

*Elements of Econometrics, 2023-2024*

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**Quiz 2.**

**Problem 1**

We estimate two linear regression to learn  $\log(\text{Price})$  determinants for Moscow flats based on CIAN data. The regressors used in the analysis are: *Dist* – distance from Red Square in km, *Brick* – dummy variable, 1 – if house is from concrete, 0 – otherwise, *Totsp* – total space in sq. m., *HouseAge* – house age in years. *Price* was measured in mln rub.

Model 1:

```
Call:
lm(formula = LogPrice ~ log(Dist) + Brick + Totsp + HouseAge,
    data = df1)

Residuals:
    Min       1Q   Median       3Q      Max
-1.30669 -0.14870 -0.01638  0.11912  1.59136

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 16.5111476  0.0177128  932.160 < 2e-16 ***
log(Dist)    -0.4609611  0.0047232  -97.594 < 2e-16 ***
Brick         0.0563552  0.0068825   8.188 3.06e-16 ***
Totsp        0.0160821  0.0001155 139.281 < 2e-16 ***
HouseAge     -0.0031191  0.0001027  -30.379 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2409 on 8042 degrees of freedom
(714 observations deleted due to missingness)
Multiple R-squared:  0.882,    Adjusted R-squared:  0.882
F-statistic: 1.503e+04 on 4 and 8042 DF,  p-value: < 2.2e-16
```

Model 2:

```
Call:
lm(formula = LogPrice ~ log(Dist) + Brick + Totsp + Totsp2 +
    HouseAge + HouseAge2, data = df1)

Residuals:
    Min       1Q   Median       3Q      Max
-1.21542 -0.15016 -0.01509  0.11991  1.58668

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.647e+01  2.400e-02  686.074 < 2e-16 ***
log(Dist)    -4.608e-01  4.749e-03  -97.038 < 2e-16 ***
Brick         4.352e-02  7.426e-03   5.861 4.79e-09 ***
Totsp        1.784e-02  4.692e-04  38.022 < 2e-16 ***
Totsp2       -1.055e-05  2.663e-06  -3.962 7.49e-05 ***
HouseAge     -4.014e-03  2.871e-04  -13.985 < 2e-16 ***
HouseAge2     9.852e-06  3.031e-06   3.250 0.00116 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2405 on 8040 degrees of freedom
(714 observations deleted due to missingness)
Multiple R-squared:  0.8824,    Adjusted R-squared:  0.8824
F-statistic: 1.006e+04 on 6 and 8040 DF,  p-value: < 2.2e-16
```

(5 points) Interpret each coefficient in Model 2.

(2 points) Which model is better. Provide appropriate statistical test to support your decision.

**Problem 2**

Consider the following model:

$$y_i = \beta_0 + \beta_1 \frac{1}{x_i} + \beta_2 z_i^2 + \beta_3 \frac{z_i}{x_i} + \epsilon_i$$

Derive how

(1 point)  $1/x_i$  affects  $y_i$ ? Interpret the effect.

(1 point)  $x_i$  affects  $y_i$ ? Interpret the effect.

(1 point)  $z_i$  affects  $y_i$ ? Interpret the effect.