

## Computation of All the Amicable Pairs Below $10^{10}$

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**Abstract.** An efficient exhaustive numerical search method for amicable pairs is described. With the aid of this method all 1427 amicable pairs with smaller member below  $10^{10}$  have been computed, more than 800 pairs being new. This extends previous exhaustive work below  $10^8$  by H. Cohen. In three appendices (contained in the supplements section of this issue), various statistics are given, including an ordered list of all the gcd's of the 1427 amicable pairs below  $10^{10}$  (which may be useful in further amicable pair research). Suggested by the numerical results, a theorem of Borho and Hoffmann for constructing APs has been extended.

**1. Introduction.** Let  $\sigma(m)$  denote the sum of all the divisors of  $m$ , including 1 and  $m$ . An *amicable* pair (AP) is a pair of positive integers  $(m, n)$ ,  $m < n$ , such that  $\sigma(m) = \sigma(n) = m + n$ . We note that  $m$  is *abundant* (since  $\sigma(m) > 2m$ ) and that  $n$  is *deficient* (since  $\sigma(n) < 2n$ ). The smallest AP is

$$(220, 284) = (2^2 \cdot 5 \cdot 11, 2^2 \cdot 71).$$

In order to check whether or not a given positive integer  $m$  is the smaller member of an amicable pair, it seems necessary, at first sight, to compute  $\sigma(m)$  and  $n := \sigma(m) - m$ , to check whether  $n > m$  (i.e., whether  $m$  is abundant), and, if so, to compute  $\sigma(n)$  and compare  $\sigma(m)$  with  $\sigma(n)$ . This involves one or two complete factorizations, in case  $m$  is deficient or abundant, respectively. However, a closer look reveals that it is often possible to find out whether a given number  $m$  is deficient (hence cannot be the smaller member of an AP) without the need to factorize it completely. Moreover, once  $\sigma(m)$  and  $n (= \sigma(m) - m)$  have been computed, it is often possible to discover that  $\sigma(n) \neq \sigma(m)$  without the need to factorize  $n$  completely.

These considerations have guided the design of an efficient exhaustive numerical AP search algorithm, the details of which are given in Section 2. With the aid of this algorithm we have extended Cohen's exhaustive list of all 236 APs with smaller member below  $10^8$  [4] to all 1427 APs with smaller member below  $10^{10}$ . Of these, 601 have been published earlier [6], [7]. The other 826 seem to be new, and are published here for the first time (9 of them have been communicated to the author already in 1983 and 1984 by Woods (2), Borho (2) and Lee (5)). Section 3 presents details of the computations together with several tables collected from this search. Moreover, a result of Borho and Hoffmann for constructing APs is extended, as was suggested by the numerical tables.

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Three appendices to this paper appear in the supplements section of this issue. These may also be obtained by writing to the author.

In Appendix I, we present the complete list of all 1427 APs with smaller member below  $10^{10}$  ordered according to the size of the smaller members of the pairs. Appendix II displays the same list with a different ordering, viz., according to the various occurring types (defined in Section 3). Finally, Appendix III tabulates all the greatest common divisors of the 1427 APs, in increasing order, together with their frequencies of occurrence, and, for each gcd  $g$ , the rank numbers of all the APs  $(m, n)$  for which  $\gcd(m, n) = g$ .

**2. Check Whether a Given  $m$  is the Smaller Member of an AP.** Let  $p_i$  be the  $i$ th prime,  $P_{ij} := \prod_{k=i}^{i+j-1} p_k$ ,  $Q_{ij} := \prod_{k=i}^{i+j-1} p_k / (p_k - 1)$ . We start with the following lemma which gives an upper bound for  $\sigma(m)/m$ .

**LEMMA 2.1.** *If  $m$  only has prime divisors  $\geq p_i$  ( $i \geq 1$ ) and if  $m < P_{i,j+1}$  ( $j \geq 1$ ) then  $\sigma(m)/m < Q_{ij}$ .*

*Proof.* Since  $m < P_{i,j+1} = p_i p_{i+1} \cdots p_{i+j}$ , and since any prime divisor of  $m$  is  $\geq p_i$ , it follows that  $m$  has at most  $j$  different prime divisors  $\geq p_i$  (otherwise we would have  $m \geq p_i p_{i+1} \cdots p_{i+j} = P_{i,j+1}$ ). This implies that

$$\frac{\sigma(m)}{m} = \prod_{p^e \parallel m} \frac{p^{e+1} - 1}{p^e(p-1)} = \prod_{p^e \parallel m} \frac{p - p^{-e}}{p-1} < \prod_{p \mid m} \frac{p}{p-1} \leq \prod_{k=i}^{i+j-1} \frac{p_k}{p_k - 1} = Q_{ij}. \quad \square$$

In the algorithm below, this lemma is invoked very frequently. Therefore, we require a precomputed table of  $P$ - and  $Q$ -values, large enough so that the values needed can be found quickly by simple table look-ups.

Now we describe an efficient algorithm to check whether a given positive integer  $m$  belongs to an AP  $(m, n)$  with  $m < n$ . This algorithm is based on the observation that when, for given  $\gamma$  and  $N$ , we want to verify one of the relations  $\sigma(N)/N > \gamma$ ,  $= \gamma$ ,  $< \gamma$ , and when the primes  $2, 3, \dots, p$  have been tried as divisors of  $N$ , it may be possible

(i) to detect, with Lemma 2.1, whether  $\sigma(N)/N < \gamma$  by using the information that the *unfactored* portion of  $N$  only has prime divisors  $> p$ , and

(ii) to detect whether  $\sigma(N)/N > \gamma$  by using the *factored* portion of  $N$ .

In this way, much unnecessary factorization time may be avoided. The price to pay for this gain lies in the time needed to consult the  $P$ - and  $Q$ -tables used in Lemma 2.1. In the algorithm, the index  $i_{\max}$  is the maximum value of  $i$  for which Lemma 2.1 is invoked. In order to restrict this table look-up time,  $i_{\max}$  should not be chosen too large. The optimal value of  $i_{\max}$  also depends on the actual implementation of the algorithm (cf. Section 3).

#### Algorithm to Check Whether $m$ is the Smaller Member of an AP.

*Step 1.* (Find out whether  $m$  is abundant; in this step, keep  $m = m_1 m_2$  where  $\gcd(m_1, m_2) = 1$ ,  $m_1$  is the factored and  $m_2$  is the unfactored portion of  $m$ ,  $\alpha := \sigma(m_1)/m_1$ ; start with  $m_1 := 1$ ,  $m_2 := m$ ,  $\alpha := 1$ .)

Start factoring  $m$  by trial dividing  $m_2$  by the primes  $p_1, p_2, \dots \leq m_2^{1/2}$ . In case a prime power divisor  $p_{i-1}^e$  ( $e \geq 1$ ) of  $m_2$  has been found, update  $m_1$ ,  $m_2$  and  $\alpha$  ( $m_1 := m_1 p_{i-1}^e$ ,  $m_2 := m/m_1$ ,  $\alpha := \alpha \cdot \sigma(p_{i-1}^e)/p_{i-1}^e$ ). After the trial division with  $p_{i-1}$  (whether or not  $p_{i-1}$  divides  $m_2$ ): if  $\alpha < 2$  and  $4 \leq i \leq i_{\max}$ , check whether  $m$

is possibly deficient as follows: by inspecting the  $P$ -table find the smallest value of  $j$  ( $=:j^*$ ) such that  $m_2 < P_{i,j+1}$ ; if  $\alpha Q_{i,j^*} < 2$ , then STOP (because, in that case,  $m$  is deficient: by Lemma 2.1 we have  $\sigma(m_2)/m_2 < Q_{i,j^*}$  so that

$$\frac{\sigma(m)}{m} = \frac{\sigma(m_1)}{m_1} \cdot \frac{\sigma(m_2)}{m_2} = \alpha \frac{\sigma(m_2)}{m_2} < \alpha Q_{i,j^*} < 2).$$

If  $\alpha \geq 2$ , or  $i < 4$  or  $i > i_{\max}$ , the deficiency check on  $m$  is left out. After the complete factorization of  $m$  (and simultaneous computation of  $\sigma(m)$ ): if  $m < \sigma(m) - m =: n$  (i.e.,  $m$  is abundant), go to Step 2, otherwise STOP.

End of Step 1

*Step 2.* (Given  $m$ ,  $\sigma(m)$  and  $n = \sigma(m) - m$ , check whether  $\sigma(n) = \sigma(m)$ ; during the factorization of  $n$  try to exclude those  $m$  for which  $\sigma(n) \neq \sigma(m)$  as early as possible by testing whether  $\sigma(n)/n \neq \beta$  where  $\beta = \sigma(m)/n$ ; in this step, keep  $n = n_1 n_2$ , where  $\gcd(n_1, n_2) = 1$ ,  $n_1$  is the factored and  $n_2$  the unfactored portion of  $n$ ,  $\alpha := \sigma(n_1)/n_1$ ; start with  $n_1 := 1$ ,  $n_2 := n$ ,  $\alpha := 1$ .)

Start factoring  $n$  by trial dividing  $n_2$  by the primes  $p_1, p_2, \dots \leq n_2^{1/2}$ . In case a prime power divisor  $p_{i-1}^e$  ( $e \geq 1$ ) of  $n_2$  has been found, update  $n_1$ ,  $n_2$  and  $\alpha$ : if the updated  $\alpha$  satisfies  $\alpha > \beta$ , then STOP (because, in that case, we have

$$\frac{\sigma(n)}{n} = \frac{\sigma(n_1)}{n_1} \frac{\sigma(n_2)}{n_2} \geq \frac{\sigma(n_1)}{n_1} = \alpha > \beta = \frac{\sigma(m)}{n},$$

so that  $\sigma(n) \neq \sigma(m)$ ). After the trial division with  $p_{i-1}$  (whether or not  $p_{i-1}$  divides  $n_2$ ): if  $4 \leq i \leq i_{\max}$  check whether  $\sigma(n)/n < \beta$  as follows: by inspecting the  $P$ -table find the smallest value of  $j$  ( $=:j^*$ ) such that  $n_2 < P_{i,j+1}$ . If  $\alpha Q_{i,j^*} < \beta$ , then STOP (because, in that case,  $\sigma(n)/n < \beta$ : by Lemma 2.1 we have  $\sigma(n_2)/n_2 < Q_{i,j^*}$  so that

$$\frac{\sigma(n)}{n} = \frac{\sigma(n_1)}{n_1} \cdot \frac{\sigma(n_2)}{n_2} = \alpha \frac{\sigma(n_2)}{n_2} < \alpha Q_{i,j^*} < \beta).$$

If  $i < 4$  or  $i > i_{\max}$ , the check on  $\sigma(n)/n < \beta$  is omitted. After the complete factorization of  $n$  (and simultaneous computation of  $\sigma(n)$ ): check whether  $\sigma(n) = \sigma(m)$ . If so,  $(m, n)$  is an AP.

End of Step 2

**3. Computing All the APs Below  $10^{10}$ .** In order to compute all the APs  $(m, n)$  with  $m < n$  and  $10^8 < m \leq 10^{10}$  (thus extending H. Cohen's computations reported in [4]), we distinguish between  $m \equiv 0 \pmod{6}$  (the easy case), and  $m \not\equiv 0 \pmod{6}$  (the hard case).

If  $m \equiv 0 \pmod{6}$  and  $n = \sigma(m) - m$  is even, then  $(m, n)$  cannot be an AP [5]. Therefore,  $n$  should be odd. In that case, we have [6]  $m = 2^\mu M^2$ ,  $n = N^2$ , with  $\mu \in \mathbb{N}$ ,  $M$  and  $N$  being odd. For all the numbers  $m = 2^\mu M^2$  with  $3 \mid M$  and  $10^8 < m \leq 10^{10}$ , we computed  $n := \sigma(m) - m$  and checked whether  $n$  was a perfect square. Not a single such case was found. Computer time was about 6 CPU seconds.

For all  $m \not\equiv 0 \pmod{6}$  with  $10^8 < m \leq 10^{10}$  we used the algorithm of Section 2 to find all APs in this range. The optimal choice of  $i_{\max}$  for our FORTRAN-implementation on a CYBER 750 was about 75. This value was chosen to be fixed for the whole range. The speed-up factor of our program was about 15, compared with a

straightforward program which, given  $m$ , computes  $\sigma(m)$  and, if  $n := \sigma(m) - m > m$ , computes  $\sigma(n)$ . A slight increase of the speed was obtained as follows. In Step 1, in case a prime (power) factor of  $m_2$  was found and  $m_1$  and  $\sigma(m_1)$  (among others) were updated, it was checked whether both  $m_1$  and  $\sigma(m_1)$  were divisible by one of the primitive abundant numbers  $20 = 2^2 \cdot 5$ ,  $28 = 2^2 \cdot 7$ ,  $70 = 2 \cdot 5 \cdot 7$  and  $88 = 2^3 \cdot 11$ . If so, the algorithm was stopped since this implied that also  $m$  and  $\sigma(m)$ , hence also  $n = \sigma(m) - m$  were divisible by this abundant number, so that both  $m$  and  $n$  were abundant. This is impossible for an AP  $(m, n)$ .

The total time to cover the range  $10^8 < m \leq 10^{10}$  was about 1000 (low priority) CPU hours, spent in the last seven months of 1984.

The total number of APs  $(m, n)$  found with  $m < n$  and  $10^8 < m \leq 10^{10}$  was 1191. In Appendix I (of the supplements section) all the APs with smaller member  $\leq 10^{10}$  are given (including the 236 APs with smaller member  $\leq 10^8$ ). For each pair we list the decimal representation and the prime factorization of the members, a rank number, a code (letter plus digit) referring to the discoverer, and the type of the pair (defined below). For example, pair #1427 reads as follows:

1427	9967523980	2E2.257.5.17.37.3083
R9 42	12890541236	2E2.257.107.117191.

Table 1 gives the meaning of the codes, and their frequencies of occurrence. Extensive information about the sources of the pairs with code L1 is given in the survey paper [6].

There are 1015 pairs with even members and 412 with odd members. The minimal and maximal values of  $m/n$  are 0.6979 and 0.999858 for the APs #567 and #1010, respectively.

Let  $A(x)$  be the number of APs  $(m, n)$  with  $m < n$  and  $m \leq x$ . From the list of APs with  $m \leq 10^8$ , Bratley et al. [3] concluded that for  $x \leq 10^8$ ,  $A(x)$  is approximately proportional to  $x^{1/2}/\ln(x)$ . In Table 2 we give, for  $x = k \cdot 10^9$  ( $1 \leq k \leq 10$ ):  $A(x)$ ,  $A(x)\ln(x)/x^{1/2}$ ,  $A(x)(\ln(x))^2/x^{1/2}$  and  $A(x)(\ln(x))^3/x^{1/2}$ . From these figures we may draw the conclusion that for  $x \leq 10^{10}$ ,  $A(x)$  is approximately proportional to  $x^{1/2}/(\ln(x))^3$ .

TABLE 1

*Status list of the first 1427 APs  $(m, n)$ ,  $m < n$ , with  $m \leq 10^{10}$*

code	#APs	references and remarks
L1	508	[6]
R2	1	[9] (#1056)
W1	73	sent to the author by D. Woods on June 29, 1982 and published in [7]
R3	19	found by the author with the methods described in [8], and published in [7]
W2	1	sent in by D. Woods on Feb. 16, 1983 (#330)
R6	1	found by the author in May, 1983 (#1375)
W3	1	sent in by D. Woods on July 11, 1983 (#1050)
L2	5	sent in by E. J. Lee in July, 1984 (# #778, 860, 894, 1241, 1261)
B4	2	sent in by W. Borho on Nov. 2, 1984 (# #809, 1393)
R9	816	found by the author during the systematic search described in this paper

TABLE 2

*Comparison of  $A(x)$  with  $x^{1/2}/(\ln(x))^i$ ,  $i = 1, 2, 3$*

$x/10^9$	$A(x)$	$A(x)\ln(x)/x^{1/2}$	$A(x)(\ln(x))^2/x^{1/2}$	$A(x)(\ln(x))^3/x^{1/2}$
1	586	0.3840	7.958	164.9
2	762	0.3649	7.815	167.4
3	898	0.3578	7.807	170.4
4	1009	0.3527	7.799	172.4
5	1100	0.3474	7.759	173.3
6	1185	0.3444	7.755	174.6
7	1256	0.3403	7.715	174.9
8	1317	0.3358	7.656	174.6
9	1377	0.3327	7.625	174.8
10	1427	0.3286	7.566	174.2

We define an AP  $(m, n)$ ,  $m < n$ , to be a *regular amicable pair of type  $(i, j)$* , if  $(m, n) = (gM, gN)$ , where  $g = \gcd(m, n)$ ,  $\gcd(g, M) = \gcd(g, N) = 1$ ,  $M$  and  $N$  are squarefree, and the numbers of prime factors of  $M$  and  $N$  are  $i$  and  $j$ , respectively. Other pairs are called *irregular* or *exotic*. There are 1082 regular and 345 irregular APs with smaller member  $\leq 10^{10}$ . It is easy to see that there are no regular pairs of type  $(1, j)$ ,  $j \geq 1$ : let  $g$  be the gcd of such an AP, so that  $(m, n) = (gp, gN)$  where  $p$  is a prime and  $\gcd(g, p) = \gcd(g, N) = 1$ . We have  $m < n$ , hence  $p < N$ . By definition,  $\sigma(gp) = \sigma(gN)$ , implying that  $p + 1 = \sigma(N)$ . Since, for any  $N \in \mathbb{N}$ ,  $\sigma(N) > N$ , this implies that  $p + 1 > N$ , a contradiction. We note that in this argument  $N$  need not be squarefree.

In Table 3 we give the frequency distribution of the various types among the first 1082 regular APs. We note that there are relatively few regular APs of type  $(i, 1)$ ,  $i \geq 2$ , and of type  $(i, j)$  with  $i < j$ .

In [7] the total number of known APs with smaller member  $\leq 10^{10}$  was 601 (these are the APs belonging to the first four codes in Table 1). Among them were 104 irregular APs, i.e., 17.3%. Comparing this figure with the 345 irregular APs in our *complete* list of APs with smaller member  $\leq 10^{10}$ , i.e., 24.2%, we see that relatively many irregular APs were found in our systematic search.

In Appendix II (of the supplements section) we present lists of all the 1082 regular APs arranged according to their types, together with a list of the 345 exotic APs. This appendix may be useful for searches of APs of a special type.

The regular pairs of type  $(i, 1)$ ,  $i \geq 2$ , play an important role as “mother” pairs in methods to generate new APs from given pairs. In [8] a substantial part of the new APs found there was constructed from such mother pairs. In [1], Borho and Hoffmann have partially generalized the methods from [8] by introducing the concept of a *breeder*: a breeder is a pair of positive integers  $(a_1, a_2)$  such that the equations

$$a_1 + a_2 x = \sigma(a_1) = \sigma(a_2)(x + 1)$$

TABLE 3  
*Frequency distribution of the first 1082 regular APs  
of type  $(i, j)$ ,  $i \geq 2$ ,  $j \geq 1$*

$i =$	$j =$	1	2	3	4	5	row totals
2		20	67	21	4	0	112
3		16	271	280	24	0	591
4		1	78	201	63	2	345
5		0	6	18	7	3	34
column totals		37	422	520	98	5	1082

have a positive integer solution  $x$ . If  $x$  is a prime, then  $(a_1, a_2x)$  is an amicable pair. For certain breeders, called “special” breeders, Borho and Hoffmann formulate the following

**THEOREM 1** [1]. *Let  $(a_1, a_2)$  be a special breeder, i.e.,  $a_1 = au$ ,  $a_2 = a$ , with  $\gcd(a, u) = 1$ . Take any factorization of  $C := \sigma(u)(u + \sigma(u) - 1)$  into two different factors  $D_1, D_2$  ( $C = D_1D_2$ ). Then, if the numbers  $s_i = D_i + \sigma(u) - 1$ , for  $i = 1, 2$ , and also  $q = u + s_1 + s_2$  are primes not dividing  $a$ , then  $(auq, as_1s_2)$  is an amicable pair.*  $\square$

Regular APs of type  $(i, 1)$ ,  $i \geq 2$ , are of the form  $(au, ap)$ ,  $p$  prime, and the numbers  $(au, a)$  are special breeders which generally produce many APs with the above theorem.

In our list of 1427 APs we found a few APs, e.g., #647 and #955, which suggested that the condition  $\gcd(a, u) = 1$  in Theorem 1 may be dropped. In fact, we have

**THEOREM 2.** *Let  $(au, a)$  be a breeder, i.e., there exists a positive integer  $x$  such that  $au + ax = \sigma(au) = \sigma(a)(x + 1)$ . Take any factorization of  $C := (x + 1)(x + u)$  into two different factors  $D_1, D_2$  ( $C = D_1D_2$ ). Then, if the numbers  $s_i = D_i + x$ , for  $i = 1, 2$ , and also  $q = u + s_1 + s_2$  are primes not dividing  $a$ , then  $(auq, as_1s_2)$  is an amicable pair.*  $\square$

The proof of this theorem is left to the reader.

If  $\gcd(a, u) = 1$ , then  $\sigma(au) = \sigma(a)\sigma(u)$ , so that  $x = \sigma(u) - 1$  and Theorem 2 reduces to Theorem 1. As an example, AP #955 gives the breeder  $(au, a)$  with  $a = 3.5.7.19$  and  $u = 7.29.47.181$ . Theorem 2 yields 16 new APs with this breeder as input.

It is known [5] that most even APs have a pair sum which is  $\equiv 0 \pmod{9}$ . Our search proves that indeed Poulet’s pair #503:  $(2^4331.19.6619, 2^4331.199.661)$  is the smallest exceptional pair. All known exceptional pairs had members  $\equiv 7 \pmod{9}$  and a pair sum  $\equiv 5 \pmod{9}$ . In our search, we found two even APs with pair sum  $\equiv 3 \pmod{9}$ , viz., the (irregular) pairs:

$$\#577: 2^4 \left\{ \begin{array}{l} 19^2 103.1627 \\ 3847.16763 \end{array} \right\} \quad \text{and} \quad \#874: 2^2 19 \left\{ \begin{array}{l} 13^2 37.43.139 \\ 41.151.6709 \end{array} \right\}$$

TABLE 4  
*The 17 APs among the first 1427, whose pair sum is  $\not\equiv 0 \pmod{9}$*

	even members	odd members
regular	# 503, type (2,2)	# 899, type (3,2)
	# 1031, type (2,2)	# 1057, type (2,2)
	# 1081, type (2,2)	# 1158, type (3,2)
irregular	# # 577, 874	# # 7, 38, 78, 113, 256, 440, 1083, 1175, 1380

TABLE 5  
*All (37) pairs from the first 1427 APs having the same pair sum*

rank numbers	pair sum	prime decomposition of the pair sum, i.e., exponents belonging to the primes										
		2	3	5	7	11	13	17	19	23	31	37
32	35	1296000	7	4	3							
105	109	20528640	9	6	1			1				
137	138	37739520	10	4	1	1			1			
172	173	75479040	11	4	1	1			1			
272	276	321408000	10	4	3							1
282	286	348364800	13	5	2	1						
350	351	556839360	6	6	1	1	1					1
347	355	579156480	9	5	1	2					1	
373	375	638668800	12	4	2	1	1					
368	377	661893120	12	5	1	1				1		
395	399	761177088	10	5		1			1	1		
411	415	796340160	6	5	1	2	1			1		
427	433	883872000	8	4	3		1					1
462	476	1181174400	7	5	2	2						1
486	491	1282417920	8	5	1	1			1		1	
574	582	2068416000	9	5	3	1						
626	630	2395008000	10	5	3	1	1					
653	665	2682408960	12	5	1	2	1					
695	697	3155023872	11	4		1	1	1				
717	730	3599769600	13	4	2	1						1
751	753	4049740800	10	6	2	1						1
798	807	4606156800	13	3	2	2		1				
786	787	4716601344	13	2		1		1	1			1
824	840	5094835200	10	7	2	1		1				
940	941	6824563200	9	3	2	2		1				1
926	952	6897623040	13	7	1	1	1					
997	998	7925299200	11	5	2	2		1				
1012	1019	8273664000	11	5	3	1				1		
1069	1097	10027929600	12	5	2			1				1
1124	1142	11195712000	9	3	3		1		1			1
1147	1150	11416204800	9	4	2	1	2	1				
1143	1181	12098211840	12	5	1		1	1	1			
1232	1233	13473008640	10	5	1	2		1	1			
1254	1265	14341017600	12	4	2	1		1		1		
1249	1255	14478912000	9	5	3	2				1		
1272	1278	15058068480	10	5	1	2		1		1		
1410	1425	19926466560	14	5	1	1	1	1				

These are the first two examples of APs of the form described in [5, Theorem I, case (b)] (also cf. the remarks immediately following Table I in [5]). Table 4 gives the rank numbers of the 17 APs with smaller member  $\leq 10^{10}$  whose pair sum is  $\not\equiv 0 \pmod{9}$ , divided into even and odd pairs, and regular and irregular pairs.

Another question, suggested by Professor C. Pomerance, is whether pairs, triples, quadruples, etc. of APs exist having the *same pair sum*. Among the first 1427 APs, we found 37 such pairs of APs, but no such triples, quadruples, etc. Table 5 gives the rank numbers of these pairs of APs, and the prime factorization of their pair sums. The pair sums only have prime divisors  $\leq 37$ . In 30 of the 37 cases at least one member of the pair was found during the exhaustive search described in the present paper.

In Appendix III (of the supplements section) we tabulate all the greatest common divisors of the first 1427 APs, ordered according to their size, with frequencies, and with the rank numbers of all the APs corresponding to a given gcd. This might be useful in further searches for special APs, and in searches for so-called *isotopic* APs (cf., [6, p. 83]). For example, new APs, isotopic with APs from the list of 1427 APs, are obtained by replacing the common factor  $3^3 5$  in # # 882 and 1087 by  $3^2 7 \cdot 13$ , by replacing the common factor  $3^3 5^3$  in # 1205 by  $3^2 5^2 31$ , and by replacing the common factor  $3^3 5^2 31$  in # # 717 and 1228 by  $3^6 5 \cdot 23 \cdot 137 \cdot 547 \cdot 1093$ , and by  $3^{10} 5 \cdot 23 \cdot 107 \cdot 3851$ .

In [8], we have presented methods to find new APs from known APs. By applying these methods to the new APs among the first 1427 APs, we have found 117 new APs (with smaller member  $> 10^{10}$ ). The new APs were found mainly from mother pairs having a relatively simple structure, like those of type  $(i, 1)$ ,  $i > 1$ . They will be published in a forthcoming report [2], together with many other new amicable pairs.

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1. W. BORHO & H. HOFFMANN, "Breeding amicable numbers in abundance," *Math. Comp.*, v. 46, 1986, pp. 281–293.
2. W. BORHO, H. HOFFMANN & H. J. J. TE RIELE, *Table of Amicable Pairs Between  $10^{10}$  and  $10^{52}$* , CWI-report. (In preparation.)
3. P. BRATLEY, F. LUNNON & JOHN MCKAY, "Amicable numbers and their distribution," *Math. Comp.*, v. 24, 1970, pp. 431–432.
4. H. COHEN, "On amicable and sociable numbers," *Math. Comp.*, v. 24, 1970, pp. 423–429.
5. E. J. LEE, "On divisibility by nine of the sums of even amicable pairs," *Math. Comp.*, v. 23, 1969, pp. 545–548.
6. E. J. LEE & J. S. MADACHY, "The history and discovery of amicable numbers," *J. Recreational Math.*, v. 5, 1972; Part I: pp. 77–93, Part II: pp. 153–173, Part III: pp. 231–249.
7. H. J. J. TE RIELE, *Table of 1869 New Amicable Pairs Generated from 1575 Mother Pairs*, Report NN 27/82, Math. Centre, Amsterdam, Oct. 1982.
8. H. J. J. TE RIELE, "On generating new amicable pairs from given amicable pairs," *Math. Comp.*, v. 42, 1984, pp. 219–223.
9. H. J. J. TE RIELE, *Further Results on Unitary Aliquot Sequences*, Report NW 2/78, Math. Centre, Amsterdam, 2nd ed., Jan. 1978.

## Supplement to Computation of All the Amicable Pairs Below $10^{10}$

By H. J. J. te Riele

### Appendix I

The first 1427 APs

1 220 2E2.5.11	3D	31 600392 2E3.13.23.251	6D
L1 21 284 2E2.71		L1 32 669688 2E3.97.863	
2 1184 2E5.37		32 669928 2E3.11.29.239	
L1 X 1210 2.5.11E2		L1 32 686072 2E3.191.449	
3 2620 2E2.5.131		33 624184 2E3.11.17.173	
L1 22 2924 2E2.17.43		L1 32 691256 2E3.71.1217	
4 5020 2E2.5.251		34 635624 2E3.11.31.233	
L1 22 5564 2E2.13.187		L1 32 712216 2E3.127.701	
5 6232 2E3.19.41		35 643336 2E3.29.47.59	
L1 X 6368 2E5.199		L1 32 652664 2E3.17.4799	
6 10744 2E3.17.79		36 667964 2E2.11.17.19.47	
L1 22 10856 2E3.23.59		L1 43 783556 2E2.31.71.89	
7 12285 3E3.5.7.13		37 726164 2E3.17.19.281	
L1 X 14595 3.5.7.139		L1 32 796696 2E3.53.1879	
8 17296 2E4.23.47		38 882725 3.5E2.7.11.139	
L1 21 18416 2E4.1151		L1 X 863835 3.5.7.19.433	
9 63020 2E2.23.5.137		39 879712 2E5.37.743	
L1 21 76084 2E2.23.827		L1 X 901424 2E4.53.1963	
10 66928 2E4.47.89		40 889216 2E3.11.59.173	
L1 22 66992 2E4.53.79		L1 32 980984 2E3.47.2609	
11 67095 3E3.5.7.71		41 947835 3E3.5.7.17.59	
L1 22 71145 3E3.5.17.31		L1 32 1125765 3E3.5.31.269	
12 69615 3E2.7.13.5.17		42 998104 2E3.17.41.179	
L1 21 87633 3E2.7.13.187		L1 32 1043099 2E3.23.5669	
13 79750 2.5E3.11.29		43 1077890 2.5.11.41.239	
L1 X 88730 2.5.19.467		L1 33 1099390 2.5.17.29.223	
14 100485 3E2.5.7.11.29		44 1154456 2.5E2.11.2099	
L1 32 124155 3E2.5.31.89		L1 22 1189150 2.5E2.17.1399	
15 122265 3E2.5.13.11.19		45 1156870 2.5.11.13.809	
L1 21 139815 3E2.5.13.239		L1 32 1292570 2.5.19.6803	
16 123268 2E9.239		46 1175265 3E2.7E2.13.5.41	
L1 X 123152 2E4.43.179		L1 21 1438983 3E2.7E2.13.251	
17 141664 2E5.19.233		47 1185376 2E5.17.2179	
L1 X 153176 2E3.41.467		L1 X 1286744 2E3.41.3923	
18 142310 2.5.7.19.107		48 1280565 3E2.5.13.11.199	
L1 32 168730 2.5.47.359		L1 22 1340235 3E2.5.13.29.79	
19 171856 2E4.23.467		49 1328470 2.5.11.13.929	
L1 22 176336 2E4.103.187		L1 X 1493850 2.5E2.59.503	
20 176272 2E4.23.479		50 1358595 3E2.5.19.7.227	
L1 22 180848 2E4.89.127		L1 22 1486845 3E2.5.19.37.47	
21 185368 2E3.17.29.47		51 1392368 2E4.17.5119	
L1 32 203432 2E3.59.431		L1 22 1464592 2E4.239.383	
22 196724 2E2.11.17.263		52 1466150 2.5E2.7.59.71	
L1 22 202444 2E2.11.43.107		L1 X 1747930 2.5.47.3719	
23 280540 2E2.5.13E2.83		53 1468324 2E2.11.13.17.151	
L1 X 365084 2E2.107.853		L1 43 1749212 2E2.37.53.223	
24 308620 2E2.5.13.1187		54 1511930 2.5.7.21599	
L1 32 389924 2E2.43.2267		L1 23 1598470 2.5.19.47.179	
25 319550 2.7.5E2.11.83		55 1669910 2.5.11.17.19.47	
L1 X 430402 2.7.71.433		L1 42 2062570 2.5.239.863	
26 356408 2E3.13.23.149		56 1798875 3E3.5E3.13.41	
L1 32 399592 2E3.199.251		L1 X 1870245 3E2.5.13.23.139	
27 437456 2E4.19.1439		57 2082464 2E5.59.1103	
L1 22 455344 2E4.149.191		L1 22 2090656 2E5.79.827	
28 469028 2E2.7E2.2393		58 2236570 2.5.7.89.359	
L1 X 486178 2.7E2.11E2.41		L1 33 2429030 2.5.23.59.179	
29 503056 2E4.23.1367		59 2652728 2E3.13.23.1109	
L1 22 514736 2E4.53.607		L1 32 2941672 2E3.71.5179	
30 522405 3E2.5.13.19.47		60 2723792 2E4.37.43.107	
L1 22 525915 3E2.5.13.29.31		L1 32 2874064 2E4.263.683	

61	2720726	2,7,11,13,29,47	7D	L1	91	757350	2,562,11,23,599	L1	121	12397552	254,23,59,571	L1	151	23358248	2E3,37,23,47,73
L1	41	307354	2,7,19,23,581	L1	32	849050	2,562,59,287	L1	32	13136528	2E3,37,82,27	L1	31	25233112	2E3,37,82,27
L1	62	239708	2,63,11,161,91	L1	92	767248	286,119,863	L1	122	1270704	253,17,41,43,53	L1	152	1396995	3E3,5,17,47,233
L1	32	292136	263,31,1,807	L1	122	7681672	266,167,719	L1	42	14236136	253,19,7E,21,863	L1	153	2513255	3E3,5,17,47,233
L1	63	280416	264,17,1093	L1	93	800544	265,43,569	L1	123	13677173	3,5,19,7E,21,863	L1	154	2668890	2E3,5,37,82,27
L1	22	294216	264,167,1103	L1	X	7916696	263,17,581	L1	X	15877065	3,5,19,17,29,113	L1	X	2748276	2E2,17,29,113
L1	64	280589	262,5,13,41,263	L1	94	856512	264,17,89,169	L1	124	13811350	2,582,29,79,269	L1	154	2748276	2E2,17,16,87
L1	42	271654	262,50,1,147	L1	X	805488	263,2,7,89,169	L1	124	14160558	2,582,29,79,139	L1	154	30355216	2E2,4,17,107,1511
L1	65	278856	263,11,23,1619	L1	95	865136	263,7,79,79	L1	125	15921528	263,19,67,1367	L1	155	2566554	2E2,7,31,11,643
L1	12	270554	233,64,719	L1	125	15986772	263,11,161,503	L1	125	15986772	263,11,161,503	L1	155	2566554	2E2,7,31,11,643
L1	66	308858	2,562,1,13,179	L1	96	863964	233,29,4,893	L1	126	16411680	233,17,47,229	L1	156	2668892	2E4,47,32,27,9
L1	67	389670	2,5,31,19,433	L1	126	949855	3,5,11,2,43,59	L1	126	16411680	233,17,47,229	L1	156	2668892	2E4,47,32,27,9
L1	13	378904	263,11,2,3,1871	L1	97	866880	3E3,1,2,81,227	L1	127	16422316	2,5,13,83,19	L1	157	2668893	3E2,11,59,1779
L1	32	430036	263,6,7,151	L1	98	1368336	3E2,4,7,19,79	L1	128	16422316	2,5,13,83,19	L1	157	2668893	3E2,11,59,1779
L1	68	380826	264,29,5,139	L1	98	7871159	5,7,1,11369	L1	128	16422316	2,5,13,83,19	L1	157	2668893	3E2,11,59,1779
L1	12	406636	264,17,179,1399	L1	99	886070	2,5,11,19,103	L1	129	15986772	2,5,19,77,457	L1	158	2668894	3E3,12,11,643
L1	69	231984	263,11,23,1439	L1	99	886070	2,5,11,19,103	L1	129	15986772	2,5,19,77,457	L1	158	2668894	3E3,12,11,643
L1	43	431661	233,11,131,179	L1	130	100399	2,5,31,179,81	L1	130	16411680	2,5,18,79,179	L1	159	2668894	3E3,12,11,643
L1	78	4246130	2,5,31,7,66559	L1	100	9671685	3E2,5,31,179,81	L1	130	15986772	2,5,18,79,179	L1	159	2668894	3E3,12,11,643
L1	23	4489110	2,5,23,29,673	L1	122	9498155	3E2,5,31,161,619	L1	131	1533334	2,55,22,21,1	L1	160	2668894	3E3,12,11,643
L1	71	4259750	2,53,11,1549	L1	101	919496	263,3,29,19,2887	L1	131	1533334	2,55,22,21,1	L1	160	2668894	3E3,12,11,643
L1	X	4494058	2,582,19,16779	L1	122	9208935	263,29,171,219	L1	132	1533334	2,55,22,21,1	L1	160	2668894	3E3,12,11,643
L1	72	4482765	3E2,5,19,7E2,107	L1	102	9208935	3,862,5,13,266	L1	132	1533334	2,55,22,21,1	L1	160	2668894	3E3,12,11,643
L1	X	1079775	3,5,7,79,1301	L1	X	1079775	3,5,7,79,1301	L1	133	1533334	2,55,22,21,1	L1	160	2668894	3E3,12,11,643
L1	73	5322115	3E2,5,19,33,113	L1	103	9339704	263,11,11,303	L1	133	16137622	232,13,13,19,131	L1	161	2668894	3E3,12,11,643
L1	74	6139692	2,7,71,13,17,293	L1	133	9362316	233,11,47,337	L1	133	16137622	232,13,13,19,131	L1	161	2668894	3E3,12,11,643
L1	75	6162444	233,11,11,571	L1	104	936584	237,19,19,383	L1	134	1671582	2,7E3,19,13,17,41	L1	162	2668894	3E3,12,11,643
L1	X	5122099	2,5,7,16,3,449	L1	105	947056	237,73,27,727	L1	134	19256598	2,7E3,19,97,107	L1	162	2668894	3E3,12,11,643
L1	33	5104091	2,5,19,59,491	L1	105	9478910	2,5,7,19,7127	L1	135	17841010	2,5,7,31,7853	L1	163	2668894	3E3,12,11,643
L1	76	5147032	233,11,25,253	L1	106	9491765	3E2,5,13,11,59	L1	135	1915W22	2,7,13,43,247	L1	163	2665256	2E2,17,47,79,139
L1	32	5640484	233,383,1997	L1	106	9491765	3E2,5,13,11,59	L1	136	17257695	3,5,7,13,47,269	L1	164	2665256	2E2,17,47,79,139
L1	77	5120595	3E2,5,19,33,113	L1	107	9491765	3E2,5,13,11,59	L1	137	17578785	3,5,7,23,39,197	L1	165	2665256	2E2,17,47,79,139
L1	73	5322115	3E2,5,19,33,113	L1	107	9491765	3E2,5,13,11,59	L1	137	1775165	3E2,5,13,11,31,89	L1	167	35501825	2E5,13,31,79,107
L1	74	607776	233,11,1822,67,71	L1	108	9502509	2,5,11,91139	L1	138	1988355	3E2,5,13,11,47,33	L1	168	35501825	2E5,13,11,47,33
L1	X	5162444	233,11,11,571	L1	108	9573505	3E2,5,13,11,47,33	L1	138	19844255	3E2,5,13,11,47,33	L1	168	35501825	2E5,13,11,47,33
L1	75	5122099	2,5,7,16,3,449	L1	108	9573505	3E2,5,13,11,47,33	L1	139	19995265	3E2,5,13,11,47,33	L1	169	35501825	2E5,13,11,47,33
L1	33	5104091	2,5,19,59,491	L1	109	10245490	2,5,11,759	L1	140	19995265	3E2,5,13,11,47,33	L1	169	35501825	2E5,13,11,47,33
L1	76	5121300	2,5,17,179,191	L1	110	10221656	2,5,11,583	L1	141	18014808	2,5,11,79,1727	L1	170	3475731	2E2,17,73,113,227
L1	88	5159717	263,17,17,23,233	L1	110	10531206	2E4,19,3699	L1	142	18576312	2,5,11,79,1727	L1	171	3475731	2E2,17,73,113,227
L1	X	5159717	263,17,17,23,233	L1	110	1099704	2E3,29,109,43	L1	143	18166388	233,17,13,23,37,113	L1	171	3475731	2E2,17,73,113,227
L1	81	5159942	2,7,72,23,1823	L1	111	1099990	2,5,11,89,167	L1	144	18194015	3E2,5,13,23,37,113	L1	172	3475731	2E2,17,73,113,227
L1	78	5157625	3,7,13,23,183	L1	111	1099990	2,5,11,89,167	L1	145	22446105	3E2,5,13,23,37,113	L1	172	3475731	2E2,17,73,113,227
L1	5684679	3E2,7,13,23,183	L1	112	1099990	2,5,11,89,167	L1	146	22446105	3E2,5,13,23,37,113	L1	172	3475731	2E2,17,73,113,227	
L1	79	5581110	2,5,17,179,191	L1	112	1099990	2,5,11,89,167	L1	147	19154336	2,55,61,9,967	L1	173	3475731	2E2,17,73,113,227
L1	33	5121300	2,5,17,179,191	L1	112	1099990	2,5,11,89,167	L1	148	20014808	2,55,61,9,967	L1	173	3475731	2E2,17,73,113,227
L1	76	5159717	263,17,17,23,233	L1	113	1099990	2,5,11,89,167	L1	149	21457192	2,55,61,9,967	L1	173	3475731	2E2,17,73,113,227
L1	84	6329416	233,23,1,3,139	L1	114	10999735	3E2,5,13,19,2,43	L1	150	20022222	2,55,61,9,967	L1	174	3475731	2E2,17,73,113,227
L1	33	5171184	233,23,1,3,139	L1	114	10999735	3E2,5,13,19,2,43	L1	151	2242332	2,55,61,9,967	L1	174	3475731	2E2,17,73,113,227
L1	85	6317184	3E2,5,13,19,127	L1	115	1117680	3E2,5,13,19,127	L1	152	2242332	2,55,61,9,967	L1	175	3475731	2E2,17,73,113,227
L1	22	6689025	3E3,5,11,2299	L1	115	1117680	3E2,5,13,19,127	L1	152	2242332	2,55,61,9,967	L1	175	3475731	2E2,17,73,113,227
L1	86	6552151	234,19,37,167	L1	116	11125518	2E3,11,71,1801	L1	153	2242332	2,55,61,9,967	L1	175	3475731	2E2,17,73,113,227
L1	31	7418864	234,4,3679	L1	117	11201272	2E3,67,107,211	L1	154	2242332	2,55,61,9,967	L1	175	3475731	2E2,17,73,113,227
L1	87	6399310	2,5,13,23,2339	L1	117	11498355	3E4,5,11,29,89	L1	155	2244425	3E3,5,11,23,23,239	L1	176	3475731	2E2,17,73,113,227
L1	22	7158719	2,5,13,23,23,2339	L1	117	12021045	3E4,5,11,2699	L1	156	2244425	3E3,5,11,23,23,239	L1	176	3475731	2E2,17,73,113,227
L1	88	7275332	262,11,37,41,109	L1	118	11546166	2E4,19,163,233	L1	157	2249532	2B3,38,13,47,43	L1	177	3475731	2E2,17,73,113,227
L1	X	7471908	262,11,23,13,359	L1	119	11693290	2,7,5,16,047	L1	158	2298145	3E3,5,11,23,659	L1	178	3475731	2E2,17,73,113,227
L1	43	8221998	2,11,5,23,43,67	L1	119	12361622	2,7,82,13,31,313	L1	159	2311155	3E3,5,11,23,659	L1	179	3475731	2E2,17,73,113,227
L1	90	789112	263,17,53,1039	L1	120	1198594	2E5,11,2619	L1	160	2268832	2B3,33,19,23,29,23	L1	180	3475731	2E2,17,73,113,227
L1	33	7674088	263,23,17,23,2339	L1	120	1337336	2E3,107,15581	L1	161	34067814	2E3,29,271,647	L1	181	34067814	2E3,29,271,647

L1	181	38633950	2.5E2	1.3	17.3499	8D	L1	211	72958556	E2	1.1	19.1943	241	108744050	2.5E2	31.29.41.59	9D	L1	271	148077644	E2	13.11.	83.3119			
L1	182	4322850	2.E2	1.1	16.699	L1	211	72958556	E2	1.1	19.1943	L1	132	11621550	2.5E2	31.17.49	L1	132	16120436	E2	13.47.6519					
L1	182	5880599	2E3	1.1	17.0019	L1	212	73032877	E3	1.1	16.689	L1	132	10940345	3E4	1.5.11.41.59	L1	132	16015550	2.5E2	19.23.47.149					
L1	182	11644468	2E3	1.1	15.797	L1	213	73465952	E3	1.5	17.2003	L1	122	11060710	3E4	1.5.11.59.419	L1	122	16339450	2.5E2	19.89.479					
L1	183	28877958	2E5	1.1	17.449	L1	213	73465952	E4	2.1	6.1	L1	122	11060710	2.5	6.7	L1	122	1590750	2.7E2	13.41.307					
L1	183	10992232	2E5	1.1	16.553	L1	213	73664448	E4	1.9	17.179	L1	132	12522230	2.5	6.7	L1	132	19889998	2.7E2	13.43.9.467					
L1	184	3396594	2E3	1.1	17.459	L1	213	73823303	E2	5.1	17.179	L1	244	114914072	E3	1.7.19.44483	L1	244	17455786	2.5E2	12.3.22.34.9.883					
L1	184	1718946	2E3	1.1	17.459	L1	213	73823303	E2	5.1	17.179	L1	244	114914072	E3	1.7.19.44483	L1	244	17610492	2.5E2	13.41.67.633					
L1	185	14118986	2E3	1.1	17.459	L1	213	73823303	E2	5.1	17.179	L1	244	114914072	E3	1.7.19.44483	L1	244	17610492	2.5E2	13.41.67.633					
L1	185	14118986	2E3	1.1	17.459	L1	215	73823303	E2	5.1	17.179	L1	245	11529958	2.5	6.7	L1	245	15797398	2.5E2	13.41.67.633					
L1	185	14118986	2E3	1.1	17.459	L1	215	73823303	E2	5.1	17.179	L1	245	11529958	2.5	6.7	L1	245	15797398	2.5E2	13.41.67.633					
L1	186	523334	2E3	1.1	15.541	L1	215	73823303	E2	5.1	17.179	L1	245	11529958	2.5	6.7	L1	245	15797398	2.5E2	13.41.67.633					
L1	186	1623716	2E3	1.1	15.541	L1	216	73178985	E3	5.3	17.349	L1	246	11547755	E3	5.3.15.1.467	L1	246	1582856	2.5E2	13.41.67.633					
L1	187	1623716	2E3	1.1	15.541	L1	216	73178985	E3	5.3	17.349	L1	246	11547755	E3	5.3.15.1.467	L1	246	1582856	2.5E2	13.41.67.633					
L1	187	1623716	2E3	1.1	15.541	L1	217	72379792	E3	5.1	15.4489	L1	247	1157934	E3	5.4.1.7.6.103	L1	247	157934	2.5E2	13.41.67.633					
L1	187	1623716	2E3	1.1	15.541	L1	217	72379792	E3	5.1	15.4489	L1	247	1157934	E3	5.4.1.7.6.103	L1	247	157934	2.5E2	13.41.67.633					
L1	188	4621745	2E2	5.1	19.1591	L1	217	72379792	E3	5.1	15.4489	L1	248	11664486	E2	5.1.35.49.883	L1	248	16081158	2.5	6.7	L1	248	16081158	2.5E2	13.41.67.633
L1	188	4621745	2E2	5.1	19.1591	L1	218	7088504	E3	5.1	15.545	L1	249	11815664	E2	1.101.23.31.161.227	L1	249	16081158	2.5	6.7	L1	249	16081158	2.5E2	13.41.67.633
L1	189	4651345	3E2	5.1	19.359	L1	218	7088504	E3	5.1	15.545	L1	249	11815664	E2	1.101.23.31.161.227	L1	249	16081158	2.5	6.7	L1	249	16081158	2.5E2	13.41.67.633
L1	189	4651345	3E2	5.1	19.359	L1	219	7088504	E3	5.1	15.545	L1	249	11815664	E2	1.101.23.31.161.227	L1	249	16081158	2.5	6.7	L1	249	16081158	2.5E2	13.41.67.633
L1	189	4651345	3E2	5.1	19.359	L1	219	7088504	E3	5.1	15.545	L1	249	11815664	E2	1.101.23.31.161.227	L1	249	16081158	2.5	6.7	L1	249	16081158	2.5E2	13.41.67.633
L1	189	4651345	3E2	5.1	19.359	L1	219	7088504	E3	5.1	15.545	L1	249	11815664	E2	1.101.23.31.161.227	L1	249	16081158	2.5	6.7	L1	249	16081158	2.5E2	13.41.67.633
L1	189	4651345	3E2	5.1	19.359	L1	220	73124278	E2	5.1	15.541	L1	250	11842175	E3	5.1.11.53.307	L1	250	11842175	2.5E2	13.41.67.633					
L1	189	4655259	2.5E2	5.1	17.179	L1	220	73124278	E2	5.1	15.541	L1	250	11842175	E3	5.1.11.53.307	L1	250	11842175	2.5E2	13.41.67.633					
L1	189	5880599	2.5E2	5.1	17.179	L1	220	73124278	E2	5.1	15.541	L1	250	11842175	E3	5.1.11.53.307	L1	250	11842175	2.5E2	13.41.67.633					
L1	190	46411890	2.5E2	5.1	17.179	L1	221	84423335	E3	5.1	15.541	L1	251	11869004	E2	5.1.11.61.103	L1	251	11869004	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	221	84423335	E3	5.1	15.541	L1	251	11869004	E2	5.1.11.61.103	L1	251	11869004	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	222	82677734	E3	5.1	15.541	L1	252	11860045	E2	5.1.11.61.103	L1	252	11860045	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	222	82677734	E3	5.1	15.541	L1	252	11860045	E2	5.1.11.61.103	L1	252	11860045	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	223	82677734	E3	5.1	15.541	L1	252	11860045	E2	5.1.11.61.103	L1	252	11860045	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	223	82677734	E3	5.1	15.541	L1	252	11860045	E2	5.1.11.61.103	L1	252	11860045	E2	5.1.11.61.103					
L1	190	46411890	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166	2.5E2	5.1	17.179	L1	224	845121745	E3	5.1	15.541	L1	253	11863395	E2	5.1.11.61.103	L1	253	11863395	E2	5.1.11.61.103					
L1	191	49215166																								

301	199880155	382, 5, 17, 19, 23, 459	352, 5, 7, 11, 17, 459	90	L1, 331	250876395	283, 19, 53, 36721	90	R9, 43	391, 347401035	383, 5, 17, 19, 21, 257
R9, 42	194954085	382, 5, 7, 16, 17, 759	382, 5, 7, 16, 17, 459	90	L1, 43	250876395	283, 19, 53, 36721	90	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
382	19585155	382, 5, 13, 19, 67, 263	332, 25, 12, 27, 70, 2, 11, 23, 71, 139	99	L1, 33	250876395	283, 19, 53, 36721	90	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, X	19611265	383, 1, 13, 19, 4861	383, 1, 13, 19, 4861	99	R9, 44	271245810	283, 19, 53, 36721	90	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
303	19642175	382, 5, 19, 37, 7, 887	382, 5, 19, 37, 7, 887	99	L1, 33	2525108	283, 17, 31, 37, 161, 19	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 32	22470405	382, 5, 19, 37, 7, 183	382, 5, 19, 37, 7, 183	99	R9, 43	27927752	283, 1, 19, 127, 137	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
304	19943948	382, 5, 19, 37, 7, 2309	382, 5, 19, 37, 7, 2309	99	L1, 33	252494845	382, 5, 11, 13, 21, 23, 17789	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, X	21348172	282, 11, 13, 151, 2309	282, 11, 13, 151, 2309	99	L1, 32	252494876	382, 5, 11, 13, 19, 17789	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
305	20032232	283, 13, 151, 2265	283, 13, 151, 2265	99	L1, 33	253103776	283, 5, 99, 83, 1619	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, X	20679368	285, 6, 42, 199	285, 6, 42, 199	99	L1, 32	26678826	285, 449, 10143	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
306	20887055	383, 5, 13, 17, 6733	383, 5, 13, 17, 6733	99	L1, 33	265675056	284, 19, 79, 10691	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, X	20839265	385, 5, 13, 19, 73, 179	385, 5, 13, 19, 73, 179	99	L1, 32	27316844	284, 24, 2591, 6599	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
307	20116592	284, 29, 491, 883	284, 29, 491, 883	99	L1, 33	25648865	383, 5, 11, 23, 57523	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 32	203314448	284, 67, 89, 231	284, 67, 89, 231	99	L1, 22	263110818	383, 5, 11, 53, 33434	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
308	20195622	284, 7, 19, 11, 29, 2393	284, 7, 19, 11, 29, 2393	99	L1, 33	258804646	284, 7, 13, 11, 79, 1637	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, X	206622578	2, 7, 72, 19, 31, 89	2, 7, 72, 19, 31, 89	99	L1, 33	266948334	2, 7, 13, 23, 59, 1091	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
309	201997715	283, 31, 1192	283, 31, 1192	99	L1, 33	266931192	283, 13, 659, 3197	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, X	20747525	IB3, 31, 31, 431	IB3, 31, 31, 431	99	L1, 33	266171608	283, 19, 593, 953	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
310	2041334385	3, 5, 7, 13, 17, 19, 463	3, 5, 7, 13, 17, 19, 463	99	L1, 34	264166336	2, 5, 17, 13, 47, 224	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 42	24486135	3, 5, 7, 18, 638, 688, 230	3, 5, 7, 18, 638, 688, 230	99	L1, 32	29041170	2, 5, 17, 13, 559, 4159	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 31	204755904	283, 11, 59, 113, 349	283, 11, 59, 113, 349	99	L1, 34	2655192208	284, 131, 21, 501	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 43	226165998	283, 79, 449, 97	283, 79, 449, 97	99	L1, 32	26548908	284, 131, 21, 501	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 32	205843365	382, 7, 21, 5, 43, 167	382, 7, 21, 5, 43, 167	99	L1, 34	26717135	382, 5, 16, 11, 23, 479	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 31	252662283	382, 7, 21, 13, 4331	382, 7, 21, 13, 4331	99	R9, X	247979705	382, 5, 16, 127, 663	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
L1, 31	299616626	382, 11, 13, 23, 547	382, 11, 13, 23, 547	99	R9, 53	25082991	283, 5, 16, 127, 663	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, X	26104556	283, 5, 16, 127, 663	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16, 23, 547	283, 11, 16, 23, 547	99	R9, 53	250829936	283, 11, 16, 23, 547	99	R9, 43	391, 347401035	383, 5, 11, 13, 19, 191
R9, 53	250829932	283, 11, 16,									

## SUPPLEMENT

## SUPPLEMENT







## SUPPLEMENT







## Appendix II

### The first 1427 APs ordered according to the various occurring types

#### AMICABLE PAIRS OF TYPE (2,1):

1 229 2E2.5..11  
 L1 21 284 2E2.71  
 8 17296 2E4.23.47  
 L1 21 18416 2E4.1151  
 9 63920 2E2.23.5.137  
 L1 21 76084 2E2.23.827  
 12 69615 3E2.7.13.5.17  
 L1 21 87633 3E2.7.13.107  
 15 122265 3E2.5.13.11.19  
 L1 21 139915 3E2.5.13.239  
 46 1175265 3E2.7E2.13.5.41  
 L1 21 1438983 3E2.7E2.13.251  
 184 9363584 2E7.191.383  
 L1 21 9437056 2E7.73727  
 117 11498356 3E4.5..11.29.89  
 L1 21 12624845 3E4.5..11.2699  
 162 31536855 3E2.5..7..53.1889  
 L1 21 32148585 3E2.5..7..53.1889  
 291 175032884 2E2.13..17.389.509  
 L1 21 175826716 2E2.13..17.198899  
 297 183408615 3E2.5..13.19..29.569  
 L1 21 190055385 3E2.5..13.19..17.099  
 303 196421715 3E2..5..19..37..7..887  
 L1 21 224703495 3E2..5..19..37..7..103  
 460 536637465 3E2..7E2..13..97..5..193  
 L1 21 646745463 3E2..7E2..13..97..1163  
 629 1191953763 3E2..7E2..11..13..41..461  
 L1 21 1223611389 3E2..7E2..11..13..19403  
 640 1225052829 3E4..7..11..29..13..521  
 L1 21 1321639011 3E4..7..11..29..7307  
 792 2172649215 2E8..257..33023  
 L1 21 2181168894 2E8..8520191  
 888 2935281375 3E3..5E3..13..149..449  
 L1 21 2961518625 3E3..5E3..13..67499  
 1030 4149186335 3E4..5..11E3..43..179  
 L1 21 4268776545 3E4..5..11E3..7919  
 1191 6066248175 3E2..5E2..13..31..149..449  
 L1 21 6120471825 3E2..5E2..13..31..67499  
 1219 6370495978 2..7E2..19..23..11..13523  
 L1 21 6950103062 2..7E2..19..23..162287

TOTAL NUMBER: 20

#### AMICABLE PAIRS OF TYPE (3,1):

86 6955216 2E4..19..137..167  
 L1 31 7418864 2E4..463679  
 151 23358248 2E3..37..23..47..73  
 L1 31 25223112 2E3..37..85247  
 164 32205616 2E4..17..167..709  
 L1 31 34352624 2E4..21..47..939  
 196 52695376 2E4..17..151..1283  
 L1 31 56208368 2E4..3513023  
 270 147366765 3E2..7E2..13..5..53..97  
 L1 31 182028483 3E2..7E2..13..31..751  
 312 285843365 3E2..7E2..13..5..43..167  
 L1 31 254264283 3E2..7E2..13..44351  
 390 347263216 2E4..17..137..9319  
 L1 31 370414864 2E4..23..150879  
 446 492275992 2E3..131..13..23..1571  
 R9 31 553544168 2E3..131..528191  
 648 1254255550 2..582..23..19..137..419  
 R9 31 133078850 2..582..23..11..159199  
 661 1309651310 2..5..11..29..571..719  
 R9 31 1359071890 2..5..11..12355199  
 753 1957374968 2E3..31..17..107..4339  
 L1 31 2892365832 2E3..31..8436959  
 782 2115211995 3E3..5..13..17..31..2287  
 R9 31 2312891685 3E3..5..13..131..7887  
 979 3693013664 2E5..41..131..21487  
 L1 31 3812143072 2E5..119129471  
 1009 3986534090 2..5..929..7..11..5573  
 L1 31 4971106870 2..5..929..535103  
 1228 6562770525 3E3..5E2..31..17..19..971  
 R9 31 7322055075 3E3..5E2..31..349919  
 1300 7696871576 2E3..19..53..127..7523  
 R9 31 7904894824 2E3..19..52005887

TOTAL NUMBER: 16

#### AMICABLE PAIRS OF TYPE (4,1):

779 2099442345 3..5..7..11..13..37..3779  
 L1 41 2533809495 3..5..7..24131519

TOTAL NUMBER: 1

AMICABLE PAIRS OF TYPE (2, 2): 204 66595130



## SUPPLEMENT

S25

TOTAL NUMBER: 271

## AMICABLE PAIRS OF TYPE (4, 2) :

## AMICABLE PAIRS OF TYPE (2, 3) :

574	965615992	283·11·23·349·1367	1078	4771436296	283·11·23·271·8699
R9	42	1128080088	R9	42	545411704
L1	42	166910	L1	42	151190
L1	42	2·5·11·17·19·47	R9	42	2·5·7·159
L1	42	2862570	L1	42	158410
L1	42	2·5·23·19·863	R9	42	5·19·47·179
L1	42	2893580	L1	42	5408836424
L1	42	2·5·13·41·263	R9	42	1583199
L1	42	3716164	L1	42	3431999
L1	42	2·5·13·23·101·4337	R9	42	448810
L1	42	4522710	L1	42	2·5·23·29·673
L1	42	2·7·5·13·187	R9	42	114·55181
L1	42	6135962	L1	42	22727504
L1	42	2·7·7·13·29·269	R9	42	14808995
L1	42	83·584660	L1	42	382·5·17·21·271
L1	42	2·5·17·47·367	R9	42	1654·561941
L1	42	7493324	L1	42	2279·1087·7919
L1	42	2·5·13·53·327	R9	42	1561·561941
L1	42	122·77004	L1	42	229·187·1847
L1	42	233·17·41·43·53	R9	42	194399
L1	42	1436·36	L1	42	158524544
L1	42	233·107·16331	R9	42	224·19·190
L1	42	16631	L1	42	158524344
L1	42	233·17·23·37·173	R9	42	223·19·189
L1	42	2862328	L1	42	158524233
L1	42	233·136·2087	R9	42	223·19·188
L1	42	22823432	L1	42	158524123
L1	42	233·136·229·223	R9	42	223·19·187
L1	42	2268832	L1	42	158524023
L1	42	233·136·2239	R9	42	223·19·186
L1	42	2575568	L1	42	158523923
L1	42	233·136·2239	R9	42	223·19·185
L1	42	325559	L1	42	158523823
L1	42	333·5·13·17·107	R9	42	223·19·184
L1	42	4326662	L1	42	158523723
L1	42	333·5·13·17·694	R9	42	223·19·183
L1	42	352559	L1	42	158523623
L1	42	233·7·19·53·191	R9	42	223·19·182
L1	42	2955592	L1	42	158523523
L1	42	233·7·19·53·191	R9	42	223·19·181
L1	42	3718961690	L1	42	158523423
L1	42	233·7·19·53·1909	R9	42	223·19·180
L1	42	97738668	L1	42	158523323
L1	42	233·7·19·53·1909	R9	42	223·19·179
L1	42	979332	L1	42	158523223
L1	42	233·7·19·53·1909	R9	42	223·19·178
L1	42	2868832	L1	42	158523123
L1	42	233·7·19·53·1909	R9	42	223·19·177
L1	42	7843	L1	42	158523023
L1	42	233·7·19·53·1909	R9	42	223·19·176
L1	42	7843	L1	42	158522923
L1	42	233·7·19·53·1909	R9	42	223·19·175
L1	42	7843	L1	42	158522823
L1	42	233·7·19·53·1909	R9	42	223·19·174
L1	42	7843	L1	42	158522723
L1	42	233·7·19·53·1909	R9	42	223·19·173
L1	42	7843	L1	42	158522623
L1	42	233·7·19·53·1909	R9	42	223·19·172
L1	42	7843	L1	42	158522523
L1	42	233·7·19·53·1909	R9	42	223·19·171
L1	42	7843	L1	42	158522423
L1	42	233·7·19·53·1909	R9	42	223·19·170
L1	42	7843	L1	42	158522323
L1	42	233·7·19·53·1909	R9	42	223·19·169
L1	42	7843	L1	42	158522223
L1	42	233·7·19·53·1909	R9	42	223·19·168
L1	42	7843	L1	42	158522123
L1	42	233·7·19·53·1909	R9	42	223·19·167
L1	42	7843	L1	42	158522023
L1	42	233·7·19·53·1909	R9	42	223·19·166
L1	42	7843	L1	42	158521923
L1	42	233·7·19·53·1909	R9	42	223·19·165
L1	42	7843	L1	42	158521823
L1	42	233·7·19·53·1909	R9	42	223·19·164
L1	42	7843	L1	42	158521723
L1	42	233·7·19·53·1909	R9	42	223·19·163
L1	42	7843	L1	42	158521623
L1	42	233·7·19·53·1909	R9	42	223·19·162
L1	42	7843	L1	42	158521523
L1	42	233·7·19·53·1909	R9	42	223·19·161
L1	42	7843	L1	42	158521423
L1	42	233·7·19·53·1909	R9	42	223·19·160
L1	42	7843	L1	42	158521323
L1	42	233·7·19·53·1909	R9	42	223·19·159
L1	42	7843	L1	42	158521223
L1	42	233·7·19·53·1909	R9	42	223·19·158
L1	42	7843	L1	42	158521123
L1	42	233·7·19·53·1909	R9	42	223·19·157
L1	42	7843	L1	42	158521023
L1	42	233·7·19·53·1909	R9	42	223·19·156
L1	42	7843	L1	42	158520923
L1	42	233·7·19·53·1909	R9	42	223·19·155
L1	42	7843	L1	42	158520823
L1	42	233·7·19·53·1909	R9	42	223·19·154
L1	42	7843	L1	42	158520723
L1	42	233·7·19·53·1909	R9	42	223·19·153
L1	42	7843	L1	42	158520623
L1	42	233·7·19·53·1909	R9	42	223·19·152
L1	42	7843	L1	42	158520523
L1	42	233·7·19·53·1909	R9	42	223·19·151
L1	42	7843	L1	42	158520423
L1	42	233·7·19·53·1909	R9	42	223·19·150
L1	42	7843	L1	42	158520323
L1	42	233·7·19·53·1909	R9	42	223·19·149
L1	42	7843	L1	42	158520223
L1	42	233·7·19·53·1909	R9	42	223·19·148
L1	42	7843	L1	42	158520123
L1	42	233·7·19·53·1909	R9	42	223·19·147
L1	42	7843	L1	42	158520023
L1	42	233·7·19·53·1909	R9	42	223·19·146
L1	42	7843	L1	42	158519923
L1	42	233·7·19·53·1909	R9	42	223·19·145
L1	42	7843	L1	42	158519823
L1	42	233·7·19·53·1909	R9	42	223·19·144
L1	42	7843	L1	42	158519723
L1	42	233·7·19·53·1909	R9	42	223·19·143
L1	42	7843	L1	42	158519623
L1	42	233·7·19·53·1909	R9	42	223·19·142
L1	42	7843	L1	42	158519523
L1	42	233·7·19·53·1909	R9	42	223·19·141
L1	42	7843	L1	42	158519423
L1	42	233·7·19·53·1909	R9	42	223·19·140
L1	42	7843	L1	42	158519323
L1	42	233·7·19·53·1909	R9	42	223·19·139
L1	42	7843	L1	42	158519223
L1	42	233·7·19·53·1909	R9	42	223·19·138
L1	42	7843	L1	42	158519123
L1	42	233·7·19·53·1909	R9	42	223·19·137
L1	42	7843	L1	42	158519023
L1	42	233·7·19·53·1909	R9	42	223·19·136
L1	42	7843	L1	42	158518923
L1	42	233·7·19·53·1909	R9	42	223·19·135
L1	42	7843	L1	42	158518823
L1	42	233·7·19·53·1909	R9	42	223·19·134
L1	42	7843	L1	42	158518723
L1	42	233·7·19·53·1909	R9	42	223·19·133
L1	42	7843	L1	42	158518623
L1	42	233·7·19·53·1909	R9	42	223·19·132
L1	42	7843	L1	42	158518523
L1	42	233·7·19·53·1909	R9	42	223·19·131
L1	42	7843	L1	42	158518423
L1	42	233·7·19·53·1909	R9	42	223·19·130
L1	42	7843	L1	42	158518323
L1	42	233·7·19·53·1909	R9	42	223·19·129
L1	42	7843	L1	42	158518223
L1	42	233·7·19·53·1909	R9	42	223·19·128
L1	42	7843	L1	42	158518123
L1	42	233·7·19·53·1909	R9	42	223·19·127
L1	42	7843	L1	42	158518023
L1	42	233·7·19·53·1909	R9	42	223·19·126
L1	42	7843	L1	42	158517923
L1	42	233·7·19·53·1909	R9	42	223·19·125
L1	42	7843	L1	42	158517823
L1	42	233·7·19·53·1909	R9	42	223·19·124
L1	42	7843	L1	42	158517723
L1	42	233·7·19·53·1909	R9	42	223·19·123
L1	42	7843	L1	42	158517623
L1	42	233·7·19·53·1909	R9	42	223·19·122
L1	42	7843	L1	42	158517523
L1	42	233·7·19·53·1909	R9	42	223·19·121
L1	42	7843	L1	42	158517423
L1	42	233·7·19·53·1909	R9	42	223·19·120
L1	42	7843	L1	42	158517323
L1	42	233·7·19·53·1909	R9	42	223·19·119
L1	42	7843	L1	42	158517223
L1	42	233·7·19·53·1909	R9	42	223·19·118
L1	42	7843	L1	42	158517123
L1	42	233·7·19·53·1909	R9	42	223·19·117
L1	42	7843	L1	42	158517023
L1	42	233·7·19·53·1909	R9	42	223·19·116
L1	42	7843	L1	42	158516923
L1	42	233·7·19·53·1909	R9	42	223·19·115
L1	42	7843	L1	42	158516823
L1	42	233·7·19·53·1909	R9	42	223·19·114
L1	42	7843	L1	42	158516723
L1	42	233·7·19·53·1909	R9	42	223·19·113
L1	42	7843	L1	42	158516623
L1	42	233·7·19·53·1909	R9	42	223·19·112
L1	42	7843	L1	42	158516523
L1	42	233·7·19·53·1909	R9	42	223·19·111
L1	42	7843	L1	42	158516423
L1	42	233·7·19·53·1909	R9	42	223·19·110
L1	42	7843	L1	42	158516323
L1	42	233·7·19·53·1909	R9	42	223·19·109
L1	42	7843	L1	42	158516223
L1	42	233·7·19·53·1909	R9	42	223·19·108
L1	42	7843	L1	42	158516123
L1	42	233·7·19·53·1909	R9	42	223·19·107
L1	42	7843	L1	42	158516023
L1	42	233·7·19·53·1909	R9	42	223·19·106
L1	42	7843	L1	42	158515923
L1	42	233·7·19·53·1909	R9	42	223·19·105
L1	42	7843	L1	42	158515823
L1	42	233·7·19·53·1909	R9	42	223·19·104
L1	42	7843	L1	42	158515723
L1	42	233·7·19·53·1909	R9	42	223·19·103
L1	42	7843	L1	42	158515623
L1	42	233·7·19·53·1909	R9	42	223·19·102
L1	42	7843	L1	42	158515523
L1	42	233			

AMICABLE PAIRS OF TYPE (3, 3):



AMICABLE PAIRS OF TYPE (4, 3):









769	204396130	2.5.-7B3.1.19.3329	923	3233166384	287.-173.-227.-643	R9 X	923	3233166384	287.-173.-227.-643	1046	4321182001	382.-7B2.13.11.17.29.-139	R9 X	923	3233166384	287.-173.-227.-643	1135	5640198115	3B2.5.19.7B2.61.2297
770	2271773870	2.5.-2B3.1.19.449	925	3287775436	285.-259.-347.-1291	R9 X	925	3287775436	285.-259.-347.-1291	1051	437738949	382.-7E.1.5.293	R9 X	925	3287775436	285.-259.-347.-1291	1137	5613545115	3E2.5.19.47.1655
775	2083894785	3E2.-5.-7B3.1.19.7B69	926	3254018635	3E2.-5.-13.1.1.1.1.1.179	R9 X	926	3254018635	3E2.-5.-13.1.1.1.1.1.179	1052	437738949	382.-7E.1.5.293	R9 X	926	3254018635	3E2.-5.-13.1.1.1.1.1.179	1138	5613545115	3E2.5.19.47.1655
776	2184265210	3E2.-5.-11.31.1.13E.-51.49	927	3269156634	283.-13.1.479.-13337	R9 X	927	3269156634	283.-13.1.479.-13337	1053	4396388533	382.-5.1E.1.5.83	R9 X	927	3269156634	283.-13.1.479.-13337	1139	5613545115	3E2.5.19.47.1655
779	2281899210	3E2.-5.-31.1.13E.-51.61	928	3395565915	3.5.-11.17.13E2.-19.39	R9 X	928	3395565915	3.5.-11.17.13E2.-19.39	1054	4396388533	382.-5.1E.1.5.83	R9 X	928	3395565915	3.5.-11.17.13E2.-19.39	1140	5613545115	3E2.5.19.47.1655
780	2387886930	2.5.-31.-29.-265687	929	339181336	2E3.-29.-97.-15B959	R9 X	929	339181336	2E3.-29.-97.-15B959	1055	4396388533	382.-5.1E.1.5.83	R9 X	929	339181336	2E3.-29.-97.-15B959	1141	5613545115	3E2.5.19.47.1655
781	2223111345	3.5.-11.17.13E2.-23.419	930	3395565915	3.5.-11.17.13E2.-23.419	R9 X	930	3395565915	3.5.-11.17.13E2.-23.419	1056	4396388533	382.-5.1E.1.5.83	R9 X	930	3395565915	3.5.-11.17.13E2.-23.419	1142	5613545115	3E2.5.19.47.1655
782	2386515555	3.-7.-19.-21.-13E2.-17.109	931	3395565915	3.5.-11.17.13E2.-17.109	R9 X	931	3395565915	3.5.-11.17.13E2.-17.109	1057	4396388533	382.-5.1E.1.5.83	R9 X	931	3395565915	3.5.-11.17.13E2.-17.109	1143	5613545115	3E2.5.19.47.1655
783	2319890155	2.-31.-11.-97.-1439	932	3396934165	3E3.-533.-13.139.-557	R9 X	932	3396934165	3E3.-533.-13.139.-557	1058	4396388533	382.-5.1E.1.5.83	R9 X	932	3396934165	3E3.-533.-13.139.-557	1144	5613545115	3E2.5.19.47.1655
784	265977790	2.-31.-111.-167.-619	933	3426320975	3E2.-532.-13.167.-2339	R9 X	933	3426320975	3E2.-532.-13.167.-2339	1059	439312175	382.-5.1E.1.5.83	R9 X	933	3426320975	3E2.-532.-13.167.-2339	1145	5613545115	3E2.5.19.47.1655
785	1914294875	3E2.-13.1.12B2.-19.-8499	934	3431182155	3E2.-51.13.11B2.-59.-823	R9 X	934	3431182155	3E2.-51.13.11B2.-59.-823	1060	4343441334	2.7.-11.1.37.-59.-811	R9 X	934	3431182155	3E2.-51.13.11B2.-59.-823	1146	5613545115	3E2.5.19.47.1655
786	2573175525	3E2.-13B2.-11.-587.-1499	935	3442360735	3E3.-51.13.617.-3457	R9 X	935	3442360735	3E3.-51.13.617.-3457	1061	4342360735	2.7.-11.1.37.-59.-811	R9 X	935	3442360735	3E3.-51.13.617.-3457	1147	5613545115	3E2.5.19.47.1655
787	2402522825	3E2.-13.1.12B2.-19.-247	936	3442360735	3E3.-51.13.617.-3457	R9 X	936	3442360735	3E3.-51.13.617.-3457	1062	4342360735	2.7.-11.1.37.-59.-811	R9 X	936	3442360735	3E3.-51.13.617.-3457	1148	5613545115	3E2.5.19.47.1655
788	24746666455	3E2.-5.1.13.11B2.-5087	937	3452360188	3.5.-7.13.22B2.-19.-247	R9 X	937	3452360188	3.5.-7.13.22B2.-19.-247	1063	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	937	3452360188	3.5.-7.13.22B2.-19.-247	1149	5613545115	3E2.5.19.47.1655
789	2451666330	2.-7.-2E.2.-5.11.131.-121	938	3459556915	3E2.-5.1.13.11B2.-121	R9 X	938	3459556915	3E2.-5.1.13.11B2.-121	1064	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	938	3459556915	3E2.-5.1.13.11B2.-121	1150	5613545115	3E2.5.19.47.1655
790	2486516052	2.-7.-13.-13E2.-17.121	939	3459556915	3E2.-5.1.13.11B2.-121	R9 X	939	3459556915	3E2.-5.1.13.11B2.-121	1065	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	939	3459556915	3E2.-5.1.13.11B2.-121	1151	5613545115	3E2.5.19.47.1655
791	2446775084	2E4.-5.-81.-63337	940	3459556915	3E2.-5.1.13.11B2.-121	R9 X	940	3459556915	3E2.-5.1.13.11B2.-121	1066	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	940	3459556915	3E2.-5.1.13.11B2.-121	1152	5613545115	3E2.5.19.47.1655
792	251314336	2E5.-57.-146839	941	3459556915	3E2.-5.1.13.11B2.-121	R9 X	941	3459556915	3E2.-5.1.13.11B2.-121	1067	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	941	3459556915	3E2.-5.1.13.11B2.-121	1153	5613545115	3E2.5.19.47.1655
793	2448891598	2E2.-11.11.-83.-141.413	942	3459556915	3E2.-5.1.13.11B2.-121	R9 X	942	3459556915	3E2.-5.1.13.11B2.-121	1068	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	942	3459556915	3E2.-5.1.13.11B2.-121	1154	5613545115	3E2.5.19.47.1655
794	2486516052	2E2.-11.121.-13.167.-616	943	3459556915	3E2.-5.1.13.11B2.-121	R9 X	943	3459556915	3E2.-5.1.13.11B2.-121	1069	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	943	3459556915	3E2.-5.1.13.11B2.-121	1155	5613545115	3E2.5.19.47.1655
795	248714556	2E2.-31.-17.-19.-467	944	3459556915	3E2.-5.1.13.11B2.-121	R9 X	944	3459556915	3E2.-5.1.13.11B2.-121	1070	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	944	3459556915	3E2.-5.1.13.11B2.-121	1156	5613545115	3E2.5.19.47.1655
796	2491666330	2.-5.-13.1.131.-1255	945	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	945	3459556915	3E2.-5.1.13.11B2.-1255	1071	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	945	3459556915	3E2.-5.1.13.11B2.-1255	1157	5613545115	3E2.5.19.47.1655
797	244641282	3E2.-13.1.12B2.-17.121	946	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	946	3459556915	3E2.-5.1.13.11B2.-1255	1072	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	946	3459556915	3E2.-5.1.13.11B2.-1255	1158	5613545115	3E2.5.19.47.1655
798	2486516052	2E2.-13.1.12B2.-19.-467	947	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	947	3459556915	3E2.-5.1.13.11B2.-1255	1073	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	947	3459556915	3E2.-5.1.13.11B2.-1255	1159	5613545115	3E2.5.19.47.1655
799	2486516052	2E2.-13.1.12B2.-19.-467	948	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	948	3459556915	3E2.-5.1.13.11B2.-1255	1074	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	948	3459556915	3E2.-5.1.13.11B2.-1255	1160	5613545115	3E2.5.19.47.1655
800	3088633115	3.-5.-17.-19.-23.-364	949	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	949	3459556915	3E2.-5.1.13.11B2.-1255	1075	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	949	3459556915	3E2.-5.1.13.11B2.-1255	1161	5613545115	3E2.5.19.47.1655
801	338257125	3.-8.-3.1.11.-47.-239	950	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	950	3459556915	3E2.-5.1.13.11B2.-1255	1076	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	950	3459556915	3E2.-5.1.13.11B2.-1255	1162	5613545115	3E2.5.19.47.1655
802	3896744688	2E6.-5.-83.-393979	951	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	951	3459556915	3E2.-5.1.13.11B2.-1255	1077	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	951	3459556915	3E2.-5.1.13.11B2.-1255	1163	5613545115	3E2.5.19.47.1655
803	323046229	3E2.-7B3.-13.-11B2.-17.-37	952	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	952	3459556915	3E2.-5.1.13.11B2.-1255	1078	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	952	3459556915	3E2.-5.1.13.11B2.-1255	1164	5613545115	3E2.5.19.47.1655
804	3568411321	3E3.-7B2.-13.-11B2.-17.-47	953	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	953	3459556915	3E2.-5.1.13.11B2.-1255	1079	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	953	3459556915	3E2.-5.1.13.11B2.-1255	1165	5613545115	3E2.5.19.47.1655
805	218129996	2E2.-11.-111.-265.-2617	954	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	954	3459556915	3E2.-5.1.13.11B2.-1255	1080	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	954	3459556915	3E2.-5.1.13.11B2.-1255	1166	5613545115	3E2.5.19.47.1655
806	3332319982	2E2.-11B2.-12B2.-123.-4999	955	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	955	3459556915	3E2.-5.1.13.11B2.-1255	1081	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	955	3459556915	3E2.-5.1.13.11B2.-1255	1167	5613545115	3E2.5.19.47.1655
807	2995738770	2.-5.-17.-19.-23.-364	956	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	956	3459556915	3E2.-5.1.13.11B2.-1255	1082	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	956	3459556915	3E2.-5.1.13.11B2.-1255	1168	5613545115	3E2.5.19.47.1655
808	3283319982	2.-5.-17.-19.-23.-364	957	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	957	3459556915	3E2.-5.1.13.11B2.-1255	1083	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	957	3459556915	3E2.-5.1.13.11B2.-1255	1169	5613545115	3E2.5.19.47.1655
809	316616184	2E2.-1.-41.-151.-6789	958	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	958	3459556915	3E2.-5.1.13.11B2.-1255	1084	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	958	3459556915	3E2.-5.1.13.11B2.-1255	1170	5613545115	3E2.5.19.47.1655
810	3183919493	2E2.-13.-13B2.-17.-239	959	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	959	3459556915	3E2.-5.1.13.11B2.-1255	1085	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	959	3459556915	3E2.-5.1.13.11B2.-1255	1171	5613545115	3E2.5.19.47.1655
811	2937182010	2E3.-31.-13.-67.-1879	960	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	960	3459556915	3E2.-5.1.13.11B2.-1255	1086	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	960	3459556915	3E2.-5.1.13.11B2.-1255	1172	5613545115	3E2.5.19.47.1655
812	2862347210	2.-5.-167.-24292	961	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	961	3459556915	3E2.-5.1.13.11B2.-1255	1087	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	961	3459556915	3E2.-5.1.13.11B2.-1255	1173	5613545115	3E2.5.19.47.1655
813	2866315555	3E2.-5.-13B2.-13.-32339	962	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	962	3459556915	3E2.-5.1.13.11B2.-1255	1088	4346676794	2.7.-13.23.-29.-151.-3863	R9 X	962	3459556915	3E2.-5.1.13.11B2.-1255	1174	5613545115	3E2.5.19.47.1655
814	3332319982	2E2.-11B2.-12B2.-123.-4999	963	3459556915	3E2.-5.1.13.11B2.-1255	R9 X	963	345955											



# Appendix III

## The gcd's of the first 1427 APs

GCD	FREQ	RANK NUMBER(S) OF AP'S WITH THIS GCD									
2	2	2 278									
4	67	1 3 4 23 24 36 53 64 83 97 115 153 154 165 209 226 238 255 267 274 294 313 323 345 347 348 502 585 570 586 632 645 721 738 748 750 763 776 800 807 811 822 842 846 852 867 877 989 920 937 975 976 1060 1119 1132 1160 1251 1307 1316 1322 1350 1355 1365 1368 1374 1399 1406									
8	208	5 6 17 21 26 31 32 33 34 35 37 40 42 47 59 62 65 67 69 74 76 80 81 84 90 93 94 95 103 110 112 116 120 122 126 131 140 143 144 148 150 159 161 163 174 180 182 184 186 192 199 201 206 208 212 217 218 239 240 244 258 266 279 280 293 296 298 300 305 311 314 315 317 318 330 333 339 353 357 361 363 374 375 376 382 387 400 405 417 432 438 447 452 455 458 459 463 467 475 498 513 523 525 546 552 553 558 571 574 579 580 587 591 599 606 631 633 639 644 646 652 658 665 668 690 702 713 716 720 722 727 737 762 771 788 806 808 814 836 845 848 854 855 858 863 869 871 876 881 912 913 919 925 942 946 953 972 973 974 978 981 982 992 999 1011 1026 1028 1043 1063 1077 1078 1079 1113 1117 1120 1126 1130 1141 1152 1153 1164 1170 1182 1184 1213 1218 1222 1235 1243 1250 1252 1253 1279 1382 1320 1329 1345 1354 1356 1361 1376 1378 1391 1393 1404 1407 1408 1417									
10	94	13 18 43 45 49 52 54 55 58 70 75 79 98 99 105 107 128 146 190 210 219 227 228 264 275 283 286 289 299 328 332 343 378 420 437 441 448 476 479 507 519 534 544 589 598 609 617 620 627 664 670 674 676 723 759 769 826 834 835 843 859 897 904 1001 1007 1023 1027 1042 1053 1062 1064 1066 1074 1093 1103 1104 1105 1108 1111 1123 1148 1159 1167 1209 1221 1240 1257 1266 1285 1287 1373 1394 1398 1419									
14	30	25 61 73 77 119 127 135 177 187 198 249 377 395 399 412 470 480 651 701 756 790 809 825 857 873 1070 1110 1342 1344 1384									
15	1	900									



## SUPPLEMENT

236	1	1301		530	1	1386																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																													
238	2	234	1414	548	1	1384																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																													
248	4	276	392	753	1421	574	1																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																												
250	1	588		585	41	1047																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																													
255	1	705			15	30	48																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																												
256	4	520	556	792	1052	168	203	251	261	1066	114	137	138	173	178																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																				
266	8	368	491	582	602	734	749	1366	1683	787	726	820	824	862	924	927	958	984																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																	
273	1	78			592	1	1390	1084	1147	1177	1286	1289	1281	1325	1362	1375																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																			
285	2	123	968		632	1	478	664	1	564	670	1	243	675	15	147	202	462	506	554	614	642	684	841	889																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																										
286	1	764			682	1	1013	1069	1195	1217	1389	688	3	1168	692	1	1078	694	5	1176	321	424	715	1239																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																											
290	2	191	1422		735	4	235	355	415	1029	752	1	965	765	3	1143	1286	1317	790	1	677	808	1	977	819	19	12	170	222	389	698	719	767	780	849																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																
296	3	151	183	1220	825	2	1050	1124	848	2	1050	1124	850	1	635	855	7	1143	1286	1317	884	1	291	891	3	416	935	1161																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																							
310	11	66	204	730	794	818	839	853	1025	1099	1311	868	3	1031	1081	1081	1162	1162	1349	1381	1381																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																														
315	13	1323	236	254	472	584	700	813	817	833	1140	890	4	1168	1239	1239	1349	1349	1381	1381	1381																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																														
322	1	1145	1197	1351	1873	1973	2073	2173	2273	2373	2473	2573	2673	2773	2873	2973	3073	3173	3273	3373	3473	3573	3673	3773	3873	3973	4073	4173	4273	4373	4473	4573	4673	4773	4873	4973	5073	5173	5273	5373	5473	5573	5673	5773	5873	5973	6073	6173	6273	6373	6473	6573	6673	6773	6873	6973	7073	7173	7273	7373	7473	7573	7673	7773	7873	7973	8073	8173	8273	8373	8473	8573	8673	8773	8873	8973	9073	9173	9273	9373	9473	9573	9673	9773	9873	9973	10073	10173	10273	10373	10473	10573	10673	10773	10873	10973	11073	11173	11273	11373	11473	11573	11673	11773	11873	11973	12073	12173	12273	12373	12473	12573	12673	12773	12873	12973	13073	13173	13273	13373	13473	13573	13673	13773	13873	13973	14073	14173	14273	14373	14473	14573	14673	14773	14873	14973	15073	15173	15273	15373	15473	15573	15673	15773	15873	15973	16073	16173	16273	16373	16473	16573	16673	16773	16873	16973	17073	17173	17273	17373	17473	17573	17673	17773	17873	17973	18073	18173	18273	18373	18473	18573	18673	18773	18873	18973	19073	19173	19273	19373	19473	19573	19673	19773	19873	19973	20073	20173	20273	20373	20473	20573	20673	20773	20873	20973	21073	21173	21273	21373	21473	21573	21673	21773	21873	21973	22073	22173	22273	22373	22473	22573	22673	22773	22873	22973	23073	23173	23273	23373	23473	23573	23673	23773	23873	23973	24073	24173	24273	24373	24473	24573	24673	24773	24873	24973	25073	25173	25273	25373	25473	25573	25673	25773	25873	25973	26073	26173	26273	26373	26473	26573	26673	26773	26873	26973	27073	27173	27273	27373	27473	27573	27673	27773	27873	27973	28073	28173	28273	28373	28473	28573	28673	28773	28873	28973	29073	29173	29273	29373	29473	29573	29673	29773	29873	29973	30073	30173	30273	30373	30473	30573	30673	30773	30873	30973	31073	31173	31273	31373	31473	31573	31673	31773	31873	31973	32073	32173	32273	32373	32473	32573	32673	32773	32873	32973	33073	33173	33273	33373	33473	33573	33673	33773	33873	33973	34073	34173	34273	34373	34473	34573	34673	34773	34873	34973	35073	35173	35273	35373	35473	35573	35673	35773	35873	35973	36073	36173	36273	36373	36473	36573	36673	36773	36873	36973	37073	37173	37273	37373	37473	37573	37673	37773	37873	37973	38073	38173	38273	38373	38473	38573	38673	38773	38873	38973	39073	39173	39273	39373	39473	39573	39673	39773	39873	39973	40073	40173	40273	40373	40473	40573	40673	40773	40873	40973	41073	41173	41273	41373	41473	41573	41673	41773	41873	41973	42073	42173	42273	42373	42473	42573	42673	42773	42873	42973	43073	43173	43273	43373	43473	43573	43673	43773	43873	43973	44073	44173	44273	44373	44473	44573	44673	44773	44873	44973	45073	45173	45273	45373	45473	45573	45673	45773	45873	45973	46073	46173	46273	46373	46473	46573	46673	46773	46873	46973	47073	47173	47273	47373	47473	47573	47673	47773	47873	47973	48073	48173	48273	48373	48473	48573	48673	48773	48873	48973	49073	49173	49273	49373	49473	49573	49673	49773	49873	49973	50073	50173	50273	50373	50473	50573	50673	50773	50873	50973	51073	51173	51273	51373	51473	51573	51673	51773	51873	51973	52073	52173	52273	52373	52473	52573	52673	52773	52873	52973	53073	53173	53273	53373	53473	53573	53673	53773	53873	53973	54073	54173	54273	54373	54473	54573	54673	54773	54873	54973	55073	55173	55273	55373	55473	55573	55673	55773	55873	55973	56073	56173	56273	56373	56473	56573	56673	56773	56873	56973	57073	57173	57273	57373	57473	57573	57673	57773	57873	57973	58073	58173	58273	58373	58473	58573	58673	58773	58873	58973	59073	59173	59273	59373	59473	59573	59673	59773	59873	59973	60073	60173	60273	60373	60473	60573	60673	60773	60873	60973	61073	61173	61273	61373	61473	61573	61673	61773	61873	61973	62073	62173	62273	62373	62473	62573	62673	62773	62873	62973	63073	63173	63273	63373	63473	63573	63673	63773	63873	63973	64073	64173	64273	64373	64473	64573	64673	64773	64873	64973	65073	65173	65273	65373	65473	65573	65673	65773	65873	65973	66073	66173	66273	66373	66473	66573	66673	66773	66873	66973	67073	67173	67273	67373	67473	67573	67673	67773	67873	67973	68073	68173	68273	68373	68473	68573	68673	68773	68873	68973	69073	69173	69273	69373	69473	69573	69673	69773	69873	69973	70073	70173	70273	70373	70473	70573	70673	70773	70873	70973	71073	71173	71273	71373	71473	71573	71673	71773	71873	71973	72073	72173	72273	72373	72473	72573	72673	72773	72873	72973	73073	73173	73273	73373	73473	73573	73673	73773	73873	73973	74073	74173	74273	74373	74473	74573	74673	74773	74873	74973	75073	75173	75273	75373	75473	75573	75673	75773	75873	75973	76073	76173	76273	76373	76473	76573	76673	76773	76873	76973	77073	77173	77273	77373	77473	77573	77673	77773	77873	77973	78073	78173	78273	78373	78473	78573	78673	78773	78873	78973	79073	79173	79273	79373	79473	79573	79673	79773	79873	79973	80073	80173	80273	80373	80473	80573	80673	80773	80873	80973	81073	81173	81273	81373	81473	81573	81673	81773	81873	81973	82073	82173	82273	82373	82473	82573	82673	82773	82873	82973	83073	83173	83273	83373	83473	83573	83673	83773	83873	83973	84073	84173	84273	84373	84473	84573	84673	84773	84873	84973	85073	85173	85273	85373	85473	85573	85673	85773	85873	85973	86073	861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