

Matching μ -Logic: Foundation of A Unifying Programming Language Framework

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PhD Final Exam

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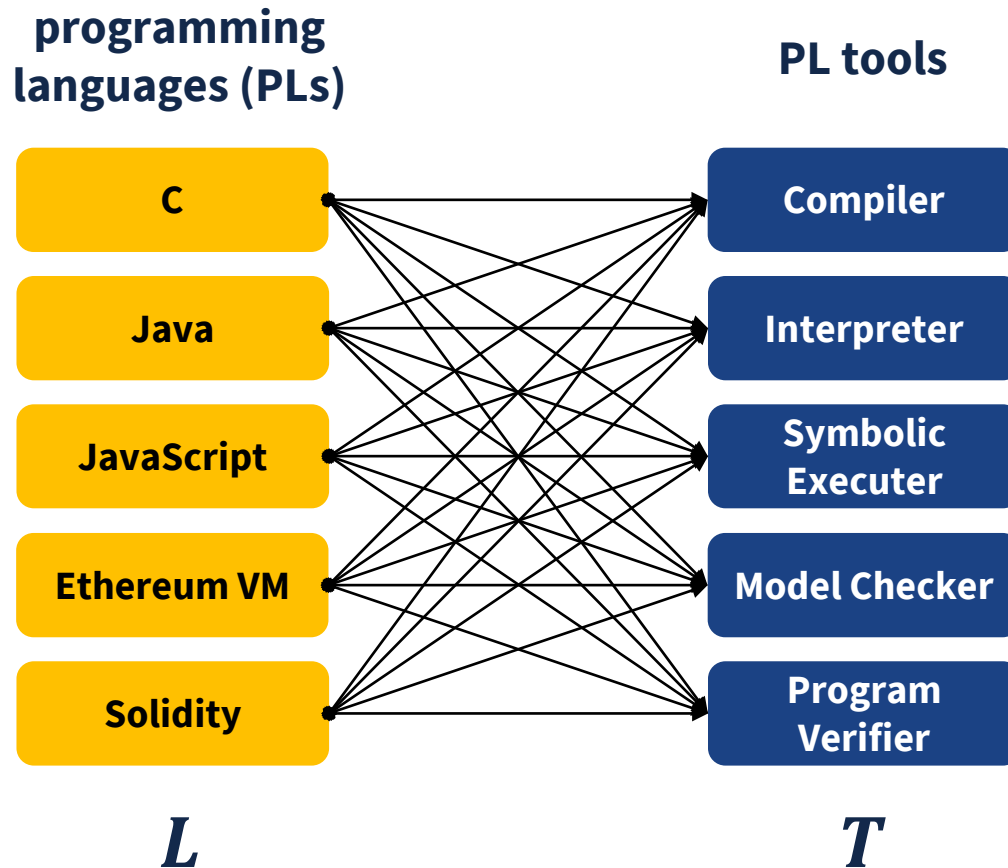
Overview

- **Introduction to a Unifying Programming Language Framework**
 - Motivating Example: The K Semantic Framework
 - Research Challenge: Ensure the Correctness of K
- **Main Contribution: Matching μ -Logic**
 - Basic Definitions
 - Expressive Power
 - Proof System and Proof Checker
 - Automatic Theorem Prover
- **Application: Proving the Correctness of K**
- **Concluding Remarks**

Overview

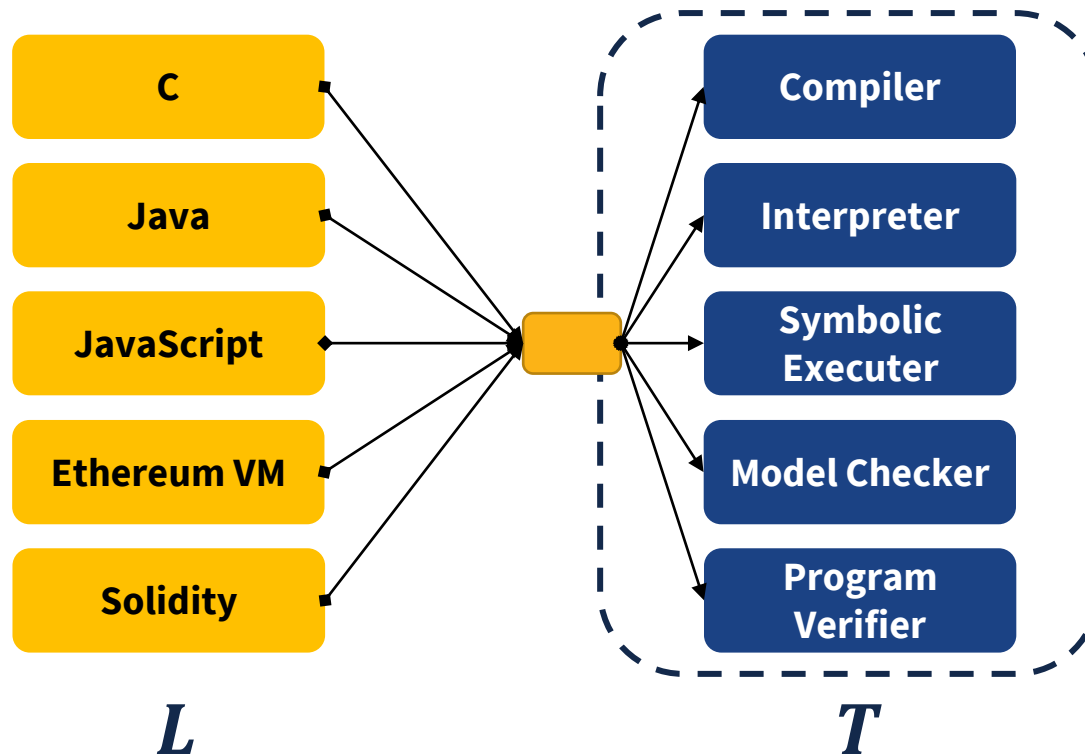
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Programming Language Design & Implementation: State-of-the-Art



$L \times T$ systems
to develop and maintain

Vision: A Unifying Programming Language Framework



$L + T$ systems
to develop and maintain

K Semantic Framework

<https://kframework.org/>

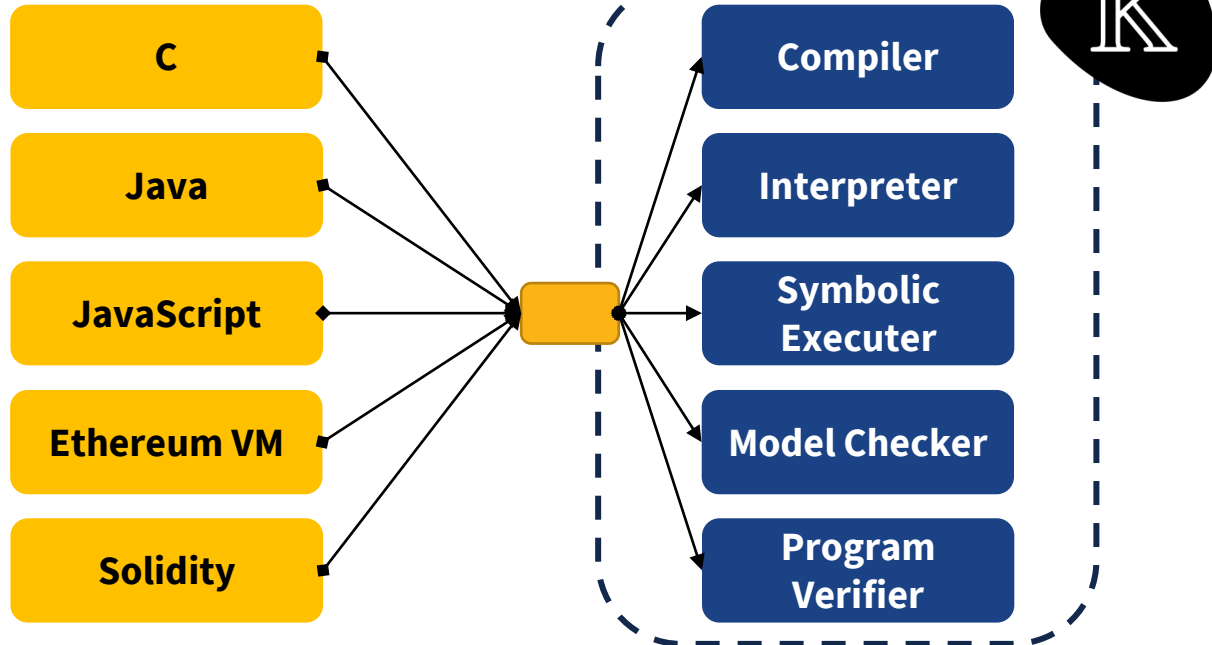
Ellison et al
[POPL'12, PLDI'15]

Bogdanas et al
[POPL'15]

Park et al
[PLDI'15]

Hildenbrandt et al
[CSF'18]

Filaretti et al
[Github Project 2019]



K has wide applications



RV-Match



RV-Monitor



Research Challenge: Proving the Correctness of K

- **K has a large code base**
 - >500k LOC in 4 programming languages
 - complex data structures, algorithms, and optimizations
- **K is constantly evolving**
 - latest release: 3 days ago



- **It's not practical to fully verify K using traditional methods.**

Main Idea: Let's translate K to logic.

K

Logical Foundation of K

A PL definition

**Ethereum
VM**

A logical theory Γ^{EVM}

Any PL task

- program execution
- formal verification

Interpreter

**Program
Verifier**

A logical theorem proved by a proof system

- $\Gamma^{\text{EVM}} \vdash t_{\text{init}} \Rightarrow_{\text{exec}} t_{\text{final}}$
- $\Gamma^{\text{EVM}} \vdash \varphi_{\text{pre}} \Rightarrow_{\text{verify}} \varphi_{\text{post}}$

Correctness of the task

Generating the proof and
checking it using a *proof checker*

**correctness of any task
done by any tool of any PL**



**correctness of 1 task
done by 1 program**

Which Logic?

- **We tried many logics/calculi/foundations**

First-order logic; Second/higher-order logic; Least fixpoint logic; Modal logics; Temporal logics (LTL, CTL, CTL*, ...), λ -calculus; Type systems (parametric, dependent, inductive, ...); μ -calculus; Hoare logics; Separation logics; Dynamic logics; Rewriting logic; Reachability logic; Equational logic; Small-/big-step SOS; Evaluation contexts; Abstract machines (CC, CK, CEK, SECD, ...); Chemical abstract machine; Axiomatic; Continuations; Denotational; Initial Algebras; ...

- **... but each of the above had limitations**

- Some only handle certain aspects of K (e.g., only execution)
- Some are “design patterns” (e.g., Hoare logics)
- Modularity and heavy notation

- **Matching μ -logic: keep advantages and avoid limitations**

- PLs defined as theories; PL tools specified by theorems
- High expressive power (K and beyond)
- A 15-rule proof system and a 200-LOC proof checker: small trust base

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Matching μ -Logic 101

Matching μ -logic formulas, called *patterns*:

$$\varphi ::= \underbrace{x \mid \sigma(\varphi_1, \dots, \varphi_n)}_{\text{structures}} \mid \underbrace{\varphi_1 \wedge \varphi_2 \mid \neg \varphi}_{\text{logical constraints}} \mid \underbrace{\exists x. \varphi}_{\text{first-order quantification}} \mid \underbrace{X \mid \mu X. \varphi}_{\text{fixpoints (in this talk)}}$$

- X a *set variable*, ranging over sets
- $\mu X. \varphi$ the *least fixpoint* of φ , explained later
- $\nu X. \varphi \equiv \neg \mu X. \neg \varphi[\neg X / X]$ the *greatest fixpoint* of φ
- $\mu X. \varphi$ and $\nu X. \varphi$ require that X occurs positively in φ

Matching μ -Logic 101

A matching μ -logic *model* has:

- a carrier set M
- a function $\sigma_M: M \times \dots \times M \rightarrow \mathcal{P}(M)$ for each symbol σ

Given a model M and a variable valuation ρ :

$$\varphi \xrightarrow{\text{pattern matching}} |\varphi|_{M,\rho} \subseteq M$$

- $|x|_{M,\rho} = \{\rho(x)\}$
- $|\sigma(\varphi_1, \dots, \varphi_n)|_{M,\rho} = \bigcup \{\sigma_M(a_1, \dots, a_n) \mid a_i \in |\varphi_i|_{M,\rho}\}$
- $|\varphi_1 \wedge \varphi_2|_{M,\rho} = |\varphi_1|_{M,\rho} \cap |\varphi_2|_{M,\rho}$
- $|\neg \varphi|_{M,\rho} = M \setminus |\varphi|_{M,\rho}$
- $|\exists x. \varphi|_{M,\rho} = \bigcup \{|\varphi|_{M,\rho}[a/x] \mid a \in M\}$
- $|X|_{M,\rho} = \rho(X)$
- $|\mu X. \varphi|_{M,\rho} = \mathbf{lfp} \left(A \mapsto |\varphi|_{M,\rho}[A/X] \right)$

Examples of Fixpoint Patterns

- **inductive datatypes** [JLAMP'21]

- `type list = Nil | Cons of int * list`
- $\mu L. \text{Nil} \vee \exists x. \text{Cons}(x, L)$
- $L =_{\text{lfp}} \{\text{Nil}\} \cup \{\text{Cons}(x, l) \mid x \in \text{int}, l \in L\}$

- **program execution** [LICS'19, CAV'21]

- an execution trace from t_{init} to t_{final}
- $t_{\text{init}} \Rightarrow_{\text{exec}} t_{\text{final}} \quad \equiv \quad t_{\text{init}} \rightarrow \underbrace{\text{eventually } t_{\text{final}}}_{\mu S. t_{\text{final}} \vee (\text{next } S)}$

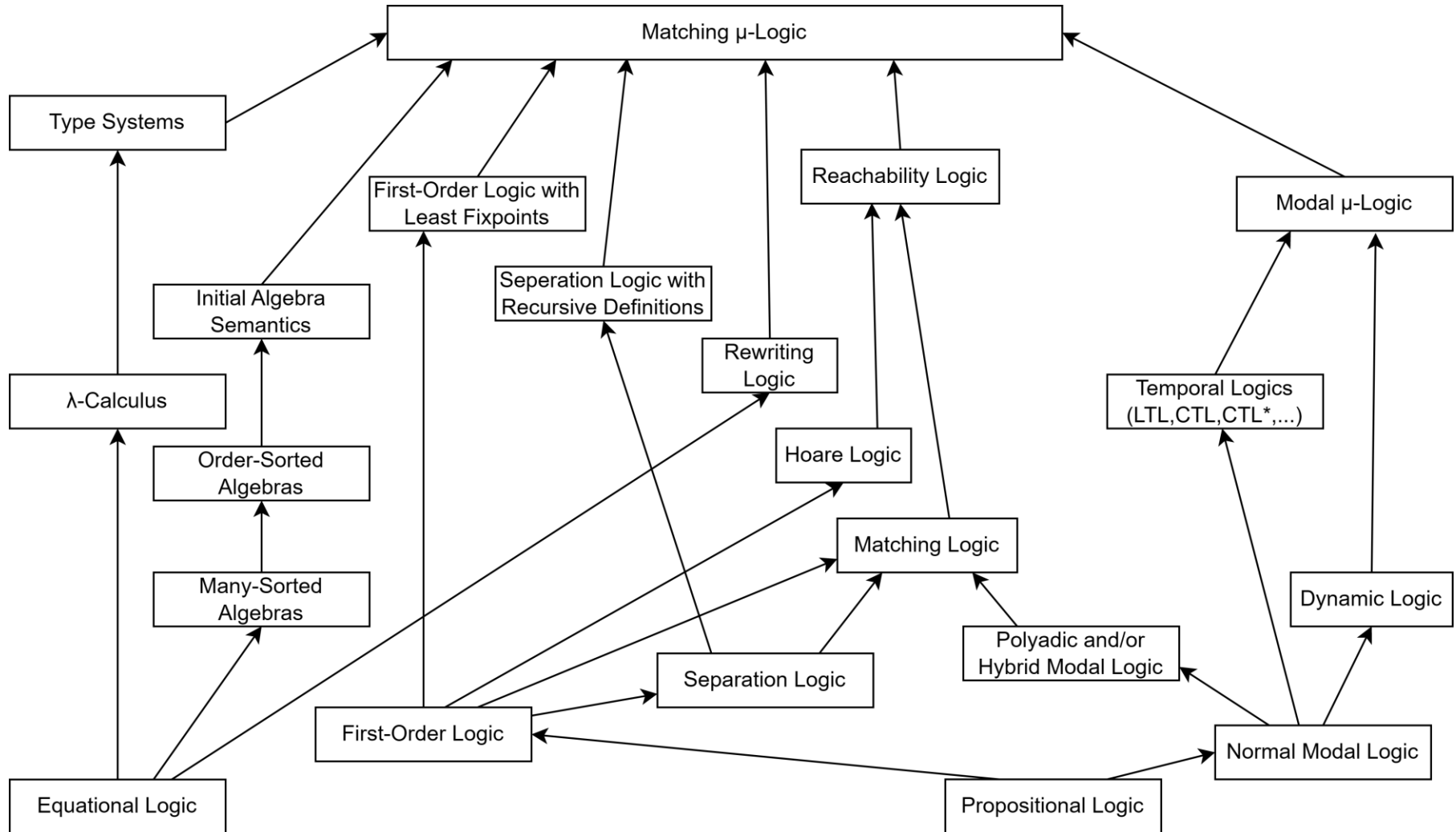
- **formal verification** [LICS'19, OOPSLA'23]

- if φ_{pre} holds when P starts, then φ_{post} holds when P terminates
- $\varphi_{\text{pre}} \Rightarrow_{\text{verify}} \varphi_{\text{post}} \quad \equiv \quad \varphi_{\text{pre}} \rightarrow \underbrace{\text{weak-eventually } \varphi_{\text{post}}}_{\nu S. \varphi_{\text{post}} \vee (\text{next } S)}$

Various forms/instances of fixpoints are definable by patterns.

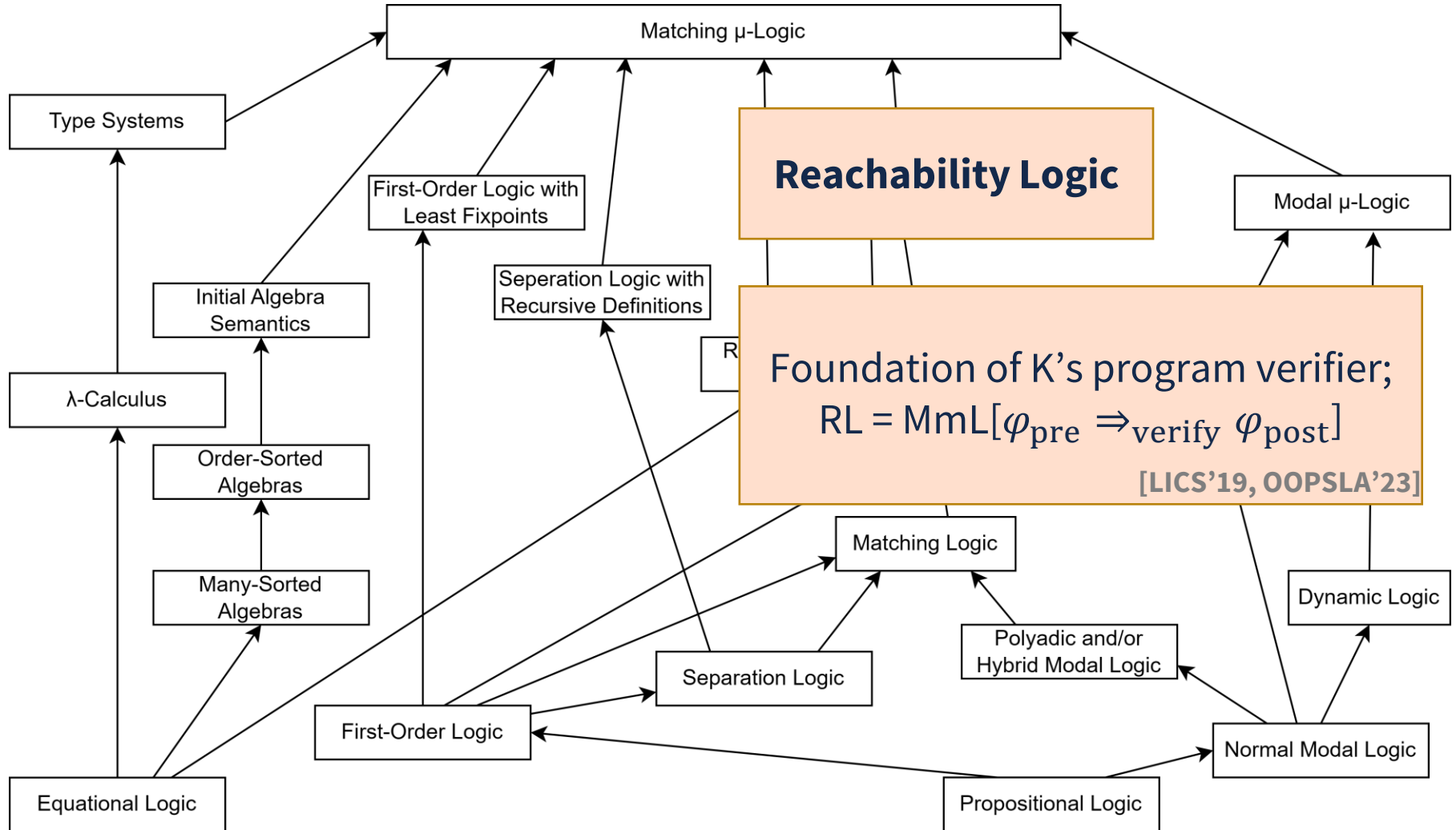
Matching μ -Logic (MmL) Expressive Power

[LICS'19, OOPSLA'20, ICFP'20, CAV'21, JLAMP'21, JLAMP'22, OOPSLA'23]



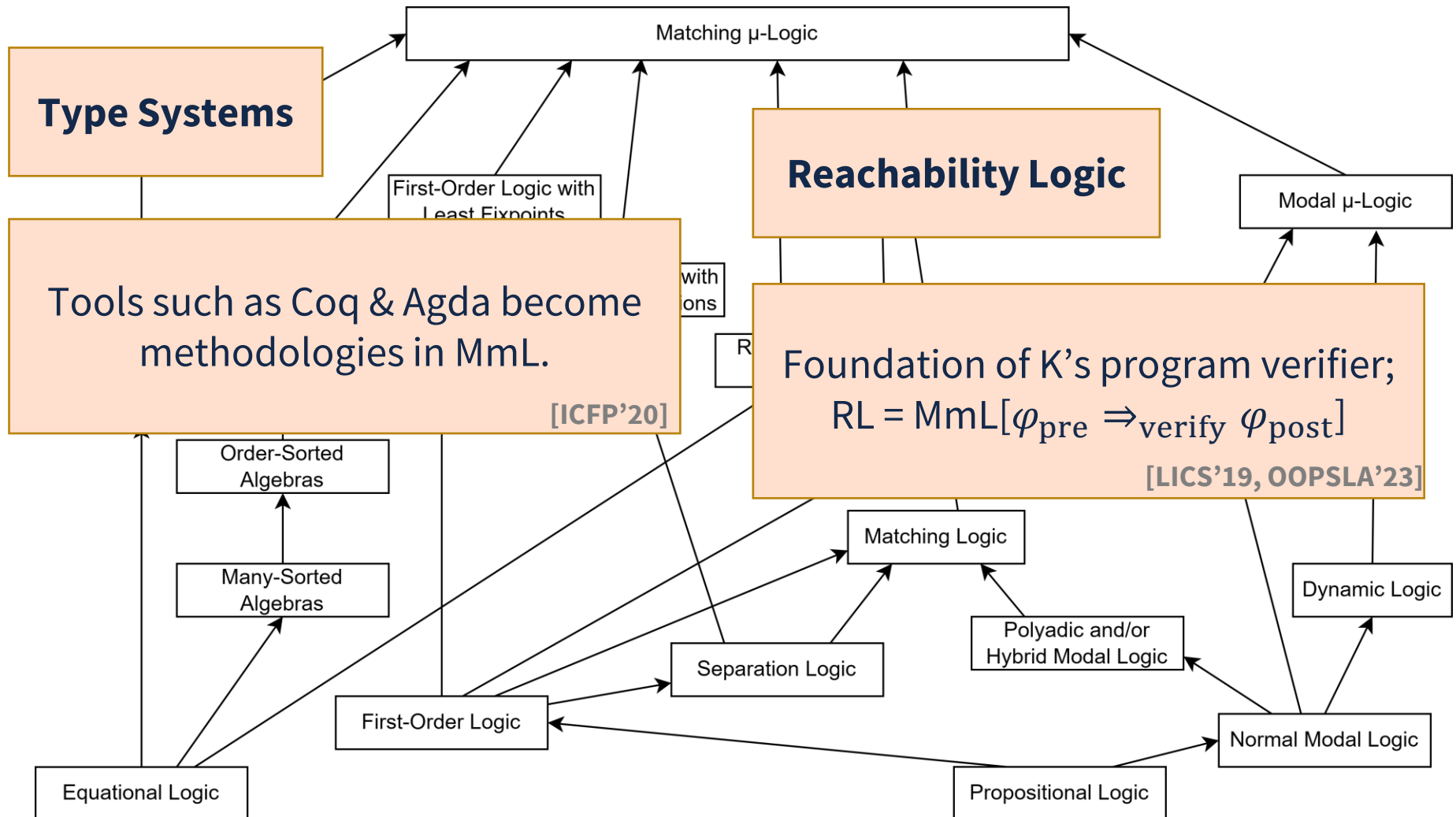
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Matching μ -Logic (MmL) Expressive Power

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Matching μ -Logic Proof System

(only 15 proof rules)

FOL Rules	(Propositional 1)	$\varphi \rightarrow (\psi \rightarrow \varphi)$	Defines provability relation
	(Propositional 2)	$(\varphi \rightarrow (\psi \rightarrow \theta)) \rightarrow ((\varphi \rightarrow \psi) \rightarrow (\varphi \rightarrow \theta))$	
	(Propositional 3)	$((\varphi \rightarrow \perp) \rightarrow \perp) \rightarrow \varphi$	
	(Modus Ponens)	$\frac{\varphi \quad \varphi \rightarrow \psi}{\psi}$	
	(\exists -Quantifier)	$\varphi[y/x] \rightarrow \exists x. \varphi$	
	(\exists -Generalization)	$\frac{\varphi \rightarrow \psi}{(\exists x. \varphi) \rightarrow \psi} \quad x \notin FV(\psi)$	
Frame Rules	(Propagation $_{\perp}$)	$C[\perp] \rightarrow \perp$	
	(Propagation $_{\vee}$)	$C[\varphi \vee \psi] \rightarrow C[\varphi] \vee C[\psi]$	
	(Propagation $_{\exists}$)	$C[\exists x. \varphi] \rightarrow \exists x. C[\varphi] \text{ with } x \notin FV(C)$	
	(Framing)	$\frac{\varphi \rightarrow \psi}{C[\varphi] \rightarrow C[\psi]}$	
Fixpoint Rules	(Substitution)	$\frac{\varphi}{\varphi[\psi/X]}$	
	(Prefixpoint)	$\varphi[(\mu X. \varphi)/X] \rightarrow \mu X. \varphi$	
	(Knaster-Tarski)	$\frac{\varphi[\psi/X] \rightarrow \psi}{(\mu X. \varphi) \rightarrow \psi}$	
Technical Rules	(Existence)	$\exists x. x$	proof rules for fixpoints
	(Singleton)	$\neg(C_1[x \wedge \varphi] \wedge C_2[x \wedge \neg\varphi])$	

$\Gamma \vdash \varphi$
theory theorem

$$\varphi[(\mu X. \varphi)/X] \leftrightarrow \mu X. \varphi$$

$$\frac{\varphi[\psi/X] \leftrightarrow \psi}{(\mu X. \varphi) \rightarrow \psi}$$

Deriving Mathematical Induction in Matching μ -Logic

Mathematical Induction: To show a property P holds for all naturals, prove:
(**basis**). The number 0 satisfies P
(**step**). If n satisfies P then $n + 1$ also satisfies P .

Step 1. Note that $\mu N. 0 \vee \mathbf{succ}(N)$ captures all natural numbers.

Step 2. Set the proof goal $\vdash (\mu N. 0 \vee \mathbf{succ}(N)) \rightarrow \psi_P$

Step 3. Apply (**Knaster Tarski**) and get two sub-goals:

Sub-Goal-1 $0 \rightarrow \psi_P$ (**basis**)

Sub-Goal-2 $\mathbf{succ}(\psi_P) \rightarrow \psi_P$ (**step**)

(**Knaster Tarski**)

$$\frac{\varphi[\psi / X] \rightarrow \psi}{\mu X. \varphi \rightarrow \psi}$$

Various forms/instances of fixpoints reasoning are supported by
(**Knaster Tarski**)

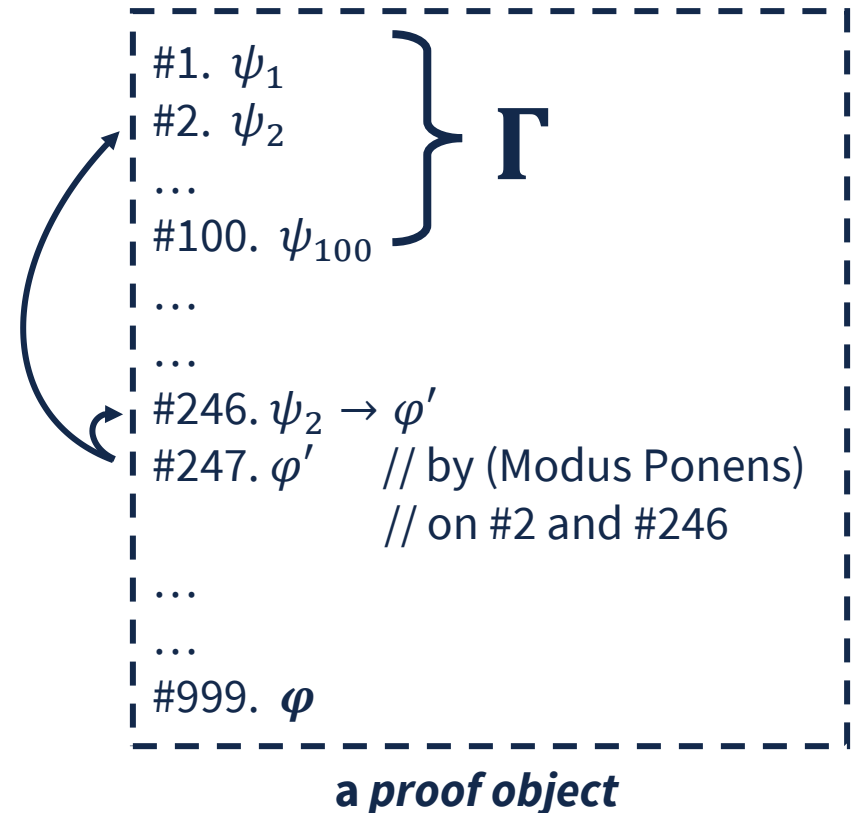
Matching μ -Logic Proof System

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	(Propagation $_{\perp}$)	$C[\perp] \rightarrow \perp$
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Technical Rules	(Existence)	$\exists x. x$
	(Singleton)	$\neg(C_1[x \wedge \varphi] \wedge C_2[x \wedge \neg \varphi])$

(Modus Ponens)

$$\frac{\varphi_1 \quad \varphi_1 \rightarrow \varphi_2}{\varphi_2}$$

$\Gamma \vdash \varphi$
theory theorem



Matching μ -Logic Proof Checker

- We use Metamath [Megill & Wheeler] <http://metamath.org> to
 - Encode proof objects and
 - Check them automatically
- Very small trust base
 - Matching μ -logic: 200 LOC
 - Metamath itself:
 - 350 LOC in Python
 - 400 LOC in Haskell
 - 550 LOC in C#
 - ...

```
1  $c \imp ( ) #Pattern |- $.
2
3  $v ph1 ph2 ph3 $.
4  ph1-is-pattern $f #Pattern ph1 $.
5  ph2-is-pattern $f #Pattern ph2 $.
6  ph3-is-pattern $f #Pattern ph3 $.
7  imp-is-pattern
8    $a #Pattern ( \imp ph1 ph2 ) $.
9
10 axiom-1
11   $a |- ( \imp ph1 ( \imp ph2 ph1 ) ) $.
12
13 axiom-2
14   $a |- ( \imp ( \imp ph1 ( \imp ph2 ph3 ) )
15             ( \imp ( \imp ph1 ph2 )
16                   ( \imp ph1 ph3 ) ) ) $.
17
18 ${
19   rule-mp.0 $e |- ( \imp ph1 ph2 ) $.
20   rule-mp.1 $e |- ph1 $.
21   rule-mp   $a |- ph2 $.
22   ...
23 }$
```

Matching μ -logic
syntax & proof rules;
Defined in 200 LOC

```
23  imp-refl $p |- ( \imp ph1 ph1 )
24  $=
25    ph1-is-pattern ph1-is-pattern
26    ph1-is-pattern imp-is-pattern
27    imp-is-pattern ph1-is-pattern
28    ph1-is-pattern imp-is-pattern
29    ph1-is-pattern ph1-is-pattern
30    ph1-is-pattern imp-is-pattern
31    ph1-is-pattern imp-is-pattern
32    imp-is-pattern ph1-is-pattern
33    ph1-is-pattern ph1-is-pattern
34    imp-is-pattern imp-is-pattern
35    ph1-is-pattern ph1-is-pattern
36    imp-is-pattern imp-is-pattern
37    ph1-is-pattern ph1-is-pattern
38    ph1-is-pattern imp-is-pattern
39    ph1-is-pattern axiom-2
40    ph1-is-pattern ph1-is-pattern
41    ph1-is-pattern imp-is-pattern
42    axiom-1 rule-mp ph1-is-pattern
43    ph1-is-pattern axiom-1 rule-mp
44    $.
```

Proof objects
(checked by Metamath)

Checking proof objects is fast and trustworthy.

Where do Proof Objects Come From?

Q1: Is there always a proof object for a true statement?

- Completeness of matching μ -logic (brief summary)

Q2: Can we find proof objects automatically?

- Automatic theorem prover for matching μ -logic (brief summary)

Q3: Can we generate proof objects from K?

- Proving the correctness of K

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Completeness of Matching μ -Logic

- Matching μ -logic is incomplete (because of \exists and μ)
- What if there is no μ ?
 - **(Local Completeness)**
$$\emptyset \models \varphi \quad \Rightarrow \quad \emptyset \vdash \varphi$$
 - **(Definedness Completeness)**
$$\Gamma \models \varphi \quad \Rightarrow \quad \Gamma \vdash \varphi, \text{ if } \Gamma \text{ includes definedness/equality.}$$
 - The rest is open problem.
- What if there is no \exists ?
 - Open problem.

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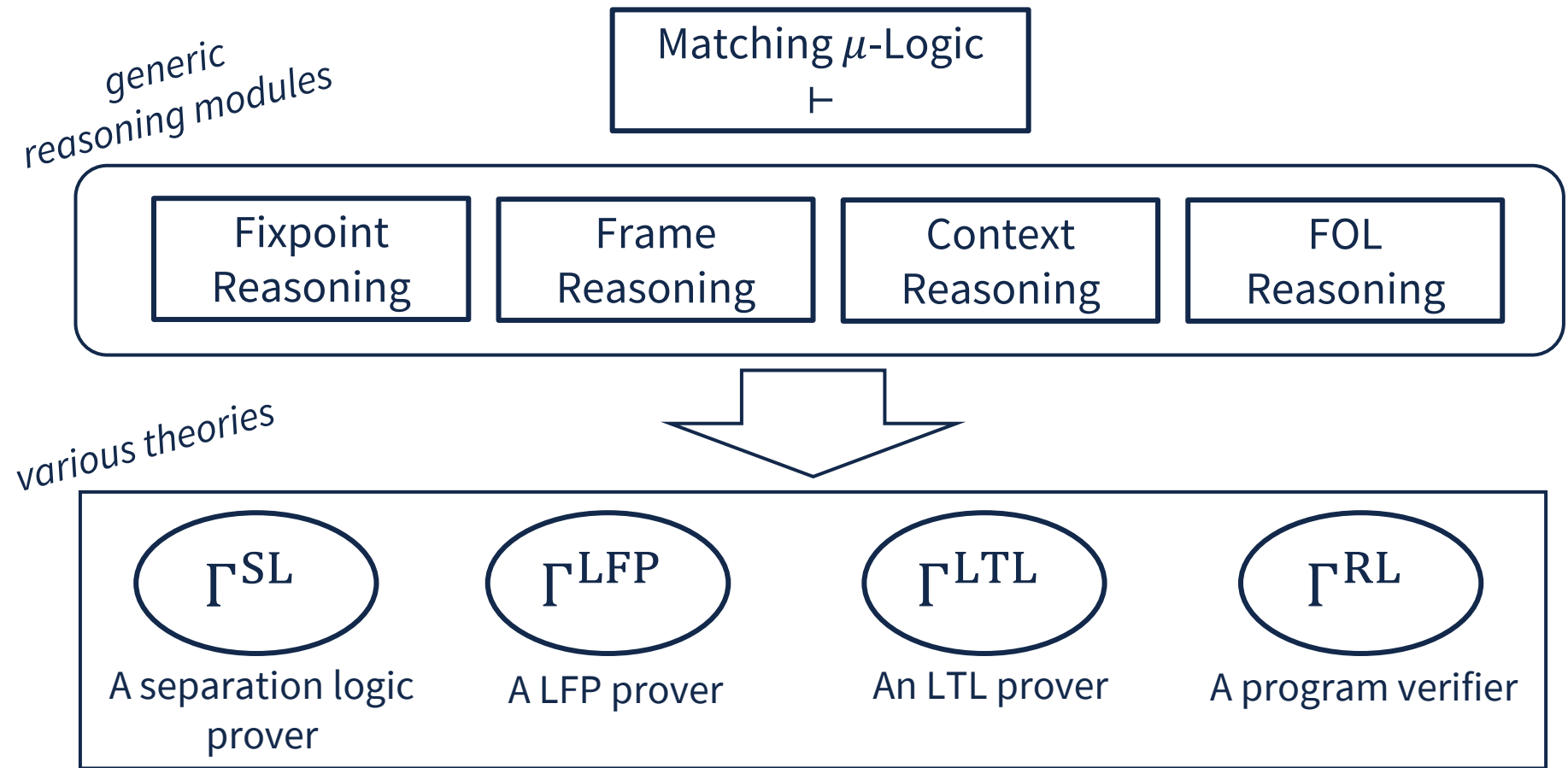
Q2: Can we find proof objects automatically?

- Automatic theorem prover for matching μ -logic (brief summary)

Q3: Can we generate proof objects from K?

- Proving the correctness of K

Automatic Theorem Prover for Matching μ -Logic



- Separation logic: Proved 265/280 benchmark tests in SL-COMP'19
- LTL: Proved all the axioms in the complete LTL proof system
- LTP & RL: Proved the correctness of the SUM program

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 - Translating K to Matching μ -Logic
 - Proving the Correctness of the K Program Verifier
- **Concluding Remarks**

Translating K to Matching μ -Logic

K

Matching μ -Logic

A PL definition

Ethereum
VM

A logical theory Γ^{EVM}

Any PL task

- program execution
- formal verification

Interpreter

Program
Verifier

A theorem proved by the 15-rule *proof system*

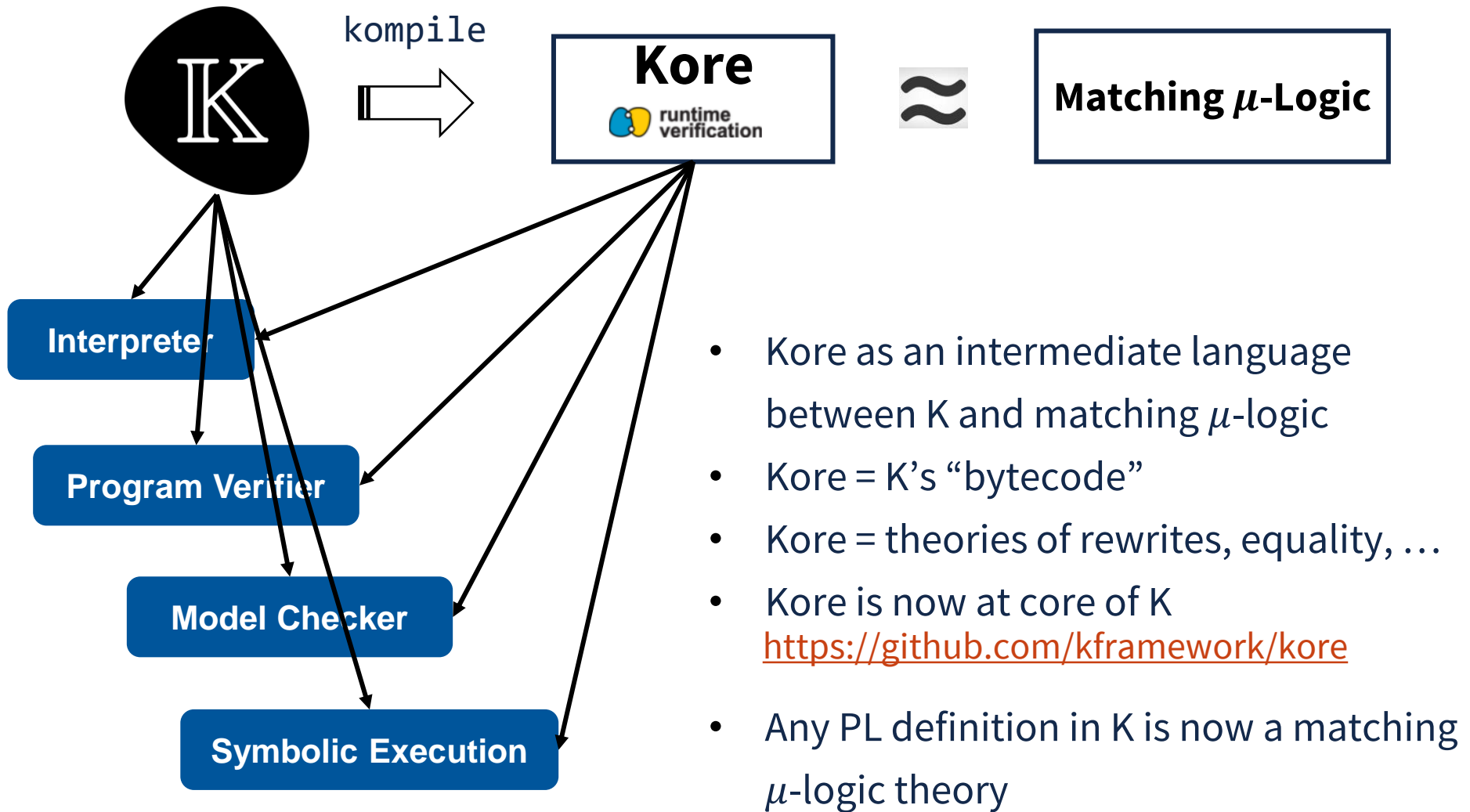
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Correctness of the task

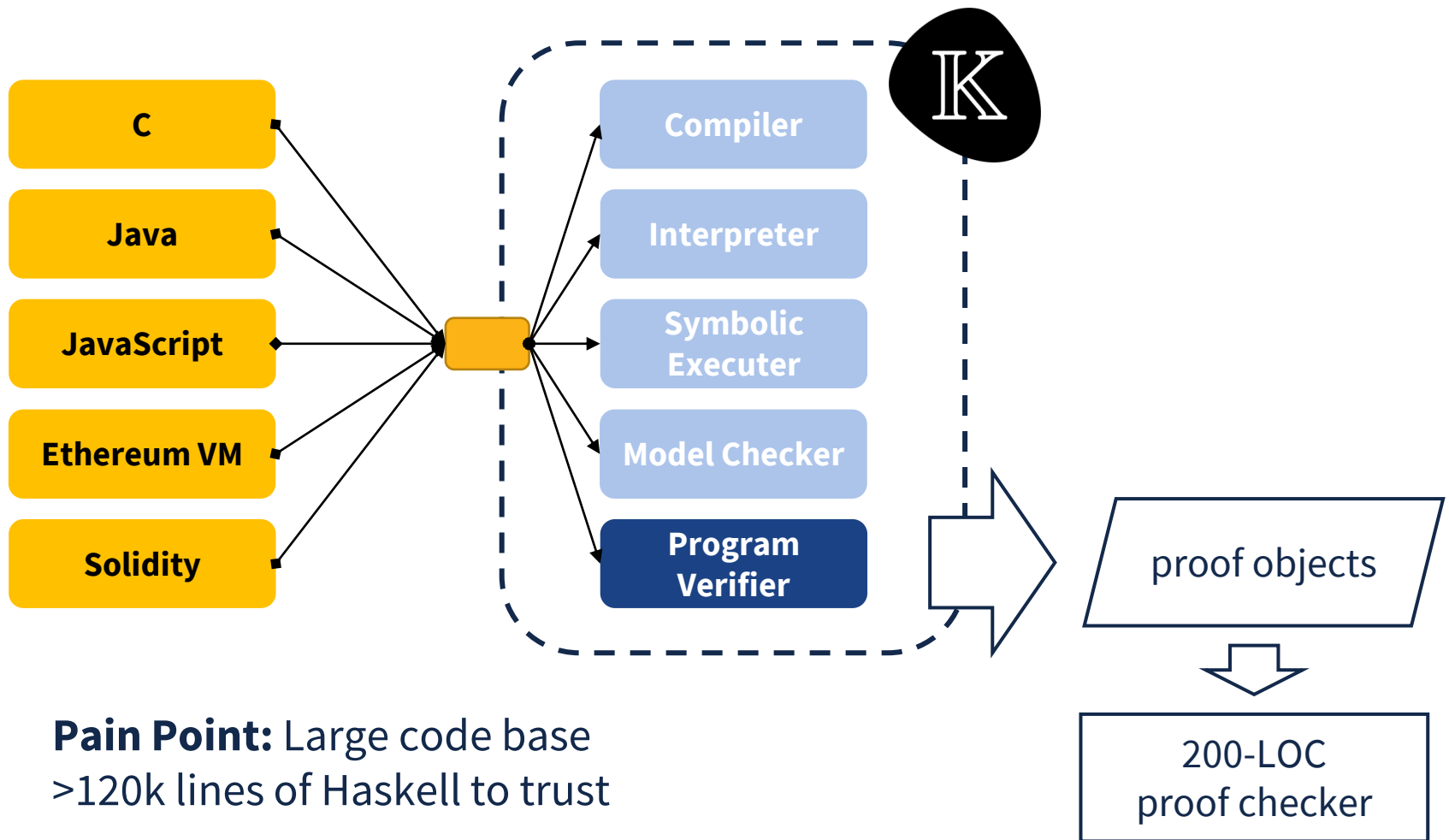
Generating the proof and
checking it using the 200-LOC *proof checker*

-
- **Task 1:** Generating the logical theory (e.g., Γ^{EVM})
 - **Task 2:** Generating the proof for a given PL task (e.g., verifying a program)

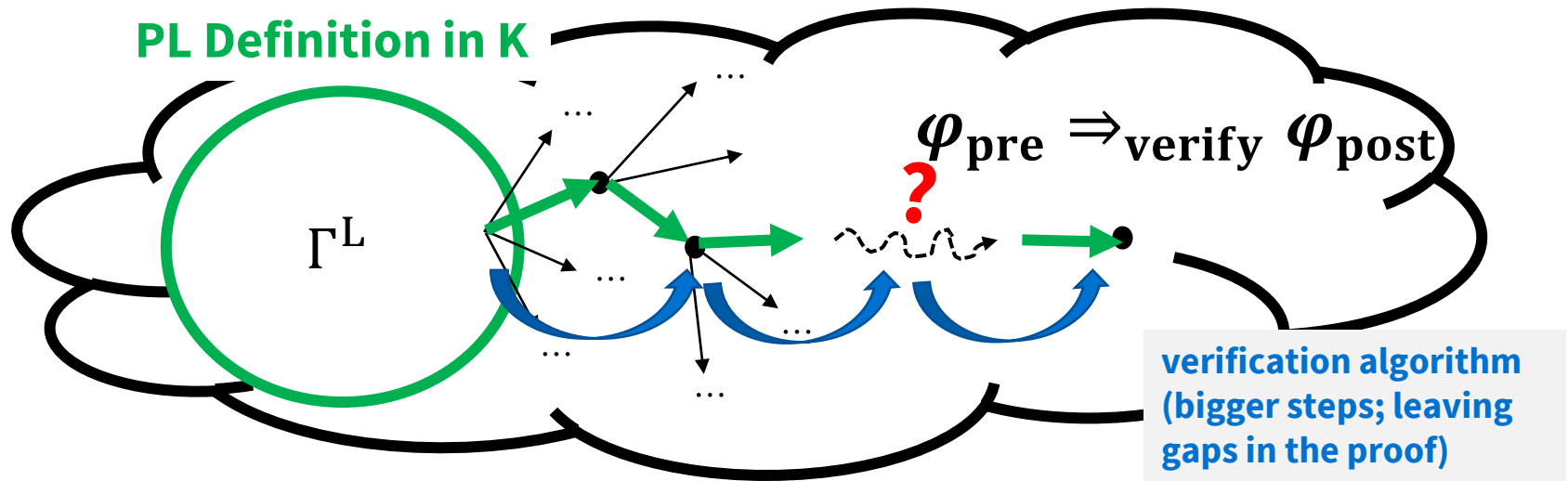
Translating PL Semantics to Matching μ -Logic Theories



Proving the Correctness of the K Program Verifier



Program Verification is Actually Proof Search



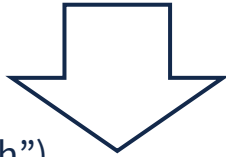
A program verifier is a specialized, optimized, proof searcher.

Proof Generation for Program Verification

The K program verifier checks that P satisfies the pre/post-conditions φ_{pre} and φ_{post} in L

proof generation

filling the “gaps” in the verification (“proof search”)



$\Gamma^L \vdash \varphi_{\text{pre}} \Rightarrow_{\text{verify}} \varphi_{\text{post}}$

a proof object

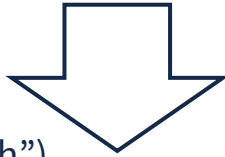
$\left. \begin{array}{l} \#1. \psi_1 \\ \#2. \psi_2 \\ \dots \\ \#100. \psi_{100} \\ \dots \\ \dots \\ \#247. \psi_2 \rightarrow \varphi \\ \#247. \varphi \quad // \text{ by (Modus Ponens)} \\ \quad \quad // \text{ on \#2 and \#246} \\ \dots \\ \dots \\ \#99999. \varphi_{\text{pre}} \Rightarrow_{\text{verify}} \varphi_{\text{post}} \end{array} \right\} \Gamma^L$

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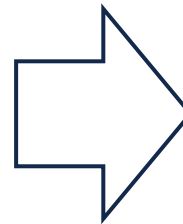
filling the “gaps” in the verification (“proof search”)



$\Gamma^L \vdash \varphi_{\text{pre}} \Rightarrow \text{verify } \varphi_{\text{post}}$

a proof object

proof checking



200-LOC
matching μ -logic
proof checker



indeed,
 P satisfies φ_P ;
check it
yourself!

something is
wrong
(verifier, proof
generator, PL
definitions, etc.)

Proof Generation: Complicated ...

top-level proof goal $\Gamma^L \vdash \varphi_{\text{pre}} \Rightarrow_{\text{verify}} \varphi_{\text{post}}$

$$\bigwedge_{(\psi_1 \Rightarrow \psi_2) \in A} \square (\forall FV(\psi_1, \psi_2). \psi_1 \Rightarrow_{\text{reach}}^+ \psi_2) \\ \wedge \bigwedge_{(\psi_1 \Rightarrow \psi_2) \in C} \circ \square (\forall FV(\psi_1, \psi_2). \psi_1 \Rightarrow_{\text{reach}}^+ \psi_2) \rightarrow (\varphi \Rightarrow_{\text{reach}}^\Delta \psi)$$



$$(t_j^{\text{hint}} \wedge p_j^{\text{hint}}) \Rightarrow_{\text{exec}} \\ (t_{j,1}^{\text{hint}} \wedge p_{j,1}^{\text{hint}}) \vee \dots \vee (t_{j,l_j}^{\text{hint}} \wedge p_{j,l_j}^{\text{hint}}) \vee (t_j^{\text{rem}} \wedge p_j^{\text{rem}})$$

sub-goal A



...

$$(t_j^{\text{hint}} \wedge p_{j,l}^{\text{hint}}) \rightarrow (lhs_{k_{j,l}} \theta_{k_{j,l}} \wedge q_{k_{j,l}} \theta_{k_{j,l}}) \\ (rhs_{k_{j,l}} \theta_{k_{j,l}} \wedge q_{k_{j,l}} \theta_{k_{j,l}}) \rightarrow (t_{j,l}^{\text{hint}} \wedge p_{j,l}^{\text{hint}})$$

sub-goal B



...

$$\square (\forall FV(\varphi, \psi). \varphi \Rightarrow_{\text{reach}} \psi) \\ \rightarrow \varphi' \Rightarrow_{\text{reach}} \varphi''$$

sub-goal C



...

... but none of the above needs to be trusted.

Evaluation

We tested on 3 PL paradigms:

- imperative
- register-based
- functional

Reduced K trust base
(~120k lines of Haskell)

Found issues in K
(missing axioms etc.)

Future work

- Apply it to more PLs

Task	Spec. LOC	Steps	Hint Size	Proof Size	K Verifier	Time (seconds)	
						Gen.	Check
sum.imp	40	42	0.58 MB	37/1.6 MB	4.2	105	1.8
sum.reg	46	108	2.24 MB	111/3.6 MB	9.1	259	5.4
sum.pcf	18	22	0.29 MB	38/1.5 MB	2.9	119	2.4
exp.imp	27	31	0.5 MB	37/1.5 MB	3.7	108	2.0
exp.reg	27	43	0.96 MB	70/2.3 MB	4.7	177	3.1
exp.pcf	20	29	0.5 MB	65/2.3 MB	3.8	199	3.1
collatz.imp	25	55	1.14 MB	49/1.7 MB	4.8	138	2.6
collatz.reg	37	100	3.66 MB	209/4.7 MB	9.3	414	5.5
collatz.pcf	26	39	1.51 MB	110/2.2 MB	5.3	247	5.2
product.imp	44	42	0.62 MB	44/1.8 MB	3.9	124	2.4
product.reg	24	42	0.81 MB	65/2.3 MB	4.3	164	4.0
product.pcf	21	48	0.82 MB	80/2.8 MB	5.3	234	4.9
gcd.imp	51	93	1.9 MB	74/2.3 MB	22.9	237	2.7
gcd.reg	27	73	1.92 MB	124/3.3 MB	18.6	306	3.6
gcd.pcf	22	38	1.35 MB	150/3.2 MB	12.8	367	5.2
ln/count-by-1	44	25	0.24 MB	28/1.3 MB	2.7	81	1.6
ln/count-by-2	44	25	0.26 MB	28/1.3 MB	9.0	88	1.4
ln/gauss-sum	51	39	0.53 MB	38/1.6 MB	4.6	107	2.0
ln/half	62	65	1.3 MB	63/2.2 MB	13.1	173	3.0
ln/nested-1	92	84	1.88 MB	104/3.4 MB	7.5	231	5.9

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Matching μ -Logic: A Unifying Foundation for Programming

