Notebook (2019)

Contents

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1 algorithms

1.1 Catalan

```
#include<bits/stdc++.h>
using namespace std;
/*
```

```
  Catalan
  also 2n!/((n+1)! n!)
  UVA 10223, 10312
*/
ll C( int n){
  if ( n <= 1 ) return 1;
  ll res = 0;
  for( int i= 0; i < n; i++)
    res += C(i) * C( n -i -1);
  return res;
}
/*
  Super Catalan
*/
ll S( int n ){
  if( n <=2 ) return 1;
  ll res =((6*n-9)*S(n-1)-(n-3)*S(n-2))/n;
  return res;
}
```

1.2 HornersRule

```
#include <iostream>
using namespace std;
typedef long long ll;
ll Horner( ll a[], ll n, ll x ){
  ll result = a[n];
  for(ll i=n-1; i >= 0 ; --i)
    result = result * x + a[i];
  return result;
}
int main(){
  int n = 4;
          //-1 -2x -6x^2 +2x^3
  ll a[] = {-1,-2,-6,2};
  ll x = 8;
  cout << Horner (a, n-1, x);
  return 0;
}
```

1.3 Kadane

```
#include <bits/stdc++.h>
#define rep(i,j,k) for(int i=j; i<k; i++)
using namespace std;
typedef long long ll;
/*
 * Largest Sum Contiguous Subarray
 * Kadane Algorithm
 * Complexity: O(n)
 * UVA 108
 */
inline ll kadane(ll data[8]){
  ll m1= data[0];
  ll m2 = data[0];
  rep(i, 1, len(data)){
    m2 = max(data[i], data[i] + m2);
    m1 = max(m1, m2);
  }
  return m1;
}
```

1.4 MinimunWord

```
/* compute the minimun lexicographical word
  in linear time, doing rotations
  UVA 719
*/

int compute( string &s ){
  int n = size( s );
  s = s+s;
  int mn = 0, i =1, step =0;
  while( i < n && mn + step +1 < n){
    if( s[mn+step] == s[i+step]){
      step++;
    }else if( s[mn+step]  < s[i+step]){
      i = i + step +1;
      step = 0;
    }else{
      mn = max(mn+step+1, i);
      i = mn+1;
      step =0;
    }
  }
  return mn;
}
```

1.5 PickTheorem

```
#include <complex>
#define F real()
#define S imag()
typedef complex<int> pt;
// magnitude pt abs(pt)
// square distance norm(pt)
// angle made by the origin arg(pt)
// rotate p 90 degrees anti-clockwise
   // p = p*polar(1.0, PI/2.0);
using namespace std;
/*
 * b boundary point
 * i interior point
 * UVA 10088
 */
double pick(int b, int i){
  return (b/2.0) + i -1;
}
```

1.6 SuffixArray

```
#include <bits/stdc++.h>
#define endl '\n'
#define debug1( x ) cout << #x << " = " <<  x << endl;
#define debug2( x, y) cout <<#x << " = " << x << " , " <<#y << " =
     " << y <<endl;
#define F first
#define S second
#define PB push_back
#define SIZE( x )   int( ( x ).size( ) )
#define endl '\n'
#define rep(i, a, b) for( __typeof(a) i =(a); i<(b);i++)
#define rept(i, a, b) for( __typeof(a) i =(a); i<=(b);i++)
#define all(x) x.begin(),x.end()
```

```cpp
using namespace std;
typedef long long ll;
typedef pair<int, int> ii;
typedef vector<int> vi;
// Taken from notebook unal 2018

/*
 * O( n*log(n) ) where n = |text|
 * sa[i] contains the starting position of the i-th
 * smallest suffix in t, ensuring that for all
 * 1 < i <= n, t[sa[i-1], n] < t[sa[i], n] holds.
 * O( n ) where n = |text|
 * lcp[i] stores the lengths of the longest common
 * prefixes between all pairs of consecutive suffixes
 * in a sorted suffix array (needs sa).
 */
int const MAXN = 1e5;
int n, mx;
string t;
int pos[ MAXN ], cnt[ MAXN ];
int aux_sa[ MAXN ], aux_pos[ MAXN ];
int sa[ MAXN ], lcp[ MAXN ];
bool check( int i, int gap ) {
  if( pos[ sa[i-1] ] != pos[ sa[i] ] ) return true;
  if( sa[ i-1 ]+gap < n && sa[ i ]+gap < n )
    return ( pos[ sa[i-1]+gap ] != pos[ sa[i]+gap ] );
  return true;
}
void radix_sort( int k ) {
  for( int i = 0; i < mx; ++i ) cnt[ i ] = 0;
  for( int i = 0; i < n; i++ )
    cnt[ (i+k < n) ? pos[ i+k ]+1 : 1 ]++;
  for( int i = 1; i < mx; i++ )
    cnt[ i ] += cnt[ i-1 ];
  for( int i = 0; i < n; i++ )
    aux_sa[ cnt[ (sa[ i ]+k < n) ? pos[ sa[i]+k ] : 0 ]++ ] = sa[
        i ];
  for( int i = 0; i < n; i++ )
    sa[ i ] = aux_sa[ i ];
}
void build_sa( ) {
  for( int i = 0; i < n; i++ ) {
    sa[ i ] = i;
    pos[ i ] = t[ i ];
  }
  for( int gap = 1; gap < n; gap <<= 1 ) {
    radix_sort( gap );
    radix_sort( 0 );
    aux_pos[ sa[0] ] = 0;
    for( int i = 1; i < n; i++ )
      aux_pos[ sa[i] ] = aux_pos[ sa[i-1] ] + check( i, gap );
    for( int i = 0; i < n; i++ )
      pos[ i ] = aux_pos[ i ];
    if( pos[ sa[n-1] ] == n-1 ) break;
  }
}
void build_lcp( ) {
  int k = 0;
  lcp[ 0 ] = 0;
  for( int i = 0; i < n; i++ ) {
    if( pos[ i ] == 0 ) continue;
    while( t[ i+k ] == t[ sa[ pos[i]-1 ]+k ] ) k++;
    lcp[ pos[ i ] ] = k;
    k = max( 0, k-1 );
  }
}
void build( string s ) {
  n = SIZE( s );
  t = s+"#";
  mx = max( 256, n );
  build_sa( );
  build_lcp( );
}

int main(){
  ios::sync_with_stdio( false );
  cin.tie( nullptr );
#ifdef LOCAL
  freopen("in", "r" , stdin);
#endif

  string word = "mississippi";
  build( word );
  rep(i,0, SIZE(word)){
    cout << ( lcp[i]) << " ";
    rep(j,sa[i], SIZE(word)){
      cout << word[j];
    }
    cout <<endl;
  }
  cout << endl;

  return 0;
}
```

2 data-structures

2.1 Fenwick

```cpp
#include<bits/stdc++.h>
#define endl '\n'
using namespace std;
typedef long long ll;
typedef vector < ll> vll;
/*
 Complexity Query O(log(n))
 UVA 12086
*/
struct fw {
  int n; vll data;
  fw(int _n) : n(_n), data(vll(_n)) { }
  void update(int at, ll by) {
   while(at < n) {
    data[at] += by;
    at |= at + 1;
   }
  }
  void update_range( int l, int r, ll by){
    update(l, by);
    update(r+1, -by);
  }
  ll query(int at) {
   ll res = 0LL;
   while(at >= 0) {
     res += data[at];
     at = (at & (at + 1)) - 1;
   }
   return res;
  }
};
```

```
int main(){
#ifdef LOCAL
  freopen("in","r", stdin);
#endif
  ios::sync_with_stdio(0);cin.tie(0);
  int n, q ,a, b;
  char op;
  cin >> n >> q;
  fw *fen  = new fw(n+1);
  for( int i = 0; i < q ; i++){
    cin >> op;
    if( '+' == op){
      cin >> a >> b;
      fen->update(a,b);
    }else{
      cin >>a; a--;
      cout <<  fen->query(a) << endl;
    }
  }

}
```

2.2 MST

```
#include<bits/stdc++.h>
using namespace std;

/*
 Complexity: nlog(n)
 UVA 11747
*/
  ///          from, to, weight
typedef tuple< int,int,int > edge;
typedef vector < int > vi;
bool customSort(const edge &a,const edge & b){
  return get<2>(a) < get<2>(b);
}
vector< edge > mst( vector< edge > &edges , int n ){
  union_find uf( n );
  vector< edge > res;
  sort( edges.begin(), edges.end(), customSort);
  int f, t , w;
  int tw =0;
  for( const edge &e: edges){
    tie(f, t, w) = e;
    if( uf.unite( f, t ) )res.push_back( e);
  }
  return res;
}
int main(){
#ifdef LOCAL
  freopen("in", "r", stdin);
#endif
  int n, m;
  int f, t , w;
  cin >> n >> m;
  vector< edge > edges( m );
  for( int i = 0 ; i <m ; i++){
    cin >> f >> t >> w;
    edges[i] = make_tuple( f, t, w);
  }
  mst( edges, n );
  return 0;
}
```

2.3 SegmentTree1

```
#include <iostream>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;
const int N = 1e5 + 10;
int n, q;
int t[2 * N]; // limit


//built the tree O(n)
void built(){
  for (int i = n - 1; i > 0; i--) {
    t[i] = t[i << 1]+ t[i << 1 | 1];
  }
}

// set y at position x O(log(n))
void update(int x, int y) {
  for (t[x += n] = y; x > 1; x >>= 1) {
    t[x >> 1] = t[x]+ t[x ^ 1];
  }
}

//operation on interval [l, r) O(log(n))
int query(int l, int r) {
  int res = 0;
  for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
    if (l & 1) res += t[l++];
    if (r & 1) res += t[--r];
  }
  return res;
}
int main() {
#ifdef LOCAL
  freopen("SegmentTree.test","r",stdin);
#endif
  cin >> n >> q;
  for (int i = 0; i < n; i++) {
    cin >> t[i + n];
  }
  built();
  int l, r, ty,pos , val;
  for (int i = 0; i < q; i++) {
    cin >> ty;
    if( ty == 1){ // query
      cin >> l >> r; l--;
      cout << query( l, r ) << endl;
    }else if( ty == 2){ //update single value
      cin >> pos >> val; // pos 1 indexed
      pos--;
      update(pos, val);
    }
  }

  return 0;
}
```

2.4 SegmentTree2

```
#include <iostream>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;
const int N = 1e5 + 10;
int n, q;
```

```
int t[2 * N], lazy[2*N];  // limit
int arr[N];

//built the tree O(n)
void built(int l, int r, int node=1){
  if( l > r) return;
  if( l == r){
    t[node] = arr[l];
    return;
  }
  int mid = (l+r)/2;
  built( l, mid, node<<1);
  built( mid+1, r, node<<1|1);
  t[node] = t[node<<1] + t[node<<1 |1];
}

// query O(lg(n))
int query(int start, int end, int l , int r, int node=1){
  if( r < start || end  < l) return 0;
  if( start >= l && end <= r) return t[ node ];
  int mid = ( start + end) >> 1;
  int lans = query( start, mid, l, r, node<<1);
  int rans = query( mid+1, end, l, r, node<<1|1);
  return lans + rans;
}

// Update a pos O(lg(n))
void update(int start, int end, int idx, int val, int node=1){
  if( start == end){
      arr[ idx ] = val; // change value in the st
      t[ node ] = val;
      return;
  }
  int mid = (start+ end)>>1;
  if( start <= idx and idx <= mid){
    update( start,mid, idx, val, node*2);
  }else{
    update( mid+1, end, idx, val, node*2+1);
  }
  t[ node ] = t[ node << 1 ] + t[node << 1 |1 ];
}

// Update Range Lazy log(n)
void updateRange( int start, int end, int l, int r, int val, int
    node =1){
  if( lazy[node] != 0){ //pending update
    t[ node ] += ( end - start +1) * lazy[ node ];
    if( start != end){
      lazy[ node << 1] += lazy[node];
      lazy[ node <<1 |1] += lazy[node];
    }
    lazy[ node] = 0;
  }
  if( start > end || start >r || end <l ) return;
  if( start >= l && end <= r){// fully in range
    t[ node] += (end - start +1) * val;
    if( start != end){
      lazy[ node<<1] += val;
      lazy[ node<<1|1] += val;
    }
    return;
  }
  int mid = ( start +end ) >> 1;
  updateRange( start, mid, l, r, val, node<<1);
  updateRange( mid+1, end, l, r, val, node<<1|1);
  t[node] = t[ node<<1] + t[node<<1|1];
}

//query lazy
int queryLazy(int start, int end, int l , int r, int node=1){
  if( start > end || start > r || end < l) return 0;
  if( lazy[ node] != 0 ){
    t[node] += (end -start +1) * lazy[ node ];
    if( start != end){
      lazy[node<<1] += lazy[ node];
      lazy[node<<1|1 ] += lazy[node];
    }
    lazy[node] = 0;
  }
  if( start >= l && end <= r) return t[ node ];
  int mid = (start + end) /2;
  int p1 = queryLazy( start, mid, l, r, node<<1);
  int p2 = queryLazy( mid+1, end, l, r, node<<1|1);
  return p1 + p2;
}

int main() {
#ifdef LOCAL
  freopen("SegmentTree.test","r",stdin);
#endif
  cin >> n >> q;
  for (int i = 0; i < n; i++){
    cin >> arr[i];
  }
  built( 0, n-1);
  int l, r, ty,pos , val;
  for (int i = 0; i < q; i++) {
    cin >> ty;
    if( ty == 1){ // query
      cin >> l >> r; l--; r--;
      cout << queryLazy(0, n-1, l, r ) << endl;
      /* cout << query( 0, n-1, l, r) <<endl; */
    }else if( ty == 2){ //update single value
      cin >> pos >> val; // pos 1 indexed
      pos--;
      update( 0, n-1, pos, val);
    }else if( ty ==3){
      cin >> l >> r >> val;
      l--;r--;
      debug(l); debug( r); debug( val );
      updateRange(0, n-1, l, r, val);
    }
  }

  return 0;
}
```

2.5 Trie

```
#include <bits/stdc++.h>
#define endl '\n'
using namespace std;
struct node{
  node* son[10];
  bool is_end = false;
  node(){
  }
};
void insert( node *n, string &num, int pos = 0){
  if( pos == size( num)){
    n->is_end = true;
    return;
  }
```

```
  int id = num[ pos ] - '0';
  if( !n->son[id] ){
    n->son[id] = new node();
  }
  insert( n->son[id], num, pos+1);
}
bool contain(node *n, string &n1, int pos = 0){
  int id = n1[ pos ] - '0';
  if( n->is_end ) return true;
  if( !n->son[ id ]) return false;
  if( size(n1) -1 == pos ) return n->son[id];
  return contain( n->son[ id ], n1, pos+1);
}
```

2.6 UnionFind

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
/*
 Complexity O(log(n))
*/
struct union_find {
  vi p;
  union_find(int n) : p(n, -1) { }
  int find(int x) {
    return p[x] < 0 ? x : p[x] = find(p[x]);
  }
  bool unite(int x, int y) {
    int xp = find(x), yp = find(y);
    if (xp == yp) return false;
    if (p[xp] > p[yp]) swap(xp,yp);
    p[xp] += p[yp];
    p[yp] = xp; //add -1 if merge
    return true;
  }
  int size(int x) {
     return -p[find(x)];
  }
};
```

3 geometry

3.1 CenterCircle

```
#include <bits/stdc++.h>
using namespace std;
const double PI = acos(-1);
#define show(x) cout << #x << " = " << x << endl;
/*
 Complexity O(1)
*/
struct pt {
  double x;
  double y;
  pt (){}
  pt (double _x, double _y){
    x = _x;
    y = _y;
  }
};
inline pt getCenter(pt p1, pt p2, pt p3){
  pt center;
  float m1 = (p2.y - p1.y)/(p2.x - p1.x);
  float m2 = (p3.y - p2.y)/(p3.x - p2.x);
  center.x = ( m1 * m2 * (p1.y - p3.y) + m2 * ( p1.x + p2.x)
                - m1 * (p2.x + p3.x) )
             / (2 * (m2 - m1) );
  center.y = -1 * (center.x - (p1.x + p2.x) / 2) / m1 +  (p1.y +
      p2.y) / 2;
  return center;
}

int main(){
  pt p1(1,1), p2(2,4), p3(5,3);
  pt res = getCenter(p1, p2, p3);
  show(res.x)
  show(res.y)
  return 0;
}
```

3.2 PolygonArea

```
#include <bits/stdc++.h>
#define f first
#define s second
#define mp make_pair
#define pb push_back
using namespace std;
typedef long double ld;
typedef pair <ld, ld> point;
typedef vector < point > polygon;
/*
 Complexity O(n)
*/
inline  point diff(point o, point d){
  return mp(d.f-o.f, d.s - o.s) ;
}
inline ld crossProduct(point o, point d){
  ld cross  = (o.f * d.s)  - ( o.s * d.f);
  return cross > 0 ? cross :  cross * -1;
}
inline ld area(polygon p){
  int num_points = p.size();
  ld area = 0;
  for (int i = 1; i < num_points -1 ; i++){
    point l1 = diff(p[0],p[i]);
    point l2 = diff(p[0],p[i+1]);
    area += crossProduct(l1,l2);
  }
  return abs(area/2.0);
}
int main(){
  polygon p;
  p.pb(mp(1,0)); p.pb(mp(2,1));
  p.pb(mp(1,2)); p.pb(mp(0,1));
  cout << area(p);
  return 0;
}
```

3.3 RayCasting

```
#include <bits/stdc++.h>
#define pb push_back
#define mp make_pair
```

```
using namespace std;
/*
 * This program implements the ray casting algorithm to check
 * if a point is inside or outside of a simple polygon
 */
typedef double ld;
struct point {
  ld x, y;
  point(){}
  point(ld x, ld y){
    this->x = x;
    this->y = y;
  }
};
struct vert {
    point o,d;
};
typedef vector < point > polygon;

inline ld cross(point o, point d){
  return(o.x * d.y)  - ( o.y * d.x); }
inline ld dot(point o, point d){
  return (o.x * d.x)  + ( o.y * d.y); }
inline point diff(point o, point d){
  return {d.x-o.x, d.y - o.y} ;}
inline ld dist(point o, point d){
  return  sqrt(dot(diff(o,d) , diff(o,d))); }

inline  bool segments_parallel(point a, point b, point c){
    return abs(cross(diff(c,a),diff(b,a)))  == 0;
}
inline bool point_on_segment(polygon v,  point c){
  int cant = v.size();
  for (int i=0;i<cant;i++){
    if (dist(v[i],c)==0) return true;
    if (dist(v[(i+1)%cant],c)==0) return true;
    if(segments_parallel(v[i], v[(i+1)%cant], c) &&
        dot(diff(c,v[i]), diff(c,v[(i+1)%cant])) < 0) {
          return true;
    }
  }
  return false;
}

/* Ray Casting algorithm
 * true inside
 * false outside
 */
bool point_in_polygon(point p, polygon a){
  bool inside = false;
  int cant = a.size();
  for (int i=0;i<cant;i++){
    int j = (i+1) % cant;
    point aux = a[i];
    point nxt = a[j];
    bool cond1 = (p.y < aux.y != p.y < nxt.y);
    bool cond2 = (p.x < aux.x + (nxt.x - aux.x) * (p.y - aux.y) /
        (nxt.y - aux.y));
    if ( cond1 && cond2 ){
      inside = !inside;
    }
  }
  return inside;
}
inline void test_point(polygon v, point pun){
  if(point_on_segment(v,pun)){
      cout << "on"<<endl;
  }else if (point_in_polygon(pun, v)){
      cout << "in"<<endl;
  }else{
      cout <<"out"<<endl;
  }
}
int main(){
    polygon p;
    p.pb(point(1,0)); p.pb(point(2,1));
    p.pb(point(1,2)); p.pb(point(0,1));
    test_point(p, point(0,0));
    test_point(p, point(1,1));
    test_point(p, point(1.5,0.5));
    return 0;

}
```

3.4 Struct

```
#include <bits/stdc++.h>
#define INF 1e9
#define EPS 1e-9
#define PI acos(-1.0)
#define debug(x) cout << #x << " " << x << endl;

using namespace std;

struct point {
  double x, y;
  point() {}
  point(double _x, double _y){
    x = _x;
    y = _y;
  }
  point operator + (point p) const {
    return point(p.x + x, p.y +y);  }
  point operator - (point p) const {
    return point(x - p.x, y -p.y);  }
  point operator *(double d) const {
    return point(x*d, y*d); }
  bool operator ==(point p) const {
    return p.x == x && p.y==y; }
  double dot(point p) {
    return x*p.x + y*p.y;};
  double cross2(point p) {
    return x*p.y - p.x*y;};
  double mag () {
    return sqrt(x*x + y*y);};
  double norm() {
    return x*x + y*y;};
  double dist(point p2){
    return hypot(x - p2.x, y - p2.y); };
  void show(){ printf("x= %lf, y=%lf\n", x, y);}
};

struct line {
  point o;//origin
  point d;//destiny
  double m;
  line (){}
  line( point _o, point _d){
    o = _o;
    d = _d;
  }
  double slope(){
    if (o.x != d.x){
      m = (double)(d.y - o.y) / (double)(d.x - o.x);
      return m;
```

```
    }
    m = INF;
    return INF;
  }

};
double cross(point &o, point &a, point &b) {
    return (a.x - o.x)*(b.y - o.y) - (a.y - o.y)*(b.x - o.x);
}
bool areParallel(line l1, line l2) {
  return fabs(l1.slope()-l2.slope())<EPS ;
}
double distToLine(point p, line l1) {
  // formula: c = a + u * ab
  point a = l1.o, b = l1.d, c;
  point ap = p-a, ab = b-a;
  double u = ap.dot(ab) / ab.norm();
  c = a + ab*u;
  return c.dist(p);
}

double distToSegment(point p, line l1) {
  point a = l1.o, b = l1.d, c;
  point ap = p-a, ab = b-a;
  double u = ap.dot(ab) / ab.norm();
  if (u < 0.0) {
    c = point(a.x, a.y);  // closer to a
    return p.dist(a);
  }
  if (u > 1.0) {
    c = point(b.x, b.y);  // closer to b
    return p.dist(b);
  }
  return distToLine(p, line(a, b));
}

int main(){
  point a(0,4);
  point b(5,0);
  point c(7,0);
  a.show();
  b.show();
  c.show();
  line l1(a,b), l2(a,c);
  cout << "m1= "<< l1.slope() << endl;
  cout << "m2= "<< l2.slope() << endl;
  cout << "parallel l1 || l2? = " << (areParallel(l1, l2)?"true":
      "false") << endl;
  cout << "dist from point to line= " << distToLine(c, l1) << endl
      ;
  cout << "dist from point to segment= " << distToSegment(c, l1)
      << endl;
  return 0;
}
```

4 graph

4.1 Dijkstra

```
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
#define INF 2e7
struct edge{
        int to, weight;
        edge(){}
        edge(int _to, int _weight){
                to = _to;
                weight = _weight;
        }
        bool operator < (edge e) const {
                return weight > e.weight;
        }
};
typedef vector < edge > ve;
typedef vector < ve > vve;
typedef vector < int > vi;
typedef priority_queue< edge> pq;
inline void dijkstra(vve &adj, int src, int num_nodes){
  vi dist = vi(num_nodes+1,INF);
        pq  q;
  q.push(edge(src,0));
  dist[src] = 0;
  while(!q.empty()){
    edge top = q.top();
    q.pop();
    int u = top.to;
    for(int i=0;i<adj[u].size();i++){
      int v = adj[u][i].to;
      if(dist[u] + adj[u][i].weight < dist[v]){
        dist[v] = dist[u] + adj[u][i].weight;
        q.push(edge(v,dist[v]));
      }
    }
  }
}

int main(){
        int nodes =5;
  vve adj(nodes);
        //from              to - weight
        adj[0].pb(edge(1, 6));
        adj[0].pb(edge(2, 2));
        adj[1].pb(edge(3, 5));
        adj[1].pb(edge(4, 7));
  int src = 1;
  dijkstra(adj, src, nodes);
  return 0;
}
```

4.2 Dinic

```
#include<bits/stdc++.h>
#define debug( x ) cout << #x << " = " << x <<endl;
using namespace std;
/// Complexity: O(|E|*|V|^2)
/// Implementation Notebook UNAL
// Codeforces 1082/G
typedef long long ll;
const int inf = 1e9+17;
struct edge { ll v, cap, inv, flow; };
struct network {
  ll n, s, t;
  vector<ll> lvl;
  vector<vector<edge>> g;
  network(int n) : n(n), lvl(n), g(n) {}
  void add_edge(int u, int v, int c) {
    g[u].push_back({v, c, g[v].size(), 0});
    g[v].push_back({u, 0, g[u].size()-1, c});
  }
  bool bfs() {
```

```
    fill(lvl.begin(), lvl.end(), -1);
    queue<int> q;
    lvl[s] = 0;
    for(q.push(s); q.size(); q.pop()) {
      int u = q.front();
      for(auto &e : g[u]) {
        if(e.cap > 0 && lvl[e.v] == -1) {
          lvl[e.v] = lvl[u]+1;
          q.push(e.v);
        }
      }
    }
    return lvl[t] != -1;
  }
  ll dfs(int u, ll nf) {
    if(u == t) return nf;
    ll res = 0;
    for(auto &e : g[u]) {
      if(e.cap > 0 && lvl[e.v] == lvl[u]+1) {
        ll tf = dfs(e.v, min(nf, e.cap));
        res += tf; nf -= tf; e.cap -= tf;
        g[e.v][e.inv].cap += tf;
        g[e.v][e.inv].flow -= tf;
        e.flow += tf;
        if(nf == 0) return res;
      }
    }
    if(!res) lvl[u] = -1;
    return res;
  }
  ll max_flow(int so, int si, ll res = 0) {
    s = so; t = si;
    while(bfs()) res += dfs(s, INT_MAX);
    return res;
  }
};

int main(){
  #ifdef LOCAL
    freopen("un","r",stdin);
#endif
  int n, m, ai, wi;
  while( cin >>n >>m ){
    int nn = n+m+20;
    int s = nn-1, t = nn-2;
    network nt( nn );
    for( int i= 0; i< n; i++){ // weights
      cin >> ai;
      nt.add_edge( i, t, ai);
    }
    int u , v, w;
    ll sum = 0;
    for( int i = 0; i< m; i++){
      cin >> u >> v >> w;
      --u; --v;
      sum += w;
      nt.add_edge( s, i+n , w);
      nt.add_edge( i+n, u, inf);
      nt.add_edge( i+n, v, inf);
    }

    ll maxFlow = nt.max_flow( s, t );
    ll res = sum - maxFlow;
    cout << res << endl;
  }

  return 0;
}
```

4.3 EdmonKarp

```
#include<bits/stdc++.h>
#define F first
#define PB push_back
#define S second
#define debug( x ) cout <<#x << " = " << x <<endl;
using namespace std;

typedef pair< int, int > ii;
const int INF = 1e9;
int n;
map< ii, int > w;
unordered_map<int, vector<int>> adj;


int bfs(int s, int t, vector<int>& pt) {
  fill(pt.begin(), pt.end(), -1);
  pt[s] = -2;
  queue<ii> q;
  q.push({s, INF});
  while (!q.empty()) {
    int cur = q.front().F;
    int flow = q.front().S; q.pop();
    for (int next : adj[cur]) {
      if (pt[next] == -1 && w[{cur,next}]) {
        pt[next] = cur;
        int new_flow = min(flow, w[{cur,next}]);
        if (next == t) return new_flow;
        q.push({next, new_flow});
      }
    }
  }
  return 0;
}

int maxflow(int s, int t) {
  int flow = 0;
  vector<int> pt(n);
  int new_flow;
  while (new_flow = bfs(s, t, pt)) {
    flow += new_flow;
    int cur = t;
    while (cur != s) {
      int prev = pt[cur];
      w[{prev,cur}] -= new_flow;
      w[{cur,prev}] += new_flow;
      cur = prev;
    }
  }
  return flow;
}


int main(){
#ifdef LOCAL
  freopen("in","r",stdin);
#endif
  int from, to, cap, m;
  while( cin >> n >>m ){

    for( int i= 0; i<m ; i++){
      cin >> from >> to >> cap;
      adj[from].PB( to );
      w[{from, to}] = cap;
    }

    int mf = maxflow( 0, 3); // from 1 to 5 maxFlow
```

```
    debug( mf );
  }
  return 0;
}
```

4.4 FloydWarshal

```
#include<iostream>
#include<stdio.h>
using namespace std;
/*
 * Floyd-Warshall gives us the shortest paths
 * from all sources to all target nodes.
 */
#define V 4  //number of vertex
#define INF 9999999

void floyd (int graph[][V]){
  int dist[V][V], i, j, k;
  for (i = 0; i < V; i++)
    for (j = 0; j < V; j++)
      dist[i][j] = graph[i][j];
  for (k = 0; k < V; k++){
    for (i = 0; i < V; i++){
      for (j = 0; j < V; j++){
        if (dist[i][k] + dist[k][j] < dist[i][j])
            dist[i][j] = dist[i][k] + dist[k][j];
      }
    }
  }
  show(dist);
}
int main(){
    int graph[V][V] =
    { {0,   5,  INF, 10},
      {INF, 0,   3, INF},
      {INF, INF, 0,   1},
      {INF, INF, INF, 0}
    };
    floyd(graph);
    return 0;
}
```

4.5 RecoveryTree

```
#include <iostream>
using namespace std;
/**Build a binary tree form a inorder and preoder string **/
int preIndex = 0;
struct node {
  char key;
  node *left, *right;
  node(int k) {
    key = k;
    left = NULL;
    right = NULL;
  }
};
int search(string word, int b, int e, char c) {
  for(int i=b; i<=e; i++) {
    if(word[i] == c) return i;
  }
  return -1;
}
//Set preIndex to 0 to build another tree
node* build(string in, string pre, int b, int e) {
  if(b > e) return NULL;
  node *root = new node(pre[preIndex++]);
  if(b == e)return root;
  int inIndex = search(in, b, e, root->key);
  root->left = build(in, pre, b, inIndex - 1);
  root->right = build(in, pre, inIndex + 1, e);
  return root;
}

int main() {
  string pre, in;
  node *tree;
  while(cin >> pre >> in) {
    tree = build(in, pre, 0, pre.size() - 1);
    preIndex = 0;
  }
  return 0;
}
```

4.6 Tsort

```
#include<bits/stdc++.h>
#define debug(x) cout << #x << " = " << x <<endl;
#define PB push_back
using namespace std;

typedef vector < bool > vb;
typedef vector < int > vi;

enum { NV, SV, V};
vb vis;
int N;
vector < vi > G;

void dfs( int src, stack < int > &S ){
  for( int son: G[src]){
    if( vis[ son ] == NV)
      dfs( son, S );
  }
  vis[src] = V;
  S.push( src );
}

void tsort( ){
  stack< int > S;
  vis.resize( N );
  vis.assign( N, NV);
  for( int i = 0; i < N; i++){
    if( vis[i]  == NV)   dfs( i, S);
  }
  while(!S.empty()){
    cout << S.top() <<endl;
    S.pop();
  }
}

int main(){

  N = 6;
  G.resize(N);
  G[0].PB( 1 );
  G[0].PB( 2 );
  G[0].PB( 3 );
```

```
  G[1].PB( 4 );
  G[4].PB( 3 );
  G[5].PB( 2 );
  G[3].PB( 2 );

  tsort( );
  return 0;
}
```

5 mathematics

5.1 Binomial

```
#include <iostream>
using namespace std;
const int MAXN = 66;
unsigned long long ch[MAXN+5][MAXN+5];

int Cnk( ll n, ll k){
  ll res =1;
  // since C(n,k) == C(n, n-k)
  if( k > n-k) k = n-k;
  for( ll i = 0; i< k; i++){
    res = res*1LL*(n-i);
    res /= (i+1);
  }
  return res;
}
void binomial(int N){
  for (int n = 0; n <= N; ++n)
    ch[n][0] = ch[n][n] = 1;
  for (int n = 1; n <= N; ++n){
    for (int k = 1; k < n; ++k){
      ch[n][k] = ch[n-1][k-1] + ch[n-1][k];
    }
  }
}
int main(){
  binomial(10);
  cout << ch[10][2] << endl;
}
```

5.2 Binomial

```
import math, sys
MAXN = 431
choose = []
for i in range (0, MAXN+5):
  choose.append([0]*(MAXN+5))
def binomial(N):
  for n in range (0, N+1):
    choose[n][0] = choose[n][n] = 1
  for n in range(1, N+1):
    for k in range(1, n):
       choose[n][k] = choose[n-1][k-1] + choose[n-1][k]
if __name__ == "__main__":
  N = 431
  binomial(N)
  n, k = 10, 4
  print(choose[n][k])
```

5.3 ChangeBases

```
#include<bits/stdc++.h>
#define endl '\n'
#define show(x) cout <<#x << " =" <<x <<endl;
using namespace std;
typedef long long ll;
string chars = "0123456789ABCDEFGHIJKLMN OPQRSTUVWXYZ";

ll to10(ll n , ll b, ll mul){
  if (n ==0 ) return 0;
  return (n % 10)*mul + to10(n / 10, b, mul*1LL*b);
}

string tob(ll n, ll b){
  if (n == 0) return "";
  return  tob(n / b, b) + chars[n % b];
}
/*
 * ob -> origin base
 * db -> destiny base
 */
string changeBase(ll num, ll ob, ll db){
  if (ob == 10) return tob(num, db);
  return tob(to10(num, ob, 1LL), db);
}
int main(){
  cout << changeBase(1000,2,10) <<endl;
}
```

5.4 CoinChange

```
#include <bits/stdc++.h>
#define MAXCOINS (10005)
#define MAXVALUE (105)
using namespace std;
typedef vector < int > vi;
int dp[MAXVALUE][MAXCOINS];
vi coins;
//recursive
int ways(int tg, int n){
  if ( 0 == tg) return 1;
  if ( 0 > tg) return 0;
  if ( n <= 0 && tg >0) return 0;
  return ways(tg, n-1) +
    ways(tg - coins[n -1], n);
}
//by dp
int waysdp(int tg, int n){
  for( int i=0; i< coins.size(); i++) dp[0][i] = 1;
  for(int i = 1 ; i<= tg; i++){
   for (int c = 0; c < n; c++){
      int x =0 , y = 0;
      if(i-coins[c] >= 0) x = dp[i - coins[c]][c];
      if( c >=1) y = dp[i][c-1];
      dp[i][c] = x + y;
              }
    }
  return dp[tg][n-1];
}

int main(){
  coins.insert(coins.end(), {1,3,9,27});
```

```
  cout <<  ways(47, coins.size()) <<endl;
  cout << waysdp(47, coins.size()) <<endl;
  return 0;
}
```

5.5 Combination

```
#include<bits/stdc++.h>
using namespace std;

vector< int > com;
int k, n ;

void comb( int off, int ki){
  if( ki == 0 ){
    for( int &c: com) cout << c << " ";
    cout <<endl;
    return;
  }
  for( int i = off; i <= n - ki ; i++){
    com.push_back( i );
    comb( i+1, ki-1);
    com.pop_back();
  }
}

int main(){
  n = 5; k = 3;
  comb( 0, k );

  return 0;
}
```

5.6 CompareDoubles

```
#include <stdio.h>
using namespace std;
const double EPS = 1e-15;
/*
 * Return
 * -1   if x < y
 *  0   if x == y
 *  1   if x > y
 */
int cmp (double x, double y){
    return (x <= y + EPS) ? (x + EPS < y) ? -1 : 0 : 1;
}
int main(){
  double d1 = 0.00000000000212;
  double d2 = 0.00000000000213;
  int res = cmp(d1,d2);
  if (res == 0){
    printf("Equal \n");
  }else if(res == 1){
    printf("Greater\n");
  }else {
    printf("Less \n");
  }
}
```

5.7 ExtendedEuclides

```
#include <bits/stdc++.h>

using namespace std;
typedef long long ll;
typedef vector < ll > vl;

vl arr(3);
/*
  returs gcd(a,b) and find the coeficcients of bezout
  such that d = ax + by
  arr[0] gcd
  arr[1] x
  arr[2] y
*/
void extended(ll a, ll b){
  ll y =0;
  ll x =1;
  ll xx =0;
  ll yy =1;
  while(b){
    ll q = a / b;
    ll t = b;
    b = a%b;
    a = t;

    t = xx;
    xx = x-q*xx;
    x = t;

    t = yy;
    yy = y -q*yy;
    y = t;
  }
  arr[0] = a;
  arr[1] = x;
  arr[2] = y;
}
/*
  ax + by  = c
  mcd(a,b) = d
  ax0 + by0 = d
  c = d * c'

  Bezouts identity
   X = x0 * c' - (b/d) * k
   Y = y0 * c' + (a/d) * k
*/
int main(){
  ll a = 20, b = 50;
  extended(a,b);
  printf("gcd(%lld, %lld) = %lld = %lld * %lld + %lld * %lld\n",
       a, b, arr[0], a,arr[1], b, arr[2]);
  return 0;
}
```

5.8 ExtendEuclidesSample

```
#include<bits/stdc++.h>
#define F first
#define S second
using namespace std;
typedef long long ll;
typedef pair<ll, ll> ii;

ll gcd;

ii extended(ll a, ll b) {
  ll y =0, x =1, xx =0, yy =1;
  while (b){
```

```
    ll q = a / b;
    ll t = b;

    b = a%b;
    a = t;
    t = xx;
    xx = x-q*xx;

    x = t;
    t = yy;
    yy = y -q*yy;

    y = t;
  }
  gcd = a;
  // a becomes gcd(a,b);
  return {x,y};
}

int main(){
#ifdef LOCAL
  freopen("in","r", stdin);
#endif
  int a, b, c;

  // ax + by = c
  while( cin >> a >> b >> c ){
    ii res = extended( a, b );
    if( c % gcd == 0 ){
      ll x = (c/gcd)*res.F, y = (c/gcd)*res.S;
      cout << x <<  " " <<  y << endl;
    }else{
      // no solution
    }
  }
  return 0;
}
```

5.9 Factorize

```
#include <bits/stdc++.h>
#define pb push_back
#define show(x) cout << #x << " = " << x << endl;
using namespace std;
const int MAXN = 1000000;
bool sieve[MAXN + 5];
typedef long long ll;
vector <ll> pri; //primes

void build_sieve(){
  memset(sieve, false, sizeof(sieve));
  sieve[0] = sieve[1] = true;
  for (ll i = 2LL; i * i <= MAXN; i ++){
    if (!sieve[i]){
      for (ll j = i * i; j <= MAXN; j += i){
        sieve[j] = true;
      }
    }
  }
  for (ll i = 2; i <= MAXN; ++i){
    if (!sieve[i]) pri.pb(i);
  }
}
//before call this call build_sieve
vector <ll> fact(long long a){
  vector <ll> ans;
  ll b = a;
  for (int i = 0; 1LL * pri[i] * pri[i] <= a; ++i){
    int p = pri[i];
    while (b % p == 0){
      ans.push_back(p);
      b /= p;
    }
  }
  if (b != 1) ans.push_back(b);
  return ans;
}
int main(){
  build_sieve();
  ll num_to_fact= 128234234LL;
  vector < ll > vll = fact(num_to_fact);
  for (int x=0; x< vll.size(); x++){
    cout << vll[x] << " ";
  }
  cout << endl;
}
```

5.10 FastPow

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
inline ll add ( ll x, ll y){
  return (x%MOD +y%MOD)%MOD;
}
inline ll mul( ll x , ll y){
  return (x%MOD*1LL*y%MOD)%MOD;
}

inline ll fpow( ll x, ll p){ // (x^p)%MOD
  ll res=1LL;
  while( p ){
    if( p & 1){
      res = mul(res,x);
    }
    p >>= 1LL;
    x = mul(x,x);
  }
  return res;
}
```

5.11 GcdLcm

```
#include<cstdio>
using namespace std;
typedef long long ll;
ll mod( ll a, ll b){
  return (b + (a %b )) %b;
}
ll gcd ( ll a, ll b){
  if (b == 0 ) return a;
  return gcd( b, mod( a , b) );
}
ll lcm(ll n1, ll n2){
    return (n1 *1LL* n2) / gcd(n1,n2);
}
int main(){
    ll n1=2366, n2=273;
    printf("gcd(%ld, %ld) = %ld\n",
            n1, n2, gcd(n1,n2));
    return 0;
```

```
}
```

5.12 IsFibo

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
bool isPerfectSquare(long long x){
  ll s = sqrt(x);
  return (s*1LL*s == x);
}
bool isFibonacci(int n){
  return isPerfectSquare(5*n*1LL*n + 4) || isPerfectSquare(5*1LL*n
      *n - 4);
}
```

5.13 IsPrime

```
import java.math.BigInteger;
import java.util.Scanner;
public class prime {
  public static void main(String[] args) {
   BigInteger a = new BigInteger("1299827");
   //User miller rabin & Lucas Lehmer
   boolean res = a.isProbablePrime(10);
   System.out.println(res? "It's prime":"It's not prime");
 }
}
```

5.14 knapsack

```
#include<bits/stdc++.h>
#define MAX (int) 1e3
using namespace std;
int v[5] = {60, 100, 120, 30, 5};
int w[5] = {10, 20, 30, 30, 5};

int memo[MAX][MAX];

int knapsack( int n , int W){
  if( n  == 0 || W == 0 ) return 0;
  int &ans = memo[n][W];
  if( ans != -1) return ans;
  if( w[n] > W ) { //not include too heavy
    ans =  knapsack(n-1, W);
  }else{
    //Include
    int a1 = v[n]+ knapsack( n-1, W-w[n] );
    //Not include
    int a2 = knapsack( n -1, W);
    ans =  max(a1, a2);
  }
  return ans;
}

int main() {
  for( int i = 0; i < MAX; i++)
    for( int j = 0; j < MAX; j++)
      memo[i][j] =  -1;


  cout << knapsack ( 5, 50) << endl;
  return 0;
}
```

5.15 MatrixExpo

```
#include <bits/stdc++.h>
#define endl '\n'
#define debug1( x ) cout << #x << " = " <<  x << endl;
#define debug2( x, y) cout <<#x << " = " << x << " , " <<#y << " =
    " << y <<endl;
#define F first
#define S second
#define PB push_back
#define size( x )   int( ( x ).size( ) )
#define endl '\n'
#define rep(i, a, b) for( __typeof(a) i =(a); i<(b);i++)

using namespace std;
typedef long long ll;
typedef pair<int, int> ii;
typedef vector<int> vi;


const int N = 100;
const int MOD = 1e9+9;
struct matrix {
  int m[N][N], r, c;
  matrix(int r, int c) : r(r), c(c) {
    memset(m, 0, sizeof m);
  }
  matrix operator * (const matrix &o) const {
    matrix ret(r, o.c);
    for(int i = 0; i < r; ++i)
      for(int j = 0; j < o.c; ++j) {
        for(int k = 0; k < c; ++k)
          ret.m[i][j] = (ret.m[i][j] + 1ll*m[i][k]*o.m[k][j]) %
              MOD;
      }
    return ret;
  }
  void show(){
    rep( i,0 ,r){
      rep( j,0, c){
        cout << m[i][j] <<" ";
      }
      cout <<endl;
    }
  }
};

matrix fastPow( matrix &x, int e){
  matrix res(x.r,x.r);
  rep(i , 0, x.r) res.m[i][i] = 1; // identity
  while( e ){
     if( e % 2){
        res = res*x;
     }
     e /= 2;
     x = x*x;
  }
  return res;
}

int main(){
  ios::sync_with_stdio( false );
  cin.tie( nullptr );
#ifdef LOCAL
```

```
  freopen("in", "r" , stdin);
#endif

  matrix ma(2,2);
  ma.m[0][0] = 2;
  ma.m[0][1] = 5;
  ma.m[1][0] = 1;
  ma.m[1][1] = 8;

  ma.show();

  ma = fastPow( ma, 2);
  ma.show();

  return 0;
}
```

5.16 MillerPollard

```
#include<bits/stdc++.h>
using namespace std;
typedef long long ll;
/*
 * algorithm taken notebook unal 2018,
 *https://github.com/mavd09/notebook_unal_2018
 * */
ll mul (ll a, ll b, ll mod) {
  ll ret = 0;
  for(a %= mod, b %= mod; b != 0;
    b >>= 1, a <<= 1, a = a >= mod ? a - mod : a) {
    if (b & 1) {
      ret += a;
      if (ret >= mod) ret -= mod;
    }
  }
  return ret;
}
ll fpow (ll a, ll b, ll mod) {
  ll ans = 1;
  for (; b; b >>= 1, a = mul(a, a, mod))
    if (b & 1)
      ans = mul(ans, a, mod);
  return ans;
}
bool witness (ll a, ll s, ll d, ll n) {
  ll x = fpow(a, d, n);
  if (x == 1 || x == n - 1) return false;
  for (int i = 0; i < s - 1; i++) {
    x = mul(x, x, n);
    if (x == 1) return true;
    if (x == n - 1) return false;
  }
  return true;
}
ll test[] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 0};
bool is_prime (ll n) {
  if (n < 2) return false;
  if (n == 2) return true;
  if (n % 2 == 0) return false;
  ll d = n - 1, s = 0;
  while (d % 2 == 0) ++s, d /= 2;
  for (int i = 0; test[i] && test[i] < n; ++i)
    if (witness(test[i], s, d, n))
      return false;
  return true;
}
```

```
ll pollard_rho(ll n, ll c) {
  ll x = 2, y = 2, i = 1, k = 2, d;
  while (true) {
    x = (mul(x, x, n) + c);
    if (x >= n) x -= n;
    d = __gcd(x - y, n);
    if (d > 1) return d;
    if (++i == k) y = x, k <<= 1;
  }
  return n;
}
void factorize(ll n, vector<ll> &f) {
  if (n == 1) return;
  if (is_prime(n)) {
    f.push_back(n);
    return;
  }
  ll d = n;
  for (int i = 2; d == n; i++)
    d = pollard_rho(n, i);
  factorize(d, f);
  factorize(n/d, f);
}

int main(){
  #ifdef LOCAL
    freopen("in","r",stdin);
  #endif
  ll num;

  while( cin>> num && num!=-1){
    vector< ll > ans;
    factorize( num, ans);
    sort( ans.begin(), ans.end());
    for( auto x: ans){
      cout << "    "<<x << endl;
    }
    cout <<endl;
  }

  return 0;
}
```

5.17 NaiveFind

```
#include <bits/stdc++.h>
using namespace std;
int main(){
  string needle = "CD", haystack ="MANICD";
  if(haystack.find(needle) != string::npos) cout << "Gotcha!!!";
  else cout << "Not Gotcha";
  cout << endl;
  return 0;
}
```

5.18 PollarRho

```
import random as r
def gcd( a, b):
    if(b == 0): return a;
    return gcd(b, a % b);
def pollardRho(N):
    if N%2==0: return 2
```

```
    x = r.randint(1, N-1)
    y = x
    c = r.randint(1, N-1)
    g = 1
    while g==1:
        x = ((x*x)%N+c)%N
        y = ((y*y)%N+c)%N
        y = ((y*y)%N+c)%N
        g = gcd(abs(x-y),N)
    return g
if(__name__=="__main__"):
    print(pollardRho(10967535067))
    print(pollardRho(113))
```

5.19 PrimalyTest

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
bool isPrime(ll n){
  if (n < 2) return false;
  if (n < 4) return true;
  if (n % 2 == 0 || n % 3 == 0) return false;
  if (n < 25) return true;
  for(int i = 5; i*i <= n; i += 6){
    if(n % i == 0 || n % (i + 2) == 0)
        return false;
  }
  return true;
}
int main(){
    cout << isPrime(23234) << endl;
    cout << isPrime(2) << endl;
    cout << isPrime(7454) << endl;
    cout << isPrime(976) << endl;
    cout << isPrime(1973) << endl;
    return 0;
}
```

5.20 RotateMatrix

```
#include<bits/stdc++.h>
using namespace std;
#define R 4
#define C 4
int arr[R][C];

void reverseColumns(){
  for (int i=0; i<C; i++)
    for (int j=0,  k=C-1; j<k; j++,k--)
      swap(arr[j][i], arr[k][i]);
}
void transpose() {
  for (int i=0; i<R; i++)
        for (int j=i; j<C; j++)
      swap(arr[i][j], arr[j][i]);
}
/* anticlockwise rotate matrix by 90 degree*/
void rotate90(){
  transpose();
  reverseColumns();
}

int main() {
  int aux [R][C]=
   { {1, 2, 3, 4},
     {5, 6, 7, 8},
     {9, 10, 11, 12},
     {13, 14, 15, 16}
   };
   rotate90();
   return 0;
}
```

5.21 Sieve

```
#include <bits/stdc++.h>
#define tam 1000
using namespace std;
typedef long long ll;
typedef vector< bool > vbool;
void show (vbool primes){
  ll cap = primes.size();
  for(ll i = 0; i< cap; i++){
    cout << i << " : " << primes[i] << endl;
  }
}
vbool sieve(ll n){
  vbool sieve (tam);
  for (ll i = 0; i < tam; i++)
    sieve[i] = true;
    sieve [0] = sieve[1] = false;
    ll root = sqrt(n);
    for (ll i = 2; i < root; i++){ //find primes
      if(sieve[i]){
        //removes all the multiples
        //of the current prime
        for (ll k = i*1LL*i; k<= n; k+=i){
          sieve[k] = false;
        }
      }
    }
    return sieve;
}
int main(){
    vbool primes = sieve(1000);
    show(primes);;
    primes.clear();
    return 0;
}
```

5.22 Sum

```
/*
  Summatories
*/
int main(){
  sum(i) from 1 to n = n(n+1)/2
  sum(i^2) from 1 to n = n(n+1)(2n+1)/6
  sum(i^3)  from 1 to n = (n^2(n+1)^2)/4

  //Geometric serie
  a * sum(r^k) from 0 to n = a * (1-r ^(n+1)) / (1 -r)
 //  ar + ar^2 + ar^3 ...
}
```

5.23 toBin

```cpp
#include <bits/stdc++.h>
using namespace std;
void toBin(int x){
  for (int i =31; i>=0; --i)
    cout << ((x&(1LL<<i))!=0);
}
int main (){
  toBin(10);
  return 0;
}
```

6 other

6.1 MergeSortPY

```python
def merge_sort(arr):
    if (len(arr)>1):
        mid = len(arr) // 2
        lefthalf, righthalf = arr[:mid] , arr[mid:]
        merge_sort(lefthalf)
        merge_sort(righthalf)

        merge(lefthalf, righthalf, arr)

def merge(lh, rh, arr):
    il = 0
    ir = 0
    k = 0
    while il < len(lh) and ir < len(rh):
        if (lh[il] < rh[ir]):
            arr[k] = lh[il]
            il = il+1
        else:
            arr[k] = rh[ir]
            ir = ir+1
        k = k+1

    while il < len (lh):
        arr[k]= lh[il]
        il = il +1
        k = k+1

    while ir < len(rh):
        arr[k] = rh[ir]
        ir = ir +1
        k = k+1

def main():
    array = [-10, 37, 98 , 0 ,12, 192, 5]
    print("Original Array")
    print(array)
    merge_sort(array)

    print("Sorted Array")
    print(array)
main()
```

6.2 Partitions

```cpp
#include<iostream>
using namespace std;
/*
  Generate all unique
  partitions of a given integer
*/

void partitions(int n){
  int p[n];
  int k = 0;
  p[k] = n;

  while (true){
   for( int i =0; i <=k ; i++) cout <<p[i] << " ";
   cout <<endl;
   int rem_val = 0;
   while (k >= 0 && p[k] == 1){
    rem_val += p[k];
    k--;
   }
   if (k < 0) return;
   p[k]--;
   rem_val++;
   // If rem_val is more, then the sorted order is violated.
      Divide
   // rem_val in different values of size p[k] and copy these
      values at
   // different positions after p[k]
   while (rem_val > p[k]){
    p[k+1] = p[k];
    rem_val = rem_val - p[k];
    k++;
   }
   // Copy rem_val to next position and increment position
   p[k+1] = rem_val;
   k++;
  }
}
int main(){
  cout << "All Unique Partitions of 7 \n";
  partitions(7);
  return 0;
}
```

6.3 TemplateC

```cpp
#include <bits/stdc++.h>
using namespace std;

// INT_MAX  -> limits.h
typedef long long ll;
typedef long double ld;
typedef vector < int > vi;
typedef vector < vi > vii;
struct point {int x, y;};

#define show(x) cout << #x << " = " << x << endl;
#define isOdd(x) (x & 0x01)
#define mod(a,b) (b + (a % b)) % b)

const double PI = acos(-1);
const ld INF = 1e18;
const double EPS = 1e-15;

void input(){
  /*
  scanf("%ld",&value); //long y long int
```

```
  scanf("%c",&value); //char
  scanf("%f",&value); //float
  scanf("%lf",&value); //double
  scanf("%s",&value); //char*
  scanf("%lld",&value); //long long int
  scanf("%x",&value); //int hexadecimal
  scanf("%o",&value); //int octal
  */
}

void tricks(){
  int a=21,b=16,c=8;
  //if the numbers are long and long long end with and l or two l
  /*ie
    int
    __builtin_popcount
    long
    __builtin_popcountl
    long long
    __builtin_popcountll
    */
  //log2 floor
  show(__lg(21));
  show(__lg(16));
  show(__lg(8));
  cout << endl;
  //count the number of ones
  show(__builtin_popcount(16));
  show(__builtin_popcount(15));
  show(__builtin_popcount(0));
  cout << endl;

  //count the trailing zeros zer
  show(__builtin_ctz(16));
  show(__builtin_ctz(5));
  cout << endl;

  //count the leading zeros
  show(__builtin_clz(32));
  show(__builtin_clz(1024));
  cout << endl;
  //Returns one plus the index of the least significant
  //1-bit of x, or if x is zero, returns zero.
  show(__builtin_ffs(5));
  cout << endl;
  //Is a number   x   power of 2?
  show(((a & (a-1))==0));
  show(((b & (b-1))==0));
  cout << endl;

  //turn on the first n bits of a mask
  show(((1LL<<10)-1));
}

//Main
int main(){
  ios::sync_with_stdio(false);
  cin.tie(0);

  tricks();
  #ifdef LOCAL
    freopen("in.txt", "r", stdin);
    freopen("out.txt", "w", stdout);
  #endif
}
```

6.4 TemplateP

```
from sys import stdin
lines = stdin.read().splitlines()
for line in lines:
  a, b = [int(y) for y in line.split()]
```

6.5 UpperLowerBound

```
#include <bits/stdc++.h>
using namespace std;
int main () {
  int myints[] = {10,20,30,30,20,10,10,20};
  vector<int> v(myints,myints+8);           // 10 20 30 30 20 10
      10 20
  sort (v.begin(), v.end());                // 10 10 10 20 20 20
      30 30
  vector<int>::iterator low,up;
  low=lower_bound (v.begin(), v.end(), 20); //          ^
  up= upper_bound (v.begin(), v.end(), 20); //                   ^
  cout << "lower_bound at position " << (low- v.begin()) << '\n';
  cout << "upper_bound at position " << (up - v.begin()) << '\n';
  return 0;
}
```

6.6 XIncludes

```
#include <vector>      vector<
#include <queue>       queue< priority_queue<
#include <set>         set< multiset<
#include <map>         map< multimap<
#include <bitset>      bitset<
#include <list>        list<
#include <deque>       deque<
#include <stack>       stack<
#include <complex>     complex<
#include <hash_map.h>  hash_map<
#include <hash_set.h>  hash_set<
#include <string>      string
#include <algorithm>   sort( stable_sort( make_heap( push_heap(
    pop_heap(
                       lower_bound( upper_bound( equal_range(
                           binary_search(
                       find( find_first_of( count( min( max( swap(
                           fill( copy(
                       next_permutation( prev_permutation(
                       remove( replace( reverse( rotate(
                           random_shuffle(
                       min_element( max_element( nth_element(
                           mismatch(
                       set_difference( set_intersection( set_union(
                       set_symmetric_difference( merge( unique(
                           adjacent_find(
                       lexicographical_compare(
                           lexicographical_compare_3way(
                       equal( includes(
#include <numeric>     accumulate( partial_sum( adjacent_difference
    (
                       inner_product(
#include <iostream>    cin cout cerr istream ostream
#include <fstream>     ifstream ofstream ifstream( ofstream(
```

```
#include <sstream>    istringstream ostringstream
#include <cassert>    assert(
#include <cmath>      sin( cos( tan( asin( acos( atan( atan2( sinh
    ( cosh( tanh(
                      sqrt( hypot( abs( exp( pow( ceil( floor(
                          fmod( log( log10(
                      fabs( M_PI
#include <cstdio>     printf( scanf( fprintf( fscanf( sprintf(
    sscanf(
                      getc( fgetc( putc( fputc( getchar( putchar(
                          ungetc(
                      FILE stdin stdout stderr feof( fclose(
                          fflush(
#include <cstdlib>    rand( srand(
#include <cstring>    memcpy( memmove( memchr( memset(
                      strcpy( strncpy( strcat( strncat( strcmp(
                          strncmp(
                      strchr( strrchr( strstr( strtok( strlen(
#include <ctime> time( clock( CLOCKS_PER_SEC
```

6.7 YGenerator

```
#include <bits/stdc++.h>
using namespace std;
int main(){
        #ifdef LOCAL
        freopen("new.c", "w", stdout);
  #endif
  srand (time(NULL));

  int numRandom = 1000;
  cout << numRandom <<endl;
  for( int i=1 ; i<=numRandom ; i++)
        int cant = rand() % 100 +2;
  return 0;

}
```

7 problems

7.1 FactoringLargeNumbers

```
#include<bits/stdc++.h>
using namespace std;
typedef long long ll;

ll mul (ll a, ll b, ll mod) {
  ll ret = 0;
  for(a %= mod, b %= mod; b != 0;
    b >>= 1, a <<= 1, a = a >= mod ? a - mod : a) {
    if (b & 1) {
      ret += a;
      if (ret >= mod) ret -= mod;
    }
  }
  return ret;
}
ll fpow (ll a, ll b, ll mod) {
  ll ans = 1;
  for (; b; b >>= 1, a = mul(a, a, mod))
    if (b & 1)
      ans = mul(ans, a, mod);
  return ans;
}
bool witness (ll a, ll s, ll d, ll n) {
  ll x = fpow(a, d, n);
  if (x == 1 || x == n - 1) return false;
  for (int i = 0; i < s - 1; i++) {
    x = mul(x, x, n);
    if (x == 1) return true;
    if (x == n - 1) return false;
  }
  return true;
}
ll test[] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 0};
bool is_prime (ll n) {
  if (n < 2) return false;
  if (n == 2) return true;
  if (n % 2 == 0) return false;
  ll d = n - 1, s = 0;
  while (d % 2 == 0) ++s, d /= 2;
  for (int i = 0; test[i] && test[i] < n; ++i)
    if (witness(test[i], s, d, n))
      return false;
  return true;
}


ll pollard_rho(ll n, ll c) {
  ll x = 2, y = 2, i = 1, k = 2, d;
  while (true) {
    x = (mul(x, x, n) + c);
    if (x >= n) x -= n;
    d = __gcd(x - y, n);
    if (d > 1) return d;
    if (++i == k) y = x, k <<= 1;
  }
  return n;
}
void factorize(ll n, vector<ll> &f) {
  if (n == 1) return;
  if (is_prime(n)) {
    f.push_back(n);
    return;
  }
  ll d = n;
  for (int i = 2; d == n; i++)
    d = pollard_rho(n, i);
  factorize(d, f);
  factorize(n/d, f);
}

int main(){
  #ifdef LOCAL
    freopen("in","r",stdin);
  #endif
  ll num;

  while( cin>> num && num!=-1){
    vector< ll > ans;
    factorize( num, ans);
    sort( ans.begin(), ans.end());
    for( auto x: ans){
      cout << "    "<<x << endl;
    }
    cout <<endl;
  }

  return 0;
}
```

7.2 FibonnaciiExpo

```
#include <bits/stdc++.h>
#define endl '\n'
#define debug1( x ) cout << #x << " = " <<  x << endl;
#define debug2( x, y) cout <<#x << " = " << x << " , " <<#y << " =
     " << y <<endl;
#define F first
#define S second
#define PB push_back
#define size( x )   int( ( x ).size( ) )
#define endl '\n'
#define rep(i, a, b) for( __typeof(a) i =(a); i<(b);i++)

using namespace std;
typedef long long ll;
typedef pair<int, int> ii;
typedef vector<int> vi;


const int N = 100;
const int MOD = 1e9+9;
struct matrix {
  int m[N][N], r, c;
  matrix(int r, int c) : r(r), c(c) {
    memset(m, 0, sizeof m);
  }
  matrix operator * (const matrix &o) const {
    matrix ret(r, o.c);
    for(int i = 0; i < r; ++i)
      for(int j = 0; j < o.c; ++j) {
        for(int k = 0; k < c; ++k)
          ret.m[i][j] = (ret.m[i][j] + 1ll*m[i][k]*o.m[k][j]) %
              MOD;
      }
    return ret;
  }
  void show(){
    rep( i,0 ,r){
      rep( j,0, c){
        cout << m[i][j] <<" ";
      }
      cout <<endl;
    }
  }
};

matrix fastPow( matrix &x, ll e){
  matrix res(x.r,x.r);
  rep(i , 0, x.r) res.m[i][i] = 1; // identity
  while( e ){
     if( e % 2)
       res = res*x;
    x = x*x;
    e /= 2;
  }
  return res;
}

int main(){
  /* ios::sync_with_stdio( false ); */
  /* cin.tie( nullptr ); */
#ifdef LOCAL
  freopen("in", "r" , stdin);
#endif

  ll n,k;
  while( cin >> k>> n){
    if( k ==0 && n == 0) break;
    matrix ma(k,k);
    rep( i, 0, k) ma.m[0][i] = 1;
    rep( i, 1, k) ma.m[i][i-1] = 1;
    ma = fastPow( ma, n);
    cout << ma.m[0][0] <<endl;
    /* ma.show(); */
  }
  return 0;
}
```

7.3 HowMany986

```
#include<bits/stdc++.h>
#define debug( x) cout <<#x << " = "<< x <<endl;
using namespace std;
int H, n, k ;
const int MAXN = 100;
int dp[50][50][50][2];
int ways( int x, int y , int r , bool isup){
  if( y < 0 || y > n) return 0;
  if( x == 2*n  ) {
    return (r == 0) && (y ==0);
  }
  int &ans = dp[x][y][r][isup];
  if( ans != -1) return ans;
  ans = 0;

  bool cond = (isup && y == k );
  // up
  ans = ways( x+1, y+1,r, true);
  // down
  ans += ways( x+1, y-1,r - cond,  false);
  return ans;
}

int main(){
#ifdef LOCAL
  freopen("in","r",stdin);
#endif
  int r;

  while( cin >> n >> r >> k){
    /* debug( n ); debug( k ); debug( r ); */
    memset( dp, -1, sizeof( dp ));
    int w = ways( 0, 0, r,  false);
    cout << w << endl;
  }
  return 0;
}
```

7.4 JAPAN2926

```
#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x <<endl;
#define F first
#define S second
using namespace std;
typedef long long ll;
typedef pair< int, int> ii;
const int MAXN = 2000+10;
ll Tree[ MAXN*2 ] ;


ll sum( ll l, ll r , ll n){
```

```
  l+= n; r+=n;
  ll s = 0;
  for( ; l < r; l >>= 1, r>>= 1){
    if( l & 1 ) s+= Tree[l++];
    if( r & 1 ) s+= Tree[--r];
  }
  return s;
}

void update( ll idx, ll n){
  idx += n;
  Tree[idx]++;
  for( ;idx > 1; idx>>=1){
    Tree[ idx >> 1] = Tree[ idx ] + Tree[ idx ^ 1];
  }
  /* for( int i = 0; i< n; i++)cout << Tree[i+n] << " ";cout <<
      endl; */
}

int main(){
#ifdef LOCAL
  freopen("in","r",stdin);
#endif
  ll t;
  cin >>t;
  ll n, m, k;
  for( int i =1; i <= t; i++){
    cout << "Test case "<< i <<": ";
    cin >> n >> m >> k;
    vector< ii > vi(k);
    for( int j= 0; j < k; j++){
      cin >> vi[j].F >> vi[j].S;
      vi[j].F--; vi[j].S--;
    }
    sort( vi.begin(), vi.end());
    memset( Tree, 0, sizeof(Tree));
    ll ans =0, s1;
    for( int j = 0; j < k; j++){
      s1 = sum( vi[j].S+1, m+1, m); // how many are there after
          him (**.S, m]
      /* cout << vi[j].S << " " << m << "  sum = " << s1 <<endl;
          */
      ans += s1;
      update( vi[j].S, m); // add 1 in that location
    }
    cout <<ans <<endl;
  }
  return 0;
}
```

7.5 NeedForSpeed

```
#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x << endl;
using namespace std;
typedef long double ld;
const int MAXN = 1005;
int d[ MAXN ];
int v[ MAXN ];
int n;
ld t;


inline ld check(ld mid){
  ld sum = 0;
  for( int i = 0; i< n; i++){
    ld aux = mid+ v[i];
    if( aux < 0) return 1.;
    ld ti = ld( d[i] ) / (aux );
    sum += ti;
  }
  return sum - t;
}

void find( ld mi ) {
  ld l = -mi, r = 0x3f3f3f3f, mid;
  for( int i = 0; i< 80; i++){
    mid = ( l+ r) /2.0 ;
    ld ck =  check( mid);
    if( ck < 0 ){
      r = mid;
    }else{
      l = mid;
    }
  }
  cout<<setprecision( 18 ) << r << endl;
}


int main(){
#ifdef LOCAL
  freopen("in","r",stdin);
#endif
  while( cin >> n >> t){
    /* cout <<n << " = "; */
    ld mi = 1e18;
    for( int i =0; i < n ; i++){
      cin >> d[i] >> v[i];
      min((ld) d[i], mi);
    }
    find( mi );
  }
  return 0;
}
```

7.6 VideoSurveillance

```
#include<bits/stdc++.h>
#define  endl '\n'
#define debug(x) cout << #x << " = " << x <<endl;
#define F first
#define S second
using namespace std;
typedef pair<int, int > ii;
typedef long double ld;

/*
 * caso 1
 *  si el mayor x de los puntos que van subiendo verticalment {mix
     } es m s grande que el menor x de los
 *  puntos que van bajando verticalmente {max} entonces no es
     posible, ejemplos
 * caso 2
 *  si el mayor y de los puntos que van izq {miy} es m s grande
     que el menor y de los
 *  puntos que van a la der {may} entonces no es posible, ejemplos
 *
3 *       _
2 *  ____| |   los que van subiendo (0,0) ( 2,2 ) mix = 2   2 <= 1
     false
1 *  |  ___|   los que van bajando  (3,3) ( 1,1)  max = 1
                  false
0 *  |_|       los que van a la izq (1,0) ( 3,1)  miy = 1   1 <= 2
     true
```

```
 *   0 1 2 3   los que van a la der (0,2) ( 2,3)  may = 2
3 *       _
2 *    /    |   los que van subiendo (0,0)  mix = 0
1 *   |  ___|   los que van bajando  (3,3) ( 1,1)  max = 1    0 <=
    1 true
0 *   |_|       los que van a la izq (1,0) ( 3,1)  miy = 1
 *   0 1 2 3   los que van a la der (0,2) ( 2,3)  may = 2    1 <=
    2 true

 */

int const inf = INT_MAX;

bool isPossible( vector<ii > &pt ){
  int s = pt.size();
  int mix = -inf, miy = -inf;
  int maxx = inf, may = inf;
  for( int i= 0; i< s ; i++){
    int j = (i+1) % s;
    if( pt[i].F == pt[j].F){
      // going up?
      if( pt[i].S < pt[j].S) mix = max( mix, pt[i].F);
      else maxx = min( maxx, pt[i].F);
    }else{
      // going right?
      if( pt[i].F < pt[j].F) may = min(may, pt[i].S);
      else  miy = max( miy, pt[i].S);
    }
  }
  return mix <= maxx && miy <= may;
}


int main(){
#ifdef LOCAL
  freopen("in", "r", stdin);
#endif
  int n, floor = 1;
  while( cin >> n && n ){
    vector< ii >  pt(n);
    for( int i = 0; i < n; i++){
      cin >> pt[i].F >> pt[i].S;
    }
    bool ans = isPossible( pt );
    cout << "Floor #"<< floor++ <<endl;
    if( ans ){
      cout<< "Surveillance is possible.\n";
    }else{
      cout<< "Surveillance is impossible.\n";
    }
    cout << '\n';

  }
  return 0;
}
```

7.7 Yahztee

```
#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;

int m[13][5];

int d[13][13];

/*
  d[0][j] value of the first dice thrown with j category
  the categories are given in the problem
  1st category : sum of all ones
  ...

 */
int dp[1<<13];

int nRepeated(int r, int t){
  int cnt[7];
  for( int i= 0; i<=7; i++ ) cnt[i] = 0;
  for( int i =0; i<5;i++) cnt[ m[r][i]]++;
  for( int i =1; i<=7;i++){
    cout << r << " " << i <<  " "<< cnt[i ] <<endl;
    if( cnt[ i] >= t)return true;
  }
  return false;
}
bool fullHouse( int r){
  set <int> s;
  for( int i =0; i < 5; i++) s.insert( m[r][i]);
  return s.size() == 2;
}
bool longStraigth( int r){
  for( int i =0; i< 5;i++){
    if( m[r][i] != (i+1))break;
    if( i== 4) return true;
  }
  for( int i =0; i< 5;i++){
    if( m[r][i] != (i+2))break;
    if( i== 4) return true;
  }
  return false;
}
bool shortStraigth( int r){
  for( int i =0; i< 3;i++){
    if( m[r][i]+1 != m[r][i+1])break;
    if( i == 2) return true;
  }
  for( int i =1; i<= 3;i++){
    if( m[r][i]+1 != m[r][i+1]) break;
    if( i == 3) return true;
  }
  return false;
}
int sum( int r, int j){
  int s =0;
  for( int i =0; i< 5; i++) if( m[r][i] == j) s+=j;
  return s;
}
int sumall( int r){
  int s =0;
  for( int i =0; i< 5; i++)  s+=m[r][i];
  return s;
}

/*
 * mask --> check with cols have already been choosen
 * r --> current rows, stands out the number of the dice thrown
 * sum --> sum of the path
 */
int find(int k,  int cat){
  if( k < 0 ) return 0;
  int &prev = dp[cat];
  if( prev != -1) return prev;

  int ans = 0;
  for( int i = 0; i < 13; i++){
```

```
    if(cat&(1<<i)){
      int sum = d[ i ][ k];
      if( ans <  sum + find(k-1, cat - (1 << i))){
        ans =  sum + find(k-1, cat - (1 << i));
      }
    }
  }
  if( k== 5 && ans >= 63 ) ans += 35;
  return dp[cat] = ans;
}

int main(){
#ifdef LOCAL
  freopen("in","r",stdin);
#endif
  while( cin >> m[0][0]){
    memset( dp, -1, sizeof(dp));
    memset( d, 0, sizeof(d));
    for( int i= 1; i <= 4; i++) cin >> m[0][i];

    for( int r =1; r<= 12;r++)
      for( int c =0; c <5;c++)
        cin >> m[r][c];

    // create matrix with value
    for( int i =0; i < 13; i++){
      // 1 to 6 sums
      for( int j= 0; j <= 5; j++) d[i][j] = sum(i, j+1);

      // sum all values
      d[i][6] = sumall(i);

      // repeated 3, 4, 5
      for( int j =3, k=0; j<=5; j++,k++)
        if( nRepeated( i, j))
          d[i][7+k] = j < 5? sumall(i): 50;

      //straight (short, long) and full house
      if( shortStraigth( i )) d[i][10] = 25;
      if( longStraigth( i)) d[i][11] = 35;
      if( fullHouse( i )) d[i][12] = 40;
    }

    // display matrix for testing purposes
    for( int i =0; i< 13; i++){
      for( int j =0; j < 13;j++)
        cout<< d[i][j] << " ";
      cout << endl;
    }
    cout <<endl;

    cout << find(12, (1<<13)-1) <<endl;

    // print dp
    for( int i= 0; i < 13; i++){
      for( int j = 0; j < ( 1<<13 )-1 ; j++){
        /* cout << dp[i][j] << " "; */
      }
      /* cout <<endl; */
    }
  }

  return 0;
}
```

8 strings

8.1 Kmp

```
#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x << endl
#define rep(i, a, b) for( __typeof(a) i = a; i < b ; i++)

using namespace std;

int* compute(const string &t) {
  int m = t.size();
  int *p = new int[m];
  p[0]= 0;
  rep( i , 1 , m){
    p[i] = p[ i - 1 ];
    while( p[i] > 0 && t[i] != t[ p[i] ] ){
      p[i] = p[ p[i] -1 ];
    }
    if( t[i] == t[ p[i] ] ) p[i]++;
  }
 return p;
}


int match( const string &ne, const string &ha ){
  debug( ne ); debug( ha);
  int m = ne.size(),  n = ha.size();
  int *p = compute( ne  );
  int s = 0;
  rep( i, 0, n){
    while( s > 0 && ha[ i ] != ne[  s ] )
      s = p[ s - 1];
    if( ha[i] == ne[s] ) s++;
    if( s == m) return i - m + 1;
  }
  delete[] p;
  return -1;
}

int main(){
#ifdef LOCAL
  freopen("in", "r" , stdin);
#endif

  string needle = "abcaby";
  string haystack  = "abcabcabyid";

  cout << match (  needle , haystack ) <<endl;


  return 0;
}
```

8.2 LCS

```
#include<bits/stdc++.h>
#define debug(x) cout <<#x << " = " << x <<endl;
using namespace std;
string a, b;
const int MAXN = 5000;
int dp[MAXN][MAXN];
int cnt = 0;

int lcs( int u, int v){
```

```
  cnt++;
  if( u == 0 || v == 0 ) return 0;
  int &res = dp[u-1][v-1];
  if( res != -1) return res;
  res = 0;
  if( a[u-1] == b[ v-1] ){
    res =  1+ lcs( u-1, v-1);
  }else{
    res = max( lcs(u, v-1), lcs(u-1, v));
  }
  return res;
}

int main(){
  a= "AGGTAB", b="GXTXAYB";
  memset( dp, -1, sizeof(dp));

  int res = lcs(a.size(), b.size());
  debug( res );
  debug(cnt);
  return 0;
}
```

8.3 LIS

```
#include<bits/stdc++.h>
using namespace std;
/*
 * Complexity Nlog(N)
 */
vector< int >  getLis( const vector < int > A){
  int n = A.size();
  if( n == 0) return {};
  vector < int > tail ( n, 0);
  vector < int > lis ( n, 1);
  int ans = 1;
  tail[0] = A[0];
  for( int i = 1; i < n ; i++){
    if( A[i] < tail[0] ) {
      tail[0] = A[i];
      lis[i] = 1;
    }else if( A[i] > tail[ ans - 1] ) {
      tail[ ans++ ] = A[i];
      lis[ i ] = ans;
    }else{
      int cp = upper_bound( tail.begin(),
                            tail.begin()+ans, A[i]) - tail.begin()
                                ;
      tail[ cp ] = A[i];
      lis[ i] = cp+1;
    }
  }
  return lis;
}

int main(){
  vector < int > A = { 1, 3, 32 ,2 ,78, 9,2};
  getLis( A );
  // 1 2 3  2 4  3 3
  return 0;
}
```

8.4 LRSubs

```
#include<bits/stdc++.h>
using namespace std;

// Returns the longest repeating non-overlapping substring
string longestRepeatedSubstring(string str){
    int n = str.length();
    int LCSRe[n+1][n+1];
    // Setting all to 0
    memset(LCSRe, 0, sizeof(LCSRe));
    string res; // To store result
    int res_length  = 0; // To store length of result

    // building table in bottom-up manner
    int i, index = 0;
    for (i=1; i<=n; i++){
      for (int j=i+1; j<=n; j++){
        // (j-i) > LCSRe[i-1][j-1] to remove
        if (str[i-1] == str[j-1] &&
          LCSRe[i-1][j-1] < (j - i)){
          LCSRe[i][j] = LCSRe[i-1][j-1] + 1;
          if (LCSRe[i][j] > res_length){
            res_length = LCSRe[i][j];
            index = max(i, index);
          }
        }
        else
          LCSRe[i][j] = 0;
      }
    }
    if (res_length > 0){
                cout <<  (index  - res_length +1)<<endl;
          for (i = index - res_length + 1; i <= index; i++)
          res.push_back(str[i-1]);
                }
    return res;
}

// Driver program to test the above function
int main(){
    string str = "hello,p23puoeouhello,oues";
    cout << longestRepeatedSubstring(str); //hello,
    return 0;
}
```

8.5 StringUtil

```
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef vector <string> vs;
int toNum(string a){
        stringstream toNum(a);
        int num;
        toNum >> num;
        return num;
}
string toString(double d){
  stringstream ss;
  ss << fixed << setprecision(10) << d;
  string num = ss.str();
  return num;
}
void tolowers(string &data){
 transform(data.begin(), data.end(), data.begin(), ::tolower);
}
void replace(string &a,  string &from, string &to){
```

```
        int pos=0;
        while((pos = a.find(from,pos)) != string::npos){
                a.replace(pos, to.size(), to);
                pos+=to.size();
        }
}
vs split(string line, char d){
        vector < string > elements;
        stringstream ss(line);
        string item;
        while(getline(ss, item, d))     elements.pb(item);
        return elements;
}

int main(){
  vs d1 = split("1990/10/5", '/');
  for (string s: d1){
    cout << toNum(s) << endl;
  }

  char a = 'a';
  cout << (isalnum(a)?"true":"false")  << endl;
  cout <<( isalpha(a)?"true":"false") << endl;
  cout << (isblank(a)?"true":"false")  << endl;
  cout << (isdigit(a)?"true":"false")  << endl;
  cout << (islower(a)?"true":"false")  << endl;
  cout << (ispunct(a)?"true":"false")  << endl;
  cout << (isupper(a)?"true":"false")  << endl;
  cout << (isxdigit(a) ?"true":"false") << endl;
  cout << (char)tolower(a) << endl;
  cout << (char)toupper(a) << endl;
  string hay ="hellohowareyouhow",  ned ="whatare", from= "how";
  replace(hay, from, ned);
  cout << hay <<endl;
  return 0;
}
```

8.6 SubstrK

```
#include<bits/stdc++.h>
#define debug(x) cout << #x << " = "<< x << endl
#define pb push_back
/*
        Algorithm to find all possible
  substrings of size k given a set of values
*/
using namespace std;
set<string> subs;
//print all possible substrings of size k
void substringSizek(char set[], string prefix, int n, int k){
  //Base case
  if( 0 == k){
    cout << prefix <<endl;
    subs.insert(prefix);
    return;
        }
  for( int i=0;  i < n ; ++i){
         string newprefix = prefix + set[i];
         //k is decreased because we add a new caracter
         substringSizek(set, newprefix, n, k-1);
        }
}
void init(char set[], int k){
  int n = strlen(set);
        substringSizek(set, "", n, k);
}
int main(){
  char set[3] ={'a', 'b'};
  int k = 3;
  init(set, k);
}
```

8.7 Zalgorithm

```
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef vector<int> vi;

/*
 *  Complexity: O(N + M)
*/
vi z_val(string s){
  int n = s.size(), L =0, R=0;
  vi z(n);
  for( int i = 1; i < n ; i++){
    if( i > R){ // not prefix-substr
      L = R = i;
      while( R < n && s[R-L] == s[R]) R++;
      z[i] = R - L; R--;
    }else {
      int k = i - L;
      //there is no longer prefix start at s[i]
      if( z[k] < R-i+1){
        z[i] = z[k];
      }else{
        L = i;
        while( R < n && s[R-L] == s[R]) R++;
        z[i] = R-L; R--;
      }
    }
  }
  return z;
}

int main() {
  string haystack = "abcabca", needle = "abc";
  int n = haystack.size(), m = needle.size();
  vi z = z_val(needle + "#" + haystack);
  for( int i = 0; i < z.size(); i ++)
    cout << i << " "<< z[i] <<endl;
  return 0;
}
```