UNDERSTANDING THE NORMAL DISTRIBUTION





LEARNING OBJECTIVES

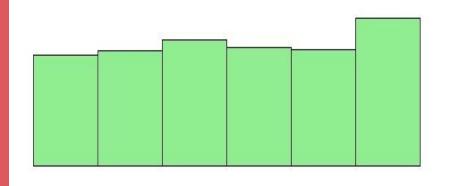
- Describe the key characteristics of a normal distribution
- Explain the meaning of standard deviation in the context of this lesson
- Apply the 68–95–99.7 rule to interpret data
- Recognize real-life examples of normally distributed variables
- Identify when data is not normally distributed

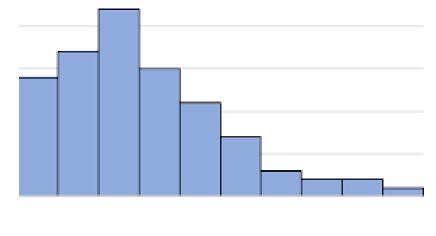


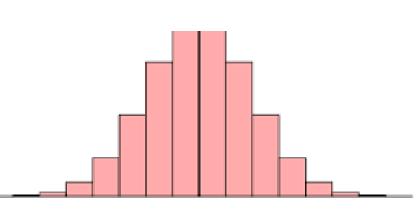
WHAT IS A DISTRIBUTION?

A distribution shows how data is spread across values.

Note: Some distributions are uniform, some are skewed, and some—like the normal distribution—are symmetrical.

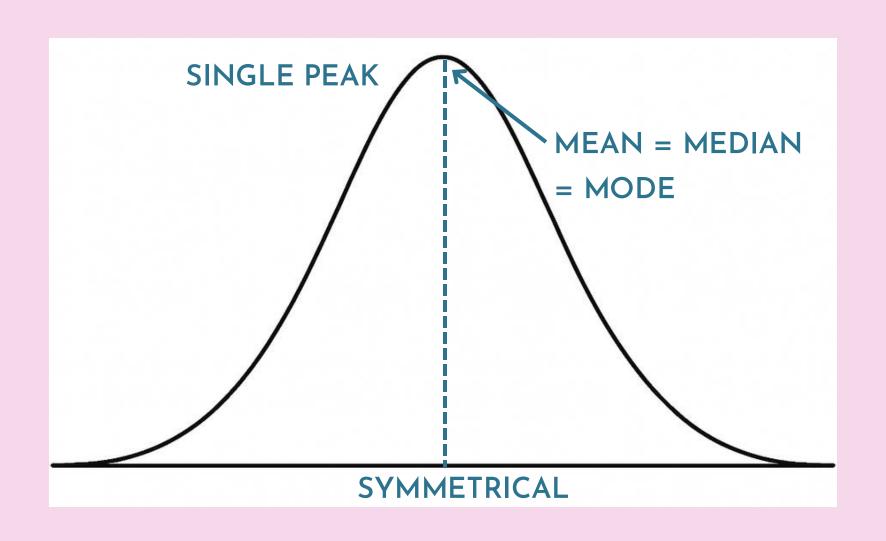








MEET THE BELL CURVE



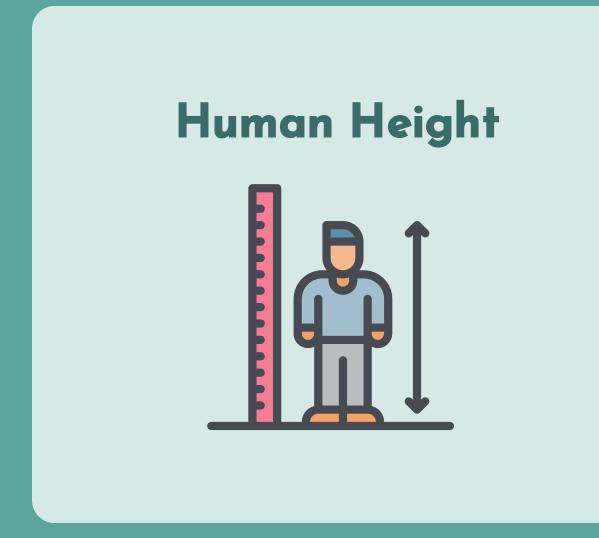
REFRESHER ON TERMS

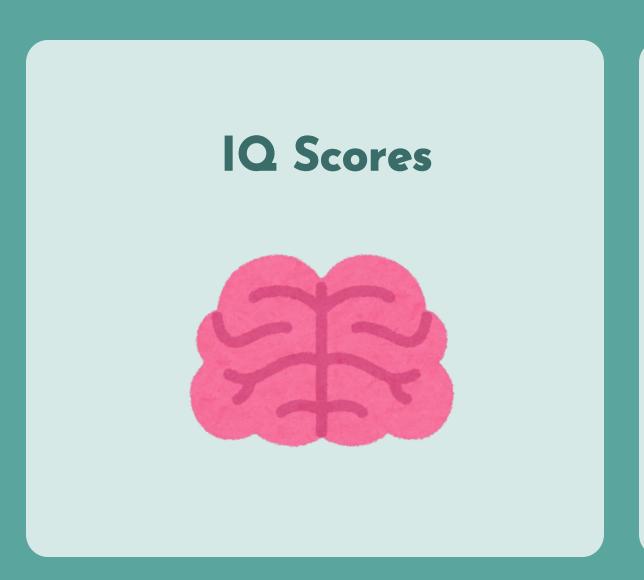
Mean - The average of all values

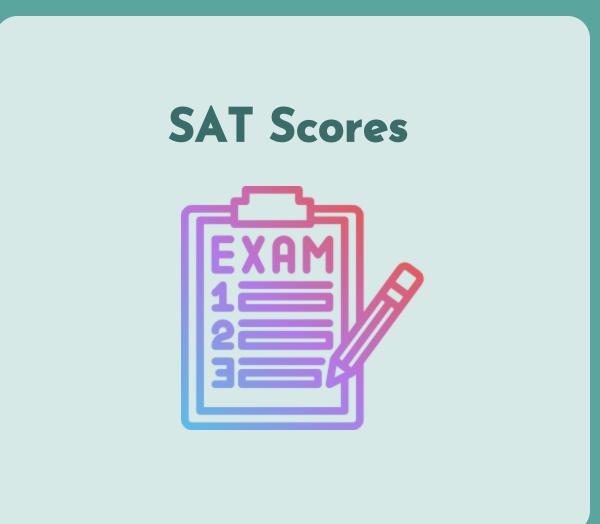
Median - The middle number when values are ordered

Mode - The most frequent value

REAL-LIFE EXAMPLES



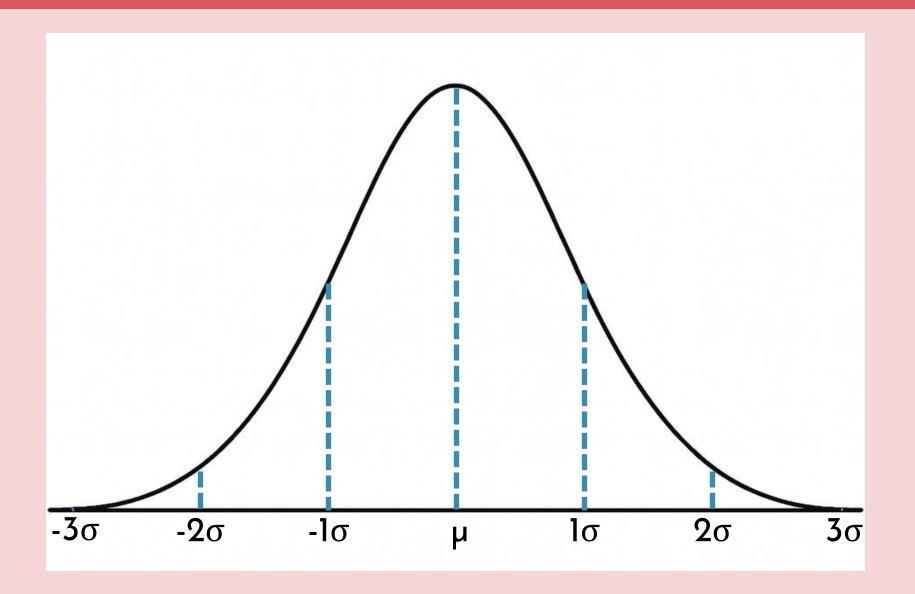




MOST PEOPLE ARE NEAR THE AVERAGE. FEW ARE AT THE EXTREMES.



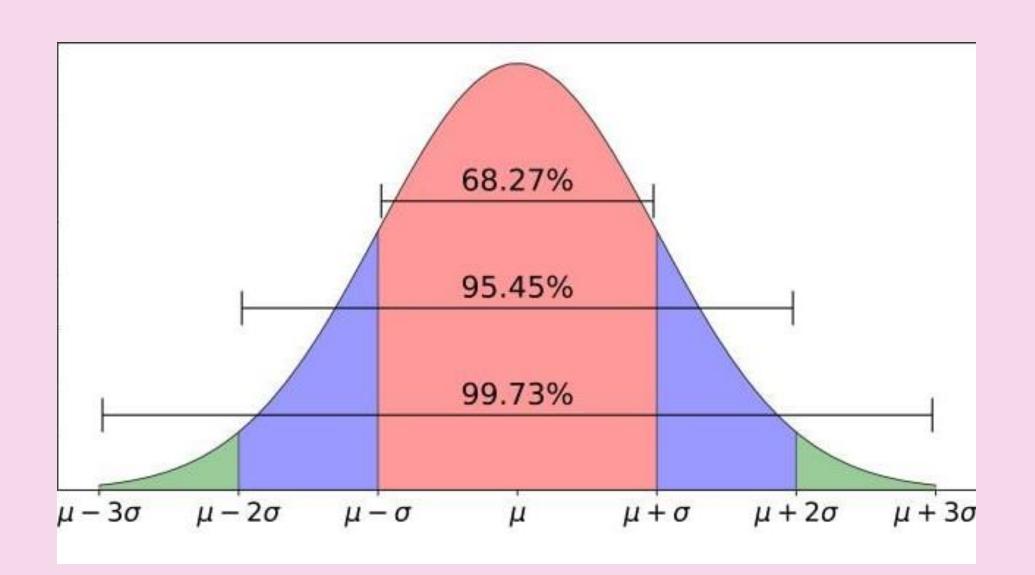
STANDARD DEVIATION



In a normal distribution, μ is the mean and σ shows the spread around it.



68-95-99.7 RULE



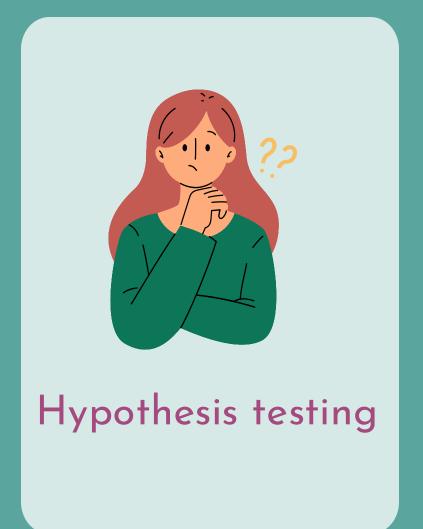
68% of data is within 1 standard deviation

95% within 2 standard deviations

99.7% within 3 standard deviations

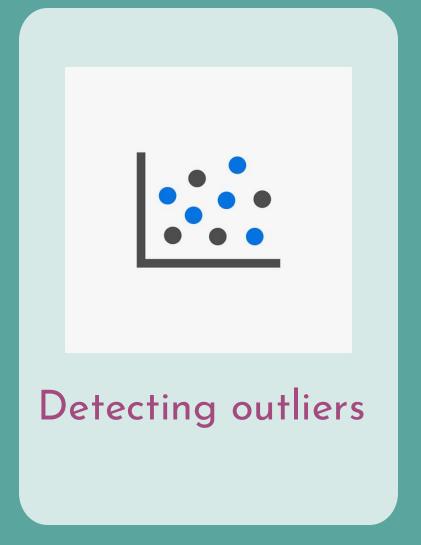


WHY IT MATTERS







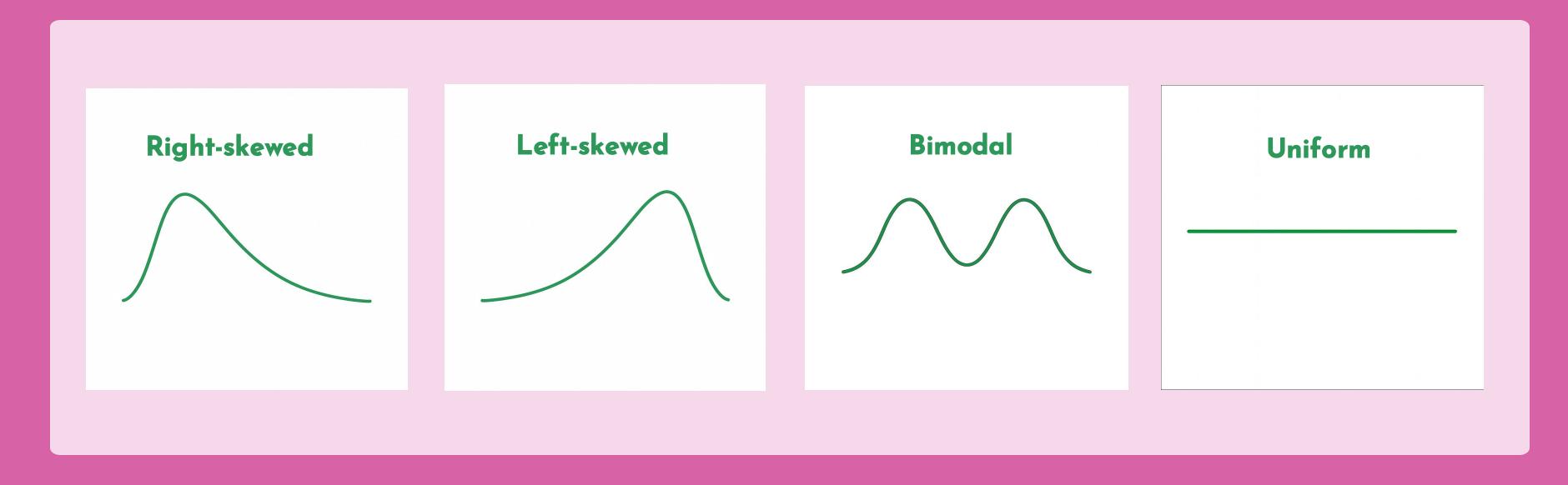




BEFORE YOU ASSUME IT'S NORMAL...

- Not all bell-shaped curves are truly normal
- Real-world data is often skewed, categorical, etc.
- The 68-95-99.7 rule only applies to normal distributions
- T-distributions and others may look similar but behave differently

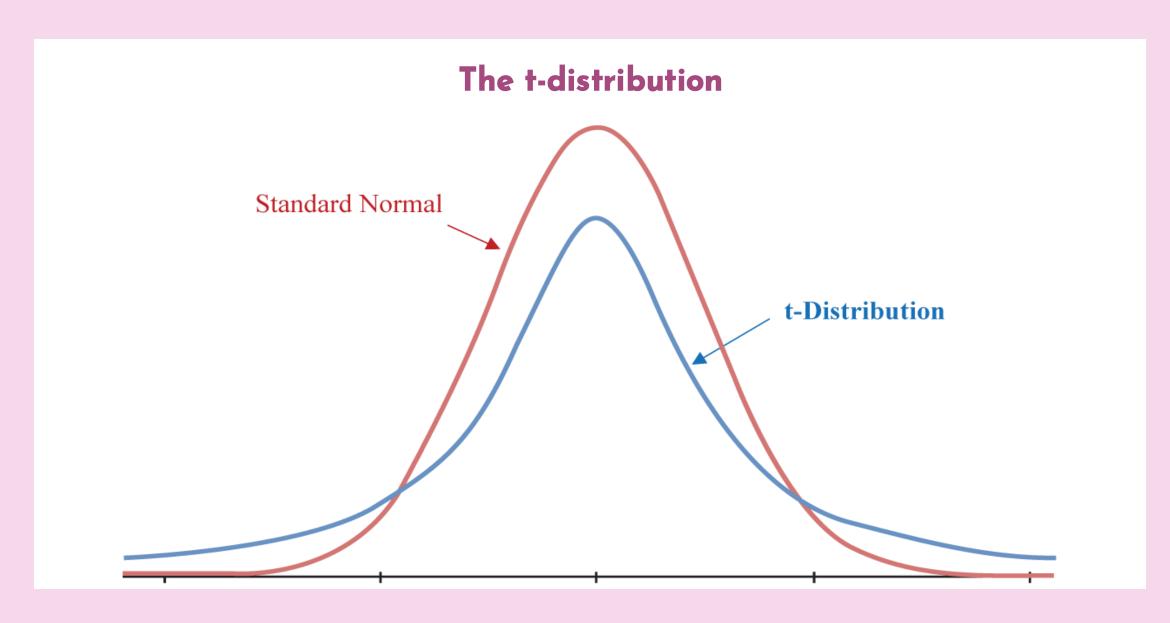
WHEN THE DATA ISN'T NORMAL



Some options: non-parametric tests, data transformations, visual analysis tools



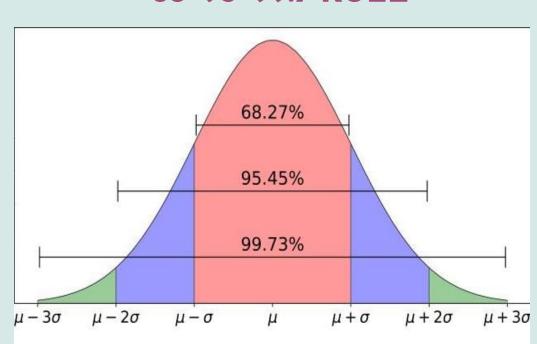
WHEN THE DATA IS APPROXIMATELY NORMAL



- Use the t-distribution for small samples
- Similar to the normal curve, but with thicker tails
- Becomes more normal as sample size grows

PRACTICAL EXAMPLE USING THE NORMAL DISTRIBUTION





 $\mu = 30$ minutes

 $\sigma = 10$ minutes

Q: What range covers about 95% of commute times?

A: Between 10 and 50 minutes



Hooray! I've Reached MEDIOCRITY

FINAL RECAP

- Symmetrical, bell-shaped curve
- Mean = median = mode
- Standard deviation controls spread
- The 68–95–99.7 Rule helps with probability
- The normal distribution helps us make sense of data in education, health, research, business, etc.
- Powerful, but not universal





