

COMPUTATION OF PERMEABILITY BY FALLING-HEAD PERMEAMETER

We will test in a specimen of soil is placed in a falling-head permeameter apparatus.

Sample:

Given:

$$A_{\text{cross-sectional area of specimen}} = 66\text{cm}^2.$$

$$\text{Height} = 8\text{cm}.$$

$$\text{time} = 1\text{hr. and } 18\text{mins}.$$

$$A_{\text{cross-sectional area of standpipe}} = 0.48\text{cm}^2$$

$$H_1 = 62 \text{ cm}.$$

$$H_2 = 40 \text{ cm}.$$

Determine the coefficient of permeability of the soil, in cms. per minute.

Calculation Procedure:

Step 1. By using literal values, equate the instantaneous discharge in the specimen to that in the standpipe The velocity at which water flows through a soil is a function of the coefficient of permeability, or hydraulic conductivity, of the soil.

By Darcy's law of laminar flow:

$$V = K i$$

Where:

i = hydraulic gradient

K = coefficient of permeability

V = velocity.

In a falling-head permeameter, water is allowed to flow vertically from a standpipe through a soil specimen. Since the water is not replenished, the water level in the standpipe drops as flow continues, and the velocity is therefore variable.

Let:

A = cross-sectional area of soil specimen

a = cross-sectional area of standpipe

L = height of soil specimen

h = head on specimen at given instant.

Q = discharge

H1 and **H2** = head at beginning and end.

t = time interval

Using literal values:

$$Q = A k i$$

Step 2. Evaluate k Since the head h is dissipated in flow through the soil.

$$i = \frac{h}{L}.$$

By substituting and rearranging:

$$\begin{aligned} Q &= K \frac{h}{L} A \\ &= -a \frac{dh}{dt} \end{aligned}$$

By integrating this equation at left side with limits from 0 to t and the right side with limits of head difference from h_1 to h_2 :

$$dt = \frac{aL}{Ak} \left(-\frac{dh}{h} \right)$$

where:

ln = denotes the natural logarithm.

Then:

$$k = \frac{aL}{At} \ln \left(\frac{h_1}{h_2} \right)$$

Substituting gives:

$$\begin{aligned} k &= \frac{0.48\text{cm}^2 \times 8\text{cm.}}{66\text{cm}^2 \times 78\text{mins.}} \ln \left(\frac{62\text{cm.}}{40\text{cm.}} \right) \\ &= 0.000326 \text{ cm/in.} \end{aligned}$$