

CS100

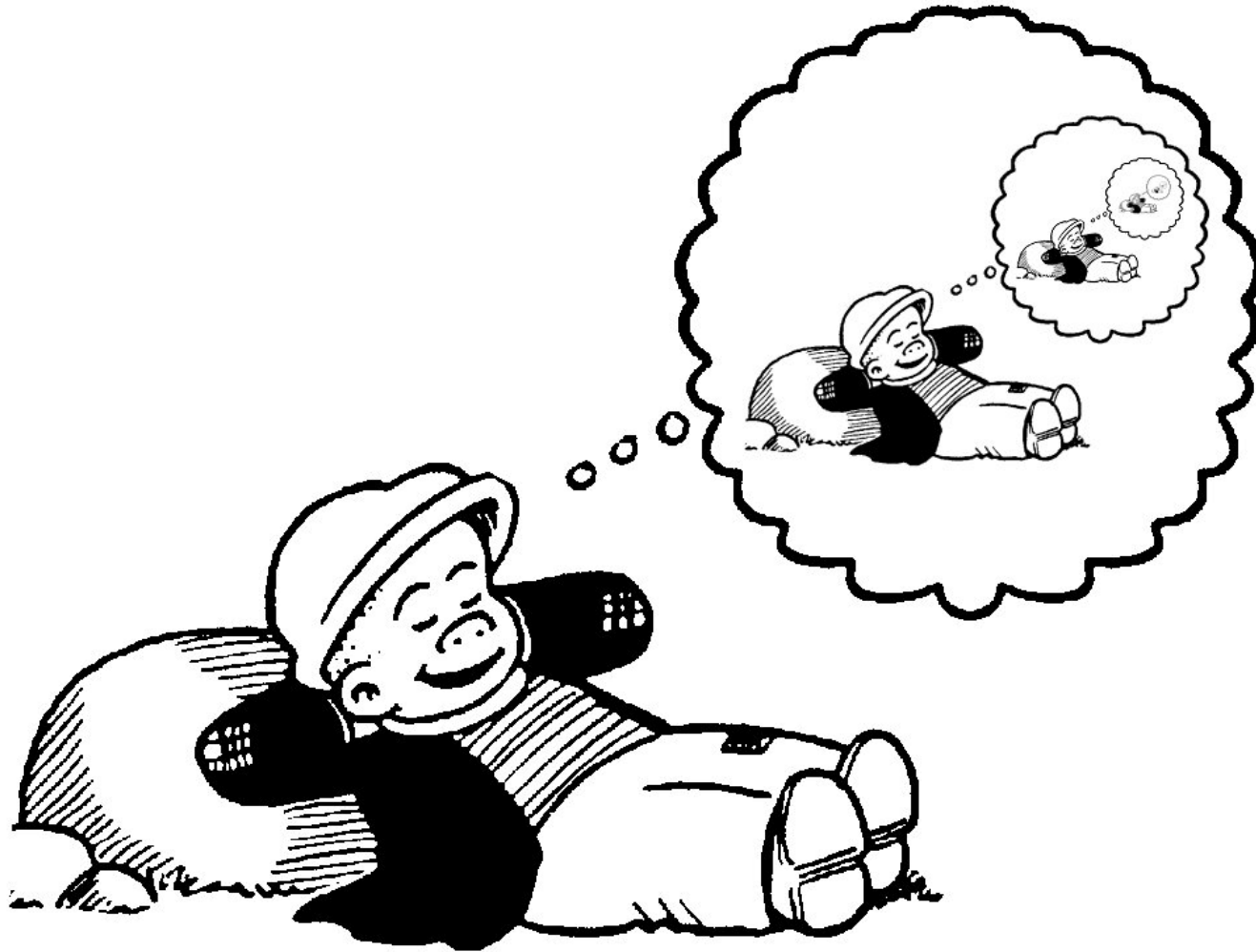
Introduction to Programming

Lecture 7. Recursion

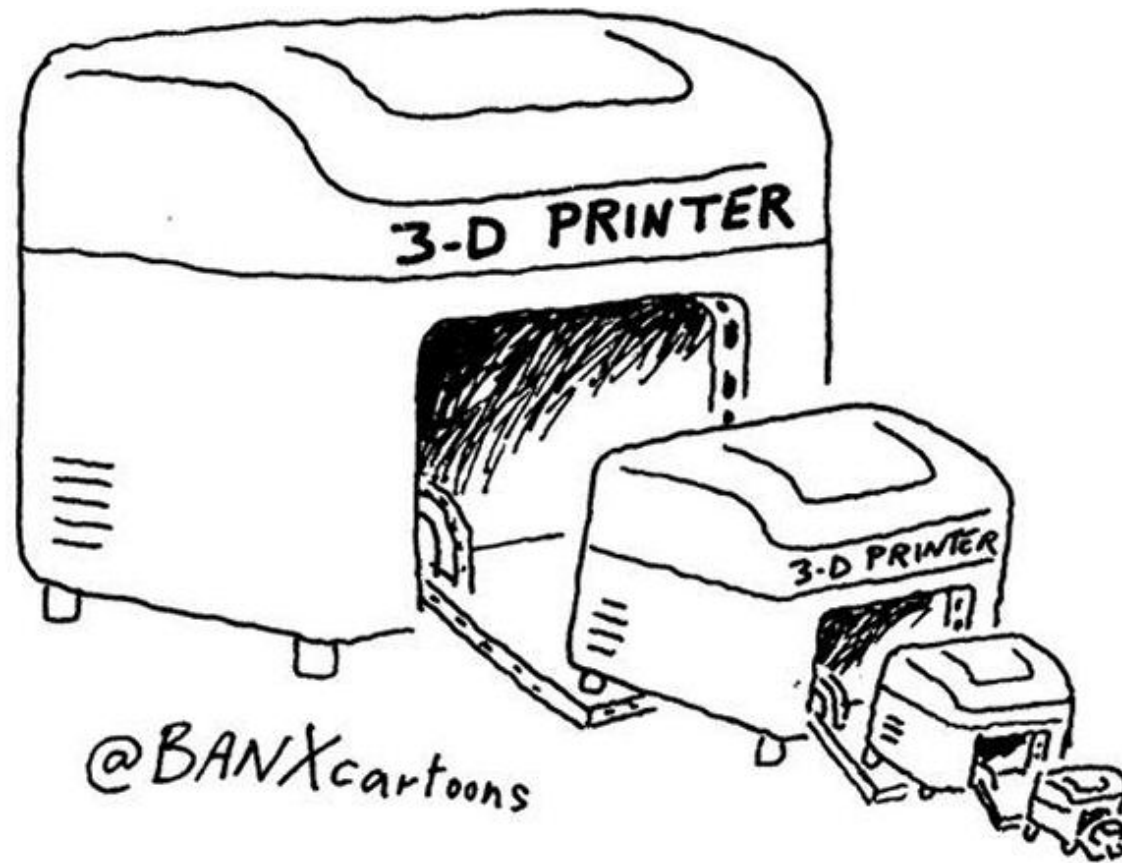
What Is Recursion?

- The method in which a problem is solved by reducing it to smaller cases of the same problem.
- Recursion is the name for the case when
 - a function calls itself, or
 - calls a sequence of other functions, one of which eventually calls the first function again.
- Two parts
 - **Base case** (with terminating condition)
 - **Recursive case** (with recursive condition)

Recursion in Art and Life



Recursion in Art and Life



Recursion in Art and Life



FROM THE MIRROR.

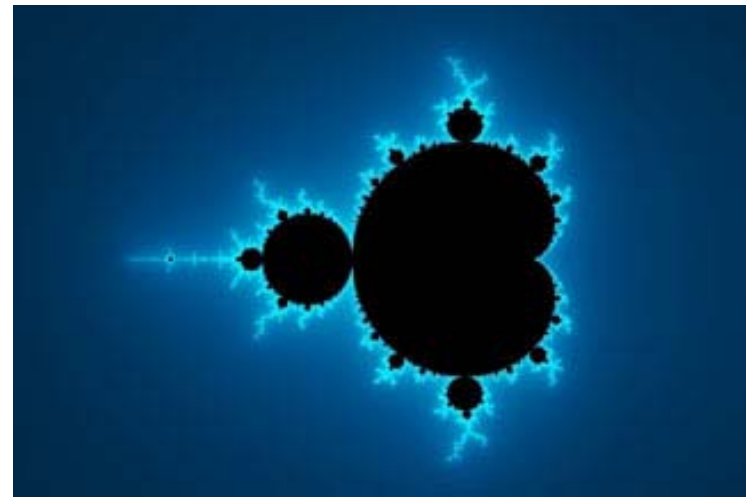
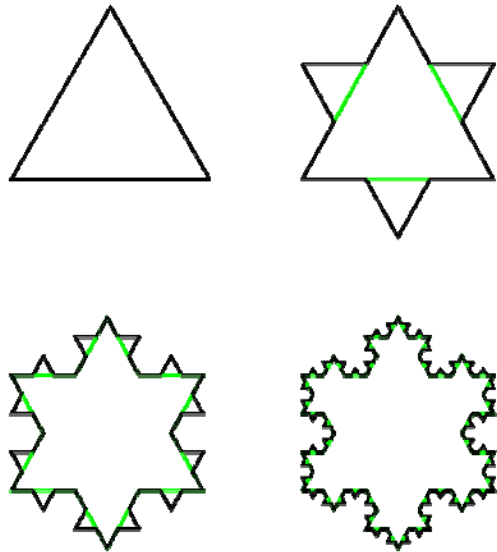
*Life Mirror Recursive (1909),
by Coles Phillips (1880 – 1927)*

Recursion in Art and Life



Recursion is similar to fractals

- **Fractals tend to appear nearly the same at different levels**
 - Can be defined recursively



Example 1: Cheers

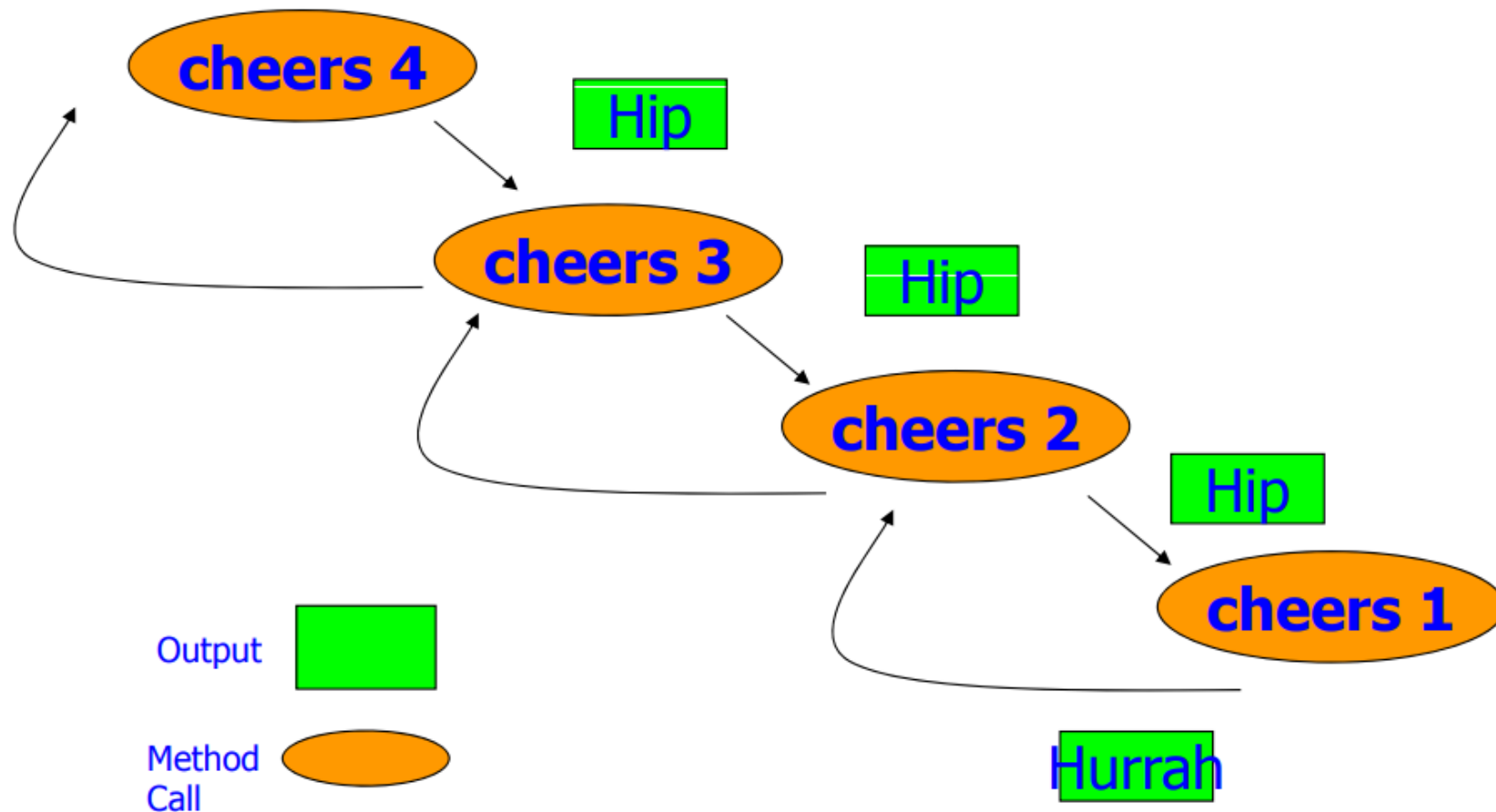
What does the following **recursive** method print when called with cheers(4)?

```
void cheers(int n)
{
    if (n <= 1)
        printf("Hurrah \n");
    else {
        printf("Hip \n");
        cheers(n-1);
    }
}
```

Output:

```
Hip
Hip
Hip
Hurrah
```


Recursive Cheers – Tracing



Recursive Cheers

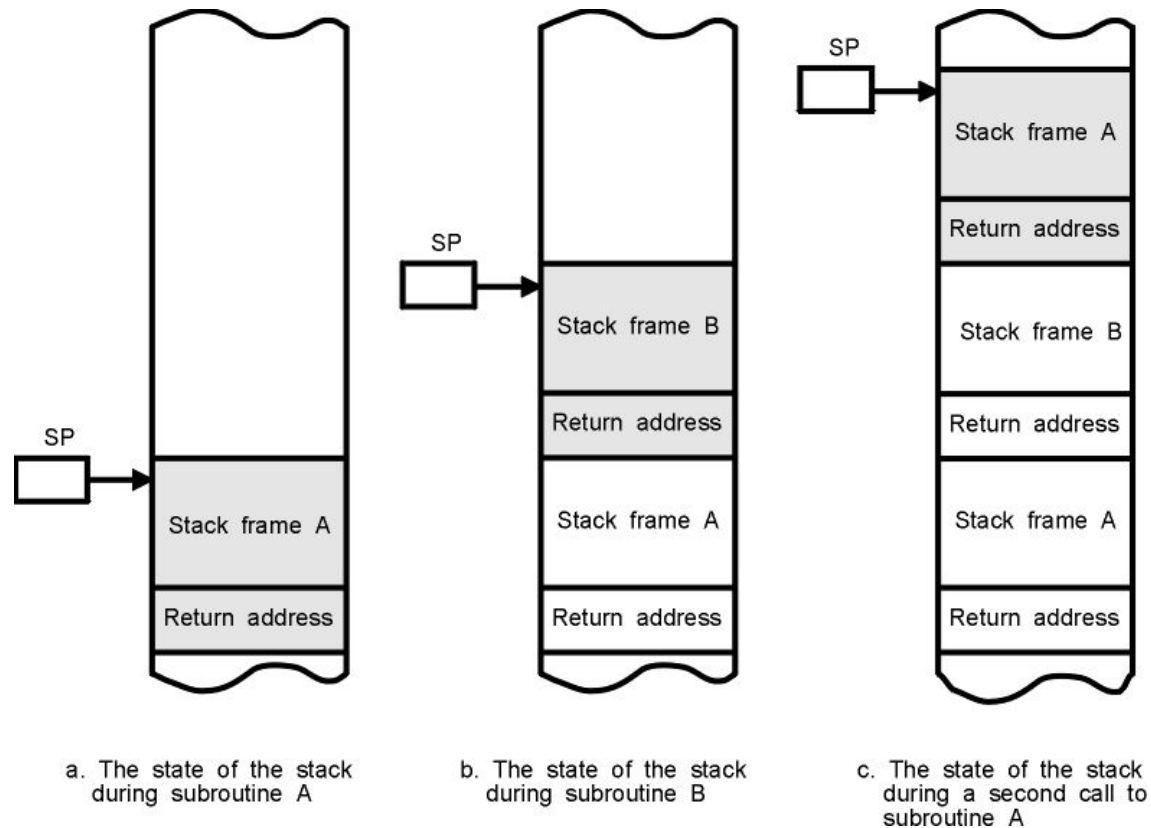
```
void cheers(int n)
{
    if (n <= 1)
        printf("Hurrah \n");
    else {
        printf("Hip \n");
        cheers(n-1);
    }
}
```

terminating condition

recursive condition
(n > 1)

How Recursive Function is Called?

- Recall function stack



Example 2: PrintSomething

What does the following **recursive** method print when called with `printSomething(3)`?

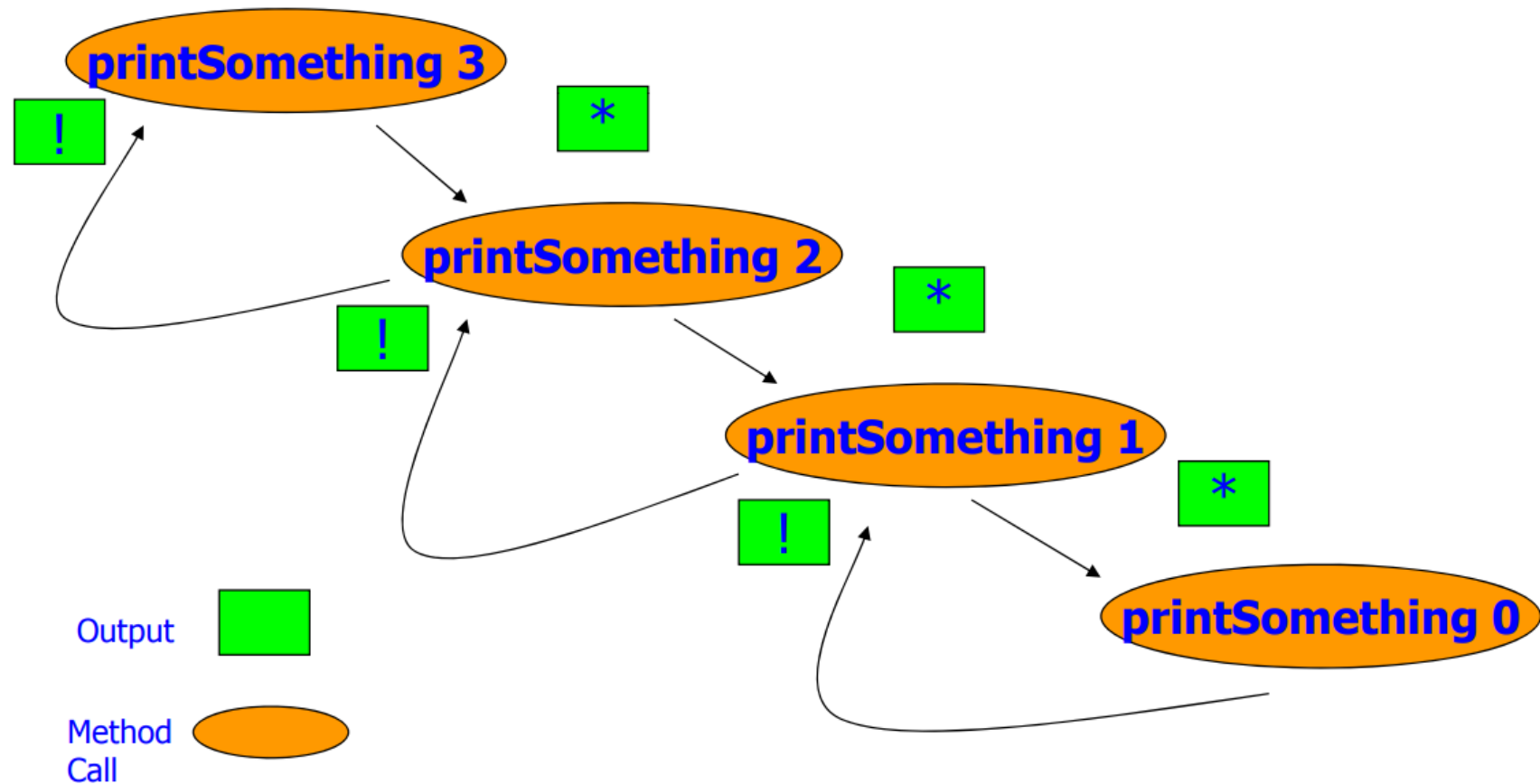
```
void printSomething(int n)
{
    if (n > 0) {
        printf("*");
        printSomething(n-1);
        printf("!");
    }
}
```

What condition is this?
Continue looping condition

Output:
***!!!

Where is the other condition?

Recursive PrintSomething – Tracing



Example 3: Factorials

- **Problem:** Find the factorial of a non-negative integer number.

- The factorial function of a positive integer is usually defined by the formula

$$n! = n \times (n - 1) \times \dots \times 1$$

- A more precise definition (*recursive definition*)

$$n! = 1 \quad \text{if } n = 0$$

$$n! = n \times (n - 1)! \text{ if } n > 0$$

Non-recursive Factorials

The following program will do the job, using a **for** loop:

```
#include <stdio.h>
int factorial(int n);
int main(void)
{
    int num;
    printf("Enter an integer:");
    scanf("%d", &num);
    printf("n! = %d\n",
        factorial(num));
    return 0;
}
```

```
int factorial(int n)
{
    int i;
    int temp = 1;
    for (i=n; i > 0; i--)
        temp *= i;
    return temp;
}
```

Output:

Enter an integer: 4
n! = 24

Recursive Factorials

- Suppose we wish to calculate $4!$

As $4 > 0$, $4! = 4 \times 3!$

- But we do not know what is $3!$

As $3 > 0$, $3! = 3 \times 2!$

As $2 > 0$, $2! = 2 \times 1!$

As $1 > 0$, $1! = 1 \times 0!$

- What is $0!$ equal to?

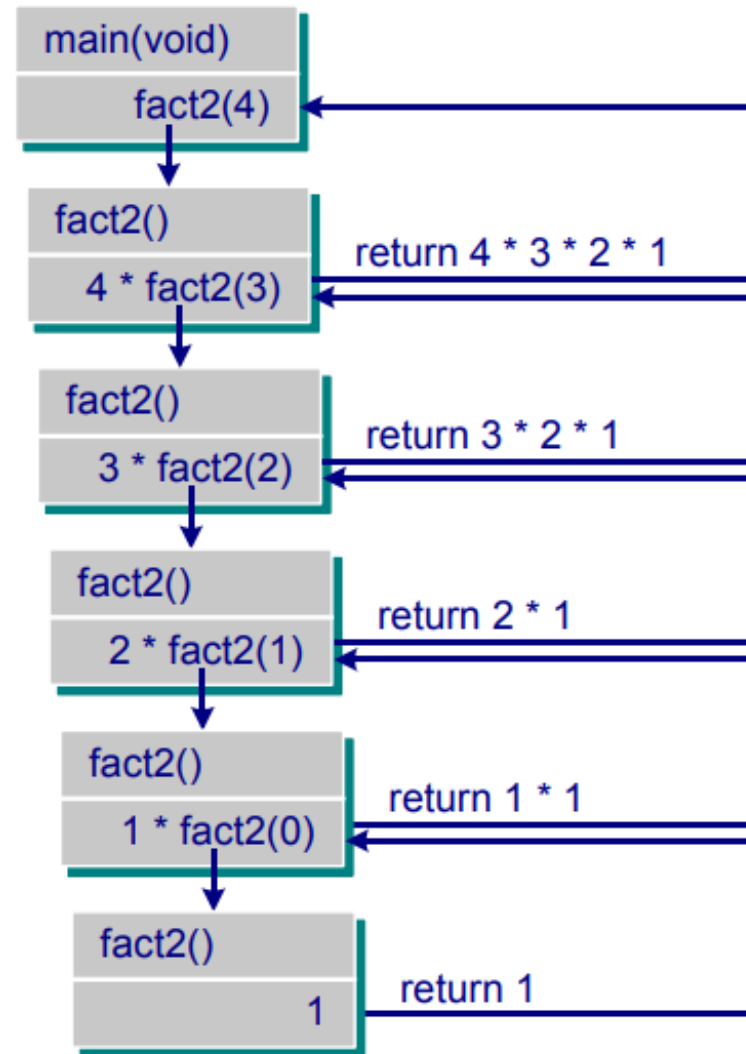
$$\begin{aligned}4! &= 4 \times 3! \\&= 4 \times (3 \times 2!) \\&= 4 \times (3 \times (2 \times 1!)) \\&= 4 \times (3 \times (2 \times (1 \times 0!))) \\&= 4 \times (3 \times (2 \times (1 \times 1))) \\&= 4 \times (3 \times (2 \times 1)) \\&= 4 \times (3 \times 2) \\&= 4 \times 6 \\&= 24\end{aligned}$$

Recursive Factorials

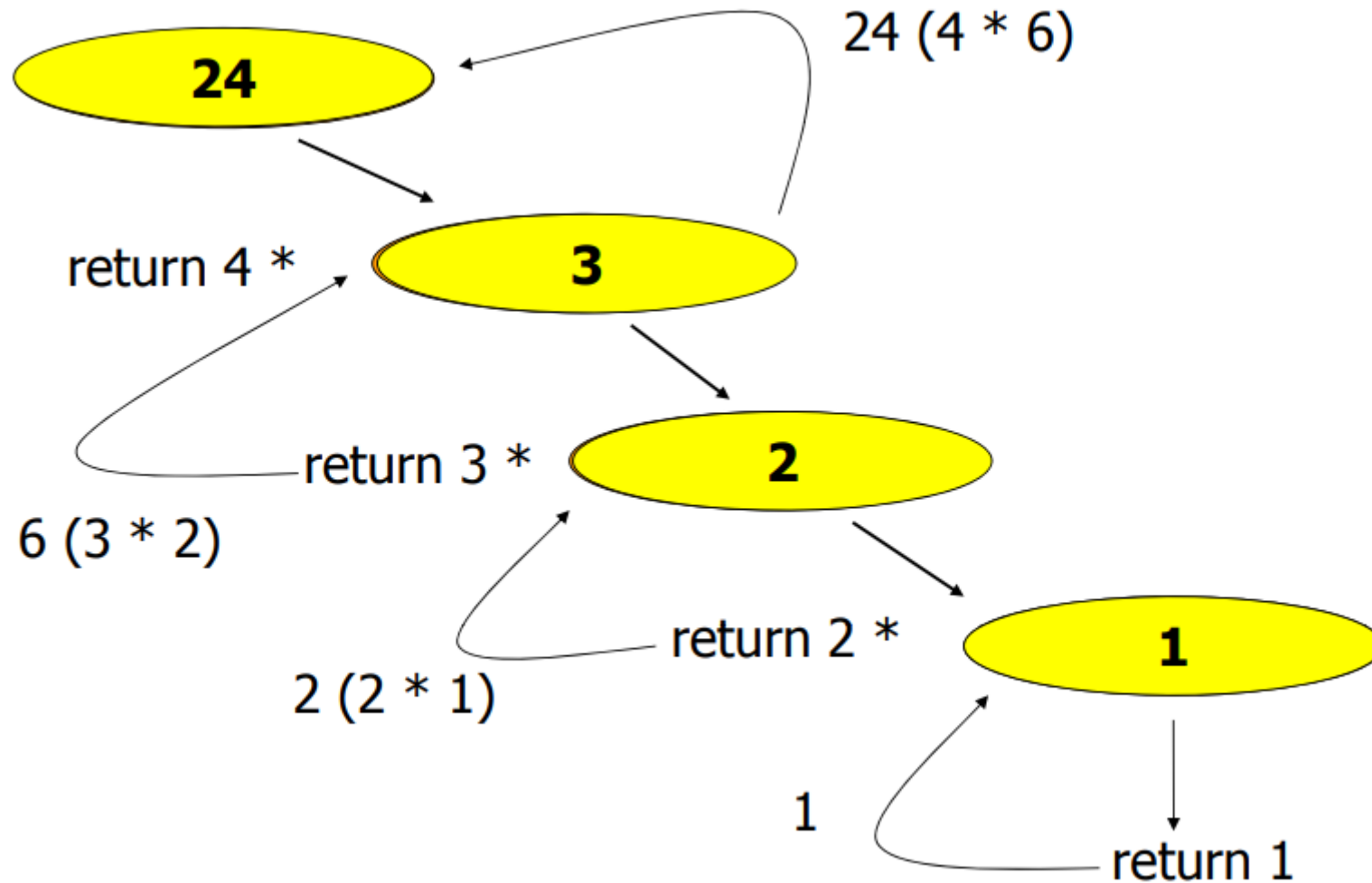
```
int factorial(int n)
{
    if (n == 0) {
        // teminating condition
        return 1;
    } else {
        // recursive condition
        return n*factorial(n-1);
    }
}
```

Output:

Enter an integer: 4
n! = 24



Recursive Factorials: Tracing



Example 4: Multiplication by Addition

- The multiplication operation

$$\text{multi}(\textcolor{red}{m}, \textcolor{red}{n}) = m \times n$$

can be defined recursively as

$$\text{multi}(\textcolor{red}{m}, \textcolor{red}{n}) = \textcolor{red}{m} \quad \text{if } \textcolor{red}{n} = 1$$

$$\text{multi}(\textcolor{blue}{m}, \textcolor{blue}{n}) = \textcolor{blue}{m} + \text{multi}(\textcolor{blue}{m}, \textcolor{blue}{n}-1) \quad \text{if } \textcolor{blue}{n} > 1$$

Using Call by Value

```
/* multiplication by addition, pass parameter using
call by value */
#include <stdio.h>
int multi1(int, int);
int main(void)
{
    printf("5 * 3 = %d\n", multi1(5, 3));
    return 0;
}
int multi1(int m, int n)
{
    if (n == 1)                // terminating condition
        return m;
    else                        // recursive condition
        return m + multi1(m, n-1);
}
```

Output:

5 * 3 = 15

Using Call by Pointer

```
/* multiplication by addition, pass parameter using call by
pointer */
#include <stdio.h>
void multi2(int, int, int*);
int main(void)
{
    int result;
    multi2(5, 3, &result);
    printf("5 * 3 = %d\n", result);
    return 0;
}
void multi2(int m, int n, int *product)
{
    if (n == 1)                // terminating condition
        *product = m;
    else {                     // recursive condition
        multi2(m, n-1, product);
        *product = *product + m;
    }
}
```

Output:

5 * 3 = 15

Recursive Call by Pointer

```
#include <stdio.h>
void fn(int x, int y, int *z);

int main(void){
    int n1=20, n2=15, n3=0;
    fn(n1, n2, &n3);
    printf("n1 = %d, n2 = %d, n3 = %d\n", n1, n2, n3);
    return 0;
}

void fn(int x, int y, int *z){
    if (x > y) {
        x = x - 2;
        y = y - 1;
        *z = x * y;
        fn(x, y, z);
    }
    printf("x = %d, y = %d, *z = %d\n", x, y, *z);
}
```

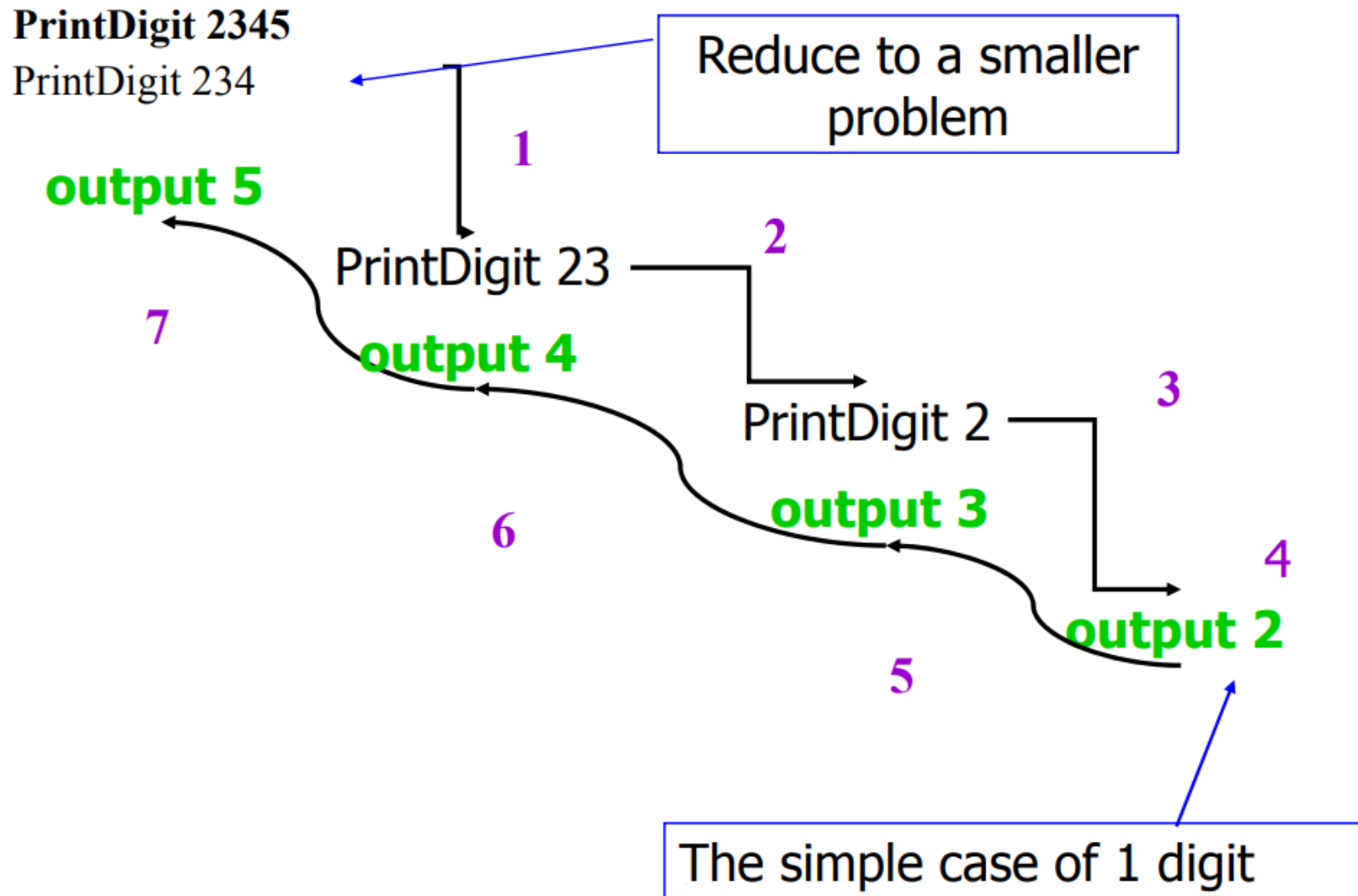
Output:

```
x = 10, y = 10, *z = 100
x = 12, y = 11, *z = 100
x = 14, y = 12, *z = 100
x = 16, y = 13, *z = 100
x = 18, y = 14, *z = 100
n1 = 20, n2 = 15, n3 = 100
```

Example 5: Printing Digits

- **Problem:** Given a number, say 2345, print each digit of the number, in the order from left to right, one per line.
- **Recursive Solution:**
 - Look for the simplest case (**terminating condition**). If the number is a single digit, just print that digit.
 - Look into reducing the problem into a smaller but same problem (**recursive condition**).

Printing Digits



Printing Digits: Recursive Solution

```
#include <stdio.h>
void printDigit(int);

int main(void) {
    int num;
    printf("Enter a number: ");
    scanf("%d", &num);
    printDigit(num);
    return 0;
}
```

```
void printDigit(int num) {
    if (num < 10)                // terminating condition
        printf("%d\n", num);
    else {                       // recursive condition
        printDigit(num/10);
        printf("%d\n", num%10);
    }
}
```

Output:

Enter a number: 2345

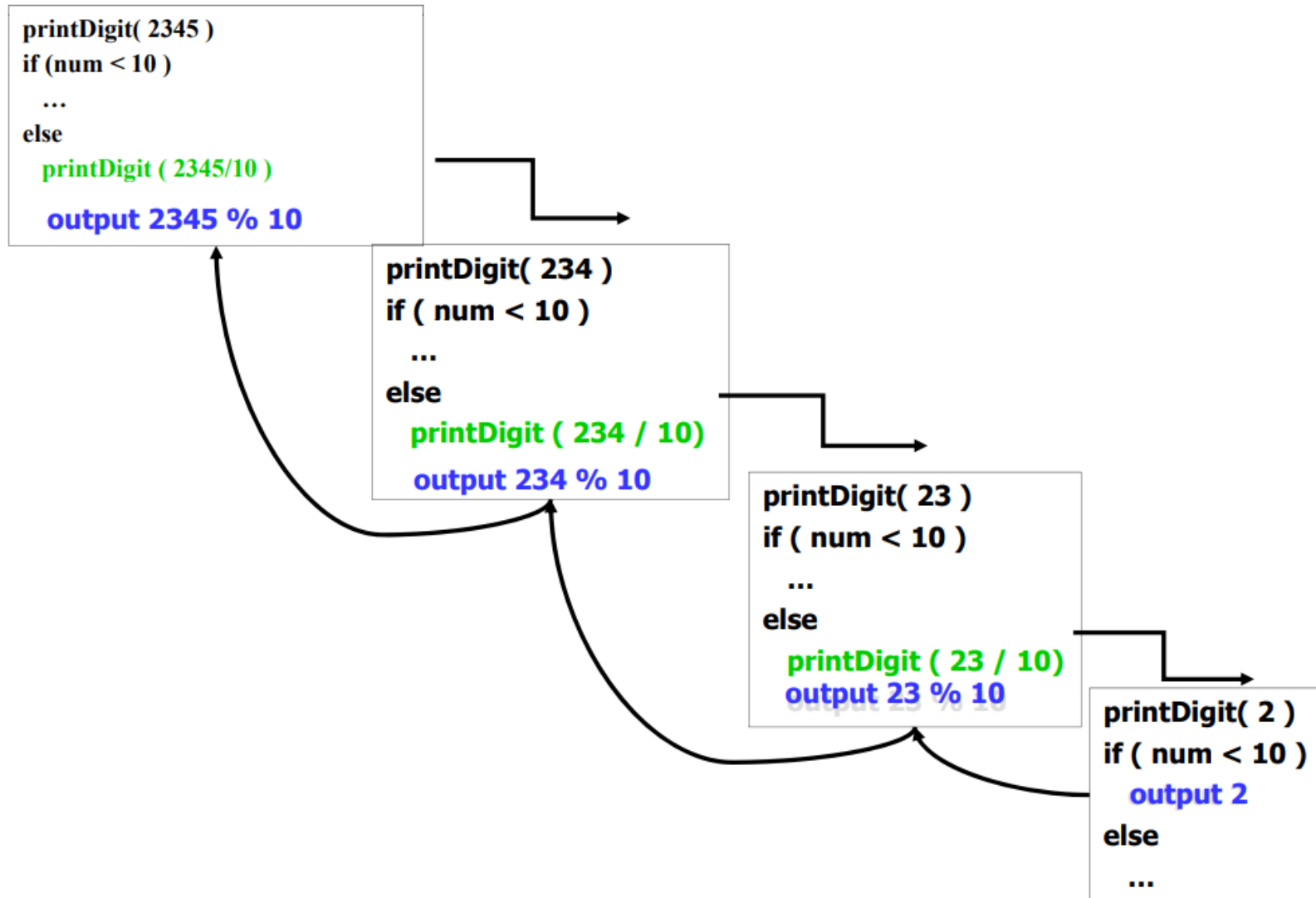
2

3

4

5

printDigit(2345);



Example 6: Summing Array of Integers

```
int sumArray(int a[], int size)
{
    int sum = 0;
    for (int i = 0; i < size; i++)
    {
        sum = sum + a[i];
    }
    return sum;
}

int recursiveSum(int a[], int size)
{
    if (size == 1)
        return a[0];
    else
        return a[size - 1] +
            recursiveSum(a, size - 1);
}
```

- Given an array of integers, write a method to calculate the sum of all the integers.

a	1	2	3	4
	[0]	[1]	[2]	[3]

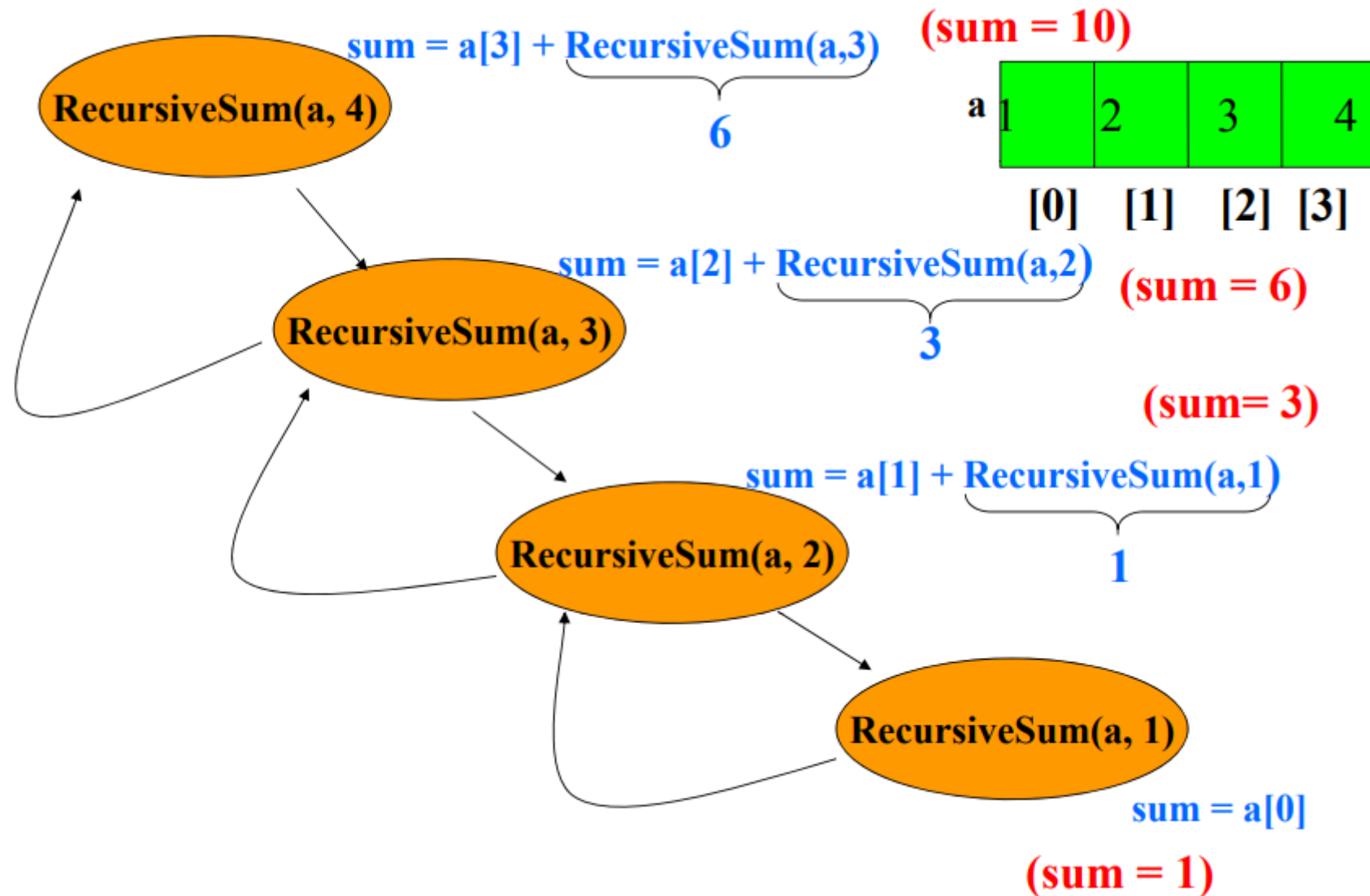
Input:

a[] = {1,2,3,4}

Output:

Sum = 10

Recursive Sum – Tracing



Recursion: Summary

- **To obtain the answer to a larger problem, a general method is used that**
 - reduces the large problem to one or more problems of a similar nature but a smaller size.
- **Recursion continues until the size of the problem is reduced to the smallest, i.e. base case**
 - where the solution is given directly without using further recursion.
- **As such, recursive methods consist of two parts:**
 - A smallest, **base case** that is processed without recursion (**terminating condition**).
 - A general method that reduces a particular case to one or more of the smaller cases (**recursive condition**).

Recursion: Summary

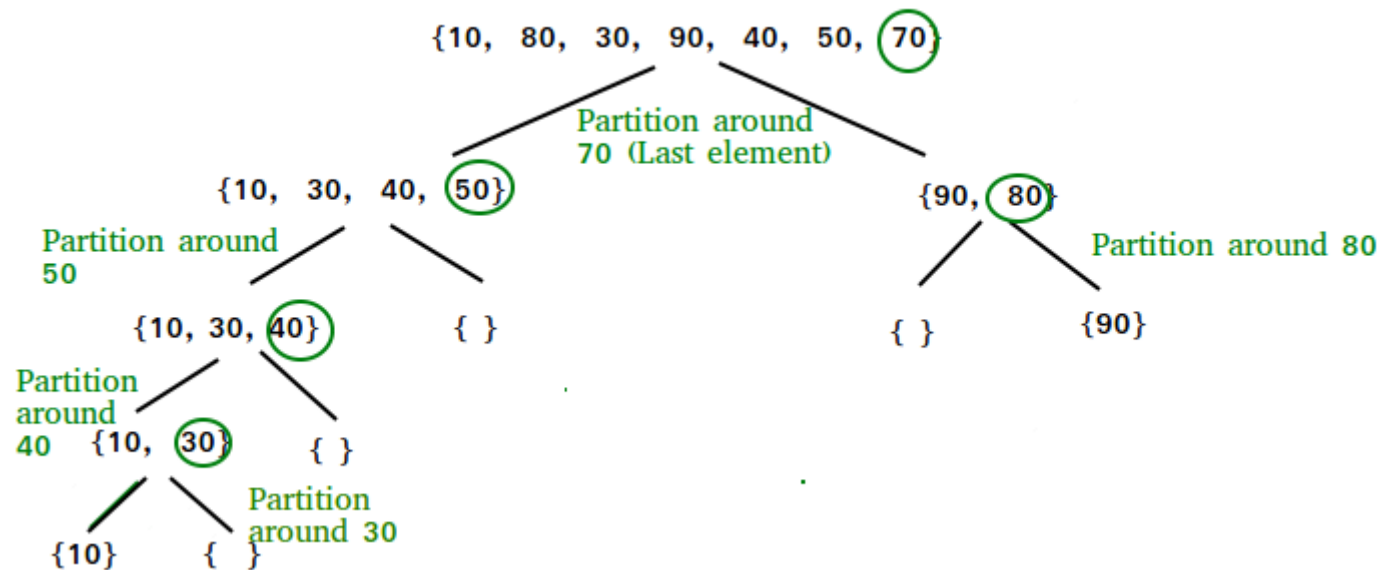
- Each function makes a **call to itself** with an argument which is closer to the terminating condition.
- Each call to a function has its **own set of values/arguments** for the formal arguments and local variables.
- When a recursive call is made, control is transferred from the calling point to the first statement of the recursive function. When a call at a certain level is finished, control returns to the calling point **one level up**.

Sorting a Sequence of Data

- **Quick sort**
 - a divide-and-conquer algorithm
 - pick an element as pivot; partition the data sequence into two sequences around the pivot
 - The left sequence contains element smaller than pivot
 - The right sequence contains element larger than pivot
 - This partition is recursively applied to the sequence until no partition can be done

Sorting a Sequence of Data

- An example of quick sort



Recursive Quick Sort

- The algorithm

- Key part: partition of the data sequence

```
partition(arr[], low, high)
{
    // pivot (Element to be placed at right position)
    pivot = arr[high];

    i = (low - 1) // Index of smaller element

    for (j = low; j <= high - 1; j++)
    {
        // If current element is smaller than the pivot
        if (arr[j] < pivot)
        {
            i++; // increment index of smaller element
            if(i != j) swap arr[i] and arr[j]
        }
    }
    swap arr[i + 1] and arr[high])
    return (i + 1)
}
```

Recursive Quick Sort

- The algorithm
 - Key part: partition of the data sequence

```
arr[] = {10, 80, 30, 90, 40, 50, 70}
```

```
Indexes: 0 1 2 3 4 5 6
```

```
low = 0, high = 6, pivot = arr[h] = 70
```

```
Initialize index of smaller element, i = -1
```

```
Traverse elements from j = low to high-1
```

```
j = 0 : Since arr[j] <= pivot, do i++ and swap(arr[i], arr[j])
```

```
i = 0
```

```
arr[] = {10, 80, 30, 90, 40, 50, 70} // No change as i and j  
// are same
```

```
j = 1 : Since arr[j] > pivot, do nothing
```

```
// No change in i and arr[]
```

Recursive Quick Sort

- The algorithm

- Key part: partition of the data sequence

j = 2 : Since `arr[j] <= pivot`, do `i++` and `swap(arr[i], arr[j])`

i = 1

`arr[] = {10, 30, 80, 90, 40, 50, 70}` // We swap 80 and 30

j = 3 : Since `arr[j] > pivot`, do nothing

// No change in `i` and `arr[]`

j = 4 : Since `arr[j] <= pivot`, do `i++` and `swap(arr[i], arr[j])`

i = 2

`arr[] = {10, 30, 40, 90, 80, 50, 70}` // 80 and 40 Swapped

j = 5 : Since `arr[j] <= pivot`, do `i++` and swap `arr[i]` with `arr[j]`

i = 3

`arr[] = {10, 30, 40, 50, 80, 90, 70}` // 90 and 50 Swapped

We come out of loop because `j` is now equal to `high-1`.

Finally we place pivot at correct position by swapping

`arr[i+1]` and `arr[high]` (or pivot)

`arr[] = {10, 30, 40, 50, 70, 90, 80}` // 80 and 70 Swapped

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Declaring dynamic array structure

```
struct ARRAY
{
    int size;
    int count;
    float* data;
};
```

Note that the size of the array (for storage) could be larger than the real number (count) of the array

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - What functions we need (by design)?

```
bool create_array(int, ARRAY*);  
void destroy_array(ARRAY*);  
  
bool array_add_element(ARRAY*, float);  
bool array_remove_element(ARRAY*, int);  
  
int get_array_count(const ARRAY*);  
int get_array_size(const ARRAY*);  
  
float& get_array_element(int, const ARRAY*);  
void set_array_element(int, float, ARRAY*);  
  
void print_array(const ARRAY*);
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Create the array

```
bool create_array(int size, ARRAY* p_array_out)
{
    if (size <= 0)
        return false;

    if (p_array_out != NULL)
    {
        p_array_out->data = (float*)malloc(sizeof(float) * size);
        if (p_array_out->data == NULL)
            return false;

        p_array_out->size = size;
        p_array_out->count = 0;

        return true;
    }
    else
        return true;
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Destroy the array

```
void destroy_array(ARRAY* p_array)
{
    if (p_array != NULL)
    {
        if (p_array->data != NULL)
            free(p_array->data);

        p_array->size = 0;
        p_array->count = 0;
    }
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**

- Add array element (dynamically)

```
bool array_add_element(ARRAY* p_array, float element_value)
{
    if (p_array == NULL || p_array->data == NULL
        || p_array->count < 0 || p_array->size <= 0)
        return false;

    if (p_array->count + 1 <= p_array->size)
    {
        p_array->count++;
        p_array->data[p_array->count - 1] = element_value;
        return true;
    }
    else
    {
        ...
    }

    return true;
}
```


Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Add array element (dynamically)

```
bool array_add_element(ARRAY* p_array, float element_value)
{
    ...
    else
    {
        float* data_prev = p_array->data;
        p_array->data = (float*)realloc(data_prev, p_array->size
                                         + ARRAY_INCREMENT_SIZE);

        if (p_array->data == NULL)
            return false;

        p_array->size += ARRAY_INCREMENT_SIZE;

        p_array->count++;
        p_array->data[p_array->count - 1] = element_value;
        return true;
    }

    return true;
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Remove array element

```
bool array_remove_element(ARRAY* p_array, int i)
{
    if (i < 0 || i >= p_array->count)
        return false;

    int rest_count = p_array->count - i - 1;
    int copy_size = sizeof(float) * rest_count;

    float* p_temp_data = (float*)malloc(copy_size);
    if (p_temp_data == NULL)
        return false;
    memcpy(p_temp_data, &p_array->data[i + 1], copy_size);

    memcpy(&p_array->data[i], p_temp_data, copy_size);
    p_array->data[p_array->count - 1] = 0.0f;

    p_array->count--;

    ...
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Remove array element

```
bool array_remove_element(ARRAY* p_array, int i)
{
    ...

    if (p_array->count < p_array->size - 2 * ARRAY_INCREMENT_SIZE)
    {
        float* p_temp_data = p_array->data;
        p_array->data = (float*)realloc(p_temp_data, p_array->size
                                         - ARRAY_INCREMENT_SIZE);

        if (p_array->data == NULL)
            return false;
    }

    return true;
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**

- Other array functions

```
int get_array_count(const ARRAY* p_array)
{
    return p_array->count;
}
```

```
int get_array_size(const ARRAY* p_array)
{
    return p_array->size;
}
```

```
float& get_array_element(int i, const ARRAY* p_array)
{
    return p_array->data[i];
}
```

```
void set_array_element(int i, float data_value, ARRAY* p_array)
{
    p_array->data[i] = data_value;
}
```

Recursive Quick Sort for Array

- **Constructing a dynamic array**
 - Print(display) the array on the screen

```
void print_array(const ARRAY* p_array)
{
    for (int i = 0; i < get_array_count(p_array) - 1; i++)
        printf("%f, ", get_array_element(i, p_array));

    printf("%f\n", get_array_element(
        get_array_count(p_array) - 1, p_array));
}
```

Recursive Quick Sort for Array

- Implementing quicksort with dynamic array
 - Partition function

```
int quick_sort_array_partition
    (ARRAY* p_array , int low, int high)
{
    float pivot = get_array_element(high, p_array);
    int i = low-1;

    for (int j = low; j < high; j++)
    {
        if (get_array_element(j, p_array) < pivot)
        {
            i++;
            if (i != j) swap_data(&get_array_element(i, p_array),
                                &get_array_element(j, p_array));
        }
    }
    swap_data(&get_array_element(i+1, p_array),
            &get_array_element(high, p_array));

    return i+1;
}
```

```
void swap_data(float* a, float* b)
{
    float t = *a;
    *a = *b;
    *b = t;
}
```

Recursive Quick Sort for Array

- **Implementing quicksort with dynamic array**
 - Recursive function call for partitioning

```
bool quick_sort_array(ARRAY* p_array_in_out, int low, int high)
{
    if (low < high)
    {
        int partition_index =
            quick_sort_array_partition(p_array_in_out, low, high);

        quick_sort_array(p_array_in_out, low, partition_index - 1);
        quick_sort_array(p_array_in_out, partition_index + 1, high);

        return true;
    }
    else
        return false;
}
```

Recursive Quick Sort for Array

- How to use the quicksort for dynamic array?

```
void test_array_sort()
{
    ARRAY a;
    if (!create_array(20, &a))
    {
        printf("unable to create the array!\n");
        return;
    }

    printf("Please input the array elements:\n");

    while (1)
    {
        char str[32];
        scanf("%s", str);
        if (strcmp(str, "quit") == 0)
            break;
        array_add_element(&a, (float)atof(str));
    }
    ...
}
```


Recursive Quick Sort for Array

- How to use the quicksort for dynamic array?

```
void test_array_sort()
{
    ...

    printf("Your input ARRAY is:\n");
    print_array(&a);

    printf("\nSorting the whole array...\n");
    quick_sort_array(&a, 0, get_array_count(&a) - 1);
    printf("Your sorted array is:\n");
    print_array(&a);

    destroy_array(&a); //don't forget to destroy the ARRAY
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Declaring double linked list structure

```
struct LIST_DATA
{
    float data;
};
```

```
struct LIST_NODE
{
    LIST_DATA data;
    LIST_NODE* prev;
    LIST_NODE* next;
};
```

```
struct LIST
{
    LIST_NODE* p_head = NULL;
    LIST_NODE* p_tail = NULL;
    LIST_NODE* p_current = NULL;
    int count = 0;
};
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - What functions we need?

```
bool add_list_head_element(LIST*, const LIST_DATA&);  
bool remove_list_head_element(LIST*);
```

```
bool add_list_tail_element(LIST*, const LIST_DATA&);  
bool remove_list_tail_element(LIST*);
```

```
bool add_current_list_element_before(LIST*, const LIST_DATA&);  
bool add_current_list_element_after(LIST*, const LIST_DATA&);  
bool add_list_element_before(LIST*, LIST_NODE*, const LIST_DATA&);  
bool add_list_element_after(LIST*, LIST_NODE*, const LIST_DATA&);
```

```
bool remove_current_list_element(LIST*);  
bool remove_list_element(LIST*, LIST_NODE*);
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - What functions we need?

```
bool move_list_pointer_to(LIST*, int);
```

```
bool destroy_list(LIST*);
```

```
int get_list_count(LIST*);
```

```
LIST_NODE* get_list_head(LIST*);
```

```
LIST_NODE* get_list_tail(LIST*);
```

```
LIST_DATA& get_list_element(const LIST_NODE*);
```

```
void set_list_element(LIST_NODE*, const LIST_DATA&);
```

```
void print_list(LIST*);
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**

- Add list element from tail

```
bool add_list_head_element(LIST* p_list, const LIST_DATA& data)
{
    if (p_list == NULL)
        return false;

    LIST_NODE* p_node = (LIST_NODE*)malloc(sizeof(LIST_NODE));
    if (p_node == NULL)
        return false;

    p_node->data = data;

    if (p_list->p_tail == NULL)
    {
        p_node->prev = p_node->next = NULL;
        p_list->p_tail = p_node;
        p_list->p_head = p_list->p_tail;
    }
    ...
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**

- Add list element from tail

```
bool add_list_head_element(LIST* p_list, const LIST_DATA& data)
{
    ...

    else
    {
        p_node->next = NULL;
        p_node->prev = p_list->p_tail;
        p_node->prev->next = p_node;
        p_list->p_tail = p_node;
    }

    p_list->count++;
    p_list->p_current = p_list->p_tail;

    return true;
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Remove list element from tail

```
bool remove_list_tail_element(LIST* p_list)
{
    if (p_list == NULL)
        return false;

    LIST_NODE* p_node = p_list->p_tail;
    if (p_node == NULL)
        return false;

    p_list->p_tail = p_list->p_head->prev;
    p_list->p_tail->next = NULL;

    free(p_node);

    p_list->count--;
    p_list->p_current = p_list->p_tail;

    return true;
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Remove list element that is currently operating

```
bool remove_current_list_element(LIST* p_list)
{
    if (p_list == NULL)
        return false;

    LIST_NODE* p_node = p_list->p_current;

    p_node->prev->next = p_node->next;
    p_node->next->prev = p_node->prev;

    p_list->count--;
    p_list->p_current = p_node->next;

    free(p_node);

    return true;
}
```


Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Destroy the whole list

```
bool destroy_list(LIST* p_list)
{
    if (p_list == NULL)
        return false;

    LIST_NODE* p_node = p_list->p_head;

    while (p_node != NULL)
    {
        LIST_NODE* p_node_temp = p_node;
        p_node = p_node->next;
        free(p_node_temp);
    }

    return true;
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Other list functions

```
int get_list_count(LIST* p_list)
{
    return p_list->count;
}
```

```
LIST_NODE* get_list_head(LIST* p_list)
{
    return p_list->p_head;
}
```

```
LIST_NODE* get_list_tail(LIST* p_list)
{
    return p_list->p_tail;
}
```

```
LIST_DATA& get_list_element
(const LIST_NODE* p_list_node)
{
    return ((LIST_NODE *)p_list_node)->data;
}
```

```
void set_list_element
(LIST_NODE* p_list_node,
 const LIST_DATA& data)
{
    p_list_node->data = data;
}
```

Recursive Quick Sort for Linked List

- **Constructing a double linked list**
 - Print(display) the array on the screen

```
void print_list(LIST* p_list)
{
    if (p_list == NULL)
        return;

    LIST_NODE* p_node = p_list->p_head;

    while (p_node != NULL)
    {
        printf("%f, ", p_node->data.data);
        p_node = p_node->next;
    }
}
```

Recursive Quick Sort for Linked List

- Implementing quicksort with linked list
 - Auxiliary list node array

```
LIST_NODE** p_list_node_array =  
    (LIST_NODE**)malloc(sizeof(LIST_NODE*) * p_list_in_out->count);  
if (p_list_node_array == NULL)  
    return false;  
  
LIST_NODE* p_node_temp = p_list_in_out->p_head;  
int i = 0;  
while (p_node_temp != NULL)  
{  
    p_list_node_array[i] = p_node_temp;  
    p_node_temp = p_node_temp->next;  
    i++;  
}
```

Recursive Quick Sort for Linked List

- Implementing quicksort with linked list
 - Partition function

```
int quick_sort_list_partition(LIST_NODE** p_list_node_array, int low, int high)
{
    float pivot = p_list_node_array[high]->data.data;
    int i = low - 1;

    for (int j = low; j < high; j++)
    {
        if (p_list_node_array[j]->data.data < pivot)
        {
            i++;
            if (i != j) swap_data(&p_list_node_array[i]->data.data,
                                &p_list_node_array[j]->data.data);
        }
    }
    swap_data(&p_list_node_array[i+1]->data.data,
              &p_list_node_array[high]->data.data);

    return i+1;
}
```

Recursive Quick Sort for Linked List

- Implementing quicksort with linked list
 - Recursive function call for partitioning

```
bool quick_sort_list(LIST* p_list_in_out, int low, int high)
{
    if (low >= high)
        return false;

    LIST_NODE** p_list_node_array =
        (LIST_NODE**)malloc(sizeof(LIST_NODE*) * p_list_in_out->count);
    if (p_list_node_array == NULL)
        return false;
    ... //previous construction of list node array

    quick_sort_list_with_array(p_list_node_array, low, high);

    free(p_list_node_array);

    return true;
}
```

Recursive Quick Sort for Linked List

- **Implementing quicksort with linked list**
 - Recursive function call for partitioning

```
void quick_sort_list_with_array
    (LIST_NODE** p_list_node_array, int low, int high)
{
    if (low < high)
    {
        int partition_index = quick_sort_list_partition
            (p_list_node_array, low, high);

        quick_sort_list_with_array
            (p_list_node_array, low, partition_index - 1);
        quick_sort_list_with_array
            (p_list_node_array, partition_index + 1, high);
    }
}
```

Recursive Quick Sort for Linked List

- How to use the quicksort for linked list?

```
void test_list_sort()
{
    LIST l;

    printf("Please input the list elements:\n");

    while (1)
    {
        char str[32];
        scanf("%s", str);
        if (strcmp(str, "quit") == 0)
            break;

        LIST_DATA data;
        data.data = (float)atof(str);
        add_list_tail_element(&l, data);
    }
    ...
}
```


Recursive Quick Sort for Linked List

- How to use the quicksort for linked list?

```
void test_list_sort()
{
    ...

    print_list(&l);
    printf("\n\n");

    printf("\nSorting the whole list...\n");
    quick_sort_list(&l, 0, get_list_count(&l) - 1);
    printf("Your sorted list is:\n");
    print_list(&l);

    destroy_list(&l); //don't forget to destroy the LIST
}
```