# DMU 2024 Online Quizzes

### March 11, 2025

### Online Quiz 1

Question 1. Consider an MDP with integer states  $(S = \mathbb{Z})$  and  $A = \{1, 2\}$ . State 3 is terminal and the discount factor is  $\gamma = 0.9$ . Suppose that you are performing reinforcement learning, and you observe an episode that takes the following trajectory:

```
 (s = 1, a = 2, r = 10, s' = 2)   (s = 2, a = 2, r = 5, s' = 1)   (s = 1, a = 1, r = 0, s' = 2)   (s = 2, a = 2, r = 0, s' = 3)
```

- 1. Suppose that you are using the SARSA algorithm starting with all Q values initialized to zero before the episode. If the learning rate is  $\alpha = 0.1$ , what are the Q-value estimates for states 1 and 2 after the episode (including an update based on the final step)?
  - Q(1,1)
  - Q(1,2)
  - Q(2,1)
  - Q(2,2)
- 2. Suppose that you are using maximum likelihood tabular model-based reinforcement learning (MLMBTRL). After the trajectory above, what are the maximum likelihood reward estimates for states 1 and 2 after the episode?
  - R(1,1)
  - R(1,2)
  - R(2,1)
  - R(2,2)

#### Solution:

1. • Q(1,1) = 0.045

- Q(1,2) = 1.0
- Q(2,1) = 0.0
- Q(2,2) = 0.45
- 2. R(1,1) = 0.0
  - R(1,2) = 10.0
  - R(2,1) = 0.0
  - R(2,2) = 2.5

**Question 2.** Consider the following neural-network-like function approximators where W's are weight matrices and b's are bias vectors and  $\sigma$  is the sigmoid function. Which of these structures is the most powerful in the sense that it can approximate the most general class of functions?

- (A)  $f(x) = W_3(W_2(W_1x^3 + b_1) + \sigma(b_2))$
- (B)  $f(x) = W_3(W_2(W_1x^2 + b_1) + \sigma(b_2))$
- (C)  $f(x) = W_3 \sigma(W_2 \sigma(W_1 x^3 + b_1) + b_2)$
- (D)  $f(x) = W_3 \sigma(W_2 \sigma(W_1 x^2 + b_1) + b_2)$

Briefly justify your answer.

**Solution:** (A) and (B) are only linear functions of  $x^2$  and  $x^3$  respectively. Regarding (D), since x is squared, the output for any x and -x must be the same. (C) is the most general and can approximate any function.

## Online Quiz 2

**Question 3.** Suppose that I want to find an optimal policy for a Markov decision process with integer states and actions  $(S = A = \mathbb{Z})$ , discount factor  $\gamma = 0.9$  and reward function  $R(s, a) = s^2$ .

I am considering training under the following modified reward functions. Which reward function would **NOT** be guaranteed to yield the same optimal policy?

- (A)  $R(s, a, s') = 2s^2$
- (B)  $R(s, a, s') = 2 s^2 \gamma s'^2$
- (C)  $R(s, a, s') = s^2 + \sin(a)$
- (D)  $R(s, a, s') = s^2 + \gamma \sin(s') \sin(s)$

Briefly justify your answer

**Solution:** The optimal policy is independent of reward scaling and potential-based reward shaping. All of the answers except (C) involve only scaling and potential-based reward shaping. (C) introduces a non-linear action term, which could change the optimal policy.

**Question 4.** Double Q learning is meant to address which of the following problems?

- (A) Insufficient exploration
- (B) Maximization bias
- (C) Incorrect credit assignment
- (D) Poor sample efficiency

Solution: Maximization Bias

Question 5. Which of the following is \*\*NOT\*\* an advantage of entropy regularization, as used in the Soft Actor Critic algorithm

- (A) It usually learns a combination of many near-optimal policies, making the resulting solution more robust to modeling errors
- (B) Given unlimited time and computational resources, it is possible to learn better policies with entropy regularization than without
- (C) The randomness incentivized by the entropy term leads to natural exploration
- (D) All of these are advantages

**Solution:** (B) is not an advantage of entropy regularization. Given unlimited time and computational resources, it is possible to learn the optimal policy with or without entropy regularization.

Question 6. In DQN, the Q network typically uses what inputs and outputs?

- (A) Input: History of states and actions; Output: The maximum Q-value
- (B) Input: A state and action; Output: A scalar Q-value for the state and action
- (C) Input: A state; Output: The maximum Q value and the action that maximizes it
- (D) Input: A state; Output: Q values for all actions at the input state

Solution: (D)

Question 7. Which of the below statements is the best description of the natural gradient?

- (A) The policy parameter adjustment expected to maximize rewards subject to a constraint on the KL divergence of trajectories under the new policy with respect to the trajectories under the old policy
- (B) The gradient of the value (expected sum of discounted rewards) with respect to the policy parameters
- (C) The policy parameter adjustment that minimizes the KL divergence of the updated policy with respect to the original policy
- (D) The gradient that will maximize the KL divergence of the rewards attained by the new policy with respect to the rewards obtained with the original policy

Solution: (A)

### Online Quiz 3

Question 8. Suppose that two roommates need to decide who will take out the trash. They decide to flip a fair coin and the loser has to take out the trash.

- 1. What type of equilibrium best describes this arrangement?
  - (A) Dominant strategy equilibrium
  - (B) Pure Nash equilibrium
  - (C) Mixed Nash equilibrium
  - (D) Correlated Equilibrium
- 2. Choose one of the other types of equilibrium listed above and explain why the coin-flip arrangement is preferable to that type of equilibrium for this game.

Solution: (D) Correlated Equilibrium.

Assuming the payoffs are such that both players would rather take out the trash than leaving it, there is a pure Nash equilibrium where one player always takes out the trash. This is unfair to the person who takes out the trash. The coin-flip arrangement is preferable because it is fair.

**Question 9.** Which of the following is a step in the fictitious play algorithm applied to a Markov Game?

- (A) Create a POMDP model where the unknown state variable includes the other players' possible strategies and solve the POMDP to find the optimal policy.
- (B) Create an MDP based on the frequency of the other players' previous plays and solve this MDP to find a best response strategy.

- (C) Perform a policy-gradient step to improve the policy of the current player based on the state trajectory from the previous episode.
- (D) Solve a linear program to find a correlated equilibrium that is the best outcome for all players.

Solution: (B)

Question 10. In a two-player partially observable Markov game, a policy  $\pi^i$  can be pruned (i.e. ignored in a Nash equilibrium computation) if

- (A) Another strategy outperforms  $\pi^i$  at some  $(s, \pi^{-i})$  pair.
- (B) At least one strategy outperforms  $\pi^i$  at each  $(s, \pi^{-i})$  pair.
- (C) There is no \*distribution\* over  $(s, \pi^{-i})$  pairs,  $b(s, \pi^{-i})$ , where  $\pi^{i}$  outperforms all other strategies.
- (D) It is impossible to prune any strategies in a POMG because all pure strategies could potentially be part of a mixed Nash equilibrium.

(In the context of this question,  $\pi^i$  "outperforms"  $\pi^{i'}$  at an  $(s, \pi^{-i})$  pair if  $U^{\pi^i, \pi^{-i}, i}(s) > U^{\pi^{i'}, \pi^{-i}, i}(s)$ )

Solution: (C)

Question 11. Which of the following is a valid reason that inverse reinforcement learning has more potential for generalization than behavioral cloning in some settings?

- (A) Inverse reinforcement learning requires less information about the MDP compared to behavioral cloning.
- (B) Behavioral cloning can only learn to imitate deterministic policies, while inverse reinforcement learning can also learn probabilistic policies.
- (C) Since inverse reinforcement learning attempts to learn the expert's reward function, it may yield expert-like policies in other environments where the reward function is the same but the dynamics differ from the environment where the data was collected.

Solution: (C)