

Notebook (2019)

Contents

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1	algorithms	1	5.14	IsPrime	13
1.1	Catalan	1	5.15	knapsack	13
1.2	HornersRule	2	5.16	MatrixFibo	13
1.3	Kadane	2	5.17	MillerTest	14
1.4	PickTheorem	2	5.18	NaiveFind	14
2	data-structures	2	5.19	PollarRho	14
2.1	Fenwick	2	5.20	PollarRho	14
2.2	MST	3	5.21	PrimalyTest	15
2.3	SegmentTree1	3	5.22	RotateMatrix	15
2.4	SegmentTree2	3	5.23	Sieve	15
2.5	Trie	4	5.24	Sum	15
2.6	UnionFind	5	5.25	toBin	15
3	geometry	5	6	other	16
3.1	CenterCircle	5	6.1	MergeSortPY	16
3.2	PolygonArea	5	6.2	Partitions	16
3.3	RayCasting	6	6.3	TemplateC	16
3.4	Struct	6	6.4	TemplateP	17
4	graph	7	6.5	UpperLowerBound	17
4.1	Dijkstra	7	6.6	XIncludes	17
4.2	DijkstraHeap	8	6.7	YGenerator	18
4.3	EdmonKarp	8	7	strings	18
4.4	FloydWarshal	9	7.1	Kmp	18
4.5	RecoveryTree	9	7.2	LIS	18
4.6	Tsort	9	7.3	LRSubs	18
5	mathematics	10	7.4	StringUtil	19
5.1	Binomial	10	7.5	SubstrK	19
5.2	Binomial	10	7.6	Zalgorithm	20
5.3	ChangeBases	10	1	algorithms	
5.4	CoinChange	10	1.1	Catalan	
5.5	Combination	11			
5.6	CompareDoubles	11			
5.7	Exponentiation	11			
5.8	ExtendedEuclides	11			
5.9	ExtendEuclidesSample	12			
5.10	Factorize	12			
5.11	FastPow	12			
5.12	GcdLcm	13			
5.13	IsFibo	13			

```

#include <bits/stdc++.h>
#define MAX 35
using namespace std;
typedef unsigned long long ll;

ll dp[MAX];
int vi[MAX];
/*
Complexity: O(n ^ 2)
*/
ll catalan( int n){
    if ( n <= 1 ) return 1;
    if( vi[n] ) return dp[n];
    vi[n] = 1;
    ll &res = dp[n];
    for( int i= 0; i < n; i++)
        res += catalan(i) * catalan( n -i -1);
    return res;
}

```

```

}
int main(){
    memset( dp, 0, sizeof(dp));
    memset( vi, 0, sizeof(dp));
    for( int i = 1; i < 10; i++)
        cout << catalan( i ) <<endl;
    return 0;
}

```

1.2 HornersRule

```

#include <iostream>
using namespace std;
/*
 * given the polynomial  $f(x) = 2x^3 - 6x^2 - 2x - 1$ 
 *  $f(8) = ?$ 
 *      |  $X^3$   $X^2$   $X^1$   $X^0$ 
 *      | 2   -6   -2   -1
 *      |      16   80   624
 *      |-----|
 *      | 2   10   78   623
 *  $f(8) = 623$ 
 * Complexity  $O(n)$ 
 */
typedef long long ll;
ll Horner( ll a[], ll n, ll x ){
    ll result = a[n];
    for(ll i=n-1; i >= 0 ; --i)
        result = result * x + a[i];
    return result;
}
int main(){
    ll grade = 3;
    // -1 -2x -6x^2 +2x^3
    ll a[] = {-1,-2,-6,2};
    ll x = 8;
    cout << Horner (a, grade, x);
    return 0;
}

```

1.3 Kadane

```

#include <bits/stdc++.h>
#define forn(i,j,k) for(int i=j; i<k; i++)
using namespace std;
typedef long long ll;
/*
 * Largest Sum Contiguous Subarray
 * Kadane Algorithm
 * Complexity:  $O(n)$ 
 */
inline ll kadane(ll data[8], int size){
    ll m1= data[0];
    ll m2 = data[0];
    forn(i, 1, size){
        m2 = max(data[i], data[i] + m1);
        m1 = max(m1, m2);
    }
    return m1;
}
int main(){
    int size = 8;
    ll data[8] = {-1,2,4,-3,5,2,-5,2};
    ll res = kadane(data, size);
}

```

```

printf("The max sum that can be done with \n \
Contiguous elements is: %lld \n", res);
return 0;
}

```

1.4 PickTheorem

```

#include <stdio.h>
using namespace std;
/*
 * Pick's theorem is a useful method for determining the area
 * of any polygon whose vertices are points on a lattice,
 * a regularly spaced array of points
 *
 * b boundary point :
 *   a lattice point on the polygon including vertices
 * i interior point :
 *   a lattice points on the polygon's interior region
 *
 * Complexity:  $O(1)$ 
 */
double area_poligon(double b, double i){
    return (b/2) + i -1;
}
int main(){
    printf("%f",area_poligon(5,5));
    return 0;
}

```

2 data-structures

2.1 Fenwick

```

#include<bits/stdc++.h>
#define endl '\n'
using namespace std;
typedef long long ll;
typedef vector < ll> vll;
/*
 * Complexity Query  $O(n)$ 
 */
struct fw {
    int n; vll data;
    fw(int _n) : n(_n), data(vll(_n)) { }
    void update(int at, ll by) {
        while(at < n) {
            data[at] += by;
            at |= at + 1;
        }
    }
    void update_range( int l, int r, ll by){
        update(l, by);
        update(r+1, -by);
    }
    ll query(int at) {
        ll res = 0LL;
        while(at >= 0) {
            res += data[at];
            at = (at & (at + 1)) - 1;
        }
        return res;
    }
};

```

```

int main(){
#ifdef LOCAL
    freopen("in","r", stdin);
#endif
    ios::sync_with_stdio(0);cin.tie(0);
    int n, q ,a, b;
    char op;
    cin >> n >> q;
    fw *fen = new fw(n+1);
    for( int i = 0; i < q ; i++){
        cin >> op;
        if( '+' == op){
            cin >> a >> b;
            fen->update(a,b);
        }else{
            cin >>a; a--;
            cout << fen->query(a) << endl;
        }
    }
}

```

2.2 MST

```

#include<bits/stdc++.h>
using namespace std;

/*
Complexity: nlog(n)
*/
// from, to, weight
typedef tuple< int,int,int > edge;
typedef vector< int > vi;
bool customSort(const edge &a,const edge & b){
    return get<2>(a) < get<2>(b);
}
vector< edge > mst( vector< edge > &edges , int n ){
    union_find uf( n );
    vector< edge > res;
    sort( edges.begin(), edges.end(), customSort);
    int f, t , w;
    int tw =0;
    for( const edge &e: edges){
        tie(f, t, w) = e;
        if( uf.unite( f, t ) )res.push_back( e);
    }
    return res;
}
int main(){
#ifdef LOCAL
    freopen("in", "r", stdin);
#endif
    int n, m;
    int f, t , w;
    cin >> n >> m;
    vector< edge > edges( m );
    for( int i = 0 ; i <m ; i++){
        cin >> f >> t >> w;
        edges[i] = make_tuple( f, t, w);
    }
    mst( edges, n );
    return 0;
}

```

2.3 SegmentTree1

```

#include <iostream>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;
const int N = 1e5 + 10;
int n, q;
int t[2 * N]; // limit

//built the tree O(n)
void built(){
    for (int i = n - 1; i > 0; i--) {
        t[i] = t[i << 1] + t[i << 1 | 1];
    }
}

// set y at position x O(log(n))
void update(int x, int y) {
    for (t[x += n] = y; x > 1; x >>= 1) {
        t[x >> 1] = t[x] + t[x ^ 1];
    }
}

//operation on interval [l, r) O(log(n))
int query(int l, int r) {
    int res = 0;
    for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
        if (l & 1) res += t[l++];
        if (r & 1) res += t[--r];
    }
    return res;
}
int main() {
#ifdef LOCAL
    freopen("SegmentTree.test","r",stdin);
#endif
    cin >> n >> q;
    for (int i = 0; i < n; i++) {
        cin >> t[i + n];
    }
    built();
    int l, r, ty,pos , val;
    for (int i = 0; i < q; i++) {
        cin >> ty;
        if( ty == 1){ // query
            cin >> l >> r; l--;
            cout << query( l, r ) << endl;
        }else if( ty == 2){ //update single value
            cin >> pos >> val; // pos 1 indexed
            pos--;
            update(pos, val);
        }
    }
    return 0;
}

```

2.4 SegmentTree2

```

#include <iostream>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;
const int N = 1e5 + 10;

```

```

int n, q;
int t[2 * N], lazy[2*N]; // limit
int arr[N];

//built the tree O(n)
void built(int l, int r, int node=1){
    if( l > r) return;
    if( l == r){
        t[node] = arr[l];
        return;
    }
    int mid = (l+r)/2;
    built( l, mid, node<<1);
    built( mid+1, r, node<<1|1);
    t[node] = t[node<<1] + t[node<<1 |1];
}

// query O(lg(n))
int query(int start, int end, int l, int r, int node=1){
    if( r < start || end < l) return 0;
    if( start >= l && end <= r) return t[ node ];
    int mid = ( start + end ) >> 1;
    int lans = query( start, mid, l, r, node<<1);
    int rans = query( mid+1, end, l, r, node<<1|1);
    return lans + rans;
}

// Update a pos O(lg(n))
void update(int start, int end, int idx, int val, int node=1){
    if( start == end){
        arr[ idx ] = val; // change value in the st
        t[ node ] = val;
        return;
    }
    int mid = (start+ end)>>1;
    if( start <= idx and idx <= mid){
        update( start,mid, idx, val, node*2);
    }else{
        update( mid+1, end, idx, val, node*2+1);
    }
    t[ node ] = t[ node << 1 ] + t[node << 1 |1];
}

// Update Range Lazy log(n)
void updateRange( int start, int end, int l, int r, int val, int
node =1){
    if( lazy[node] != 0){ //pending update
        t[ node ] += ( end - start +1) * lazy[ node ];
        if( start != end){
            lazy[ node << 1] += lazy[node];
            lazy[ node <<1 |1] += lazy[node];
        }
        lazy[ node] = 0;
    }
    if( start > end || start >r || end <l ) return;
    if( start >= l && end <= r){ // fully in range
        t[ node] += (end - start +1) * val;
        if( start != end){
            lazy[ node<<1] += val;
            lazy[ node<<1|1] += val;
        }
        return;
    }
    int mid = ( start +end ) >> 1;
    updateRange( start, mid, l, r, val, node<<1);
    updateRange( mid+1, end, l, r, val, node<<1|1);
    t[node] = t[ node<<1] + t[node<<1|1];
}

```

```

}

//query lazy
int queryLazy(int start, int end, int l, int r, int node=1){
    if( start > end || start > r || end < l) return 0;
    if( lazy[ node] != 0 ){
        t[node] += (end -start +1) * lazy[ node ];
        if( start != end){
            lazy[node<<1] += lazy[ node];
            lazy[node<<1|1] += lazy[node];
        }
        lazy[node] = 0;
    }
    if( start >= l && end <= r) return t[ node ];
    int mid = (start + end) /2;
    int p1 = queryLazy( start, mid, l, r, node<<1);
    int p2 = queryLazy( mid+1, end, l, r, node<<1|1);
    return p1 + p2;
}

int main() {
#ifdef LOCAL
    freopen("SegmentTree.test","r",stdin);
#endif
    cin >> n >> q;
    for (int i = 0; i < n; i++){
        cin >> arr[i];
    }
    built( 0, n-1);
    int l, r, ty,pos, val;
    for (int i = 0; i < q; i++) {
        cin >> ty;
        if( ty == 1){ // query
            cin >> l >> r; l--; r--;
            cout << queryLazy(0, n-1, l, r) << endl;
            /* cout << query( 0, n-1, l, r) <<endl; */
        }else if( ty == 2){ //update single value
            cin >> pos >> val; // pos 1 indexed
            pos--;
            update( 0, n-1, pos, val);
        }else if( ty ==3){
            cin >> l >> r >> val;
            l--;r--;
            debug(l); debug( r); debug( val );
            updateRange(0, n-1, l, r, val);
        }
    }
    return 0;
}

```

2.5 Trie

```

#include <bits/stdc++.h>
using namespace std;
/*
 * Struct for a trie
 */
struct node {
    node * son[26];
    bool is_end;
    int num_times;
    node(){
        memset(son, 0, sizeof(son));
        is_end =false;
        num_times =0;
    }
}

```

```

};
/*
 * insert a word in the trie
 */
void insert(node* nd, char *s){
    if(*s){
        int pos = *s - 'a';
        if(!nd->son[pos]) nd->son[pos]=new node();
        insert(nd->son[pos], s+1);
    }else{
        nd->is_end = true;
    }
}
/*
 * Check if the word is in the trie
 */
int contains(node *nd, char *s){
    if(*s){
        int pos = *s - 'a';
        if(!nd->son[pos]) return false;
        return contains(nd->son[pos], s+1);
    }else{
        return nd->is_end;
    }
}
int main(){
    node * trie = new node();
    string a = "word";
    char *cstr = new char[a.length() + 1];
    strcpy(cstr, a.c_str());
    insert (trie, cstr);
    string b = "banani";
    strcpy(cstr, b.c_str());
    insert (trie, cstr);
    if (contains(trie, cstr)){
        cout << "ohh holly xx." << endl;
    }else{
        cout << "mother ..." << endl;
    }
    return 0;
}

```

2.6 UnionFind

```

#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
/*
 * Complexity O(log(n))
 */
struct union_find {
    vi p;
    union_find(int n) : p(n, -1) {}
    int find(int x) {
        return p[x] < 0 ? x : p[x] = find(p[x]);
    }
    bool unite(int x, int y) {
        int xp = find(x), yp = find(y);
        if (xp == yp) return false;
        if (p[xp] > p[yp]) swap(xp, yp);
        p[xp] += p[yp];
        p[yp] = xp; //add -1 if merge
        return true;
    }
    int size(int x) {

```

```

        return -p[find(x)];
    }
};

int main() {
    union_find uf(10);
    uf.unite(0, 2);
    cout << uf.find(0) << endl;
    cout << uf.find(2) << endl;
    assert(uf.find(0) == uf.find(2));
    assert(uf.find(0) != uf.find(1));
    return 0;
}

```

3 geometry

3.1 CenterCircle

```

#include <bits/stdc++.h>
using namespace std;
const double PI = acos(-1);
#define show(x) cout << #x << " = " << x << endl;
/*
 * Complexity O(1)
 */
struct pt {
    double x;
    double y;
    pt (){}
    pt (double _x, double _y){
        x = _x;
        y = _y;
    }
};
inline pt getCenter(pt p1, pt p2, pt p3){
    pt center;
    float m1 = (p2.y - p1.y)/(p2.x - p1.x);
    float m2 = (p3.y - p2.y)/(p3.x - p2.x);
    center.x = ( m1 * m2 * (p1.y - p3.y) + m2 * ( p1.x + p2.x)
                - m1 * (p2.x + p3.x) )
                / (2 * (m2 - m1) );
    center.y = -1 * (center.x - (p1.x + p2.x) / 2) / m1 + (p1.y +
        p2.y) / 2;
    return center;
}

int main(){
    pt p1(1,1), p2(2,4), p3(5,3);
    pt res = getCenter(p1, p2, p3);
    show(res.x)
    show(res.y)
    return 0;
}

```

3.2 PolygonArea

```

#include <bits/stdc++.h>
#define f first
#define s second
#define mp make_pair
#define pb push_back
using namespace std;
typedef long double ld;

```

```

typedef pair<ld, ld> point;
typedef vector< point > polygon;

/*
Complexity O(n)
*/
inline point diff(point o, point d){
    return mp(d.f-o.f, d.s - o.s);
}
inline ld crossProduct(point o, point d){
    ld cross = (o.f * d.s) - (o.s * d.f);
    return cross > 0 ? cross : cross * -1;
}
inline ld area(polygon p){
    int num_points = p.size();
    ld area = 0;
    for (int i = 1; i < num_points - 1; i++){
        point l1 = diff(p[0], p[i]);
        point l2 = diff(p[0], p[i+1]);
        area += crossProduct(l1, l2);
    }
    return abs(area/2.0);
}
int main(){
    polygon p;
    p.pb(mp(1,0)); p.pb(mp(2,1));
    p.pb(mp(1,2)); p.pb(mp(0,1));
    cout << area(p);
    return 0;
}

```

3.3 RayCasting

```

#include <bits/stdc++.h>
#define pb push_back
#define mp make_pair
using namespace std;
/*
This program implements the ray casting algorithm to check
if a point is inside or outside of a simple polygon
*/
typedef double ld;
struct point {
    ld x, y;
    point(){}
    point(ld x, ld y){
        this->x = x;
        this->y = y;
    }
};
struct vert {
    point o,d;
};
typedef vector< point > polygon;

inline ld cross(point o, point d){
    return(o.x * d.y) - (o.y * d.x);
}
inline ld dot(point o, point d){
    return (o.x * d.x) + (o.y * d.y);
}
inline point diff(point o, point d){
    return {d.x-o.x, d.y - o.y};
}
inline ld dist(point o, point d){
    return sqrt(dot(diff(o,d), diff(o,d)));
}

inline bool segments_parallel(point a, point b, point c){
    return abs(cross(diff(c,a), diff(b,a))) == 0;
}

```

```

}
inline bool point_on_segment(polygon v, point c){
    int cant = v.size();
    for (int i=0; i<cant; i++){
        if (dist(v[i], c)==0) return true;
        if (dist(v[(i+1)%cant], c)==0) return true;
        if (segments_parallel(v[i], v[(i+1)%cant], c) &&
            dot(diff(c, v[i]), diff(c, v[(i+1)%cant])) < 0) {
            return true;
        }
    }
    return false;
}

/* Ray Casting algorithm
true inside
false outside
*/
bool point_in_polygon(point p, polygon a){
    bool inside = false;
    int cant = a.size();
    for (int i=0; i<cant; i++){
        int j = (i+1) % cant;
        point aux = a[i];
        point nxt = a[j];
        bool cond1 = (p.y < aux.y != p.y < nxt.y);
        bool cond2 = (p.x < aux.x + (nxt.x - aux.x) * (p.y - aux.y) /
            (nxt.y - aux.y));
        if (cond1 && cond2){
            inside = !inside;
        }
    }
    return inside;
}
inline void test_point(polygon v, point pun){
    if(point_on_segment(v, pun)){
        cout << "on"<<endl;
    }else if (point_in_polygon(pun, v)){
        cout << "in"<<endl;
    }else{
        cout << "out"<<endl;
    }
}
int main(){
    polygon p;
    p.pb(point(1,0)); p.pb(point(2,1));
    p.pb(point(1,2)); p.pb(point(0,1));
    test_point(p, point(0,0));
    test_point(p, point(1,1));
    test_point(p, point(1.5,0.5));
    return 0;
}

```

3.4 Struct

```

#include <bits/stdc++.h>
#define INF 1e9
#define EPS 1e-9
#define PI acos(-1.0)
#define debug(x) cout << #x << " " << x << endl;

using namespace std;

struct point {
    double x, y;
    point() {}
}

```

```

point(double _x, double _y){
    x = _x;
    y = _y;
}
point operator + (point p) const {
    return point(p.x + x, p.y + y); }
point operator - (point p) const {
    return point(x - p.x, y - p.y); }
point operator *(double d) const {
    return point(x*d, y*d); }
bool operator ==(point p) const {
    return p.x == x && p.y == y; }
double dot(point p) {
    return x*p.x + y*p.y;};
double cross2(point p) {
    return x*p.y - p.x*y;};
double mag () {
    return sqrt(x*x + y*y);};
double norm() {
    return x*x + y*y;};
double dist(point p2){
    return hypot(x - p2.x, y - p2.y); };
void show(){ printf("x= %lf, y=%lf\n", x, y);}
};

struct line {
    point o; //origin
    point d; //destiny
    double m;
    line (){}
    line( point _o, point _d){
        o = _o;
        d = _d;
    }
    double slope(){
        if (o.x != d.x){
            m = (double)(d.y - o.y) / (double)(d.x - o.x);
            return m;
        }
        m = INF;
        return INF;
    }
};

double cross(point &o, point &a, point &b) {
    return (a.x - o.x)*(b.y - o.y) - (a.y - o.y)*(b.x - o.x);
}
bool areParallel(line l1, line l2) {
    return fabs(l1.slope()-l2.slope())<EPS ;
}
double distToLine(point p, line l1) {
    // formula: c = a + u * ab
    point a = l1.o, b = l1.d, c;
    point ap = p-a, ab = b-a;
    double u = ap.dot(ab) / ab.norm();
    c = a + ab*u;
    return c.dist(p);
}

double distToSegment(point p, line l1) {
    point a = l1.o, b = l1.d, c;
    point ap = p-a, ab = b-a;
    double u = ap.dot(ab) / ab.norm();
    if (u < 0.0) {
        c = point(a.x, a.y); // closer to a
        return p.dist(a);
    }
    if (u > 1.0) {

```

```

        c = point(b.x, b.y); // closer to b
        return p.dist(b);
    }
    return distToLine(p, line(a, b));
}

int main(){
    point a(0,4);
    point b(5,0);
    point c(7,0);
    a.show();
    b.show();
    c.show();
    line l1(a,b), l2(a,c);
    cout << "m1= " << l1.slope() << endl;
    cout << "m2= " << l2.slope() << endl;
    cout << "parallel l1 || l2? = " << (areParallel(l1, l2)?"true":
        "false") << endl;
    cout << "dist from point to line= " << distToLine(c, l1) << endl;
    ;
    cout << "dist from point to segment= " << distToSegment(c, l1)
        << endl;
    return 0;
}

```

4 graph

4.1 Dijkstra

```

#include <bits/stdc++.h>
#define V 9
int minDis(int dist[], bool is_set[]){
    int min = INT_MAX, min_index;
    for (int v = 0; v < V; v++){
        if (is_set[v] == false && dist[v] <= min){
            min = dist[v], min_index = v;
        }
    }
    return min_index;
}

inline void dijkstra(int graph[V][V], int src){
    int dist[V];
    bool is_set[V];
    for (int i = 0; i < V; i++){
        dist[i] = INT_MAX, is_set[i] = false;
    }
    dist[src] = 0;
    for (int count = 0; count < V-1; count++){
        int u = minDis(dist, is_set);
        is_set[u] = true;
        for (int v = 0; v < V; v++){
            if (!is_set[v] && graph[u][v]
                && dist[u] != INT_MAX
                && dist[u]+graph[u][v] < dist[v])
                dist[v] = dist[u] + graph[u][v];
        }
    }
    for( int i= 0; i < V; i++)
        cout << i << " " << dist[i] <<endl;
}

int main(){
    int graph[V][V] =
        {{0, 4, 0, 0, 0, 0, 0, 0, 8, 0},

```

```

{4, 0, 8, 0, 0, 0, 0, 11, 0},
{0, 8, 0, 7, 0, 4, 0, 0, 2},
{0, 0, 7, 0, 9, 14, 0, 0, 0},
{0, 0, 0, 9, 0, 10, 0, 0, 0},
{0, 0, 4, 14, 10, 0, 2, 0, 0},
{0, 0, 0, 0, 0, 2, 0, 1, 6},
{8, 11, 0, 0, 0, 0, 1, 0, 7},
{0, 0, 2, 0, 0, 0, 6, 7, 0}
};
//distances from all points to 1
dijkstra(graph, 1);
return 0;
}

```

4.2 DijkstraHeap

```

#include <bits/stdc++.h>
#define pb push_back
using namespace std;
#define forn(i,a) for (int i=0; i<a ; i++)
#define INF 2e7
struct edge{
    int to, weight;
    edge(){}
    edge(int _to, int _weight){
        to = _to;
        weight = _weight;
    }
    bool operator < (edge e) const {
        return weight > e.weight;
    }
};
typedef vector < edge > ve;
typedef vector < ve > vve;
typedef vector < int > vi;
typedef priority_queue< edge> pq;
inline void dijkstra(vve &adj, int src, int num_nodes){
    vi dist = vi(num_nodes+1, INF);
    pq q;
    //by default
    q.push(edge(src,0));
    dist[src] = 0;
    //apply bfs
    while(!q.empty()){
        edge top = q.top();
        q.pop();
        int u = top.to;
        for(int i=0; i<adj[u].size(); i++){
            int v = adj[u][i].to;
            if(dist[u] + adj[u][i].weight < dist[v]){
                dist[v] = dist[u] + adj[u][i].weight;
                q.push(edge(v, dist[v]));
            }
        }
    }
    //Show results of distances
    cout << "Distancias desde el origen ";
    cout << src << endl;
    forn(i, num_nodes){
        cout << "Costo al nodo: " << i;
        cout << " = " << dist[i] << endl;
    }
}

int main(){
    int nodes =5;

```

```

vve adj(nodes);
//from to - weight
adj[0].pb(edge(1, 6));
adj[0].pb(edge(2, 2));
adj[1].pb(edge(3, 5));
adj[1].pb(edge(4, 7));
int src = 1;
dijkstra(adj, src, nodes);
return 0;
}

```

4.3 EdmonKarp

```

#include<bits/stdc++.h>
#define F first
#define PB push_back
#define S second
#define debug( x ) cout <<#x << " = " << x <<endl;
using namespace std;

typedef pair< int, int > ii;
const int INF = 1e9;
int n;
map< ii, int > w;
unordered_map<int, vector<int>> adj;

int bfs(int s, int t, vector<int>& pt) {
    fill(pt.begin(), pt.end(), -1);
    pt[s] = -2;
    queue<ii> q;
    q.push({s, INF});
    while (!q.empty()) {
        int cur = q.front().F;
        int flow = q.front().S; q.pop();
        for (int next : adj[cur]) {
            if (pt[next] == -1 && w[{cur,next}]) {
                pt[next] = cur;
                int new_flow = min(flow, w[{cur,next}]);
                if (next == t) return new_flow;
                q.push({next, new_flow});
            }
        }
    }
    return 0;
}

int maxflow(int s, int t) {
    int flow = 0;
    vector<int> pt(n);
    int new_flow;
    while (new_flow = bfs(s, t, pt)) {
        flow += new_flow;
        int cur = t;
        while (cur != s) {
            int prev = pt[cur];
            w[{prev,cur}] -= new_flow;
            w[{cur,prev}] += new_flow;
            cur = prev;
        }
    }
    return flow;
}

int main(){
#ifdef LOCAL

```



```

    freopen("in","r",stdin);
#endif
    int from, to, cap, m;
    while( cin >> n >> m ){
        for( int i= 0; i<m ; i++){
            cin >> from >> to >> cap;
            adj[from].PB( to );
            w[{from, to}] = cap;
        }

        int mf = maxflow( 0, 3); // from 1 to 5 maxFlow
        debug( mf );
    }
    return 0;
}

```

4.4 FloydWarshal

```

#include<iostream>
#include<stdio.h>
using namespace std;
/*
 * Floyd-Warshall gives us the shortest paths
 * from all sources to all target nodes.
 */
#define V 4 //number of vertex
#define INF 9999999

void floyd (int graph[][V]){
    int dist[V][V], i, j, k;
    for (i = 0; i < V; i++)
        for (j = 0; j < V; j++)
            dist[i][j] = graph[i][j];
    for (k = 0; k < V; k++){
        for (i = 0; i < V; i++){
            for (j = 0; j < V; j++){
                if (dist[i][k] + dist[k][j] < dist[i][j])
                    dist[i][j] = dist[i][k] + dist[k][j];
            }
        }
    }
    show(dist);
}

int main(){
    int graph[V][V] =
    { {0, 5, INF, 10},
      {INF, 0, 3, INF},
      {INF, INF, 0, 1},
      {INF, INF, INF, 0}
    };
    floyd(graph);
    return 0;
}

```

4.5 RecoveryTree

```

#include <iostream>
using namespace std;
/**Build a binary tree form a inorder and preorder string */
int preIndex = 0;
struct node {
    char key;

```

```

    node *left, *right;
    node(int k) {
        key = k;
        left = NULL;
        right = NULL;
    }
};

int search(string word, int b, int e, char c) {
    for(int i=b; i<=e; i++) {
        if(word[i] == c) return i;
    }
    return -1;
}

//Set preIndex to 0 to build another tree
node* build(string in, string pre, int b, int e) {
    if(b > e) return NULL;
    node *root = new node(pre[preIndex++]);
    if(b == e) return root;
    int inIndex = search(in, b, e, root->key);
    root->left = build(in, pre, b, inIndex - 1);
    root->right = build(in, pre, inIndex + 1, e);
    return root;
}

int main() {
    string pre, in;
    node *tree;
    while(cin >> pre >> in) {
        tree = build(in, pre, 0, pre.size() - 1);
        preIndex = 0;
    }
    return 0;
}

```

4.6 Tsort

```

#include<bits/stdc++.h>
#define debug(x) cout << #x << " = " << x <<endl;
#define PB push_back
using namespace std;

typedef vector < bool > vb;
typedef vector < int > vi;

enum { NV, SV, V};
vb vis;
int N;
vector < vi > G;

void dfs( int src, stack < int > &S ){
    for( int son: G[src]){
        if( vis[ son ] == NV)
            dfs( son, S );
    }
    vis[src] = V;
    S.push( src );
}

void tsort(){
    stack< int > S;
    vis.resize( N );
    vis.assign( N, NV);
    for( int i = 0; i < N; i++){
        if( vis[i] == NV)    dfs( i, S);
    }
    while(!S.empty()){
        cout << S.top() <<endl;

```

```

    S.pop();
}
}

int main(){
    N = 6;
    G.resize(N);
    G[0].PB( 1 );
    G[0].PB( 2 );
    G[0].PB( 3 );
    G[1].PB( 4 );
    G[4].PB( 3 );
    G[5].PB( 2 );
    G[3].PB( 2 );

    tsort( );

    return 0;
}

```

5 mathematics

5.1 Binomial

```

#include <iostream>
using namespace std;
const int MAXN = 66;
unsigned long long ch[MAXN+5][MAXN+5];

int Cnk( ll n, ll k){
    ll res =1;
    // since C(n,k) == C(n, n-k)
    if( k > n-k) k = n-k;
    for( ll i = 0; i < k; i++){
        res = res*1LL*(n-i);
        res /= (i+1);
    }
    return res;
}

void binomial(int N){
    for (int n = 0; n <= N; ++n)
        ch[n][0] = ch[n][n] = 1;
    for (int n = 1; n <= N; ++n){
        for (int k = 1; k < n; ++k){
            ch[n][k] = ch[n-1][k-1] + ch[n-1][k];
        }
    }
}

int main(){
    binomial(10);
    cout << ch[10][2] << endl;
}

```

5.2 Binomial

```

import math, sys
MAXN = 431
choose = []
for i in range (0, MAXN+5):
    choose.append([0]*(MAXN+5))
def binomial(N):

```

```

    for n in range (0, N+1):
        choose[n][0] = choose[n][n] = 1
    for n in range(1, N+1):
        for k in range(1, n):
            choose[n][k] = choose[n-1][k-1] + choose[n-1][k]
if __name__ == "__main__":
    N = 431
    binomial(N)
    n, k = 10, 4
    print(choose[n][k])

```

5.3 ChangeBases

```

#include <bits/stdc++.h>
#define endl '\n'
#define show(x) cout <<#x << " = " <<x <<endl;
using namespace std;
typedef long long ll;
string chars = "0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZ";

ll to10(ll n , ll b, ll mul){
    if (n ==0 ) return 0;
    return (n % 10)*mul + to10(n / 10, b, mul*1LL*b);
}

string tob(ll n, ll b){
    if (n == 0) return "";
    return tob(n / b, b) + chars[n % b];
}

/*
 * ob -> origin base
 * db -> destiny base
 */
string changeBase(ll num, ll ob, ll db){
    if (ob == 10) return tob(num, db);
    return tob(to10(num, ob, 1LL), db);
}

int main(){
    cout << changeBase(1000,2,10) <<endl;
}

```

5.4 CoinChange

```

#include <bits/stdc++.h>
#define MAXCOINS (10005)
#define MAXVALUE (105)
using namespace std;
typedef vector < int > vi;
int dp[MAXVALUE][MAXCOINS];
vi coins;
//recursive
int ways(int tg, int n){
    if ( 0 == tg) return 1;
    if ( 0 > tg) return 0;
    if ( n <= 0 && tg >0) return 0;
    return ways(tg, n-1) +
        ways(tg - coins[n -1], n);
}

//by dp
int waysdp(int tg, int n){
    for( int i=0; i< coins.size(); i++) dp[0][i] = 1;
    for(int i = 1 ; i<= tg; i++){
        for (int c = 0; c < n; c++){
            int x =0 , y = 0;

```

```

        if(i-coins[c] >= 0) x = dp[i - coins[c]][c];
        if( c >=1) y = dp[i][c-1];
        dp[i][c] = x + y;
    }
}
return dp[tg][n-1];
}

int main(){
    coins.insert(coins.end(), {1,3,9,27});
    cout << ways(47, coins.size()) <<endl;
    cout << waysdp(47, coins.size()) <<endl;
    return 0;
}

```

5.5 Combination

```

#include<bits/stdc++.h>
using namespace std;

vector< int > com;
int k, n ;

void comb( int off, int ki){
    if( ki == 0 ){
        for( int &c: com) cout << c << " ";
        cout <<endl;
        return;
    }
    for( int i = off; i <= n - ki ; i++){
        com.push_back( i );
        comb( i+1, ki-1);
        com.pop_back();
    }
}

int main(){
    n = 5; k = 3;
    comb( 0, k );

    return 0;
}

```

5.6 CompareDoubles

```

#include <stdio.h>
using namespace std;
const double EPS = 1e-15;
/*
 * Return
 * -1 if x < y
 * 0 if x == y
 * 1 if x > y
 */
int cmp (double x, double y){
    return (x <= y + EPS) ? (x + EPS < y) ? -1 : 0 : 1;
}

int main(){
    double d1 = 0.000000000000212;
    double d2 = 0.000000000000213;
    int res = cmp(d1,d2);
    if (res == 0){
        printf("Equal \n");
    }else if(res == 1){
        printf("Greater\n");
    }
}

```

```

    }else {
        printf("Less \n");
    }
}

```

5.7 Exponentiation

```

#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
// (a^b)%c
ll expo(ll a, ll b, ll c){
    if (b == 0) return 1;
    if (b % 2 == 0) {
        ll temp = expo(a, b/2, c);
        return (temp * temp) % c;
    } else {
        ll temp = expo(a, b-1, c);
        return (temp * a) % c;
    }
}

int main(){
    cout << expo(2, 100, 1025);
    return 0;
}

```

5.8 ExtendedEuclides

```

#include <bits/stdc++.h>

using namespace std;
typedef long long ll;
typedef vector < ll > vl;

vl arr(3);
/*
 * returns gcd(a,b) and find the coeficcients of bezout
 * such that d = ax + by
 * arr[0] gcd
 * arr[1] x
 * arr[2] y
 */
void extended(ll a, ll b){
    ll y =0;
    ll x =1;
    ll xx =0;
    ll yy =1;
    while(b){
        ll q = a / b;
        ll t = b;
        b = a%b;
        a = t;

        t = xx;
        xx = x-q*xx;
        x = t;

        t = yy;
        yy = y-q*yy;
        y = t;
    }
    arr[0] = a;
    arr[1] = x;
    arr[2] = y;
}
/*

```

```

ax + by = c
mcd(a,b) = d
ax0 + by0 = d
c = d * c'

Bezouts identity
X = x0 * c' - (b/d) * k
Y = y0 * c' + (a/d) * k
*/
int main(){
    ll a = 20, b = 50;
    extended(a,b);
    printf("gcd(%lld, %lld) = %lld = %lld * %lld + %lld * %lld\n",
        a, b, arr[0], a,arr[1], b, arr[2]);
    return 0;
}

```

5.9 ExtendEuclidesSample

```

#include <bits/stdc++.h>
#define F first
#define S second
using namespace std;
typedef long long ll;
typedef pair<ll, ll> ii;

ll gcd;

ii extended(ll a, ll b) {
    ll y = 0, x = 1, xx = 0, yy = 1;
    while (b){
        ll q = a / b;
        ll t = b;

        b = a%b;
        a = t;
        t = xx;
        xx = x-q*xx;

        x = t;
        t = yy;
        yy = y-q*yy;

        y = t;
    }
    gcd = a;
    // a becomes gcd(a,b);
    return {x,y};
}

int main(){
#ifdef LOCAL
    freopen("in","r", stdin);
#endif
    int a, b, c;

    // ax + by = c
    while( cin >> a >> b >> c ){
        ii res = extended( a, b );
        if( c % gcd == 0 ){
            ll x = (c/gcd)*res.F, y = (c/gcd)*res.S;
            cout << x << " " << y << endl;
        } else {
            // no solution
        }
    }
    return 0;
}

```

5.10 Factorize

```

#include <bits/stdc++.h>
#define pb push_back
#define show(x) cout << #x << " = " << x << endl;
using namespace std;
const int MAXN = 1000000;
bool sieve[MAXN + 5];
typedef long long ll;
vector <ll> pri; //primes

void build_sieve(){
    memset(sieve, false, sizeof(sieve));
    sieve[0] = sieve[1] = true;
    for (ll i = 2LL; i * i <= MAXN; i++){
        if (!sieve[i]){
            for (ll j = i * i; j <= MAXN; j += i){
                sieve[j] = true;
            }
        }
    }
    for (ll i = 2; i <= MAXN; ++i){
        if (!sieve[i]) pri.pb(i);
    }
}

//before call this call build_sieve
vector <ll> fact(long long a){
    vector <ll> ans;
    ll b = a;
    for (int i = 0; 1LL * pri[i] * pri[i] <= a; ++i){
        int p = pri[i];
        while (b % p == 0){
            ans.push_back(p);
            b /= p;
        }
    }
    if (b != 1) ans.push_back(b);
    return ans;
}

int main(){
    build_sieve();
    ll num_to_fact = 128234234LL;
    vector < ll > vll = fact(num_to_fact);
    for (int x=0; x< vll.size(); x++){
        cout << vll[x] << " ";
    }
    cout << endl;
}

```

5.11 FastPow

```

#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
inline ll add( ll x, ll y){
    return (x%MOD + y%MOD)%MOD;
}
inline ll mul( ll x, ll y){
    return (x%MOD * y%MOD)%MOD;
}

inline ll fpow( ll x, ll p){ // (x^p)%MOD
    ll res = 1LL;
    while( p ){

```

```

    if( p & 1){
        res = mul(res,x);
    }
    p >>= 1LL;
    x = mul(x,x);
}
return res;
}

```

5.12 GcdLcm

```

#include<cstdio>
using namespace std;
typedef long long ll;
ll mod( ll a, ll b){
    return (b + (a %b )) %b;
}
ll gcd ( ll a, ll b){
    if (b == 0 ) return a;
    return gcd( b, mod( a , b) );
}
ll lcm(ll n1, ll n2){
    return (n1 *1LL* n2) / gcd(n1,n2);
}
int main(){
    ll n1=2366, n2=273;
    printf("gcd(%ld, %ld) = %ld\n",
        n1, n2, gcd(n1,n2));
    return 0;
}

```

5.13 IsFibo

```

#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
bool isPerfectSquare(long long x){
    ll s = sqrt(x);
    return (s*1LL*s == x);
}
bool isFibonacci(int n){
    // n is Fibonacci if one of 5*n*n + 4 or 5*n*n - 4 or both
    // is a perfect square, this is deduced of the discriminant
    // of binet's formule
    return isPerfectSquare(5*n*1LL*n + 4) || isPerfectSquare(5*1LL*n
        *n - 4);
}
// A utility function to test above functions
int main() {
    for (int i = 1; i <= 10; i++)
        isFibonacci(i)? cout << i << " is a Fibonacci Number \n":
            cout << i << " is a not Fibonacci Number \n"
                ;
    return 0;
}

```

5.14 IsPrime

```

import java.math.BigInteger;
import java.util.Scanner;
public class prime {

```

```

    public static void main(String[] args) {
        BigInteger a = new BigInteger("1299827");
        //User miller rabin & Lucas Lehmer
        boolean res = a.isProbablePrime(10);
        System.out.println(res? "It's prime":"It's not prime");
    }
}

```

5.15 knapsack

```

#include<bits/stdc++.h>
#define MAX (int) 1e3
using namespace std;
int v[5] = {60, 100, 120, 30, 5};
int w[5] = {10, 20, 30, 30, 5};

int memo[MAX][MAX];

int knapsack( int n , int W){
    if( n == 0 || W == 0 ) return 0;
    int &ans = memo[n][W];
    if( ans != -1) return ans;
    if( w[n] > W ) { //not include too heavy
        ans = knapsack(n-1, W);
    }else{
        //Include
        int a1 = v[n]+ knapsack( n-1, W-w[n] );
        //Not include
        int a2 = knapsack( n -1, W);
        ans = max(a1, a2);
    }
    return ans;
}

int main() {
    for( int i = 0; i < MAX; i++)
        for( int j = 0; j < MAX; j++)
            memo[i][j] = -1;

    cout << knapsack ( 5, 50) << endl;
    return 0;
}

```

5.16 MatrixFibo

```

#include <bits/stdc++.h>
using namespace std;

const int MAX = 1000;
int f[MAX] = {0};
// Returns n'th fibonacci number using table f[]
int fib(int n){
    // Base cases
    if (n == 0) return 0;
    if (n == 1 || n == 2) return (f[n] = 1);
    // If fib(n) is already computed
    if (f[n]) return f[n];
    int k = (n & 1)? (n+1)/2 : n/2;
    // Applying above formula [Note value n&1 is 1
    // if n is odd, else 0.
    f[n] = (n & 1)? (fib(k)*fib(k) + fib(k-1)*fib(k-1))
        : (2*fib(k-1) + fib(k))*fib(k);

    return f[n];
}

```

```

}

/* Driver program to test above function */
int main(){
    int n = 9;
    printf("%d ", fib(n));
    return 0;
}

```

5.17 MillerTest

```

#include <bits/stdc++.h>
using namespace std;
typedef unsigned long long ll;
ll power(ll x, ll y, ll p){
    ll res = 1;
    x = x % p;
    while (y > 0){
        if (y & 1) res = (res*1LL*x) % p;
        y = y >> 1;
        x = (x * x) % p;
    }
    return res;
}
bool miillerTest(ll d, ll n){
    ll a = 2 + rand() % (n - 4);
    ll x = (1LL)power(a, d, n);
    if (x == 1 || x == n-1)
        return true;
    while (d != n-1){
        x = (x *1LL* x) % n;
        d *= 2;
        if (x == 1) return false;
        if (x == n-1) return true;
    }
    return false;
}
bool isPrime(ll n, ll k){
    if (n <= 1 || n == 4) return false;
    if (n <= 3) return true;
    ll d = n - 1;
    while (d % 2 == 0) d /= 2;
    // Iterate given nber of 'k' times
    for (ll i = 0; i < k; i++)
        if (miillerTest(d, n) == false)
            return false;
    return true;
}
int main(){
    ll k = 4; // Number of iterations
    ll n = 982451653;
    cout << (isPrime(n, k)?"True":"False") << endl;
    return 0;
}

```

5.18 NaiveFind

```

#include <bits/stdc++.h>
using namespace std;
int main(){
    string needle = "CD", haystack = "MANICD";
    if(haystack.find(needle) != string::npos) cout << "Gotcha!!!";
    else cout << "Not Gotcha";
    cout << endl;
}

```

```

    return 0;
}

```

5.19 PollarRho

```

#include<bits/stdc++.h>
using namespace std;

typedef long long ll;
ll num;

int modular_pow(ll base, int exponent, ll modulus){
    ll result = 1;
    while (exponent > 0){
        if (exponent & 1)
            result = (result * base) % modulus;
        exponent = exponent >> 1;
        base = (base * base) % modulus;
    }
    return result;
}

//take care if its' prime infinite loop
ll PollardRho(ll n){
    srand (time(NULL));
    if (n==1) return n;
    if (n % 2 == 0) return 2;
    ll x = (rand()%(n-2))+2;
    ll y = x;
    ll c = (rand()%(n-1))+1;
    ll d = 1;
    cout << n << endl;
    while (d==1){
        cout << d<<endl;
        x = (modular_pow(x, 2, n) + c + n)%n;
        y = (modular_pow(y, 2, n) + c + n)%n;
        y = (modular_pow(y, 2, n) + c + n)%n;
        d = __gcd(abs(x-y), n);
        if (d==n) return PollardRho(n);
    }
    return d;
}

int main(){
    num = 982451653;
    printf("One of the divisors for %lld is %lld.", num,
        PollardRho(num));
    return 0;
}

```

5.20 PollarRho

```

import random as r
def gcd( a, b):
    if(b == 0): return a;
    return gcd(b, a % b);
def pollardRho(N):
    if N%2==0: return 2
    x = r.randint(1, N-1)
    y = x
    c = r.randint(1, N-1)
    g = 1
    while g==1:
        x = ((x*x)%N+c)%N
        y = ((y*y)%N+c)%N
        y = ((y*y)%N+c)%N

```

```

        g = gcd(abs(x-y),N)
    return g
if(__name__=="__main__"):
    print(pollardRho(10967535067))
    print(pollardRho(113))

```

5.21 PrimalityTest

```

#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
bool isPrime(ll n){
    if (n < 2) return false;
    if (n < 4) return true;
    if (n % 2 == 0 || n % 3 == 0) return false;
    if (n < 25) return true;
    for(int i = 5; i*i <= n; i += 6){
        if(n % i == 0 || n % (i + 2) == 0)
            return false;
    }
    return true;
}
int main(){
    cout << isPrime(23234) << endl;
    cout << isPrime(2) << endl;
    cout << isPrime(7454) << endl;
    cout << isPrime(976) << endl;
    cout << isPrime(1973) << endl;
    return 0;
}

```

5.22 RotateMatrix

```

#include<bits/stdc++.h>
using namespace std;
#define R 4
#define C 4
int arr[R][C];

void reverseColumns(){
    for (int i=0; i<C; i++)
        for (int j=0, k=C-1; j<k; j++,k--)
            swap(arr[j][i], arr[k][i]);
}

void transpose() {
    for (int i=0; i<R; i++)
        for (int j=i; j<C; j++)
            swap(arr[i][j], arr[j][i]);
}

/* anticlockwise rotate matrix by 90 degree*/
void rotate90(){
    transpose();
    reverseColumns();
}

int main() {
    int aux [R][C]=
    { {1, 2, 3, 4},
      {5, 6, 7, 8},
      {9, 10, 11, 12},
      {13, 14, 15, 16}
    };
    rotate90();
}

```

```

    return 0;
}

```

5.23 Sieve

```

#include <bits/stdc++.h>
#define tam 1000
using namespace std;
typedef long long ll;
typedef vector< bool > vbool;
void show (vbool primes){
    ll cap = primes.size();
    for(ll i = 0; i< cap; i++){
        cout << i << " : " << primes[i] << endl;
    }
}
vbool sieve(ll n){
    vbool sieve (tam);
    for (ll i = 0; i < tam; i++)
        sieve[i] = true;
    sieve [0] = sieve[1] = false;
    ll root = sqrt(n);
    for (ll i = 2; i < root; i++){ //find primes
        if(sieve[i]){
            //removes all the multiples
            //of the current prime
            for (ll k = i*1LL*i; k<= n; k+=i){
                sieve[k] = false;
            }
        }
    }
    return sieve;
}
int main(){
    vbool primes = sieve(1000);
    show(primes);;
    primes.clear();
    return 0;
}

```

5.24 Sum

```

/*
Summatories
*/
int main(){
    sum(i) from 1 to n = n(n+1)/2
    sum(i^2) from 1 to n = n(n+1)(2n+1)/6
    sum(i^3) from 1 to n = (n^2(n+1)^2)/4

    //Geometric serie
    a * sum(r^k) from 0 to n = a * (1-r^(n+1)) / (1 -r)
    // ar + ar^2 + ar^3 ...
}

```

5.25 toBin

```

#include <bits/stdc++.h>
using namespace std;
void toBin(int x){
    for (int i =31; i>=0; --i)

```

```

    cout << ((x&(1LL<<i))!=0);
}
int main(){
    toBin(10);
    return 0;
}

```

6 other

6.1 MergeSortPY

```

def merge_sort(arr):
    if (len(arr)>1):
        mid = len(arr) // 2
        lefthalf, righthalf = arr[:mid] , arr[mid:]
        merge_sort(lefthalf)
        merge_sort(righthalf)

        merge(lefthalf, righthalf, arr)

def merge(lh, rh, arr):
    il = 0
    ir = 0
    k = 0
    while il < len(lh) and ir < len(rh):
        if (lh[il] < rh[ir]):
            arr[k] = lh[il]
            il = il+1
        else:
            arr[k] = rh[ir]
            ir = ir+1
        k = k+1

    while il < len (lh):
        arr[k]= lh[il]
        il = il +1
        k = k+1

    while ir < len(rh):
        arr[k] = rh[ir]
        ir = ir +1
        k = k+1

def main():
    array = [-10, 37, 98 , 0 ,12, 192, 5]
    print("Original Array")
    print(array)
    merge_sort(array)

    print("Sorted Array")
    print(array)
main()

```

6.2 Partitions

```

#include<iostream>
using namespace std;
/*
    Generate all unique
    partitions of a given integer
*/
void partitions(int n){

```

```

int p[n];
int k = 0;
p[k] = n;

while (true){
    for( int i =0; i <=k ; i++) cout <<p[i] << " ";
    cout <<endl;
    int rem_val = 0;
    while (k >= 0 && p[k] == 1){
        rem_val += p[k];
        k--;
    }
    if (k < 0) return;
    p[k]--;
    rem_val++;
    // If rem_val is more, then the sorted order is violated.
    // Divide
    // rem_val in different values of size p[k] and copy these
    // values at
    // different positions after p[k]
    while (rem_val > p[k]){
        p[k+1] = p[k];
        rem_val = rem_val - p[k];
        k++;
    }
    // Copy rem_val to next position and increment position
    p[k+1] = rem_val;
    k++;
}

int main(){
    cout << "All Unique Partitions of 7 \n";
    partitions(7);
    return 0;
}

```

6.3 TemplateC

```

#include <bits/stdc++.h>
using namespace std;

// INT_MAX -> limits.h
typedef long long ll;
typedef long double ld;
typedef vector < int > vi;
typedef vector < vi > vii;
struct point {int x, y;};

#define show(x) cout << #x << " = " << x << endl;
#define isOdd(x) (x & 0x01)
#define mod(a,b) (b + (a % b)) % b

const double PI = acos(-1);
const ld INF = 1e18;
const double EPS = 1e-15;

void input(){
    /*
    scanf("%ld",&value); //long y long int
    scanf("%c",&value); //char
    scanf("%f",&value); //float
    scanf("%lf",&value); //double
    scanf("%s",&value); //char*
    scanf("%lld",&value); //long long int
    scanf("%x",&value); //int hexadecimal
    scanf("%o",&value); //int octal
    */

```



```

}

void tricks(){
    int a=21,b=16,c=8;
    //if the numbers are long and long long end with and l or two l
    /*ie
        int
        __builtin_popcount
        long
        __builtin_popcountl
        long long
        __builtin_popcountll
    */
    //log2 floor
    show(__lg(21));
    show(__lg(16));
    show(__lg(8));
    cout << endl;
    //count the number of ones
    show(__builtin_popcount(16));
    show(__builtin_popcount(15));
    show(__builtin_popcount(0));
    cout << endl;

    //count the trailing zeros zer
    show(__builtin_ctz(16));
    show(__builtin_ctz(5));
    cout << endl;

    //count the leading zeros
    show(__builtin_clz(32));
    show(__builtin_clz(1024));
    cout << endl;
    //Returns one plus the index of the least significant
    //1-bit of x, or if x is zero, returns zero.
    show(__builtin_ffs(5));
    cout << endl;
    //Is a number x power of 2?
    show(((a & (a-1))==0));
    show(((b & (b-1))==0));
    cout << endl;

    //turn on the first n bits of a mask
    show(((1LL<<10)-1));
}

//Main
int main(){
    ios::sync_with_stdio(false);
    cin.tie(0);

    tricks();
    #ifdef LOCAL
        freopen("in.txt", "r", stdin);
        freopen("out.txt", "w", stdout);
    #endif
}

```

6.4 TemplateP

```

from sys import stdin
lines = stdin.read().splitlines()
for line in lines:
    a, b = [int(y) for y in line.split()]

```

6.5 UpperLowerBound

```

#include <bits/stdc++.h>
using namespace std;
int main () {
    int myints[] = {10,20,30,30,20,10,10,20};
    vector<int> v(myints,myints+8);           // 10 20 30 30 20 10
                                              10 20
    sort (v.begin(), v.end());                // 10 10 10 20 20 20
                                              30 30
    vector<int>::iterator low,up;
    low=lower_bound (v.begin(), v.end(), 20); //
    up= upper_bound (v.begin(), v.end(), 20); //
    cout << "lower_bound at position " << (low- v.begin()) << '\n';
    cout << "upper_bound at position " << (up - v.begin()) << '\n';
    return 0;
}

```

6.6 XIncludes

```

#include <vector>           vector<
#include <queue>            queue< priority_queue<
#include <set>              set< multiset<
#include <map>              map< multimap<
#include <bitset>          bitset<
#include <list>            list<
#include <deque>           deque<
#include <stack>           stack<
#include <complex>         complex<
#include <hash_map.h>      hash_map<
#include <hash_set.h>      hash_set<
#include <string>          string
#include <algorithm>       sort( stable_sort( make_heap( push_heap(
                                pop_heap(
                                lower_bound( upper_bound( equal_range(
                                binary_search(
                                find( find_first_of( count( min( max( swap(
                                fill( copy(
                                next_permutation( prev_permutation(
                                remove( replace( reverse( rotate(
                                random_shuffle(
                                min_element( max_element( nth_element(
                                mismatch(
                                set_difference( set_intersection( set_union(
                                set_symmetric_difference( merge( unique(
                                adjacent_find(
                                lexicographical_compare(
                                lexicographical_compare_3way(
                                equal( includes(
                                accumulate( partial_sum( adjacent_difference(
                                #include <numeric>
                                (
                                inner_product(
                                #include <iostream>      cin cout cerr istream ostream
                                #include <fstream>      ifstream ofstream ifstream( ofstream(
                                #include <sstream>        istringstream ostringstream
                                #include <cassert>        assert(
                                #include <cmath>          sin( cos( tan( asin( acos( atan( atan2( sinh
                                ( cosh( tanh(
                                sqrt( hypot( abs( exp( pow( ceil( floor(
                                fmod( log( log10(
                                fabs( M_PI
                                #include <cstdio>         printf( scanf( fprintf( fscanf( sprintf(
                                sscanf(

```

```

        getc( fgetc( putc( fputc( getchar( putchar(
            ungetc(
FILE stdin stdout stderr feof( fclose(
        fflush(
#include <cstdlib>    rand( srand(
#include <cstring>    memcpy( memmove( memchr( memset(
                    strcpy( strncpy( strcat( strncat( strcmp(
                    strncmp(
#include <ctime>    time( clock( CLOCKS_PER_SEC

```

6.7 YGenerator

```

#include <bits/stdc++.h>
using namespace std;
int main(){
    #ifdef LOCAL
        freopen("new.c", "w", stdout);
    #endif
    srand (time(NULL));

    int numRandom = 1000;
    cout << numRandom << endl;
    for( int i=1 ; i<=numRandom ; i++)
        int cant = rand() % 100 +2;
    return 0;
}

```

7 strings

7.1 Kmp

```

#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x << endl
#define rep(i, a, b) for( __typeof(a) i = a; i < b ; i++)
using namespace std;

int* compute(const string &t) {
    int m = t.size();
    int *p = new int[m];
    p[0]= 0;
    rep( i , 1 , m){
        p[i] = p[ i - 1 ];
        while( p[i] > 0 && t[i] != t[ p[i] ] ){
            p[i] = p[ p[i] -1 ];
        }
        if( t[i] == t[ p[i] ] ) p[i]++;
    }
    return p;
}

int match( const string &ne, const string &ha ){
    debug( ne ); debug( ha);
    int m = ne.size(), n = ha.size();
    int *p = compute( ne );

    int s = 0;
    rep( i, 0, n){
        while( s > 0 && ha[ i ] != ne[ s ] )
            s = p[ s - 1];

```

```

        if( ha[i] == ne[s] ) s++;
        if( s == m) return i - m + 1;
    }
    delete[] p;
    return -1;
}

int main(){
#ifdef LOCAL
    freopen("in", "r" , stdin);
#endif

    string needle = "abcaby";
    string haystack = "abcabcabyid";

    cout << match ( needle , haystack ) <<endl;

    return 0;
}

```

7.2 LIS

```

#include<bits/stdc++.h>
using namespace std;
/*
 * Complexity Nlog(N)
 */
vector< int > getLis( const vector < int > A){
    int n = A.size();
    if( n == 0) return {};
    vector < int > tail ( n, 0);
    vector < int > lis ( n, 1);
    int ans = 1;
    tail[0] = A[0];
    for( int i = 1; i < n ; i++){
        if( A[i] < tail[0] ) {
            tail[0] = A[i];
            lis[i] = 1;
        }else if( A[i] > tail[ ans - 1] ) {
            tail[ ans++ ] = A[i];
            lis[ i ] = ans;
        }else{
            int cp = upper_bound( tail.begin(),
                                tail.begin()+ans, A[i]) - tail.begin();

            tail[ cp ] = A[i];
            lis[ i] = cp+1;
        }
    }
    return lis;
}

int main(){
    vector < int > A = { 1, 3, 32 ,2 ,78, 9,2};
    getLis( A );
    // 1 2 3 2 4 3 3
    return 0;
}

```

7.3 LRSubs

```

#include<bits/stdc++.h>
using namespace std;

```

```
// Returns the longest repeating non-overlapping substring
string longestRepeatedSubstring(string str){
    int n = str.length();
    int LCSRe[n+1][n+1];
    // Setting all to 0
    memset(LCSRe, 0, sizeof(LCSRe));
    string res; // To store result
    int res_length = 0; // To store length of result

    // building table in bottom-up manner
    int i, index = 0;
    for (i=1; i<=n; i++){
        for (int j=i+1; j<=n; j++){
            // (j-i) > LCSRe[i-1][j-1] to remove
            if (str[i-1] == str[j-1] &&
                LCSRe[i-1][j-1] < (j - i)){
                LCSRe[i][j] = LCSRe[i-1][j-1] + 1;
                if (LCSRe[i][j] > res_length){
                    res_length = LCSRe[i][j];
                    index = max(i, index);
                }
            }
            else
                LCSRe[i][j] = 0;
        }
    }
    if (res_length > 0){
        cout << (index - res_length + 1) << endl;
        for (i = index - res_length + 1; i <= index; i++)
            res.push_back(str[i-1]);
    }

    return res;
}

// Driver program to test the above function
int main(){
    string str = "hello,p23puoeouhello,oues";
    cout << longestRepeatedSubstring(str); //hello,
    return 0;
}
```

7.4 StringUtil

```
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef vector <string> vs;
int toNum(string a){
    stringstream toNum(a);
    int num;
    toNum >> num;
    return num;
}
string toString(double d){
    stringstream ss;
    ss << fixed << setprecision(10) << d;
    string num = ss.str();
    return num;
}
void tolowers(string &data){
    transform(data.begin(), data.end(), data.begin(), ::tolower);
}
void replace(string &a, string &from, string &to){
    int pos=0;
    while((pos = a.find(from,pos)) != string::npos){
        a.replace(pos, to.size(), to);
    }
}
```

```
pos+=to.size();
}
}
vs split(string line, char d){
    vector < string > elements;
    stringstream ss(line);
    string item;
    while(getline(ss, item, d))    elements.pb(item);
    return elements;
}

int main(){
    vs d1 = split("1990/10/5", '/');
    for (string s: d1){
        cout << toNum(s) << endl;
    }

    char a = 'a';
    cout << (isalnum(a)?"true":"false") << endl;
    cout << (isalpha(a)?"true":"false") << endl;
    cout << (isblank(a)?"true":"false") << endl;
    cout << (isdigit(a)?"true":"false") << endl;
    cout << (islower(a)?"true":"false") << endl;
    cout << (ispunct(a)?"true":"false") << endl;
    cout << (isupper(a)?"true":"false") << endl;
    cout << (isxdigit(a)?"true":"false") << endl;
    cout << (char)tolower(a) << endl;
    cout << (char)toupper(a) << endl;
    string hay ="hellohowareyouhow", ned ="whatare", from= "how";
    replace(hay, from, ned);
    cout << hay << endl;
    return 0;
}
```

7.5 SubstrK

```
#include <bits/stdc++.h>
#define debug(x) cout << #x << " = " << x << endl
#define pb push_back
/*
    Algorithm to find all possible
    substrings of size k given a set of values
*/
using namespace std;
set<string> subs;
//print all possible substrings of size k
void substringSizek(char set[], string prefix, int n, int k){
    //Base case
    if( 0 == k){
        cout << prefix << endl;
        subs.insert(prefix);
        return;
    }
    for( int i=0; i < n ; ++i){
        string newprefix = prefix + set[i];
        //k is decreased because we add a new character
        substringSizek(set, newprefix, n, k-1);
    }
}
void init(char set[], int k){
    int n = strlen(set);
    substringSizek(set, "", n, k);
}

int main(){
    char set[3] ={'a', 'b'};
    int k = 3;
}
```

```
    init(set, k);
}
```

7.6 Zalgorithm

```
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef vector<int> vi;

/*
 * Complexity:  $O(N + M)$ 
 */
vi z_val(string s){
    int n = s.size(), L = 0, R = 0;
    vi z(n);
    for( int i = 1; i < n ; i++){
        if( i > R){ // not prefix-substr
            L = R = i;
            while( R < n && s[R-L] == s[R]) R++;
            z[i] = R - L; R--;
        }else {
```

```
            int k = i - L;
            //there is no longer prefix start at s[i]
            if( z[k] < R-i+1){
                z[i] = z[k];
            }else{
                L = i;
                while( R < n && s[R-L] == s[R]) R++;
                z[i] = R-L; R--;
            }
        }
    }
    return z;
}

int main() {
    string haystack = "abcaabca", needle = "abc";
    int n = haystack.size(), m = needle.size();
    vi z = z_val(needle + "#" + haystack);
    for( int i = 0; i < z.size(); i ++){
        cout << i << " " << z[i] << endl;
    }
    return 0;
}
```