

Computer Vision

Exercise Session 2

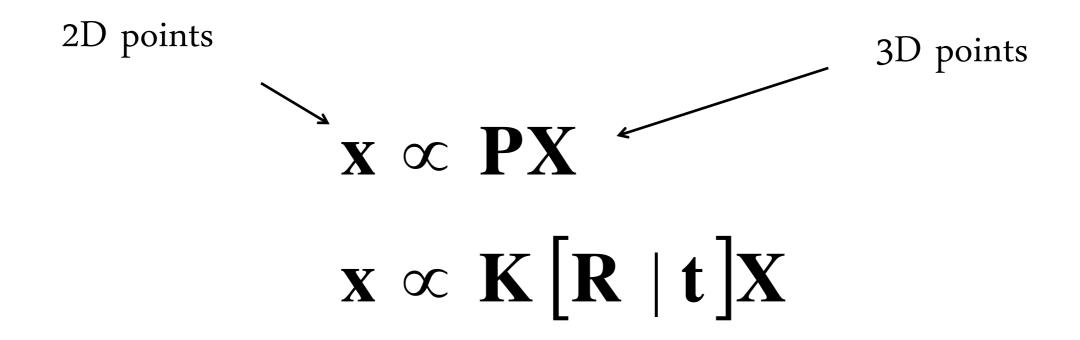




Camera Calibration

- Intrinsic parameters

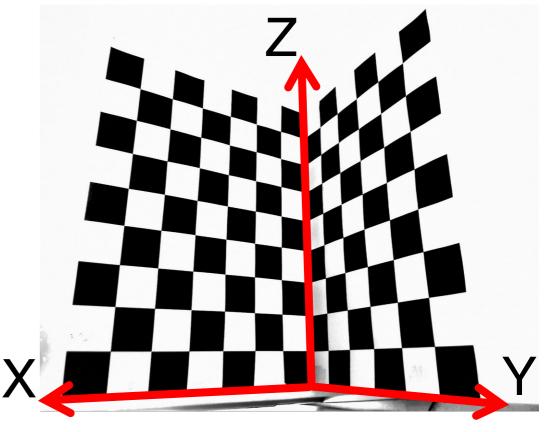
 - Radial distortion coefficients



Camera Calibration

- Use your own camera
- Build your own calibration object
 - Print checkerboard patterns

Stich to two orthogonal planes





Camera Calibration

- 4 Tasks:
 - Data normalization
 - Direct Linear Transform (DLT)
 - Gold Standard algorithm
 - Bouguet's Calibration Toolbox
- Use the same settings for all tasks!
- Good reference:

 Multiple View Geometry in computer vision
 (Richard Hartley & Andrew Zisserman)



Data normalization

- Shift the centroid of the points to the origin
- Scale the points so that average distance to the origin is $\sqrt{3}$ and $\sqrt{2}$, respectively.
- Determine $\hat{\mathbf{P}}$ using normalized points.
- Determine $P = T^{-1}\hat{P}U$

$$\mathbf{T} = \begin{bmatrix} s_{2D} & c_x \\ s_{2D} & c_y \\ 1 \end{bmatrix}^{-1}$$

$$\mathbf{U} = \begin{bmatrix} s_{3D} & c_x \\ s_{3D} & c_y \\ s_{3D} & c_z \\ 1 \end{bmatrix}^{-1}$$





Direct Linear Transform (DLT)

$$\mathbf{AP} = \begin{bmatrix} w_i X_i^T & 0^T & -x_i X_i^T \\ 0^T & -w_i X_i^T & y_i X_i^T \end{bmatrix} \begin{bmatrix} \mathbf{P}^1 \\ \mathbf{P}^2 \\ \mathbf{P}^3 \end{bmatrix} = 0$$

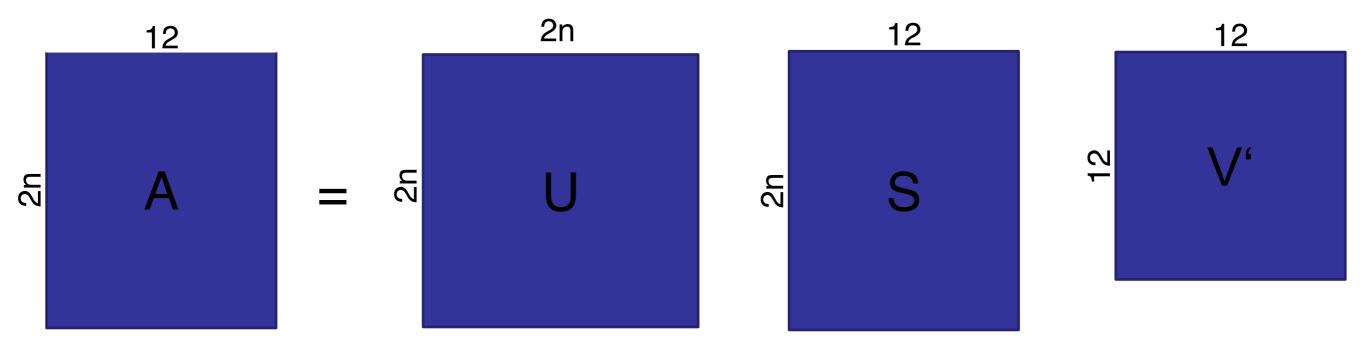
$$=\begin{bmatrix} X_{ix} & X_{iy} & X_{iz} & 1 & 0 & 0 & 0 & -x_{i}X_{ix} & -x_{i}X_{iy} & -x_{i}X_{iz} & -x_{i} \\ 0 & 0 & 0 & 0 & -X_{ix} & -X_{iy} & -X_{iz} & -1 & y_{i}X_{ix} & y_{i}X_{iy} & y_{i}X_{iz} & y_{i} \end{bmatrix} \begin{bmatrix} P_{1,1} \\ P_{1,2} \\ \vdots \\ P_{3,3} \\ P_{3,4} \end{bmatrix}$$





Direct Linear Transform (DLT)

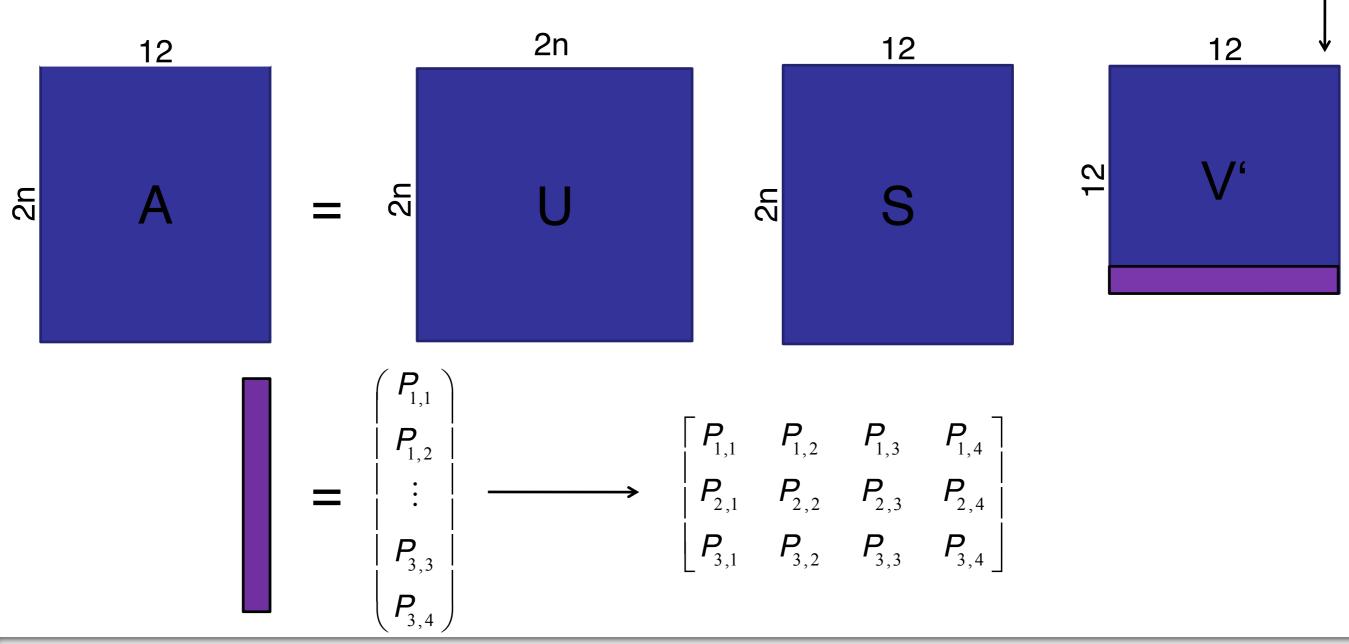
Singular Value Decomposition





Direct Linear Transform (DLT)

Singular Value Decomposition





Camera Matrix Decomposition (K and R)

$$\mathbf{P} = \mathbf{K} \begin{bmatrix} \mathbf{R} \mid \mathbf{t} \end{bmatrix} = \begin{bmatrix} \mathbf{K} \mathbf{R} \mid -\mathbf{K} \mathbf{R} \mathbf{C} \end{bmatrix}$$

- K is upper triangular
- **R** is orthonormal
- \blacksquare **QR** decomposition **A** = **QR**
 - **Q** is orthogonal
 - **R** is upper triangular





Camera Matrix Decomposition (K and R)

$$\mathbf{P} = \mathbf{K} \begin{bmatrix} \mathbf{R} \mid \mathbf{t} \end{bmatrix} = \begin{bmatrix} \mathbf{K} \mathbf{R} \mid -\mathbf{K} \mathbf{R} \mathbf{C} \end{bmatrix}$$
$$\mathbf{M} = \mathbf{K} \mathbf{R}$$

 $\mathbf{M}^{-1} = \mathbf{R}^{-1} \mathbf{K}^{-1}$

- Run **QR** decomposition on the inverse of the left 3x3 part of **P**
- Invert both result matrices to get **K** and **R**



Camera Matrix Decomposition (C)

The camera center is the point for which

$$\mathbf{PC} = 0$$

This is the right null vector of \mathbf{P} (\rightarrow SVD)

Gold Standard Algorithm

- Normalize data
- Run DLT to get initial values
- Compute optimal **P** by minimizing the sum of squared reprojection errors

$$\min_{\hat{\mathbf{P}}} \sum_{i=1}^{N} d(\hat{\mathbf{x}}_{i}, \hat{\mathbf{P}}\hat{\mathbf{X}}_{i})^{2}$$

■ Denormalize **P**



Bouguet's Calibration Toolbox

- Download and install the toolbox: (http://www.vision.caltech.edu/bouguetj/calib_doc/index.html)
- Go through the tutorial and learn how to calibrate a camera with that toolbox
- Print your own calibration pattern (available on the website)
- Use the toolbox for calibration and compare the result with the results of your own calibration algorithm





Hand-in

- Source code
- Matlab .mat file with hand-clicked 3D-2D correspondences
- Image used for calibration
- Visualize hand-clicked points and reprojected 3D points
- Discuss and compare values of calibration obtained for all methods
- Discuss average reprojection error of all methods.



Some hints

- Work with normalized homogeneous coordinates always. Camera calibration **K** should respect this convention.
- Check that the obtained orientation **R** correspond to the expected world value, otherwise **K** will have negative values in its diagonal.
- When reprojecting points use average of reprojection error for comparison and remember to normalize reprojected coordinates to w = 1.
- Remember to use the same camera with the same settings for all tasks!



Hand-in

Example reprojection of the the 3D points

