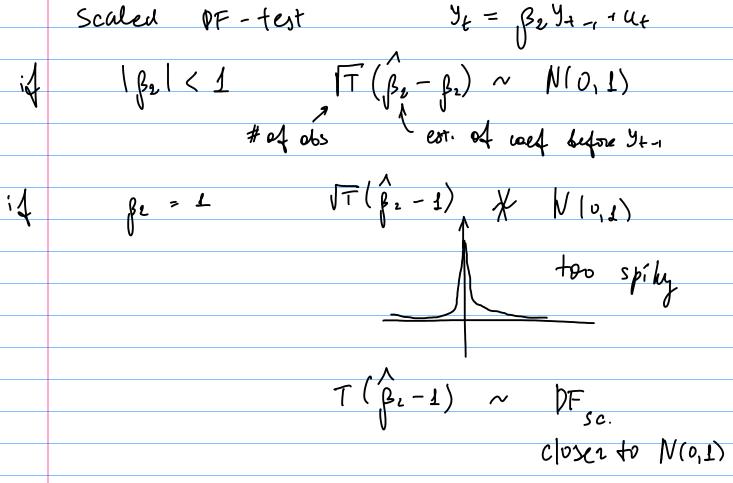
**(4)** 

(b) Now for equations (1-4) carry out the Dickey-Fuller test using the scaled estimator of the slope coefficient  $T(\hat{\beta}_2 - 1)$  to test series  $P_t$ ,  $DP_t$  and  $VOL_t$  for nonstationarity where  $\beta_2$  is the slope coefficient of the autoregression  $Y_t = \beta_2 Y_{t-1} + u_t$ . Indicate in each case the null hypothesis and used critical values. Do the results of these tests coincide with your conclusions based on t-tests? Comment the meaning of  $T(\hat{\beta}_2 - 1)$  statistic and explain why the difference  $(\hat{\beta}_2 - 1)$  should be multiplied by T rather than by  $\sqrt{T}$ .

 $\Delta VOL_t = 1.55 \cdot 10^8 - 0.143 VOL_{t-1} - 0.224 \Delta (VOL_{t-1})$ 

(65210866) (0.044)



$$\begin{array}{lll} & \mathcal{E}q & (1) & \mathcal{D}P_{t} = \beta_{1} + (\beta_{2} - 1)P_{t-1} + \mu \\ & \mathcal{D}F_{SC. OBS} = 183 \cdot (-902) = -3,66 \\ & \mathcal{D}F_{SC. CRIT} = -13,72 \end{array}$$

(c) The student obtained for equation (1)  $\Delta P_t = \beta_1 + (\beta_2 - 1)P_{t-1} + u_t$ , the value of F-statistics for testing simultaneously two restrictions  $\beta_1 = 0$ ,  $\beta_2 = 1$  F = 1.00. How to use this information to conduct Dickey-Fuller F-test for the nonstationarity of the  $P_t$ ? Following this approach describe how you can investigate also eqations (2-4) to test the series  $DP_t$  and  $VOL_t$  for the nonstationarity using Dickey-Fuller F-test: for each case indicate theoretical equation, restriction(s), and the rule for choosing the critical value of ADF F-statistic from the appropriate table. Indicate also in each case the random processes which the test allows to discriminate. What are comparative advantages and disadvantages of three different ADF tests for nonstationarity?

$$P_{t} = \beta_{1} + \beta_{2} P_{t-1} + U_{t}$$

$$\Delta P_{t} = \beta_{1} + (\beta_{2} - 1) P_{t-1} + U_{t}$$

$$U_{0}: \quad \beta_{1} = 0, \quad \beta_{2} - 1 = 0$$

$$V_{0}: \quad V_{0} = 1$$

## Cointegration

$$I(1) \rightarrow OY_4 - stationary$$

$$I(0) - e.g. MA(1), AP(1)$$

$$I(2) \rightarrow D(SY_4) - stationary$$

**Problem 2.** Explain what do you understand by difference-stationary and trend-stationary time series. Why it is important to know whether a variable is difference- or trend-stationary?

**Problem 3.** Consider a time series process

$$\ln Y_t = \alpha + \beta t + u_t; \ t = 1, 2, ..., T$$

Examine the order of integration of In  $Y_{i}$ .

P2. 
$$X_{t} = \chi_{0} + \chi_{1} + \mu_{1}$$

$$I_{t} = \chi_{t} - \chi_{1} = \chi_{0} + \mu_{1}$$

$$E(I_{t}) = \chi_{0}$$

$$Var(I_{t}) = 6^{2}u$$

$$Cov(I_{t}, I_{t} - S) = 0, \quad \forall S > 1$$

$$In Y_{t} = \chi_{t} + \beta_{t} + \mu_{t}$$

$$E(I_{t}, Y_{t}) = \chi_{t} + \beta_{t}$$

$$\delta(I_{t}, Y_{t}) = \chi_{t} + \beta_{t}$$

$$E(s \ln y_{+}) = \beta$$
  
 $Van(s \ln y_{+}) = 2\delta_{L}^{2}$   
 $Cov(s \ln y_{+}, s \ln y_{+-s}) = \beta_{S=1}^{2}$ 

**Problem 4.** What time series are called cointegrated?

is stationary

E.g. 
$$X_{t}$$
,  $Z_{t}$ ,  $Y_{t}$  -  $I(1)$ 

Q.  $f$  Q.  $X_{t}$  + Q.  $Y_{t}$  + Q.  $Z_{t}$  =  $C_{t}$  - Stationary

Q.  $Z_{t}$  = 1

9 = - 00 - a, Xt - az 2+ -et