## Forces breakdown

- hydrodynamucs solving for five variables over computational grid
- By setting grid points to 1, 1 dimensional thing to x
  - Finding value of five variables (but really three b/c velocity in y and z set to 0) at each grid point
- 3d moving in any direction
  - Theta = colatitude 0 to pi
  - Phi = longitude 0 to pi/2
- Five variables
  - Mass density (ex: g/cm<sup>3</sup>)
    - Some things incompressible
    - Air is different
      - Air goes down as you go up
      - Density of air different where it's hot vs where it's cold
      - Very large changes in densities associated with shocks
      - Hydrodynamic shock = sudden discontinuous change in fluid variables
        - Density
        - Velocity
        - Pressure
  - Vx, vy, vz
  - Energy density
    - Both kinetic and thermal dynamic energy of random motion
    - Enthalpy = specific thermodynamic energy that appears
    - Energy/volume
- Five equations
  - Three equations = conservation of momentum
    - Either momentum equation and Euler equations
    - In three dimensions
  - Two other
    - Conservation of mass
    - Conservation of energy
- Conservation of mass, momentum, and energy
- Momentum conservation
  - F = ma for a fluid
  - Ma part = multiple particles —> mass per volume of a fluid\*acceleration
  - F = all the forces
    - $d^2y/dt^2 = a$
    - Have to know forces in system

- Pressure forces
- High pressure on one side, low pressure on other side, flow from high to low
- Gradient of scalar quantity
  - Gradient of pressure(\*-1)
  - DP/dz = vertical component
  - ALWAYS SAY PRESSURE GRADIENT FORCE
- Winds don't point towards high to low because influence of Coriolis force
  - Balance of horizontal pressure forces against Coriolis
  - Geostrophic balance

## - Forces:

- Pressure forces
  - Weather driven by horizontal
  - Vertical pressure gradient pushing out
  - Stable equilibrium on earth
    - If gravity went away, then the atmosphere would explode
    - Shocktube = sudden change in pressure/imbalance —> moves to right/moving away from discontinuity
      - Higher density on left, lower on right
      - When everything same = no more forces
  - Force per volume
- Gravity forces per volume
  - Mass density G\*newtons constant/rad^2
- Conservation laws for mass and energy
  - Mass conservation
    - Mass doesn't appear or disappear
    - box: how to change total mass in the box?
      - Moving things in and out of a boundary
  - Energy conservation
    - Internal energy
    - Transformed into different forms but total is conserved
    - Three different type
      - Grav potential
      - Bulk motion of entire fluid
      - Internal fluid
        - Ind. move faster when hot and vice versa
    - Adiabatic motion
      - As fluid moving around
        - No heating and cooling = non adiabatic
        - Entropy is constant
        - Fluid with volume change and expand —> cools

- Impose heating and cooling by prescription of heating on day, cooling at night
  - Newtonian cooling = prescribe temperature that fluid should have (equilibrium temp)
  - Write func = less than eq, heating and vice versa
- Having simulations in three dimensions with spherical
  - Lower boundary with not much happening
  - Region of strong day nigh heating
  - Upper layer
  - Vertical gravity
  - Horizontal pressure gradients driving winds
  - Understand when you have winds, do they cause density variations that star can hold on to
- Switch from cartesian to spherical coordinates
  - Blast wave example?
    - 3d version of shock tube
    - Small r = huge overpressure in comparison to larger r
    - Cause shock —> fluid move outward
  - Try running case in spherical coordinates
  - See if you can get plots to work
  - Density, radial velocity, internal energy in r
- coordinates:
  - X1 = r
  - X2 = theta
  - -X3 = phi
  - X2 and x3 = 1 for this blast wave
- Run blast wave and read one of the time slots
  - Then plot density vs radius