

Remedial interchange, Contrary-to-duties, and Commutation

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Introduction

Research idea

- Can deontic logic be used to capture the normative aspect(s) of dialogues?

Standard ACL approach in MAS

- Conversation policies = hard constraints

What I'm after: a more flexible approach

- NorMAS: breach of dialogue rules allowed ...
- ... and dealt with
 - ▶ Norm violation: a hot topic in deontic logic
 - ▶ No easy answers

Talk overview

Focus on

- Logic for conditional obligation (Hansson, ...)

Case study (sort of)

- “Remedial Interchange” (Ervin Goffman)
 - ▶ Norms

Point twofold

- Contrary-to-duty paradox
- Solution using iterated belief change theory

What we get

- Dialogue model based on obligations
 - ▶ Rules of turn-taking
 - ▶ Tailored for a specific application domain

Layout

- CTD and remedial interchange
- Framework
- Example analysis

Contrary-to-duty (CTD)

Weakening the Consequent

$$\frac{\bigcirc(B/A) \quad \Box(B \rightarrow C)}{\bigcirc(C/A)} (WC)$$

Factual Detachment

$$\frac{\bigcirc(B/A) \quad A}{\bigcirc B} (FD)$$

Contrary-to-duty (CTD)

Weakening the Consequent

$$\frac{\bigcirc(B/A) \quad \Box(B \rightarrow C)}{\bigcirc(C/A)} (WC)$$

Factual Detachment

$$\frac{\bigcirc(B/A) \quad A}{\bigcirc B} (FD)$$

CTD paradox

$$\frac{\bigcirc \neg A \quad \frac{\Box(B \rightarrow A)}{\Box(\neg A \rightarrow \neg B)}}{\bigcirc \neg B} (WC)$$

$$\frac{\bigcirc(B/A) \quad A}{\bigcirc B} (FD)$$

Contrary-to-duty (CTD)

Weakening the Consequent

$$\frac{\bigcirc(B/A) \quad \Box(B \rightarrow C)}{\bigcirc(C/A)} (WC)$$

Factual Detachment

$$\frac{\bigcirc(B/A) \quad A}{\bigcirc B} (FD)$$

CTD paradox

$$\frac{\bigcirc\neg A \quad \frac{\Box(B \rightarrow A)}{\Box(\neg A \rightarrow \neg B)}}{\bigcirc\neg B} (WC)$$

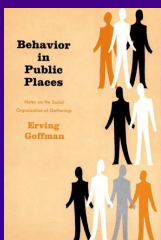
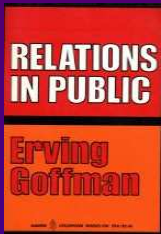
$$\frac{\bigcirc(B/A) \quad A}{\bigcirc B} (FD)$$

‘Gentle murderer’ scenario

$$\{\bigcirc\neg k, \Box(k \wedge g \rightarrow k), \bigcirc(k \wedge g/k), k\} \vdash \perp$$

Remedial interchange

Chap. 3 of *Relations in Public* (1971)



- Social life as norm-governed
- "Territories of the self"
 - ▶ Personal space
 - ▶ Possessionnal territory
 - ▶ Etc
- Remedial interchange
 - ▶ Offensive → acceptable
 - ▶ Social order

Remedial interchange

Goffman, *Relations in Public*, 1971

A: “Can I use your phone to make a local call?”

B: “Sure, go ahead”

A: “That’s very good of you”

B: “It’s okay”

Remedial interchange

Goffman, *Relations in Public*, 1971

remedy

A: “Can I use your phone to make a local call?”

relief

B: “Sure, go ahead”

appreciation

A: “That’s very good of you”

minimization

B: “It’s okay”

Remedial interchange

Goffman, *Relations in Public*, 1971

remedy

A: “Can I use your phone to make a local call?”

relief

B: “Sure, go ahead”

appreciation

A: “That’s very good of you”

minimization

B: “It’s okay”

Goffman’s suggestion

By making a move, I put the other participant under the *obligation* to make the next one.

Dialogue game rules are soft rather than hard constraints

Logical representation

	Normative premisses (α)	Integrity constraints (β)
(I)	$\bigcirc \neg o$	
(II)	$\bigcirc(r_1/o)$ $\bigcirc(r_2/o \wedge r_1)$	$\Box(r_1 \rightarrow o)$ $\Box(r_2 \rightarrow (o \wedge r_1))$
(III)	$\bigcirc(a/o \wedge r_1 \wedge r_2)$ $\bigcirc(m/o \wedge r_1 \wedge r_2 \wedge a)$	$\Box(a \rightarrow (o \wedge r_1 \wedge r_2))$ $\Box(m \rightarrow (o \wedge r_1 \wedge r_2 \wedge a))$

with o = offence r_2 = relief m = minimization
 r_1 = remedy a = appreciation

Conditional obligation

Preference-based semantics *à la* Hansson (1969)

$$\mathcal{M} \models \bigcirc(B/A) \Leftrightarrow \min_{\mathcal{M}}(A) \subseteq [B]_{\mathcal{M}}. \quad (\text{Def}\bigcirc)$$

Intuitively: \mathcal{M} satisfies $\bigcirc(B/A)$ iff in the most perfect worlds, where A holds, B holds too.

$\bigcirc B$ short for $\bigcirc(B/\top)$

Before the violation

$$S = \{ \bigcirc \neg o, \bigcirc(r_1/o), \bigcirc(r_2/o \wedge r_1), \\ \bigcirc(a/o \wedge r_1 \wedge r_2), \bigcirc(m/o \wedge r_1 \wedge r_2 \wedge a) \}$$

Model \mathcal{M}_1

$w_1 : \neg o, \neg r_1, \neg r_2, \neg a, \neg m$

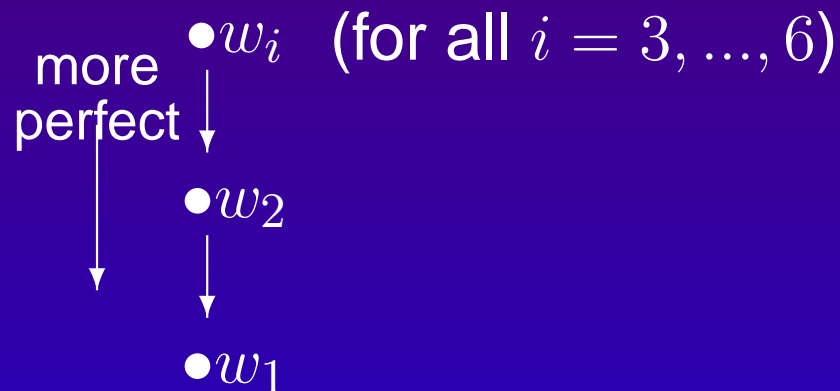
$w_2 : o, r_1, r_2, a, m$

$w_3 : o, \neg r_1, \neg r_2, \neg a, \neg m$

$w_4 : o, r_1, \neg r_2, \neg a, \neg m$

$w_5 : o, r_1, r_2, \neg a, \neg m$

$w_6 : o, r_1, r_2, a, \neg m.$



Before the violation

$$S = \{ \bigcirc \neg o, \bigcirc(r_1/o), \bigcirc(r_2/o \wedge r_1), \\ \bigcirc(a/o \wedge r_1 \wedge r_2), \bigcirc(m/o \wedge r_1 \wedge r_2 \wedge a) \}$$

Model \mathcal{M}_1

$$w_1 : \neg o, \neg r_1, \neg r_2, \neg a, \neg m$$

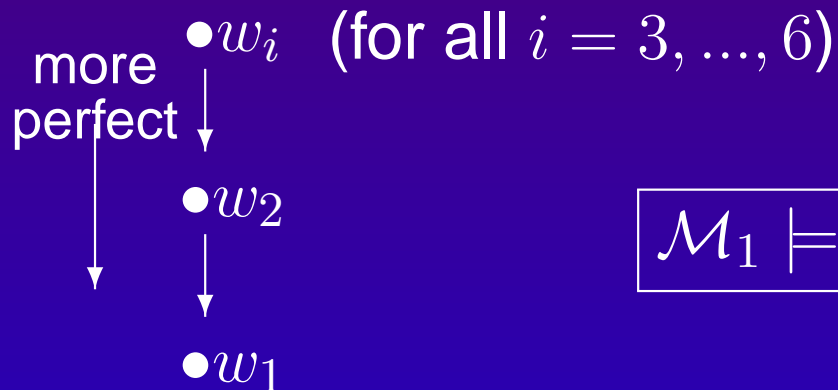
$$w_2 : o, r_1, r_2, a, m$$

$$w_3 : o, \neg r_1, \neg r_2, \neg a, \neg m$$

$$w_4 : o, r_1, \neg r_2, \neg a, \neg m$$

$$w_5 : o, r_1, r_2, \neg a, \neg m$$

$$w_6 : o, r_1, r_2, a, \neg m.$$



$$\boxed{\mathcal{M}_1 \models \bigcirc \neg r_1, \mathcal{M}_1 \not\models \bigcirc r_1}$$

(WC) vs (FD)

$$(WC) \frac{\bigcirc \neg o \quad \frac{\frac{\Box(r_1 \rightarrow o)}{\Box(\neg o \rightarrow \neg r_1)}}{\bigcirc \neg r_1}}{\bigcirc \neg r_1}$$

$$\frac{\bigcirc(r_1/o)}{\bigcirc r_1}$$

(WC) vs (FD)

$$\begin{array}{c}
 \text{(WC)} \quad \frac{\frac{\frac{\Box(r_1 \rightarrow o)}{\Box(\neg o \rightarrow \neg r_1)}}{\Box \neg r_1}}{\bigcirc \neg o} \\
 \text{(FD)} \quad \frac{\bigcirc(r_1/o)}{\bigcirc r_1} \quad \textcolor{red}{o}
 \end{array}$$

(WC) vs (FD)

$$\begin{array}{c}
 \text{(WC)} \quad \frac{\frac{\bigcirc \neg o}{\text{---}} \quad \frac{\frac{\Box(r_1 \rightarrow o)}{\Box(\neg o \rightarrow \neg r_1)}}{\bigcirc \neg r_1}}{\text{---}}
 \end{array}
 \qquad
 \frac{\bigcirc(r_1/o)}{\bigcirc r_1} \overset{o}{\text{(FD)}}$$

An old idea ...

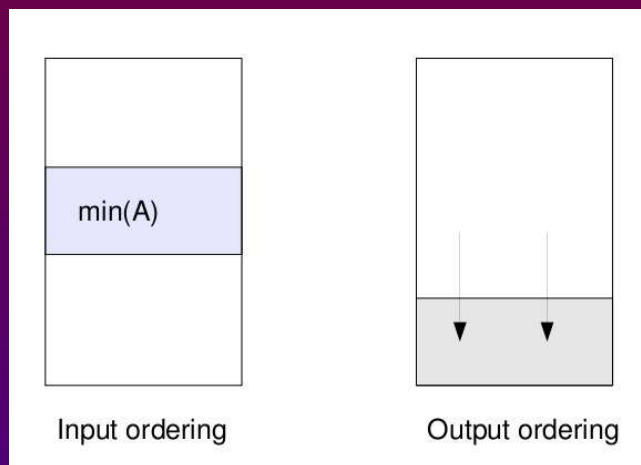
- Both rules allowed
- In case of conflict, (FD) overrides (WC)

An old idea ...

- ## ... in a new guise

-

Natural Revision



(**P**₁) If $w_1 \in \min_{\mathcal{M}}(A)$ then:

$w_1 \preceq' w_2$ for all $w_2 \in W$ and (a)

$w_2 \preceq' w_1$ iff $w_2 \in \min_{\mathcal{M}}(A)$ (b)

(**P**₂) If $w_1, w_2 \notin \min_{\mathcal{M}}(A)$ then: $w_1 \preceq' w_2$ iff $w_1 \preceq w_2$.

Commutation

Model \mathcal{M}_1 (Before the offence)

$o = \text{offence}$

$r_1 = \text{remedy}$

In \mathcal{M}_1 :

$\bigcirc \neg r_1$
not- $\bigcirc r_1$

$\bullet w_3 : o \neg r_1$



$\bullet w_2 : o r_1$



$\bullet w_1 : \neg o \neg r_1$

$\mathcal{M}_1^* o$
 \Longrightarrow

$\bullet w_3$



$\bullet w_1$



$\bullet w_2$

In $\mathcal{M}_1^* o$:

$\bigcirc r_1$
not- $\bigcirc \neg r_1$

Commutation

Model \mathcal{M}_1 (Before the offence)

$o = \text{offence}$

$r_1 = \text{remedy}$

In \mathcal{M}_1 :

$\bigcirc \neg r_1$
not- $\bigcirc r_1$

$\bullet w_3 : o \neg r_1$



$\bullet w_2 : o r_1$



$\bullet w_1 : \neg o \neg r_1$

$\mathcal{M}_1^* o$



$\bullet w_3$



$\bullet w_1$



$\bullet w_2$

In $\mathcal{M}_1^* o$:

$\bigcirc r_1$
not- $\bigcirc \neg r_1$

Round 1

Input	Induced ordering		Perms	Output
o	$\mathcal{M}_1^* o$	$w_2 \prec w_1 \prec w_{i(i \geq 3)}$	1	$\bigcirc r_1$
$\neg o$	$\mathcal{M}_1^* \neg o$	$w_1 \prec w_2 \prec w_{i(i \geq 3)}$	0	$\bigcirc \neg r_1$

Turn-taking & obligation update

Round 2

o =offence

r_1 =remedy

r_2 =*relief*

Input sequence	Induced ordering		Perms	Output
1. o, r_1	$(\mathcal{M}_1^* o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$
2. $o, \neg r_1$	$(\mathcal{M}_1^* o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg r_2$
3. $\neg o, r_1$	$(\mathcal{M}_1^* \neg o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$
4. $\neg o, \neg r_1$	$(\mathcal{M}_1^* \neg o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg r_2$

Turn-taking & obligation update

Round 2

$o = \text{offence}$

$r_1 = \text{remedy}$

$r_2 = \text{relief}$

Input sequence	Induced ordering		Perms	Output
1. o, r_1	$(\mathcal{M}_1^* o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$
3. $\neg o, r_1$	$(\mathcal{M}_1^* \neg o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$

Turn-taking & obligation update

Round 2

$o = \text{offence}$

$r_1 = \text{remedy}$

$r_2 = \text{relief}$

Input sequence	Induced ordering		Perms	Output
2. $o, \neg r_1$	$(\mathcal{M}_1^* o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg r_2$
4. $\neg o, \neg r_1$	$(\mathcal{M}_1^* \neg o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg r_2$

Turn-taking & obligation update

Round 2

o =offence

r_1 =remedy

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Input sequence	Induced ordering		Perms	Output
1. o, r_1	$(\mathcal{M}_1^* o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$
2. $o, \neg r_1$	$(\mathcal{M}_1^* o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg r_2$
3. $\neg o, r_1$	$(\mathcal{M}_1^* \neg o)^* r_1$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc r_2$
4. $\neg o, \neg r_1$	$(\mathcal{M}_1^* \neg o)^* \neg r_1$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg r_2$

Turn-taking & obligation update

$o = \text{offence}$ $r_1 = \text{remedy}$

$r_2 = \text{relief}$ $a = \text{appreciation}$

Round 3

Input sequence	Induced ordering		Perm	Output
1. o, r_1, r_2	$((\mathcal{M}_1^* o)^* r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc a$
2. $o, r_1, \neg r_2$	$((\mathcal{M}_1^* o)^* r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
3. $o, \neg r_1, r_2$	$((\mathcal{M}_1^* o)^* \neg r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc a$
4. $o, \neg r_1, \neg r_2$	$((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
5. $\neg o, r_1, r_2$	$((\mathcal{M}_1^* \neg o)^* r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc a$
6. $\neg o, r_1, \neg r_2$	$((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
7. $\neg o, \neg r_1, r_2$	$((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	2	$\bigcirc a$
8. $\neg o, \neg r_1, \neg r_2$	$((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg a$

Turn-taking & obligation update

$o = \text{offence}$ $r_1 = \text{remedy}$

$r_2 = \text{relief}$ $a = \text{appreciation}$

Round 3

Input sequence	Induced ordering		Perm	Output
1. o, r_1, r_2	$((\mathcal{M}_1^* o)^* r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc a$
3. $o, \neg r_1, r_2$	$((\mathcal{M}_1^* o)^* \neg r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc a$
5. $\neg o, r_1, r_2$	$((\mathcal{M}_1^* \neg o)^* r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc a$
7. $\neg o, \neg r_1, r_2$	$((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2$	$w_2 \prec w_1 \prec w_i$	2	$\bigcirc a$

Turn-taking & obligation update

o = offence r_1 = remedy

r_2 = relief a = appreciation

Round 3

Input sequence	Induced ordering		Perm	Output
2. $o, r_1, \neg r_2$	$((\mathcal{M}_1^* o)^* r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
4. $o, \neg r_1, \neg r_2$	$((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
6. $\neg o, r_1, \neg r_2$	$((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg a$
8. $\neg o, \neg r_1, \neg r_2$	$((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg a$

Turn-taking & obligation update

Round 4

Revision sequence	Induced ordering	Perm	Output
1. $((\mathcal{M}_1^* o)^* r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i (i \geq 3)$	1	$\bigcirc m$
2. $((\mathcal{M}_1^* o)^* r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
3. $((\mathcal{M}_1^* o)^* r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
4. $((\mathcal{M}_1^* o)^* r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
5. $((\mathcal{M}_1^* o)^* \neg r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
6. $((\mathcal{M}_1^* o)^* \neg r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	4	$\bigcirc \neg m$
7. $((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
8. $((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
9. $((\mathcal{M}_1^* \neg o)^* r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$
10. $((\mathcal{M}_1^* \neg o)^* r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
11. $((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
12. $((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
13. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$
14. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
15. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$
16. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg m$

o = offence
 r_1 = remedy
 r_2 = relief
 a = appreciation
 m = minimization

Turn-taking & obligation update

Round 4

Revision sequence	Induced ordering	Perm	Output
1. $((\mathcal{M}_1^* o)^* r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i (i \geq 3)$	1	$\bigcirc m$
3. $((\mathcal{M}_1^* o)^* r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
5. $((\mathcal{M}_1^* o)^* \neg r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
7. $((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
9. $((\mathcal{M}_1^* \neg o)^* r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$
11. $((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	3	$\bigcirc m$
13. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$
15. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2)^* a$	$w_2 \prec w_1 \prec w_i$	1	$\bigcirc m$

o = offence
 r_1 = remedy
 r_2 = relief
 a = appreciation
 m = *minimization*

Turn-taking & obligation update

Round 4

Revision sequence	Induced ordering	Perm	Output
2. $((\mathcal{M}_1^* o)^* r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i (i \geq 3)$	2	$\bigcirc \neg m$
4. $((\mathcal{M}_1^* o)^* r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
6. $((\mathcal{M}_1^* o)^* \neg r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	4	$\bigcirc \neg m$
8. $((\mathcal{M}_1^* o)^* \neg r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
10. $((\mathcal{M}_1^* \neg o)^* r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
12. $((\mathcal{M}_1^* \neg o)^* r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
14. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	2	$\bigcirc \neg m$
16. $((\mathcal{M}_1^* \neg o)^* \neg r_1)^* \neg r_2)^* \neg a$	$w_1 \prec w_2 \prec w_i$	0	$\bigcirc \neg m$

$o = \text{offence}$
 $r_1 = \text{remedy}$
 $r_2 = \text{relief}$
 $a = \text{appreciation}$
 $m = \text{minimization}$

Conclusion

Main contribution

- Dialogue model based on obligations
 - ▶ Rules of turn-taking

Related research

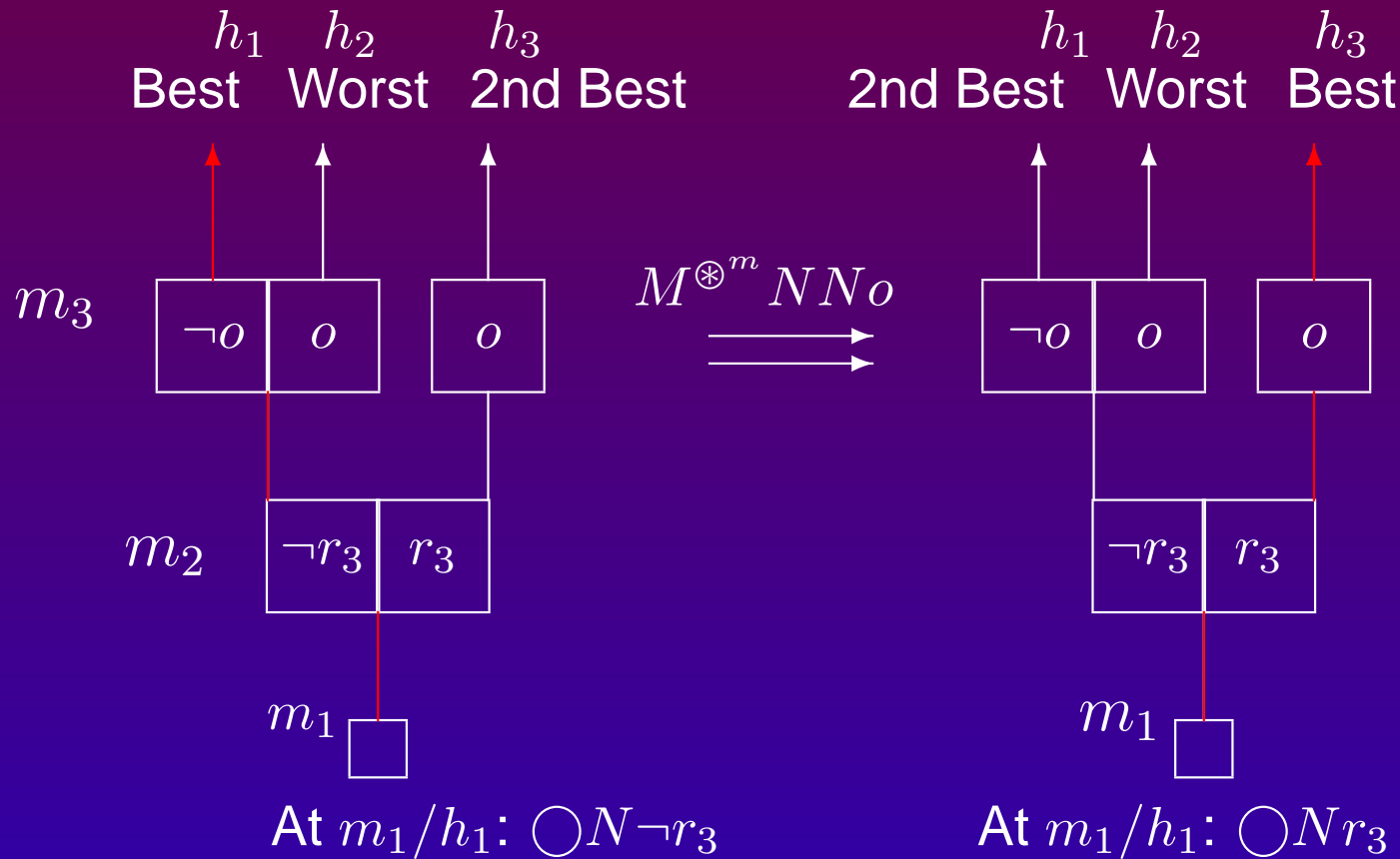
- Hulstijn and Maudet 2003, 'Uptake and conditional obligations'

Problems with my account

- Request: Consequent Before the Antecedent
- Drowning problem - revise too much

Consequent Before the Antecedent

$$\{\bigcirc NN\neg o, \bigcirc(Nr_3/NNo), \Box(Nr_3 \rightarrow NNo)\}$$



For $\mathfrak{M}^{\oplus m} \phi$, read “the model obtained from \mathfrak{M} once the happening of ϕ has been anticipated at moment m ”