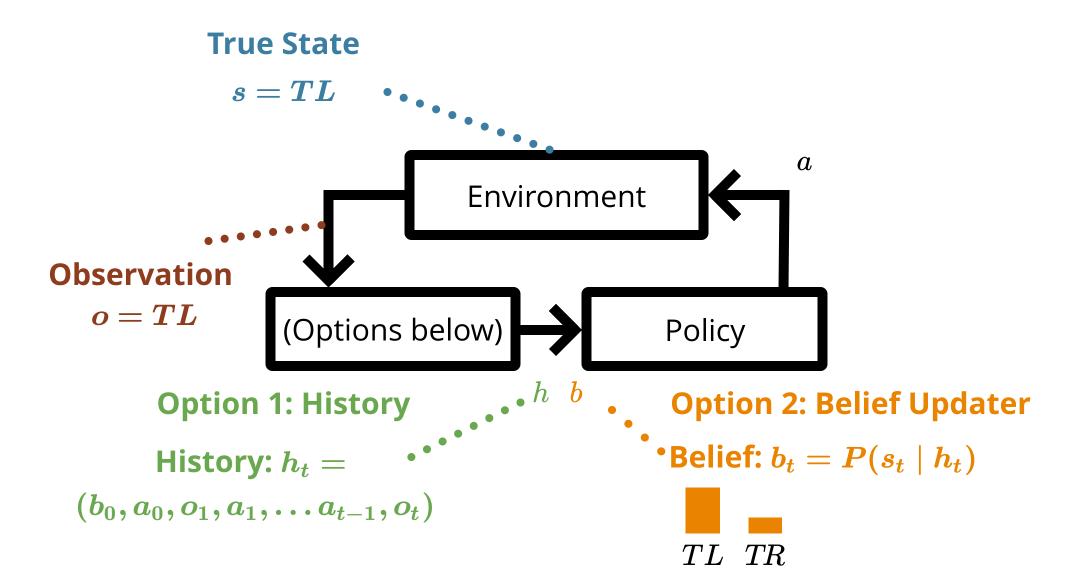
Particle Filters

POMDP Sense-Plan-Act Loop



```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
end
if sum(b') ≈ O.O
        fill!(b', 1)
end
return normalize!(b', 1)
end
```

$$b_t(s) = P(s_t = s \mid h_t)$$

```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
end
if sum(b') ≈ O.O
        fill!(b', 1)
end
return normalize!(b', 1)
end
```

$$b_t(s) = P(s_t = s \mid h_t)$$
 $b' = au(b, a, o)$

```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
    end
    if sum(b') ≈ O.O
        fill!(b', 1)
    end
    return normalize!(b', 1)
end
```

$$b_t(s) = P(s_t = s \mid h_t)$$
 $b' = au(b, a, o)$

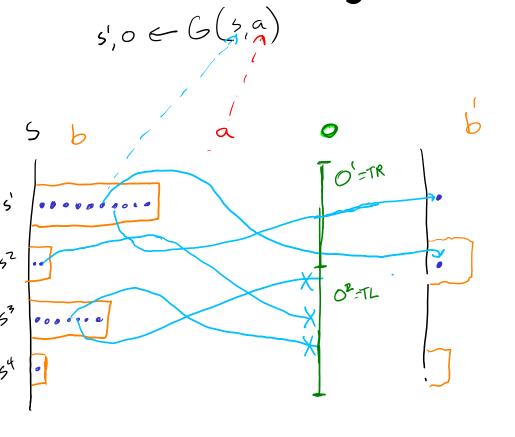
$$b'(s') \propto Z(o \mid a, s') \sum_s T(s' \mid s, a) \, b(s)$$
 —

```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
end
if sum(b') ≈ 0.0
    fill!(b', 1)
end
return normalize!(b', 1)
end
```

Rejection Particle Filter

Rejection Particle Filter

state



```
b a=L o=TR update (filter, ponde, a, o)
```

```
function update (b::RejectionParticleFilter, 4, a, o)
     \overline{T}, 0 = \mathcal{P}.T, \overline{\mathcal{P}}.0
     states = similar(b.states)
     while i ≤ length(states)
          s = rand(b.states)

s' = rand(T(s,a))

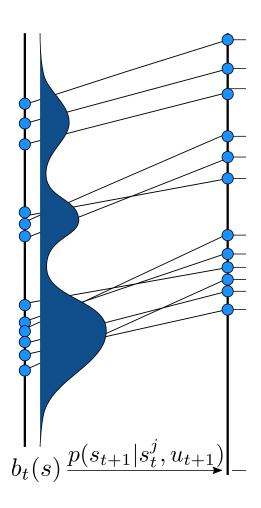
if rand(O(a,s')) == 0
               states[i] = s
               i += 1
          end
     end

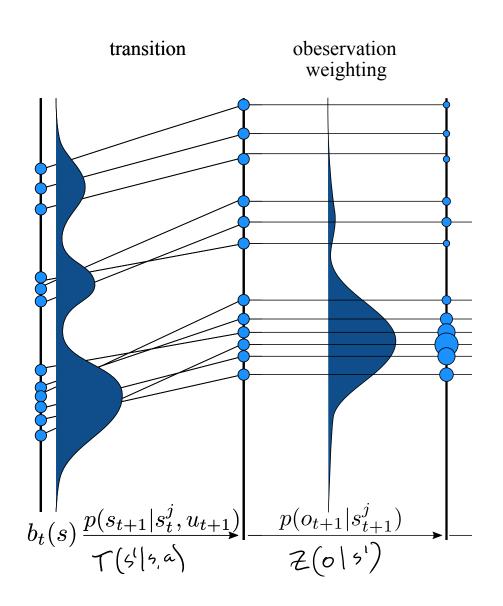
→ return RejectionParticleFilter(states)

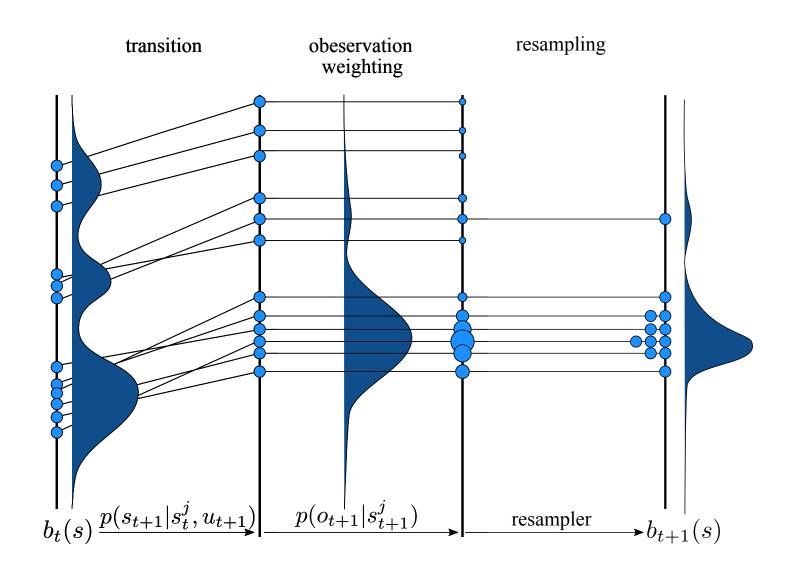
end
```



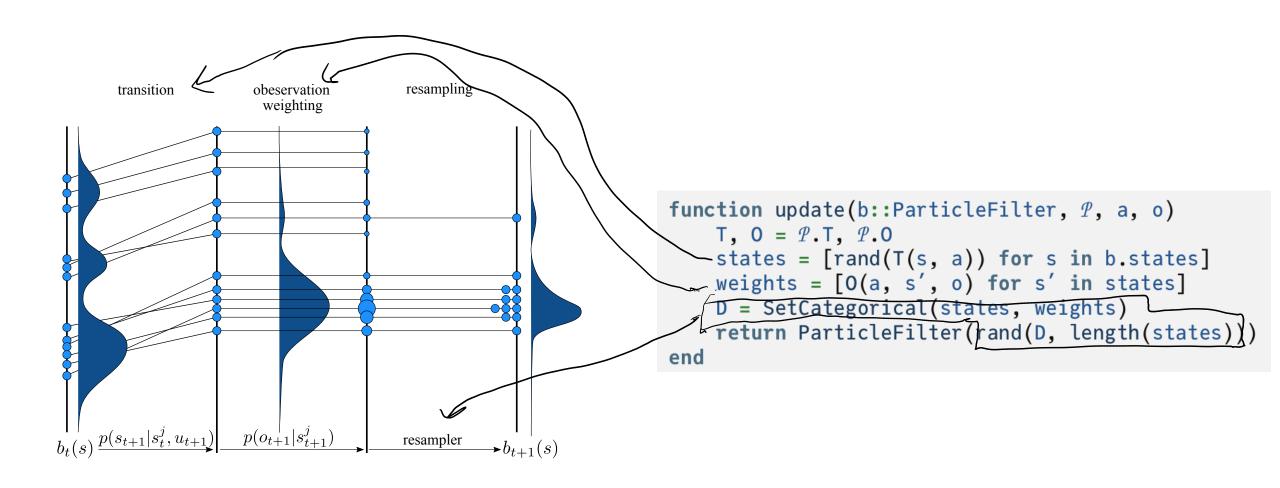
 $5' \leftarrow 6(5,a)$ transition

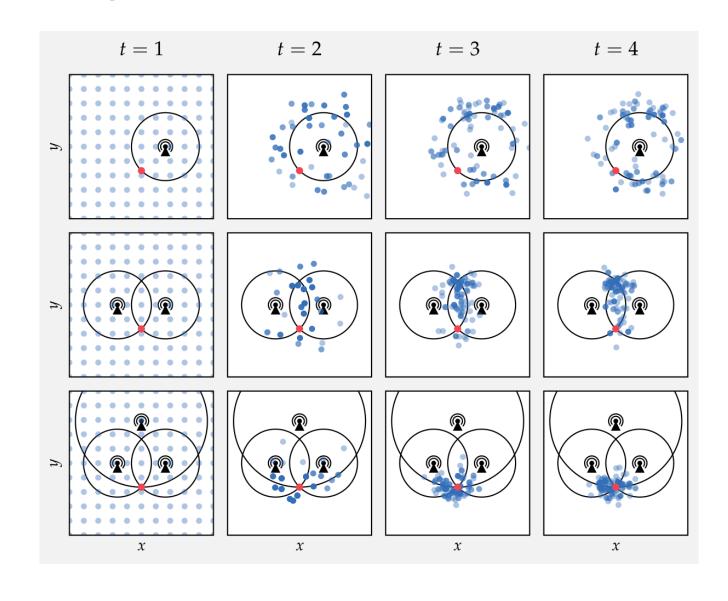


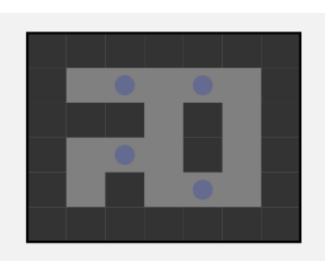


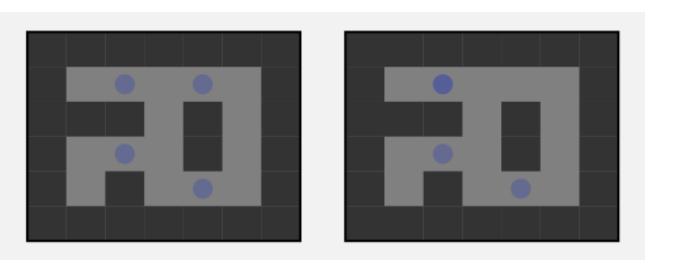


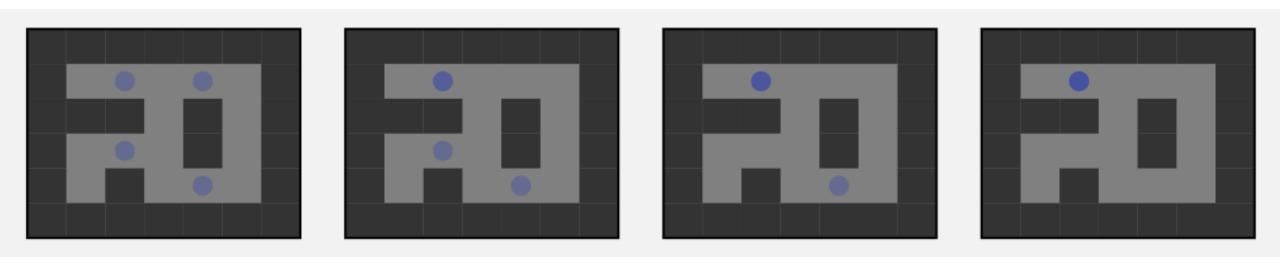
```
function update(b::ParticleFilter, P, a, o)
    T, 0 = P.T, P.O
    states = [rand(T(s, a)) for s in b.states]
    weights = [0(a, s', o) for s' in states]
    D = SetCategorical(states, weights)
    return ParticleFilter(rand(D, length(states)))
end
```

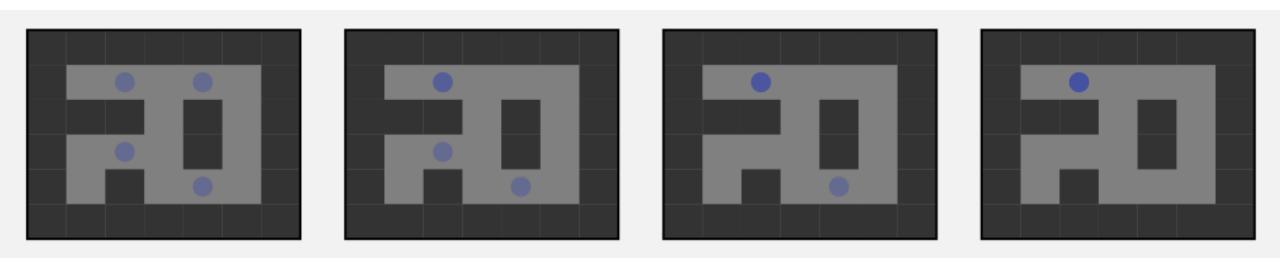




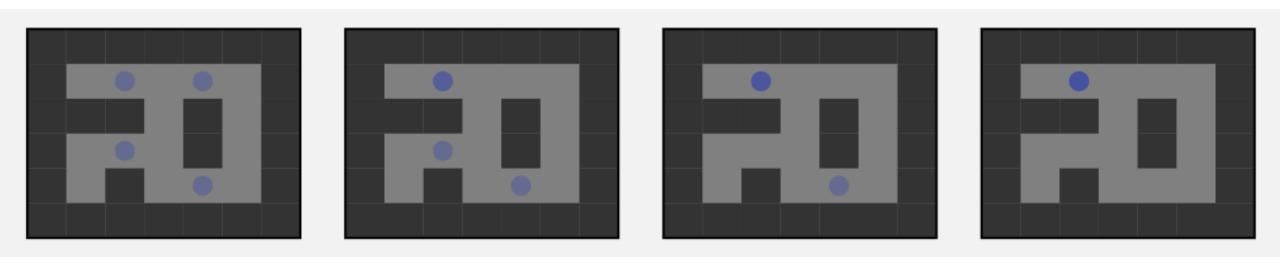






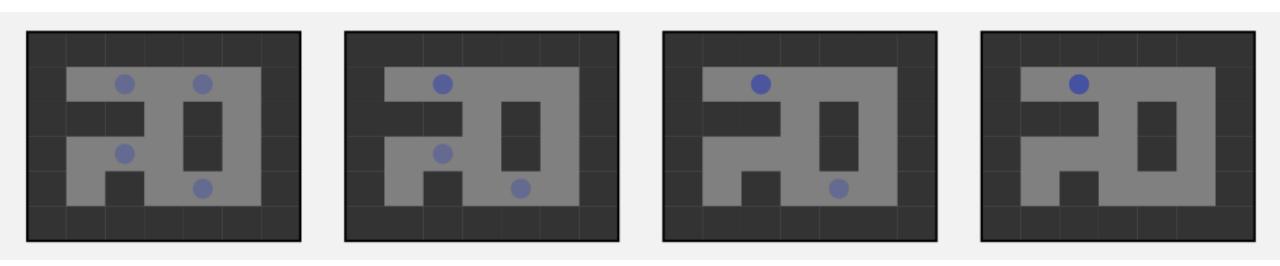


Solution: Domain specific particle injection based on:



Solution: Domain specific particle injection based on:

Weights



Solution: Domain specific particle injection based on:

- Weights
- Particle Diversity

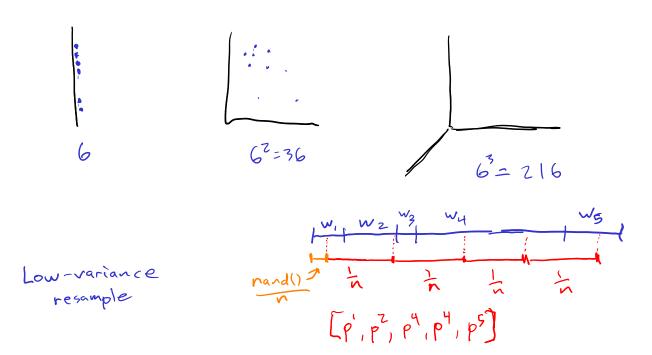
Important Particle Filter Properties

Important Particle Filter Properties

• When only estimating the reward, the number of particles does **NOT** need to scale exponentially with the dimension (i.e. $n \neq k^d$)

Important Particle Filter Properties

- When only estimating the reward, the number of particles does **NOT** need to scale exponentially with the dimension (i.e. $n \neq k^d$)
- Implementation should have O(n) complexity. $\bigcirc (n^2)$ $\bigcirc (n^3)$



SEM =
$$\frac{s+d}{\sqrt{N}}$$

D = Categorical(particles)

for i in 1:n

push(bp, rand(D))

end