Neural Network Function Approximation

Map of RL Algorithms

Model Based

Model Free

Q-learning

MLMBTRL (Learn T, R)

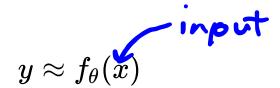
Tabular

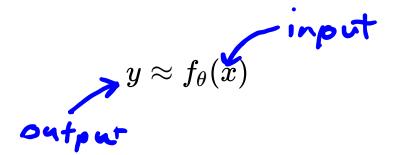
This Time

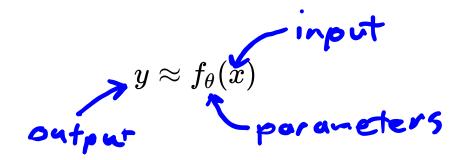
Challenges in Reinforcement Learning:

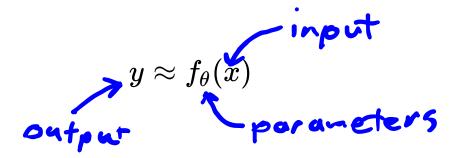
- Exploration vs Exploitation Bandit
- Credit Assignment

$$ypprox f_{ heta}(x)$$



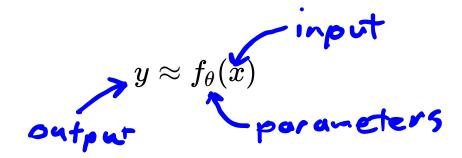






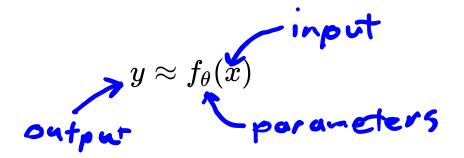
Previously, Linear:

$$f_{ heta}(x) = heta^ op eta(x)$$



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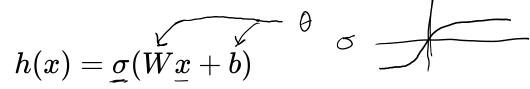
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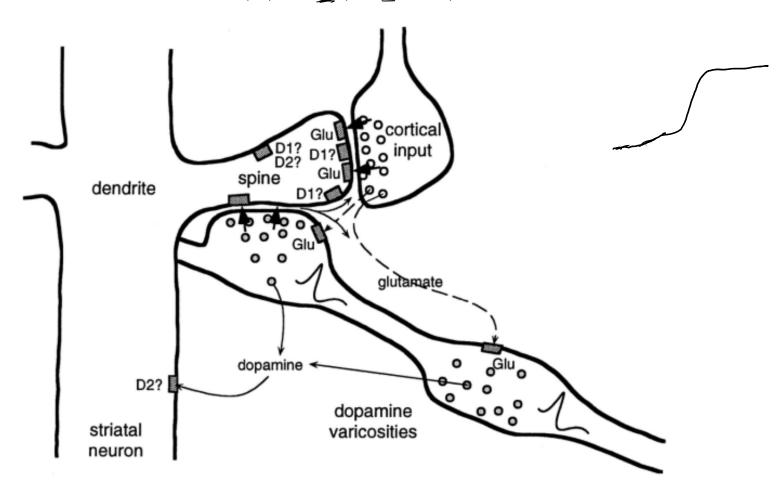
$$f_{ heta}(x) = heta^ op eta(x)$$

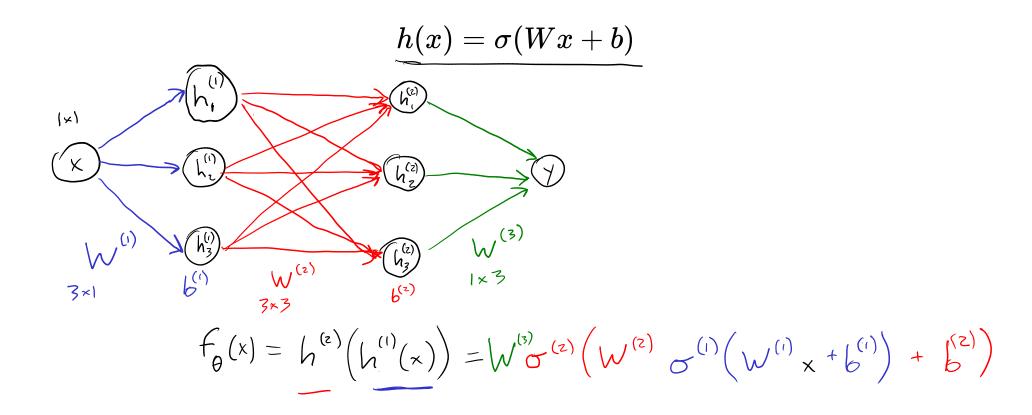
e.g.
$$\beta_i(x) = \sin(i\pi x)$$

$$h(x) = \sigma(Wx + b)$$

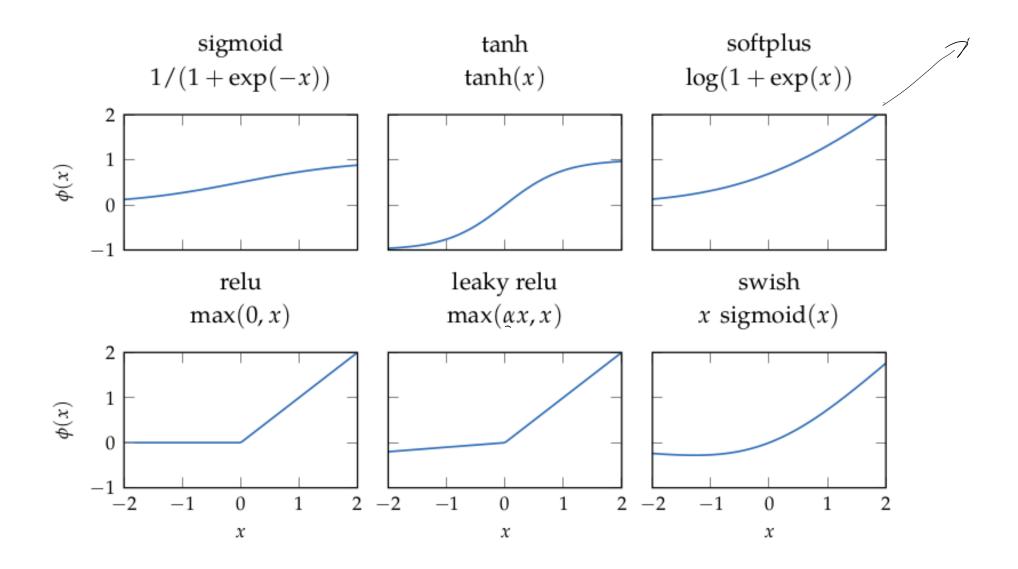
 $h_{3}(h_{2}(h,(\times)))$

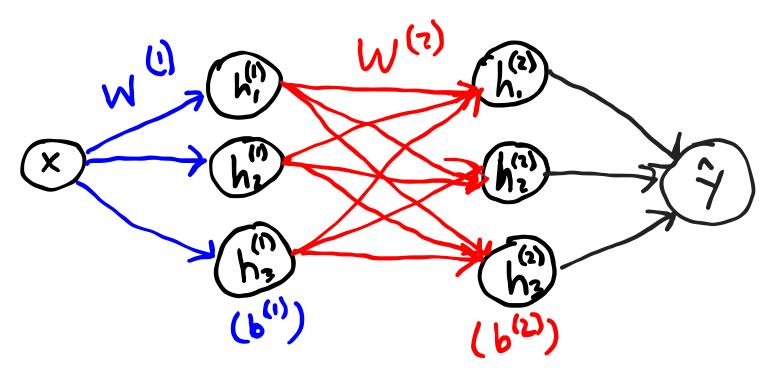


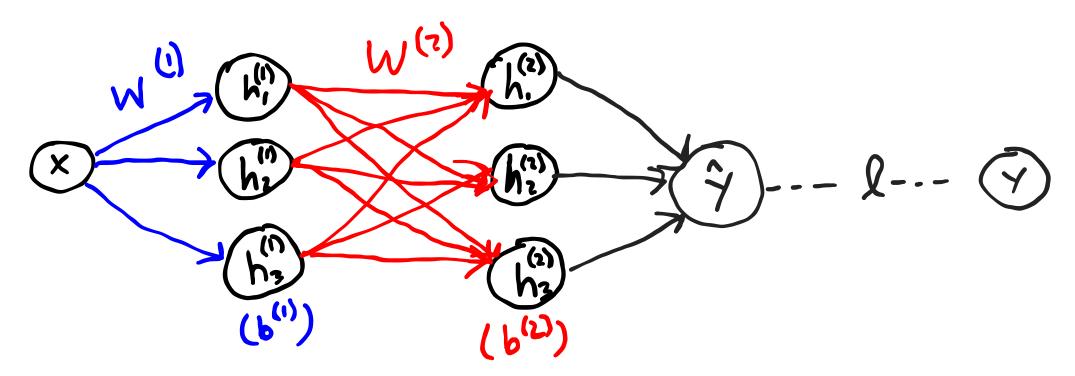


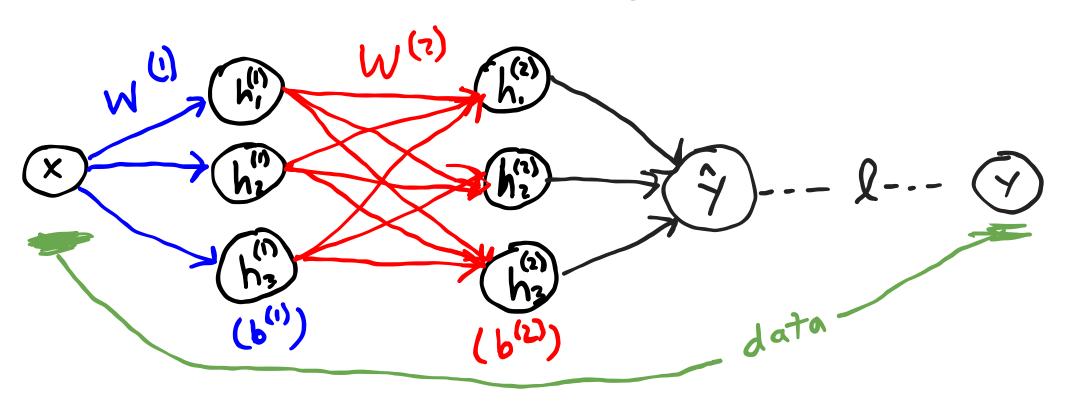


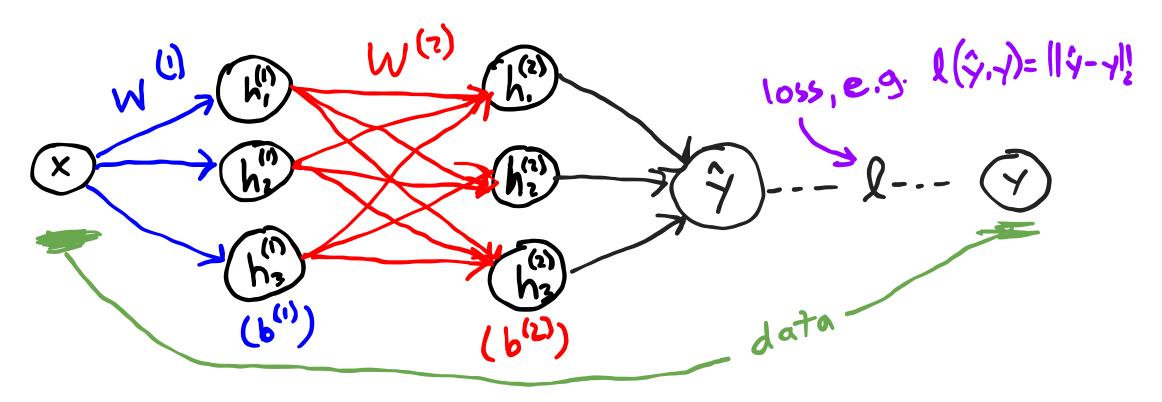
Nonlinearities

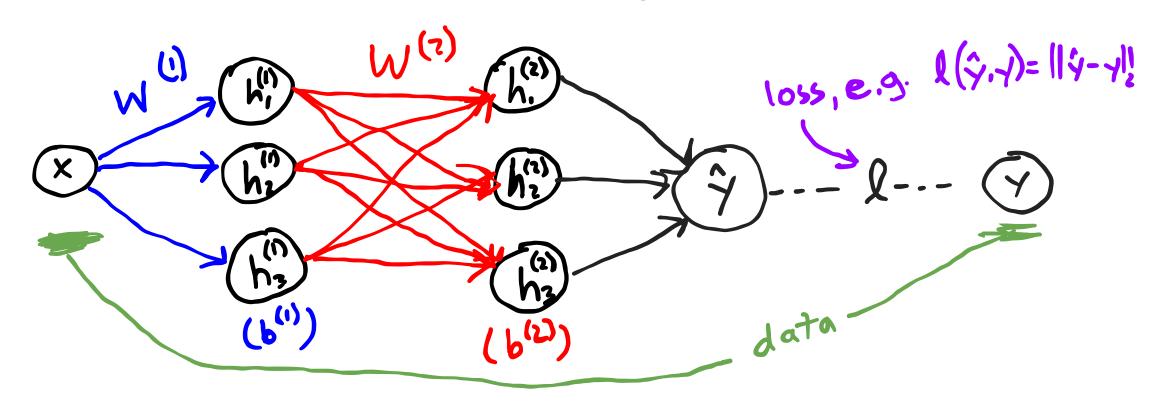




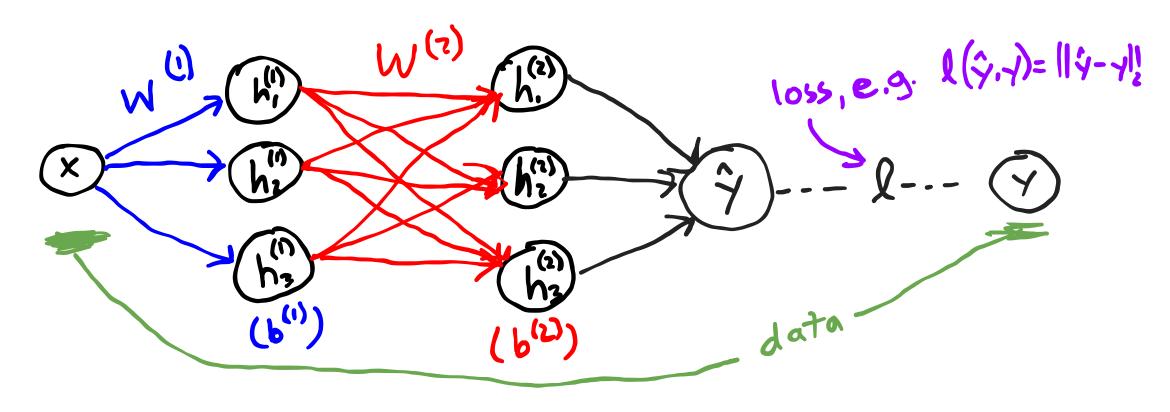








$$heta^* = rg\min_{ heta} \sum_{(x,y) \in \mathcal{D}} l(f_{ heta}(x),y)$$



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Stochastic Gradient Descent: $heta \leftarrow heta - lpha \, \overline{
abla_{ heta} \, l(f_{ heta}(x), y)}$

Chain Rule

$$h_o = h(x_o)$$

$$\nabla_{\!\!\!o} l(f_{o}(x), y)$$

$$\Theta = \left(W^{(1)}, b^{(1)}, W^{(2)}, b^{(2)} \right)$$

$$\frac{\partial f \cdot g \cdot h}{\partial x} \Big|_{x_{o}} = \frac{\partial f(g(k(x)))}{\partial x} \Big|_{x_{o}} = \frac{\partial f(g(h))}{\partial h} \Big|_{h_{o}} \frac{\partial h}{\partial x} \Big|_{x_{o}}$$

$$= \frac{\partial f(g)}{\partial g} \Big|_{g_{o}} \frac{\partial g(h)}{\partial h} \Big|_{h_{o}} \frac{\partial h}{\partial x} \Big|_{x_{o}}$$

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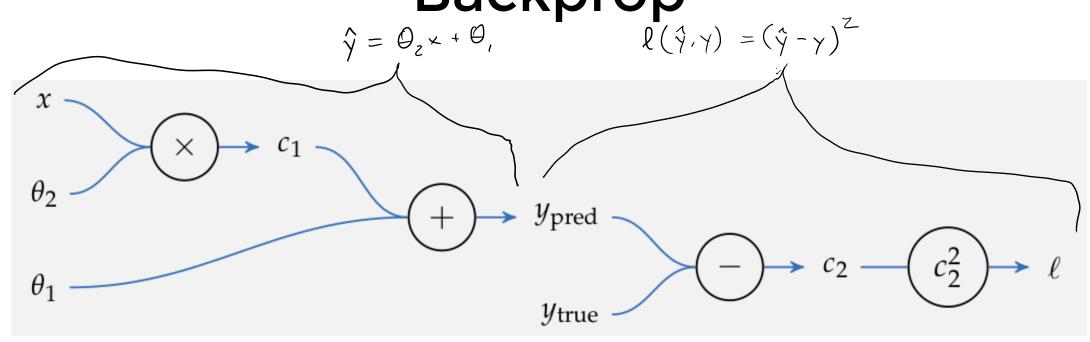
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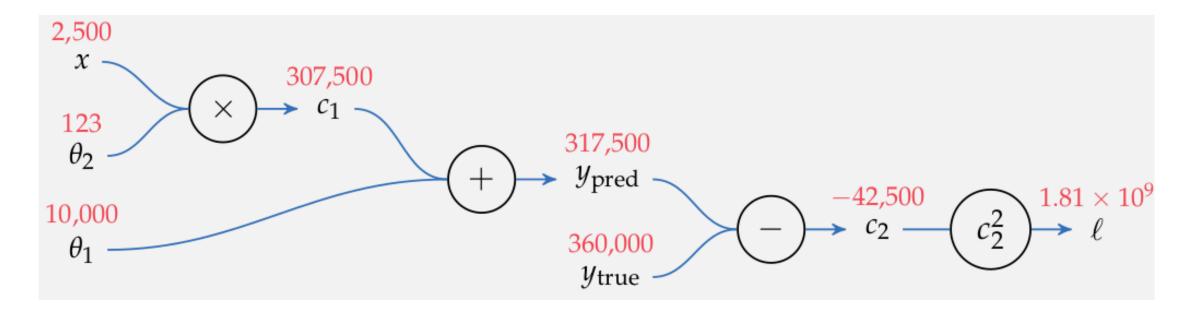
$$= \frac{\partial f(g)}{\partial g} \Big|_{g_{o}} \frac{\partial g(h)}{\partial h} \Big|_{h_{o}} \frac{\partial g(h)}{\partial h} \Big|_{h_{o}} \frac{\partial g(h)}{\partial h} \Big|_{h_{o}}$$

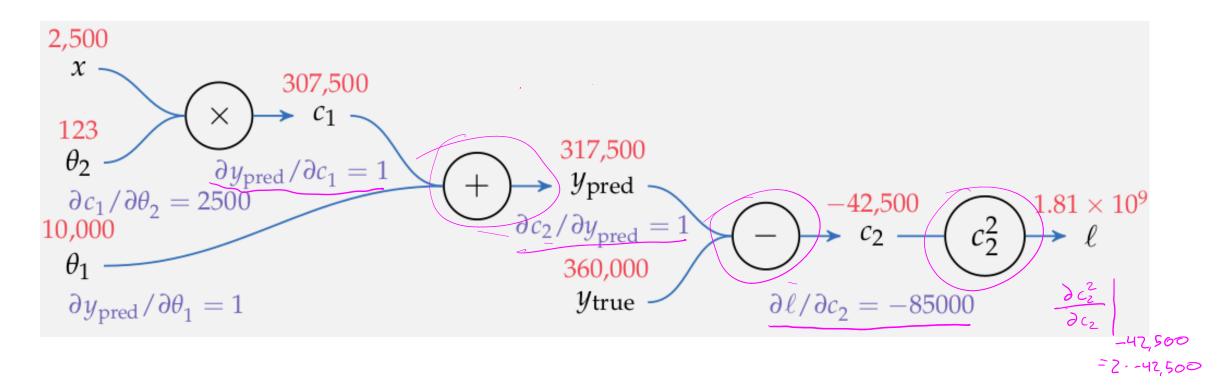
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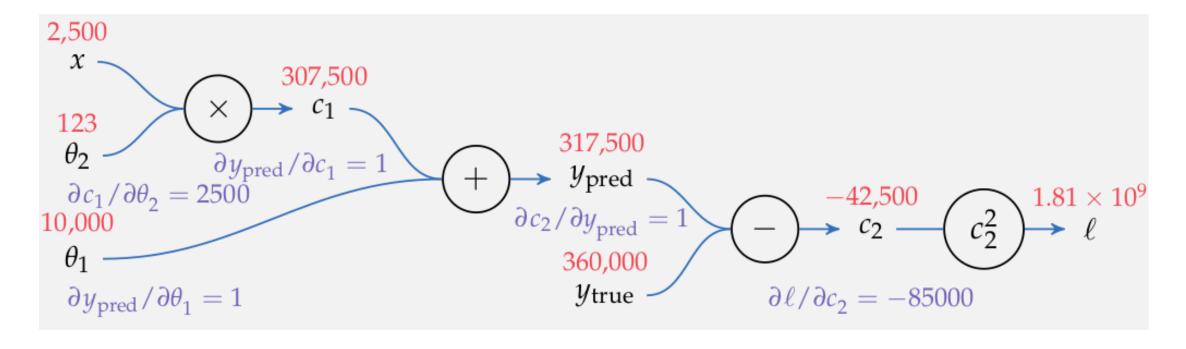


forward: calculate values

backward: use chain rule to calculate derivatives







back wards from
$$\ell$$
 to θ ,

$$\frac{\partial \ell}{\partial \theta_1} = \frac{\partial \ell}{\partial c_2} \frac{\partial c_2}{\partial y_{\text{pred}}} \frac{\partial y_{\text{pred}}}{\partial \theta_1} = -85,000 \cdot 1 \cdot 1 = -85,000$$

$$\frac{\partial \ell}{\partial \theta_2} = \frac{\partial \ell}{\partial c_2} \frac{\partial c_2}{\partial y_{\text{pred}}} \frac{\partial y_{\text{pred}}}{\partial c_1} \frac{\partial c_1}{\partial \theta_2} = -85,000 \cdot 1 \cdot 1 \cdot 2500 = -2.125 \times 10^8$$

a "fast and furious" approach to training neural networks does not work and only leads to suffering. Now, suffering is a perfectly natural part of getting a neural network to work well, but it can be mitigated by being thorough, defensive, paranoid, and obsessed with visualizations of basically every possible thing. The qualities that in my experience correlate most strongly to success in deep learning are patience and attention to detail.

Keep calm and lower your learning rate

- Andrej Karpathy

Adaptive Step Size: RMSProp

SGD
$$\Theta \leftarrow \Theta - \alpha \sqrt[3]{(f_{\theta}(x), y)}$$

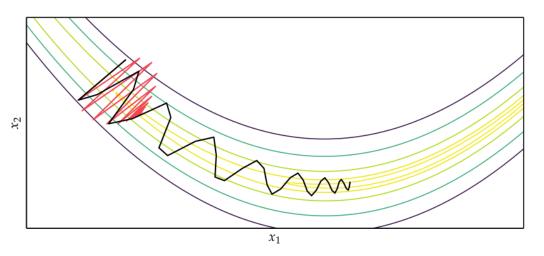
$$g^{(k)}$$

$$RMS prop$$

$$estimate
of g \(\text{g} \) \(\text{g}^{(k+1)} \) \(\text{g}^{(k)} \) \(\text{g}^{(k)}$$

Adaptive Step Size: ADAM

(Adaptive Moment Estimation)

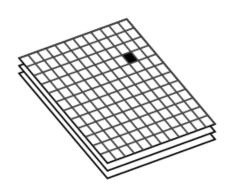


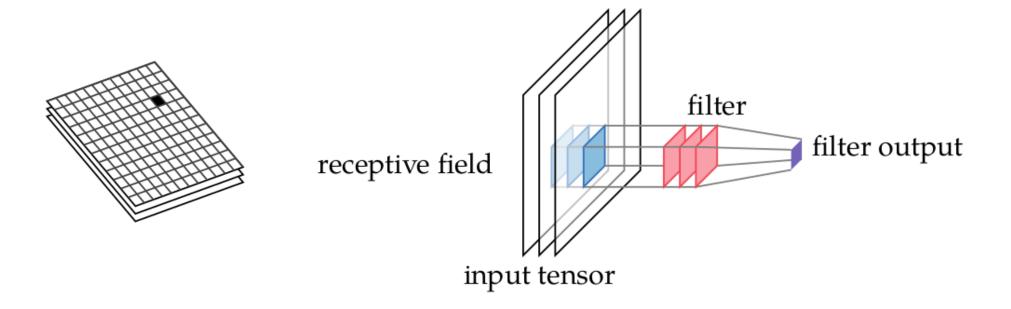
gradient descent — momentum

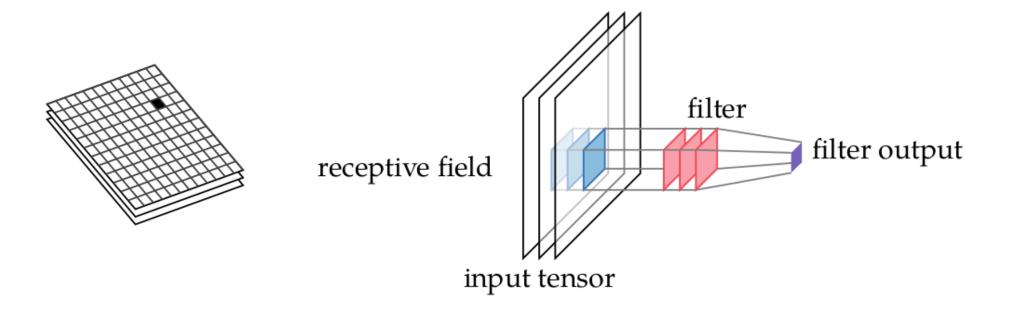
Figure 5.5. Gradient descent and the momentum method compared on the Rosenbrock function with b = 100; see appendix B.6.

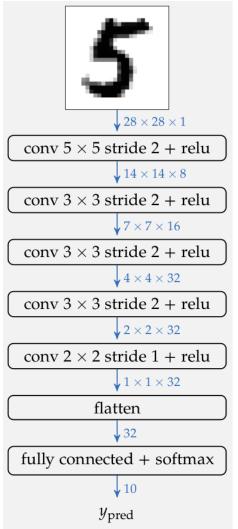
biased decaying momentum
$$V^{(k+1)} = y_v V^{(k)} + (1-y_v)g^{(k)}$$

biased decaying sq. grad. $S^{(k+1)} = y_s S^{(k)} + (1-y_s)(g^{(k)} \odot g^{(k)})$









On Your Radar: Regularization

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$$\underset{\boldsymbol{\theta}}{\operatorname{arg\,min}} \sum_{(x,y)\in\mathbf{D}} \ell(f_{\boldsymbol{\theta}}(x),y) - \beta \|\boldsymbol{\theta}\|^2$$

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$$\underset{\boldsymbol{\Theta}}{\operatorname{arg\,min}} \sum_{(x,y)\in\mathbf{D}} \ell(f_{\boldsymbol{\Theta}}(x),y) - \beta \|\boldsymbol{\Theta}\|^2$$

e.g. Batch norm, layer norm, dropout

On Your Radar: Skip Connections (Resnets)

Resources

OpenAl Spinning up