Voltage, Current and Resistance on Primary Side

$$|V'| = 3.036 \text{ V}$$
 (28)

$$|I'| = 1.8 \text{ A}$$
 (29)

Per-phase DC resistance:

$$R_0 = \frac{1.687}{38.4} = 0.04392(p.u.) \tag{30}$$

DMM measurement of the phase voltages to primary neutral on the secondary side

$$|V_a^{"}| = 0.1 \text{ V}$$
 (31)

$$|V_b^{"}| = 0.1 \text{ V}$$
 (32)

$$|V_c^{"}| = 0.1 \text{ V}$$
 (33)

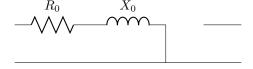
Measured secondary current

$$|I_d| = 3.34 \text{ A (rms)}$$
 (34)

Transformer's calculated parameters (referred to the primary)

$$Z_0 = R_0 + jX_0 = 0.04392 + j0.124 (p.u.)$$
(35)

Zero-sequence equivalent of the transformer



Explain:

The impedance can only be seen from the primary side.

If a secondary line terminal was shorted to the "earth" (primary neutral), what would be the resulting current?

Negative of the primary current.

Is Z_0 a leakage or magnetising impedance?

Magnetising.

Is the delta secondary a short-circuit to zero sequence currents?

j++j

Comparison of the \mathbb{Z}_0 for the three configurations

Configuration One ;++;

Configuration Two ;++;

Configuration Three ;++;

Positive & Negative Sequence Impedance

Primary Voltage:

$$|V_{sc}| = 7.89 \text{ V (rms)}$$
 (36)

Primary Current:

$$|I_{sc}|5.4 \text{ A (rms)}$$
 (37)

Primary Power:

$$P_{sc} = 31 \text{ W} \tag{38}$$

Transformer's Calculated Parameters

$$R_1 = \frac{P_{sc}}{|I_{sc}|^2} = \tag{39}$$

Comparing this with that found in Part 1: i++i.

$$|Z_1| = |Z_2| = \frac{|V_{sc}|}{|I_{sc}|} = <++>$$
 (40)

$$X_1 = \sqrt{|Z_1|^2 - R_1^2} = \tag{41}$$

Comparing R1 and R0

j++j

Explain

j++;

Positive & negative sequence test circuit for magnetising Z

Why such a circuit is used:

1++;

Determining R_{1m} X_{1m} and Z_{1m}

j++;

Determining Z_{0m}

j++;

Equivalent Circuits

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Relevant Equations

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Experimental setup and equipment



