Übungsblatt 6 "Mustererkennung"

J. Cavojska, N. Lehmann, R. Toudic 16.06.2015

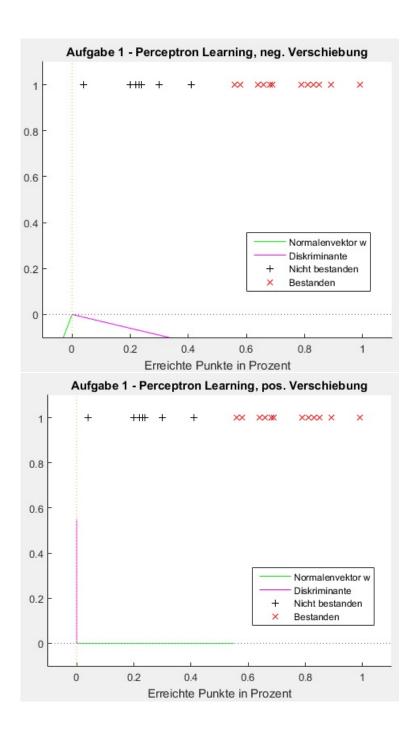
Inhaltsverzeichnis

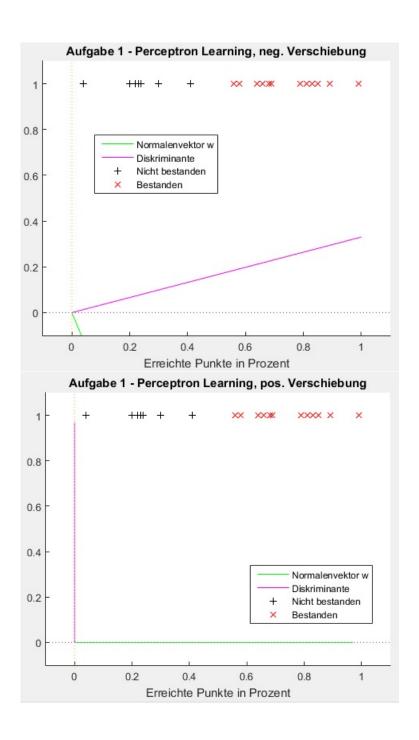
1	Perzeptron Lernalgorithmus													2						
2	Sch	wellwerte																		8
	2.1	Aufgabe 2A																		8
	2.2	Aufgabe 2B																		10

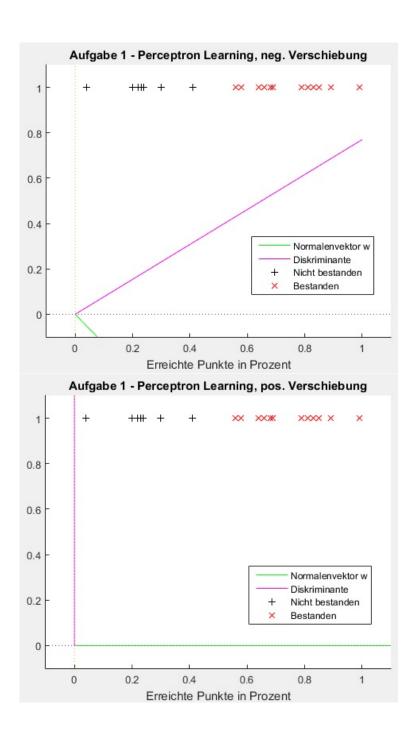
1 Perzeptron Lernalgorithmus

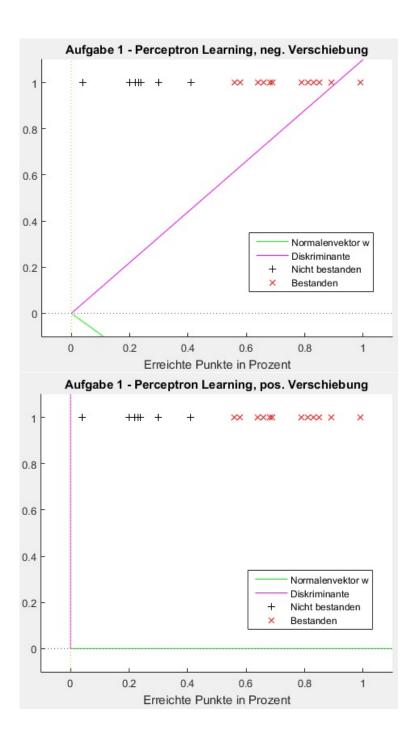
```
% Clean up
     clear all
 2
 3
    close all
 5
    % Datenaufbereitung
               = load('klausur.txt');
    Data
    Punkte = Data(:,1);
    Features = horzcat(Punkte, ones(size(Punkte,1), 1));
10
     Noten
              = Data(:,2);
     Punkte0 = Data((Data(:,2)==0),:);
     {\tt Punkte1} \ = \ {\tt Data}\left(\left(\, {\tt Data}\left(\, :\, ,2\, \right) = = 1\right)\, ,:\,\right)\, ;
12
13
                 = linspace(0,1);
    x1
14
    x2
                 = linspace(-5,5);
15
16
     w = [0 \ 0]; \% random choosen vector w
17
18
     limit = size(Data, 1); % number of iterations | Abbruchkriterium
19
     for i = 1:limit
          if w(1) == 0 \&\& w(2) == 0
20
21
                w_norm = [0 \ 0];
22
           else
23
                w_norm = w / norm(w);
24
25
          \mathtt{lineNum} \, = \, \mathtt{mod} \, \big( \, \mathtt{i} \, \, , \, \, \, \, \mathbf{size} \, \big( \, \mathtt{Features} \, \, , 1 \, \big) \, \big) \, + 1;
          proj = Features(lineNum, :) * w_norm'; % scalar projection
26
27
28
           if Noten(lineNum) == 1
29
                if proj < 0 \% wrong classification
30
31
                      Features(lineNum, :);
                      w = w + Features(lineNum, :);
32
33
                      w_norm = w / norm(w);
34
                      \mathbf{w}_{\mathbf{x}} = \mathbf{w}(1) * \mathbf{x1};
35
                      if w(2) == 0
36
37
                           w_y = w_x * 0;
38
                           \mathtt{coeff\_w} \, = \, \mathtt{w} \, (\, 2\, ) \ / \ \mathtt{w} \, (\, 1\, )
39
40
                            w_y = w_x * coeff_w;
41
42
                      \mathtt{diskriminante} \, = \, \left[ -\mathtt{w} \, (\, 2\,) \ \mathtt{w} \, (\, 1\,) \, \right];
43
44
                      diskriminante_x = diskriminante(1) * x1;
45
                      \quad \text{if diskriminante} \, (1) \, = \!\!\! = 0
46
                           diskriminante_y = linspace(0, diskriminante(2));
47
48
49
                           {\tt coeff\_d} = {\tt diskriminante}(2) / {\tt diskriminante}(1);
50
                            diskriminante_y = diskriminante_x * coeff_d;
51
                      end
```

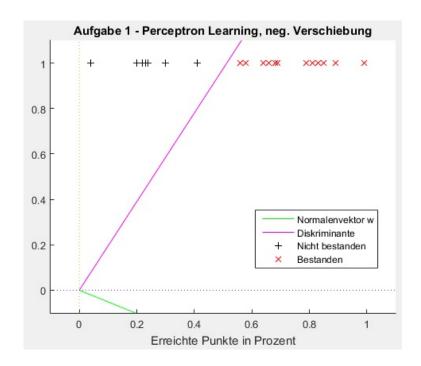
```
53
                         % plot
 54
                         figure ('NumberTitle', 'off', 'Name', 'Aufgabe 1 - Perceptron ←
                               Learning ');
 55
                         hold on
 56
 57
                         plot(w_x, w_y, 'g');
 58
                         {\color{red} \textbf{plot}} \left( \, \texttt{diskriminante\_x} \; , \; \; {\color{red} \textbf{diskriminante\_y}} \; , \; \; {\color{red} \mbox{'}} m^{\scriptscriptstyle \top} \right);
 59
                         \texttt{gscatter}\left(\texttt{Punkte}\;,\;\; \texttt{ones}\left(\;\texttt{size}\left(\;\texttt{Punkte}\;,1\right)\;,\;\;1\right)\;,\;\; \texttt{Noten}\;,\;\; ^{|}\texttt{krb}\;^{|}\;,\; ^{|}+\texttt{x}^{|}\;,[]\;,\;\; ^{|}\leftarrow\;\;
                               off');
 60
                         title ('Aufgabe 1 - Perceptron Learning, pos. Verschiebung');
 61
 62
                         xlabel('Erreichte Punkte in Prozent');
 63
                         axis([-0.1 \ 1.1 \ -0.1 \ 1.1]);
                         \textbf{legend('Normalenvektor w', 'Diskriminante', 'Nicht bestanden','} \leftarrow
 64
                               Bestanden ');
                         xL = xlim;
 65
 66
                         yL = ylim;
                         plot([0 0], yL, ':');
plot(xL, [0 0], ':');
 67
 68
 69
                   end
 70
             end
 71
             if Noten(lineNum) == 0
 72
                   if proj >= 0 % wrong classification
 73
                         w = w - Features(lineNum,:);
 74
 75
                         w_norm = w / norm(w);
                         \texttt{coeff\_w} \, = \, \texttt{w} \, (\, 2\, ) \ \ / \ \ \texttt{w} \, (\, 1\, ) \; ; \\
 76
 77
                         w_x = w(1) * x1;
 78
                         w_y = w_x * coeff_w;
                         diskriminante = [-w(2) w(1)];
 79
 80
                         coeff_d = diskriminante(2) / diskriminante(1);
 81
                         {\tt diskriminante\_x} \, = \, {\tt diskriminante} \, (1) \, * \, {\tt x1} \, ;
 82
                         diskriminante_y = diskriminante_x * coeff_d;
 83
 84
                         figure ('NumberTitle', 'off', 'Name', 'Aufgabe 1 − Perceptron ←
 85
                               Learning ');
 86
                         hold on
 87
                         plot(w_x, w_y, 'g');
 88
 89
                         plot(diskriminante_x, diskriminante_y, 'm');
 90
                         \texttt{gscatter}\left(\texttt{Punkte}\;,\;\; \texttt{ones}\left(\;\texttt{size}\left(\;\texttt{Punkte}\;,1\right)\;,\;\;1\right)\;,\;\; \texttt{Noten}\;,\;\; ^{|}\texttt{krb}\;^{|}\;,\; ^{|}+\texttt{x}^{|}\;,[]\;,\;\; ^{|}\leftarrow\;\;
                               off ');
 91
                         title ( 'Aufgabe 1 - Perceptron Learning, neg. Verschiebung ');
 92
 93
                         xlabel('Erreichte Punkte in Prozent');
 94
                         axis([-0.1 \ 1.1 \ -0.1 \ 1.1]);
                         \textbf{legend('Normalenvektor w', 'Diskriminante', 'Nicht bestanden', '} \leftarrow
 95
                               Bestanden ');
 96
                         xL = xlim;
 97
                         yL = ylim;
                         plot([0 0], yL, ':');
plot(xL, [0 0], ':');
 98
 99
100
                   end
101
             end
102
      end
```











2 Schwellwerte

2.1 Aufgabe 2A

```
schwellwerte = [];
 2
     for iter = 1:100
 3
           randOrder = randperm(size(Features, 1));
           {\tt randFeatures} \; = \; {\tt Features} \, (\, {\tt randOrder}^{\; !} \,) \; ;
 4
 5
          w = [max(Punkte) max(Noten)]; % random choosen vector w
           t = 0;
 6
          limit = size(Data, 1); % number of iterations
 7
 8
           for i = 1:limit
 9
                {\tt w\_norm} \ = \ {\tt w} \ \ / \ \ \frac{{\tt norm}}{{\tt norm}} \, (\, {\tt w}\, ) \; ;
10
                proj = randFeatures(lineNum, :) * w_norm'; % scalar projection
11
                 if Noten(lineNum) = 1
12
13
                       if proj < 0
14
                            {\tt t} \, = \, {\tt t} \, + \, 1;
15
                            w = w + randFeatures(lineNum, :);
16
                            \mathtt{diskriminante} \, = \, \left[ -\,\mathtt{w} \, (\, 2\,) \, \, \, \mathtt{w} \, (\, 1\,) \, \, \right];
17
                      end
18
                end
19
                 \quad \text{if} \ \ \texttt{Noten}(\texttt{lineNum}) \, = \!\!\! = 0
                       if proj >= 0 % wrong classification t = t + 1;
20
21
```

```
22
                                           {\tt w} \; = \; {\tt w} \; - \; {\tt randFeatures} \, (\, {\tt lineNum} \; , \; \; : \, ) \; ; \\
23
24
                                           \label{eq:diskriminante} \mbox{diskriminante} \; = \; \left[ -\,\mbox{w} \left( \, 2 \, \right) \,\,\,\mbox{w} \left( \, 1 \, \right) \, \right];
                                 end
                        end
25
26
27
                {\tt schwellwerte} \ = \ {\tt vertcat} \, (\, {\tt schwellwerte} \, \, , \  \, {\tt w} \, ) \, ;
28
        \quad \text{end} \quad
29
      % output schwellwerte
30
31
```

2.2 Aufgabe 2B

```
figure('NumberTitle','off','Name','Aufgabe 2 - Lin. Regression');
 3
       % calculate
       \mathtt{onesVector} \, = \, \mathtt{ones} \, (\, \mathbf{size} \, (\, \mathtt{Data} \, , 1 \,) \, \, , \quad 1 \,) \, ;
 4
       X = horzcat(onesVector, Punkte);
       beta = inv(X'*X) * X' * Noten;
       fx = beta(1) + beta(2)*x2;

pkt = (0.5 - beta(1))/beta(2);
       \% \text{ pkt} = 0.4804
10
11
       % plot
12
       hold on
       \texttt{scatter} \left( \texttt{Punkte} \;,\;\; \texttt{Noten} \;,\;\; {}^{\scriptscriptstyle \top} x^{\scriptscriptstyle \top} \;,\;\; {}^{\scriptscriptstyle \top} b^{\scriptscriptstyle \top} \right)
13
       plot (x2,fx, 'g')
scatter(pkt,0.5, 'o', 'r')
14
15
16
       \begin{array}{ll} axis\left(\left[-0.1\ 1.1\ -0.1\ 1.1\right]\right);\\ legend\left(\ ^{\mid}Noten\ ^{\mid},\ ^{\mid}Diskriminante\ ^{\mid},\ ^{\mid}Schwellenwert\ ^{\mid}\right); \end{array}
17
```

