

Perception & Multimedia Computing

Week 15 – Music Perception Pt. 2; Intro. To Signals & Systems

Michael Zbyszyński
Lecturer, Department of Computing
Goldsmiths University of London



Melody, Harmony, Tempo, & Rhythm

Melody

Definition and structural use of melody varies among cultures (e.g., rock, classical, gamelan, ...)

Basic definition:
Sequence of
pitched events
(notes) perceived
as a single entity,
unfolding in time

Harmony

*Perceptual quality when
pitched sounds (notes) occur
simultaneously*

Relative intervals determine
harmony/chord, not *absolute*
notes/pitches

e.g., C-E-G equivalent to D-F#-A
C-Eb-G equiv. to D-F-A

Music theory: Certain chords tend
to follow other chords; certain notes
tend to move to other notes when
chord changes

Cultural exposure leads to learned expectations

We learn through repeated exposure that certain **melodic** patterns are likely to resolve in certain ways, and that certain **harmonies** follow others.

Composers and songwriters work within learned system of expectations, surprising us or satisfying us through careful deviation from & adherence to “the rules.”

Individual compositions also develop and then break their own systems of expectations.



Schematic expectation

Expectation learned from cultural context of music

How do you expect a scale to resolve?

How do you feel when it resolves?
satisfaction (“prediction response”)

How do you feel when it doesn't?
attention (“tension response”)



Attention

Certain musical phenomena demand attention: unexpected phenomena, increases in volume, approaching sounds, ...

Arousal: physiological response to attention (increasing heart rate, perspiration); stress!

Can be pleasurable or stressful




Veridical expectation

Expectation learned by exposure to a piece of music

Satisfaction also arises when we know what note is coming next in *this particular song*

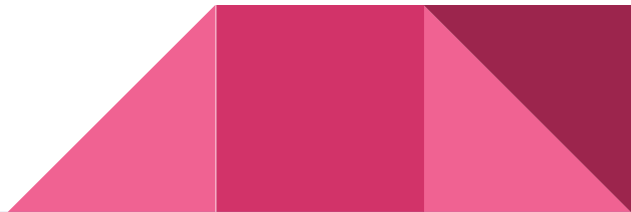
But schematic expectations are strong, and unusual phenomena in a familiar piece of music still “surprise” us



Consequences

Your unique listening history shapes the way you hear.

Composers & musicians manipulate expectations to capture your attention, surprise you, satisfy you, ...

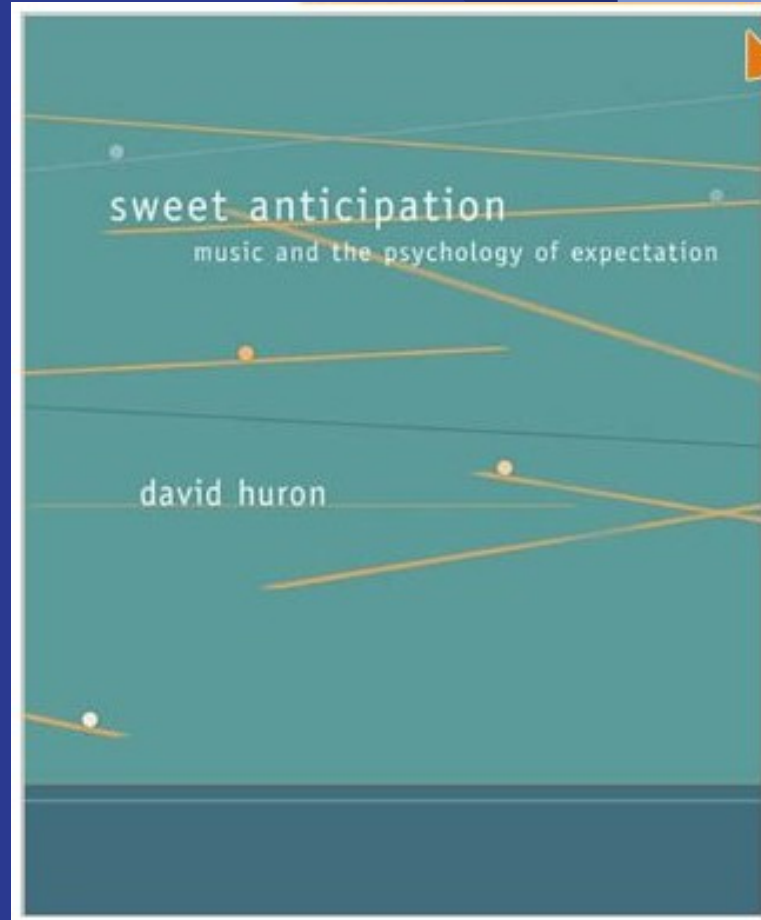


Consequences

Your unique listening history shapes the way you hear.

Composers & musicians manipulate expectations to capture your attention, surprise you, satisfy you, ...

Recommended reading!



Also:

[http://www.music-cog.ohio-state.edu/Music829D/Notes/Expectation.html#Reality versus Appearances](http://www.music-cog.ohio-state.edu/Music829D/Notes/Expectation.html#Reality%20versus%20Appearances)

Tempo

Natural “pulse” speed of music

Often ambiguous (half/double speed)

Humans’ preferred beat interval: around 0.2-0.8s

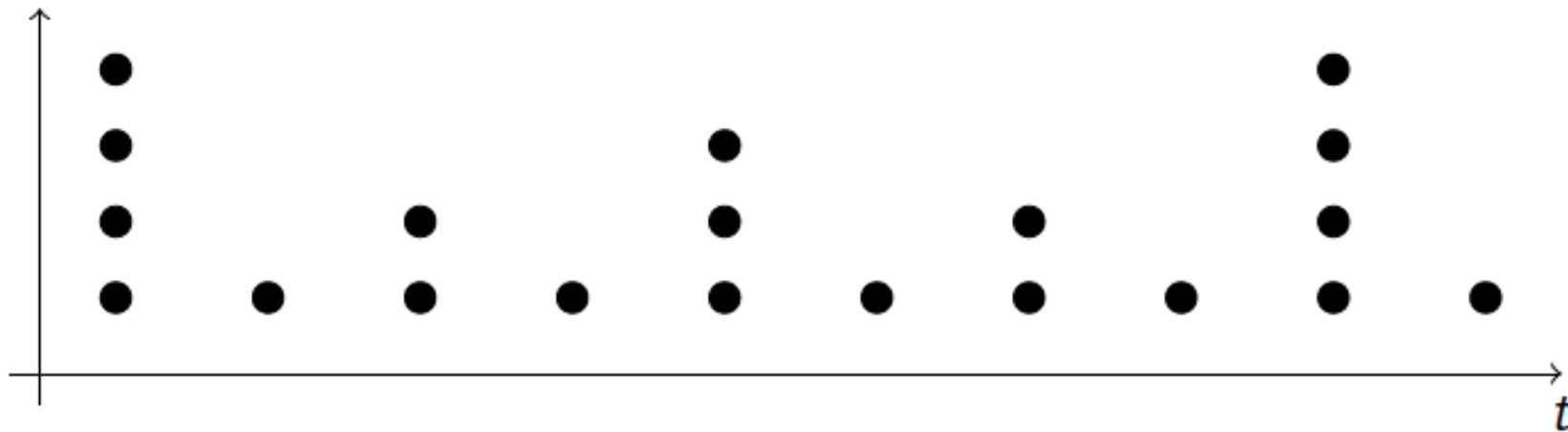


Metrical structure

Hierarchy of temporal groups:

Beats – Bars – Four-bar patterns – larger groups (e.g., 12- or 16-bar segments)

intensity



Rhythm

In a nutshell, which elements of the hierarchy to emphasize?

Music Summary:

- When do you hear sound as consonant/dissonant? Pitched/unpitched? Single/multiple sound sources?
- What are timbre, pitch, melody, harmony, tempo, rhythm?
- How do amplitude, frequency, and phase impact what we hear?
- What is a spectrum? Why is spectrum useful in reasoning about sound perception?
- Can you look at a spectrum and reason about what you will hear?
- Can you reason about how your expectations for melody, rhythm, harmony impact your experience of music?



Signals & Systems

What is a Signal?

- Any quantity varying over space or time
- Maths: *function* Physics: *field*



What is a Signal?

- Any quantity varying over space or time
- Maths: *function* Physics: *field*
 - *Electrical current at a point in a circuit*
 - *Count of students in weekly lectures*
 - *Temperature at all points in room*



For now, one-dimensional signals:

- Continuous time signals
 - Current at a point in a circuit
 - Temperature at a location
 - Sound pressure level



For now, one-dimensional signals:

- Discrete time signals
 - Current at a point in a circuit, measured once per second
 - Temperature at a location, measured hourly
 - Sound pressure level, measured 44,100 times per second



1-dimensional, discrete-time signals in Python

```
x = [1, 2, 3]
t = np.arange(0, 1, 1/44100)
s = sin(2*pi*100*t)
```

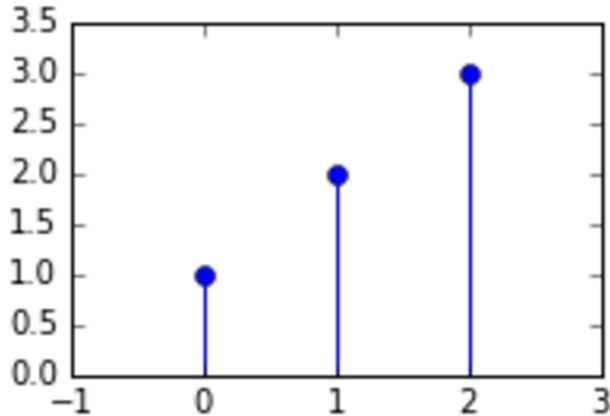
These are just arrays!

We interpret each element as happening at a certain time

e.g., $s[10]$ happens 10 samples after “time 0”

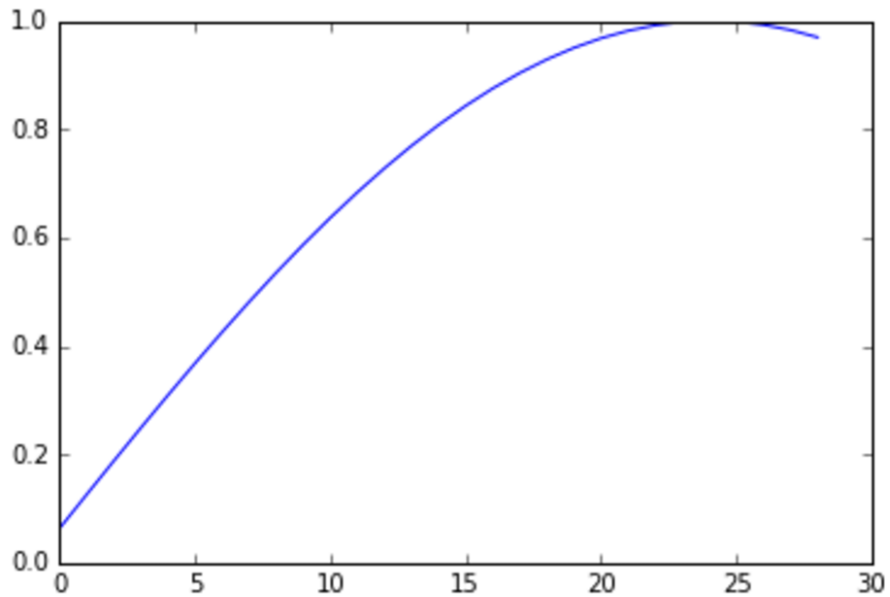
```
x = [1,2,3]
print x
fig, axes = plt.subplots(figsize=(3,2))
axes.stem(x)
ylim([0, 3.5])
plt.xticks(np.arange(-1, 4, 1.0))
```

```
[1, 2, 3]
```



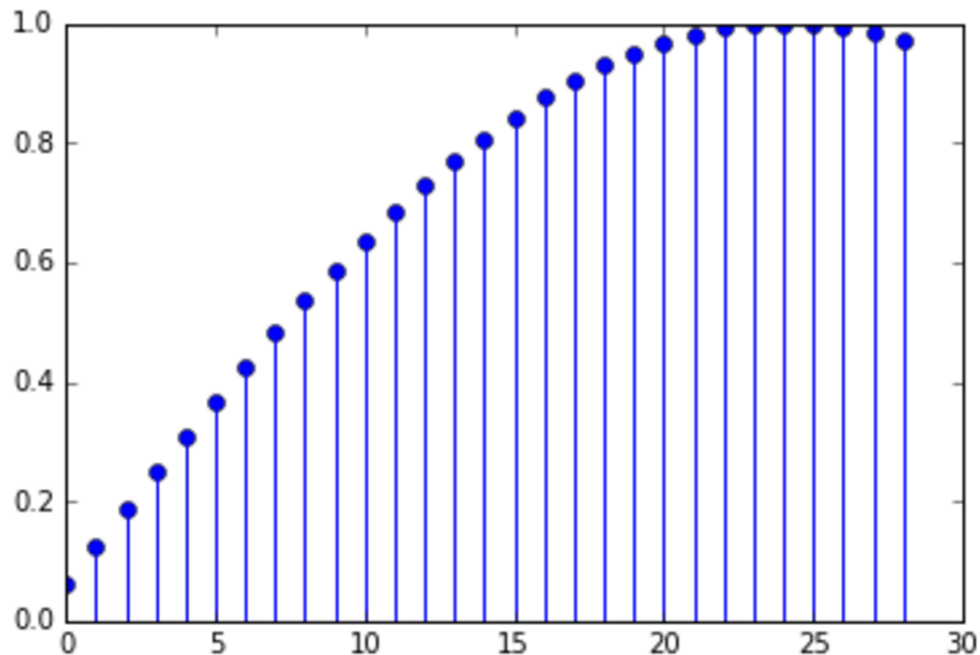
```
t = np.arange(0, 1, 1/44100)  
s = sin(2*pi*440*t)  
plot(s[1:30])
```

[<matplotlib.lines.Line2D at 0x10ff02210>]



```
t = np.arange(0, 1, 1/44100)  
s = sin(2*pi*440*t)  
stem(s[1:30])
```

<Container object of 3 artists>



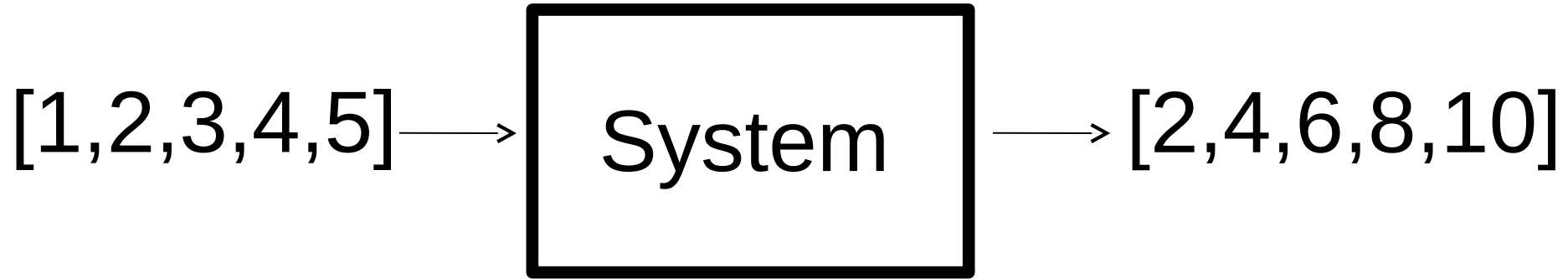
Systems

- Systems “construct” new signals from existing ones
- Examples
 - Computer monitor (in: electrical signal, out: light)
 - Violin (in: bow movement; out: sound)
 - Car suspension (in: bumps; out: smooth ride)



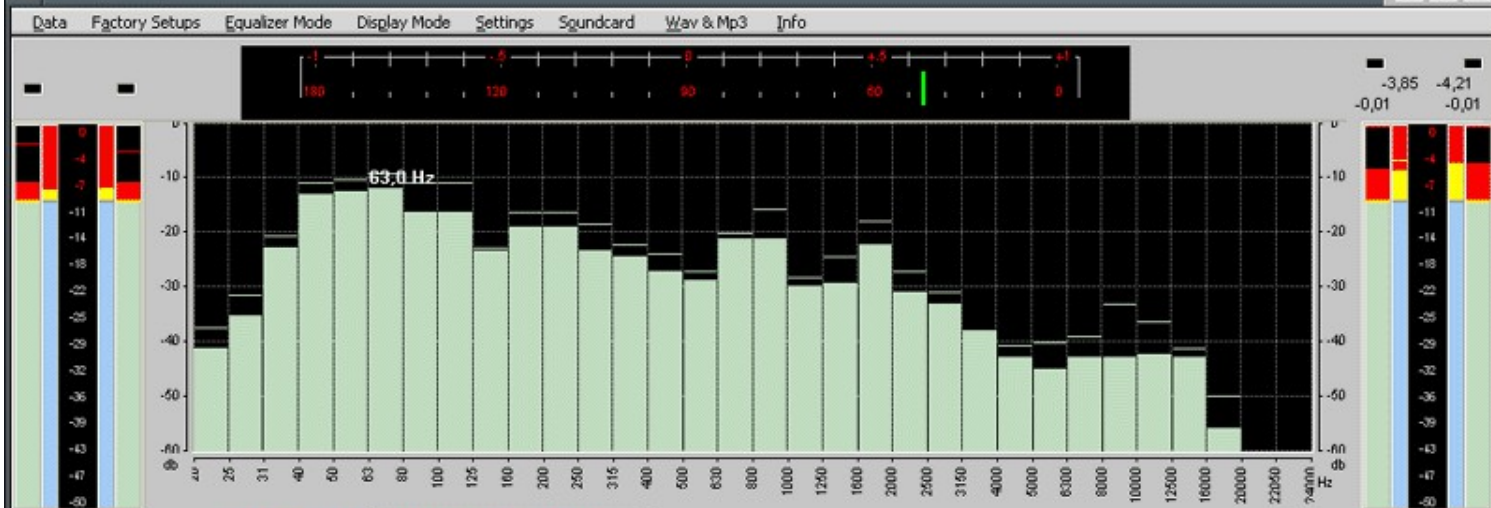
Systems

Compute output signal (response) from input



Examples of systems used in multimedia

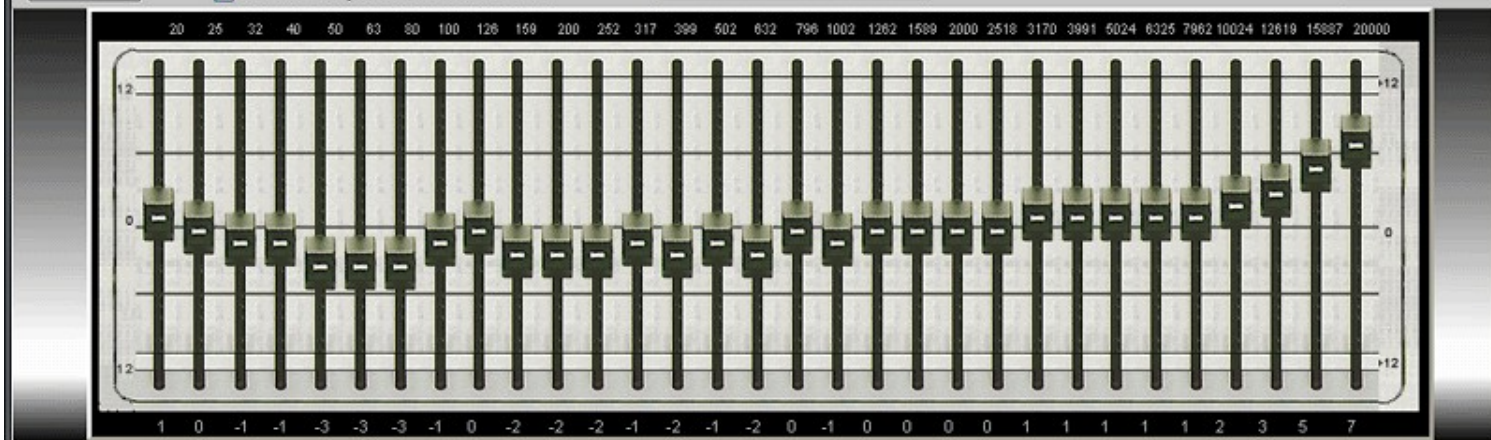




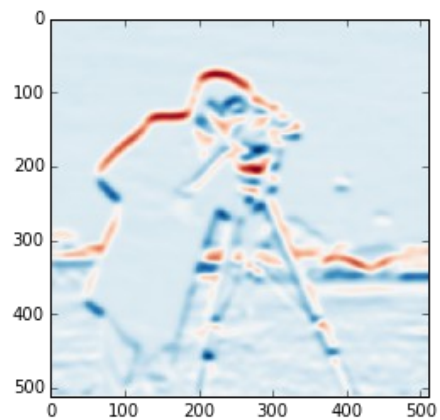
EQ list

☒ Activate Compressor/Limiter/Enhancer

SETUP STUDIO









Tracking hands





The magical system-building genie

“I wish I had a system (e.g., an audio or image filter) that could change the spectrum of my signal in *exactly this way...*”

e.g., “Remove frequencies at 60Hz and leave everything else untouched’

or “Boost all frequencies in 1000Hz to 3000Hz range”

or “Remove the high-frequency noise in this image”



Done!!!

(If you meet just a few conditions, then follow my instructions)



“I have a system here that I like. I wish I could re-create this system in my own software...”

e.g., “I like how music sounds when played in this giant cathedral. I wish I could make all my music sound like it’s recorded here.”

or

“I really like a ‘blur’ effect in this photo editing software. I wish I could make this effect in my own software.”



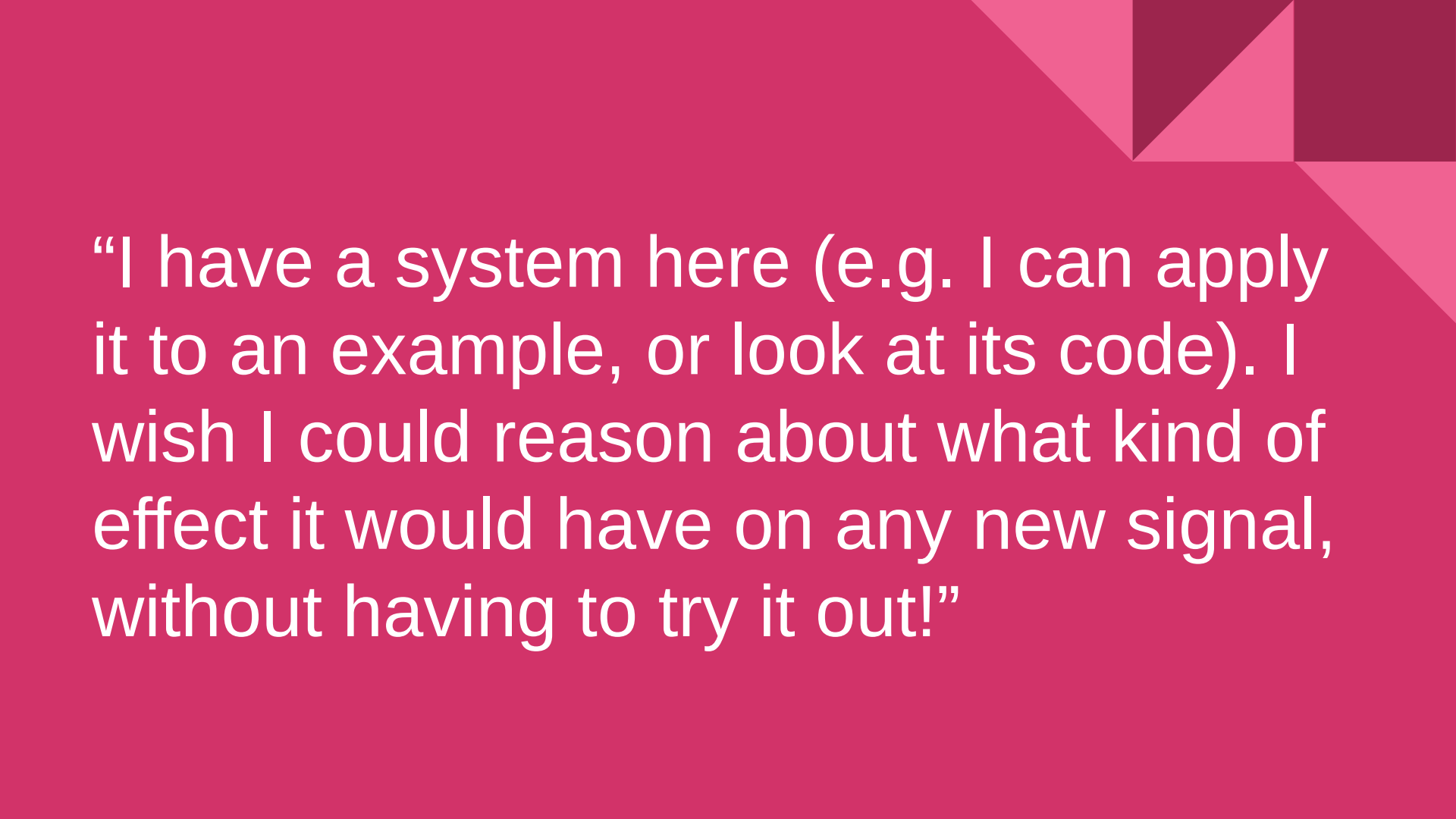
Done!!!

(If you meet just a few conditions, then follow my instructions)





The magical
system-analysis
genie



“I have a system here (e.g. I can apply it to an example, or look at its code). I wish I could reason about what kind of effect it would have on any new signal, without having to try it out!”

Done!!!

(If you meet just a few conditions, then follow my instructions)



What are the conditions?

Systems have to be

1. Linear

2. Time-invariant

(Or for images, shift-invariant)



Notation + Linearity & Time- Invariance

Signal notation

These are all equivalent:

- $x[n] = [3, 5, 12]$

- $x[0] = 3, x[1] = 5, x[2] = 12$

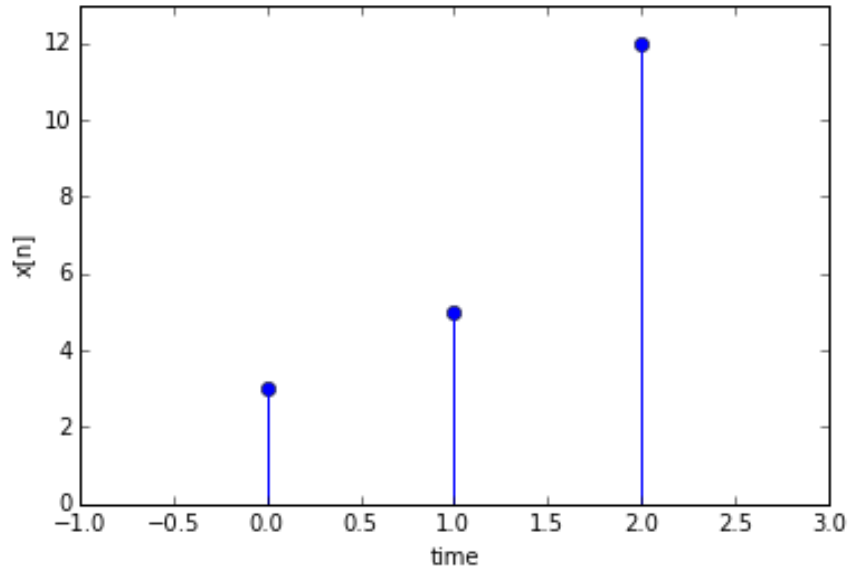
- $x[n] = [3, 5, 12, 0, 0, 0, \dots]$

and $x[-1] = 0, x[-100] = 0$, etc.



Signal notation

Also equivalent: $x[n] = [3, 5, 12]$



Notation: applying a system to a signal

Given an input signal x , the action of a system H on that signal, producing an output signal y is denoted:

$$y = H\{x\}$$



Notation: applying a system to a signal

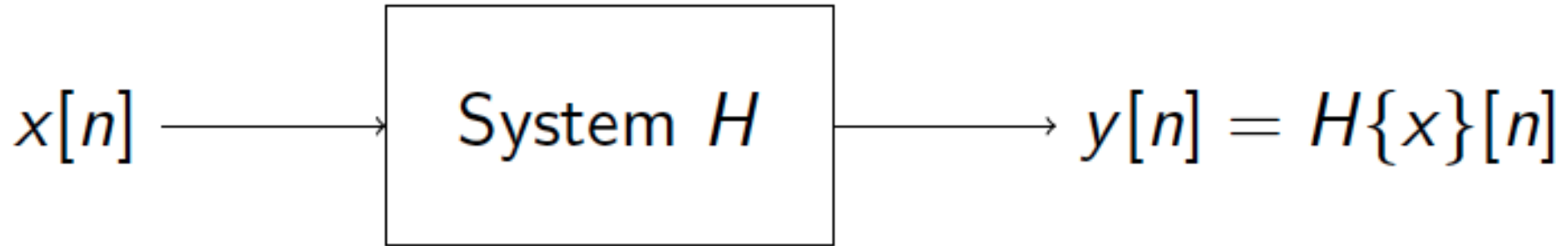
For a discrete-time signal $x[n]$:

$$y[n] = H\{x[n]\} \text{ or } y[n] = H\{x\}[n]$$



Notation: applying a system to a signal

For a discrete-time signal $x[n]$:



Example

A system:

$$H\{x[n]\} = 0.5 * x[n]$$

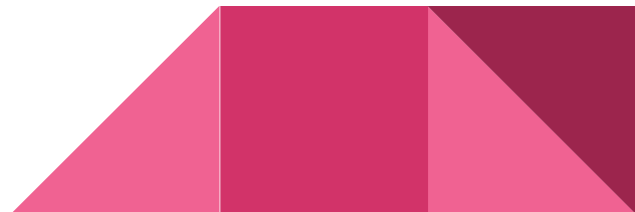
A signal:

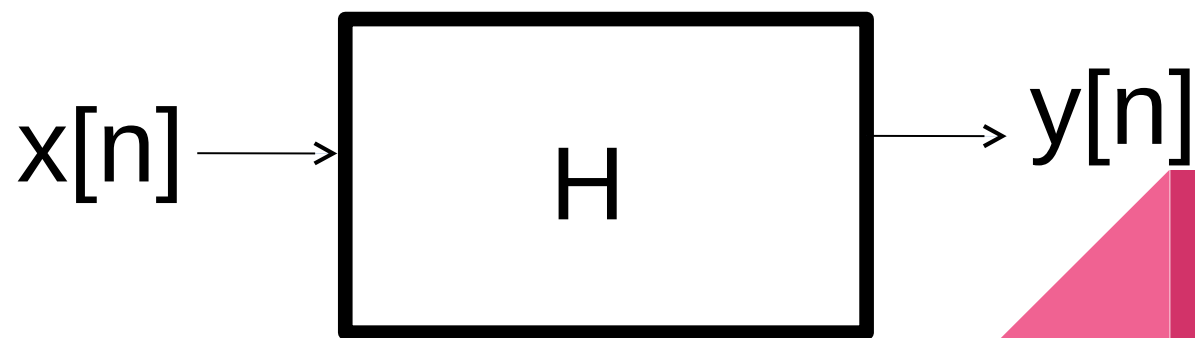
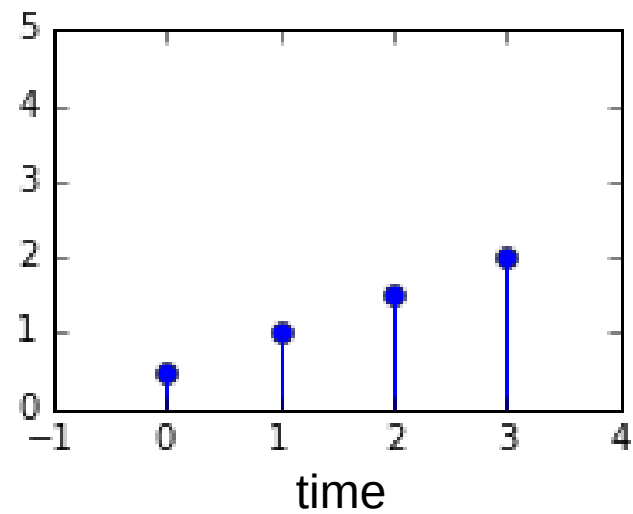
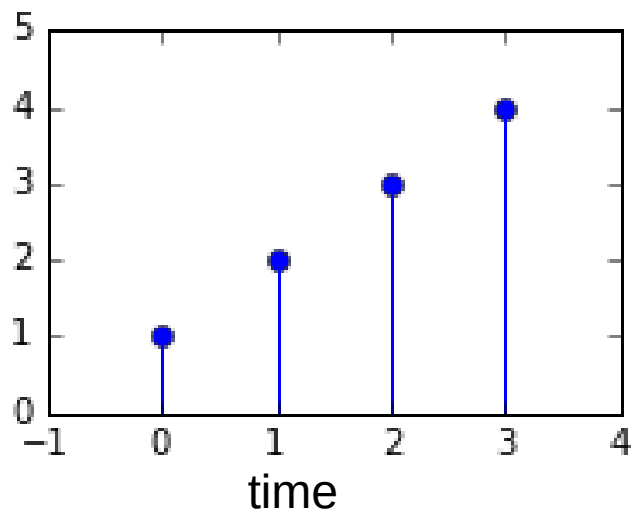
$$x[n] = [1, 2, 3, 4]$$

$$y[n] = H\{x[n]\} = ???$$

$$y[n] = [0.5, 1, 1.5, 2]$$

What kind of
system might
 H be?

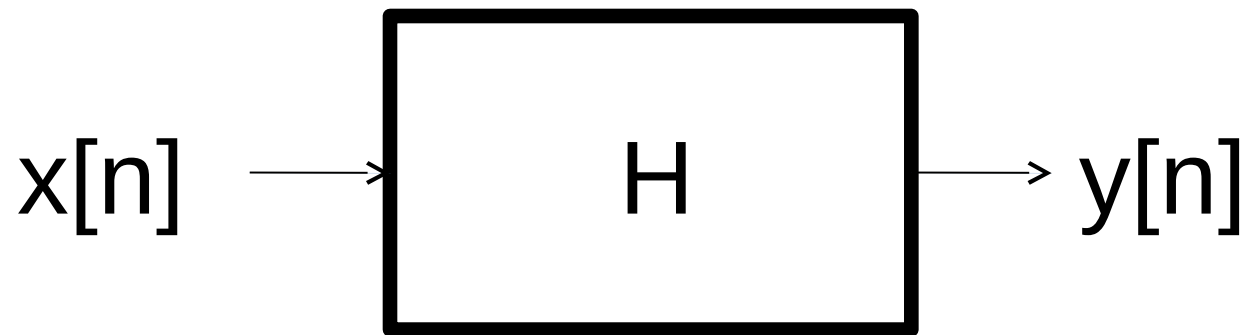




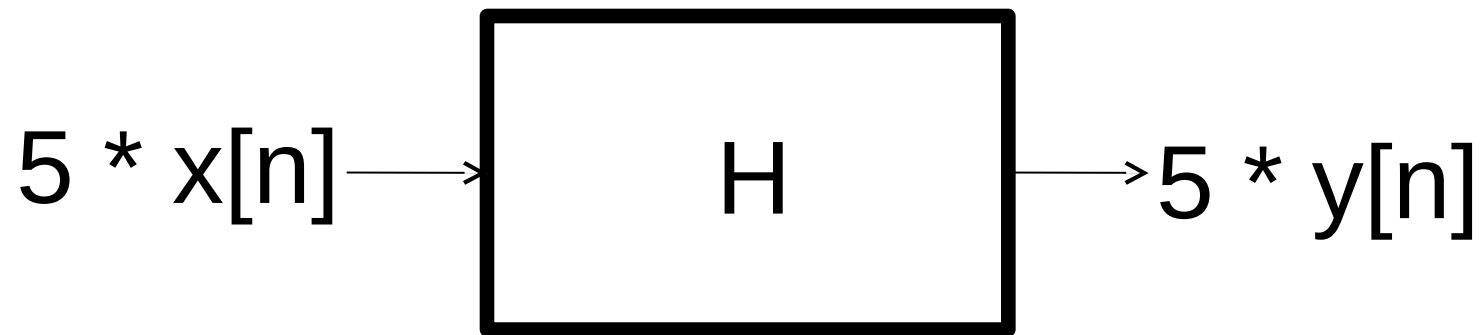
Linearity

Linear systems have the property that *scaling* and *superposition* of their input signals lead to a corresponding scaled superposition of their outputs.

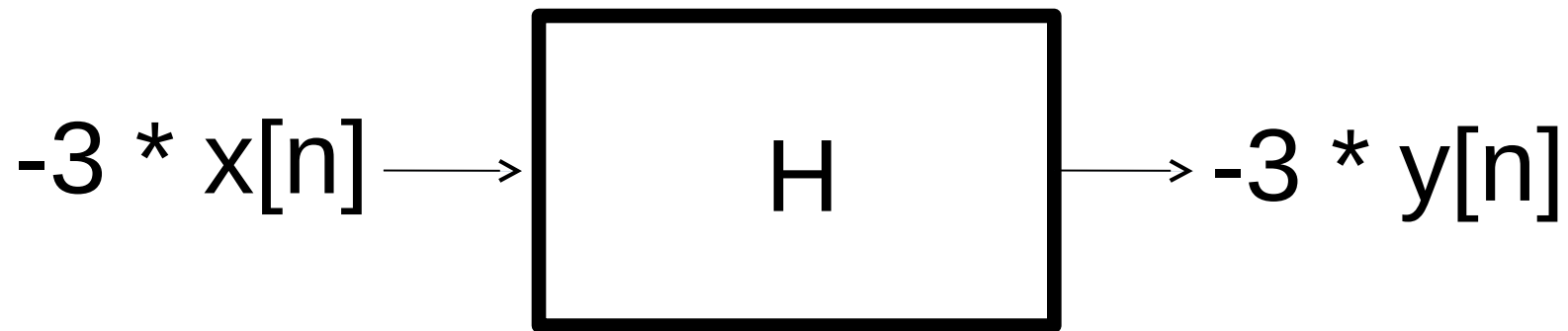
Scaling



Scaling



Scaling



Example

Scaling: for any input signal x_1 where $y_1 = H\{x_1\}$,
 $H\{\alpha x_1\} = \alpha y_1$ for any scalar value α

$$x1 = [2, 4, 6]$$

$$x2 = [4, 8, 12]$$

$$x1 = 2 * x1$$

$$y1 = H\{x1\} = [3, 18, 4]$$

$$y2 = H\{x2\} = ?$$

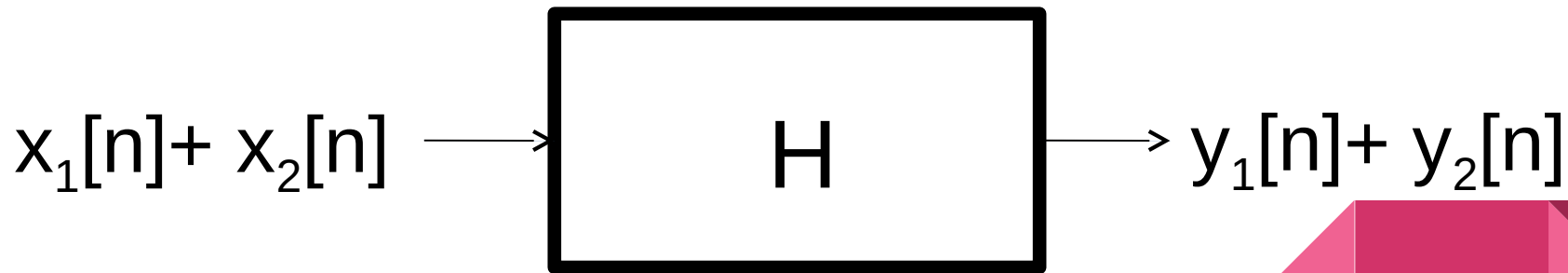
$$\text{so } y2 = 2 * y1$$



Linearity

Linear systems have the property that *scaling* and *superposition* of their input signals lead to a corresponding scaled superposition of their outputs.

Superposition



Example

Scaling: for any two input signals x_1 and x_2 where
 $y_1 = H\{x_1\}$ and $y_2 = H\{x_2\}$, $H\{x_1 + x_2\} = y_1 + y_2$

$$x1 = [2, 4, 6]$$

$$y1 = H\{x1\} = [3, 18, 4]$$

$$x2 = [1, 5]$$

$$y2 = H\{x2\} = [1, -3, 5]$$

$$X3 = [5, 2, 4]$$

$$y3 = ???$$

$$x3 = x1 + x2$$

$$\text{so } y3 = y1 + y2$$

$$y3 = [4, 13, 7]$$

Linearity

Linear systems have the property that *scaling* and *superposition* of their input signals lead to a corresponding scaled superposition of their outputs.

Example

$$x_1 = [5]$$

$$x_2 = [0, 1, 2]$$

$$x_3 = [5, 2, 4]$$

$$y_1 = H\{x_1\} = [-5]$$

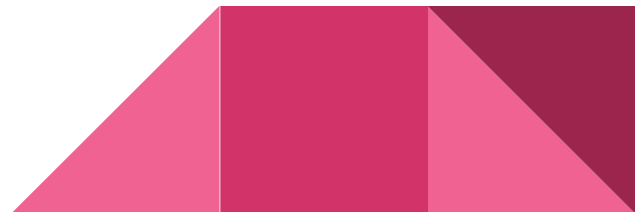
$$y_2 = H\{x_2\} = [0, 6, 3]$$

$$y_3 = ?$$

$$x_3 = x_1 + 2 * x_2$$

$$\text{so } y_3 = y_1 + 2 * y_2$$

$$y_3 = [-5, 12, 6]$$

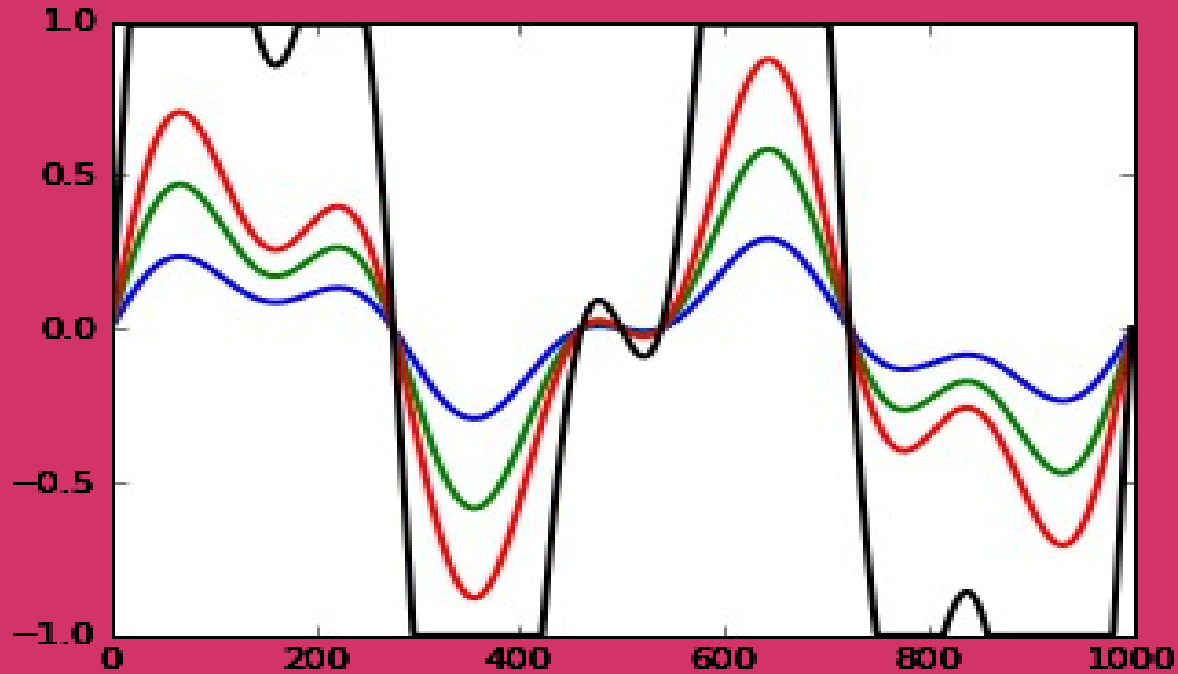


Linearity

Almost all systems in the real world are linear systems for *small enough signals*.

e.g. audio signal that doesn't clip

Nonlinear: Volume clipping



Time-invariance

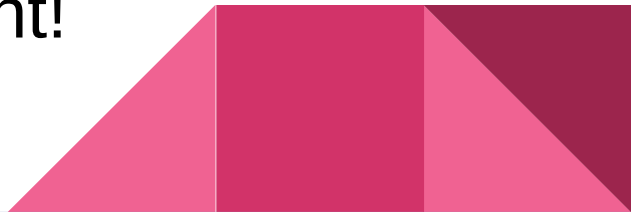
Time-invariant systems have the property that the output signal of the system for a given input signal does not depend explicitly on absolute time.

Time-invariance

E.g., does your guitar amp affect your guitar differently on Monday than on Tuesday?

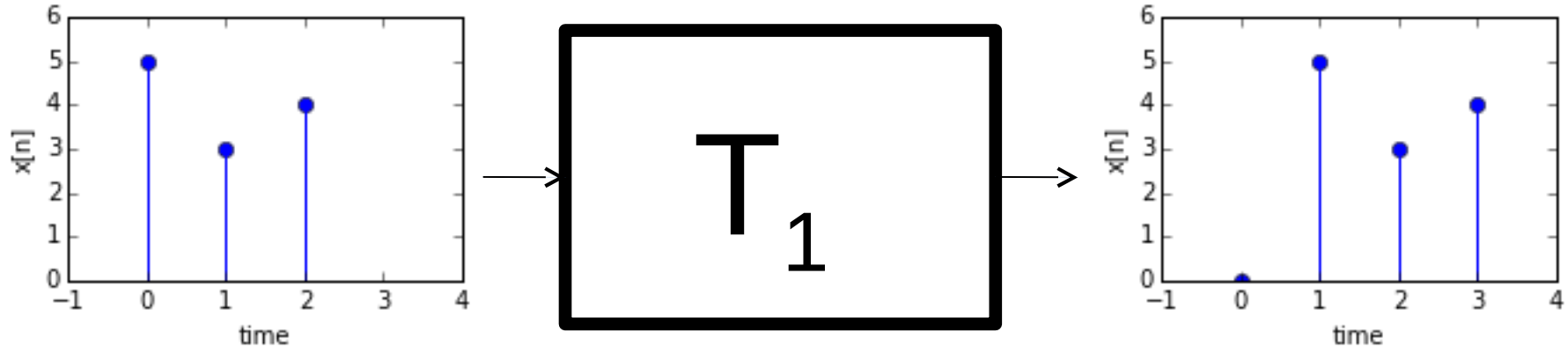
Does your image filter blur your image differently at 12:00 than at 11:00?

Probably not: These are time-invariant!



Unit Delay System

Just delays signal by 1 sample



The Unit Delay System


A special linear system T_1 whose output signal is the input signal, but delayed by one time unit.

$$y = T_1\{x\}$$

Or with discrete time explicitly represented:

$$y[n] = x[n - 1]$$

This unit delay system is the building block of the systems we will cover in this course.



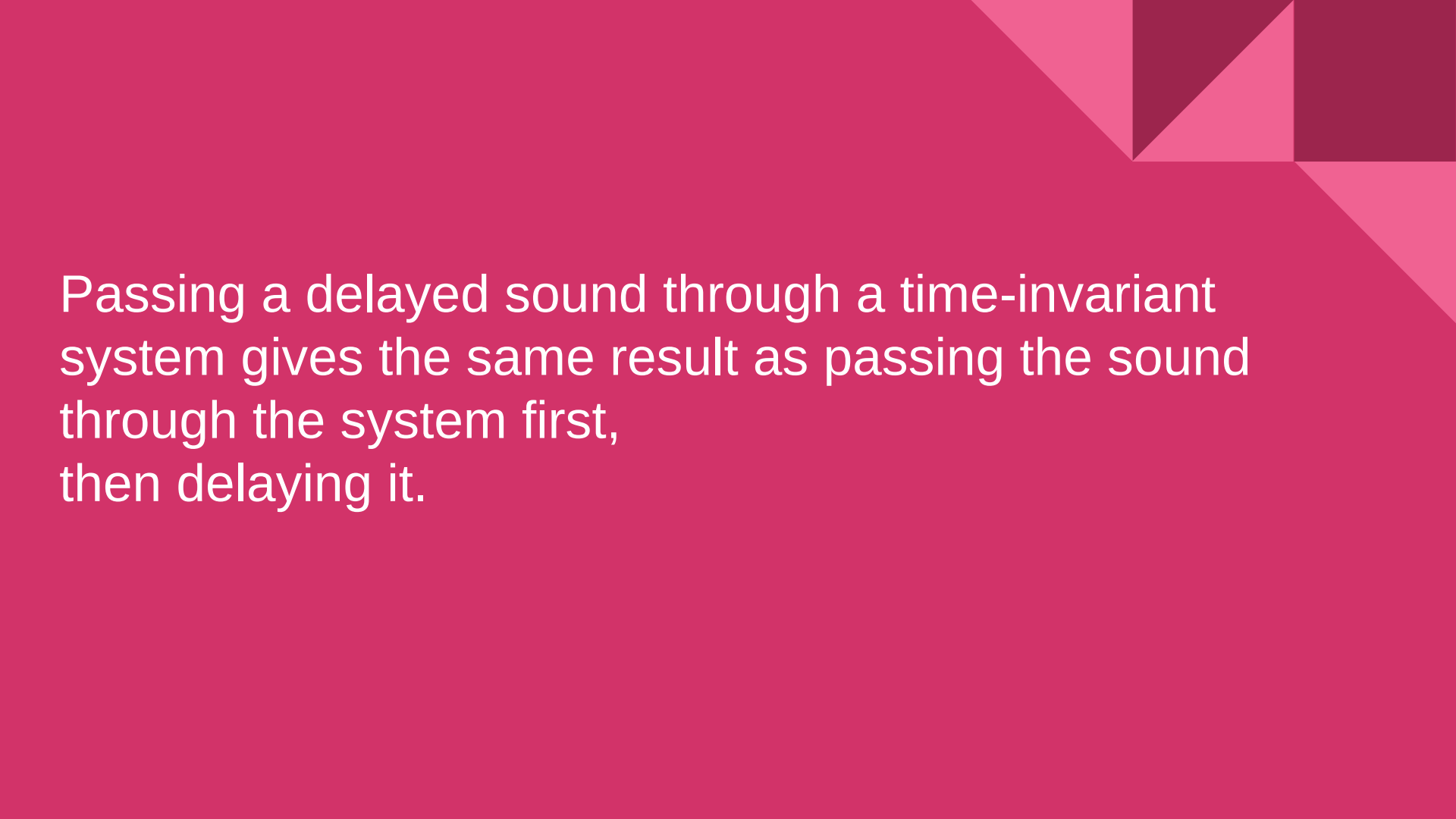
Time-invariant systems have the property that the output signal of the system for a given input signal does not depend explicitly on absolute time.

For any input signal x with $y = H\{x\}$, the system H is time-invariant if:

$$H \{T_{\delta}\{x\}\} = T_{\delta}\{y\}$$

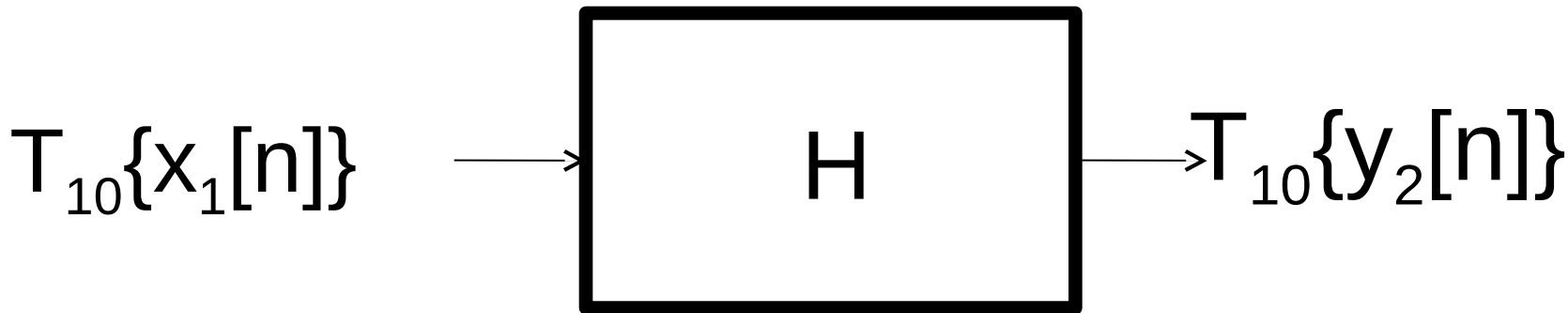
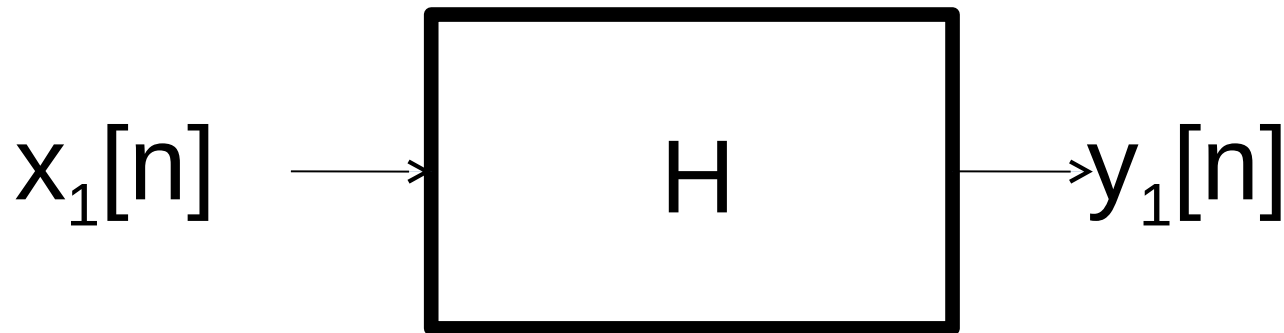
Where T_{δ} is a delay system for arbitrary delay.





Passing a delayed sound through a time-invariant system gives the same result as passing the sound through the system first, then delaying it.

Time invariance



Example

H is time-invariant

$$x_1 = [1, 2, 3]$$

and $y_1 = H\{x_1\} = [3, 4, 5]$

$$x_2 = [0, 0, 1, 2, 3]$$

$$y_2 = H\{x_2\} = ?$$

$$x_2 = T_2\{x_1\}$$

so $y_2 = T_2\{y_1\} = [0, 0, 3, 4, 5]$



Linear Time-Invariant or **LTI** Systems have both the linear property and the time-invariant property.

Why do we care?

Reason 1:

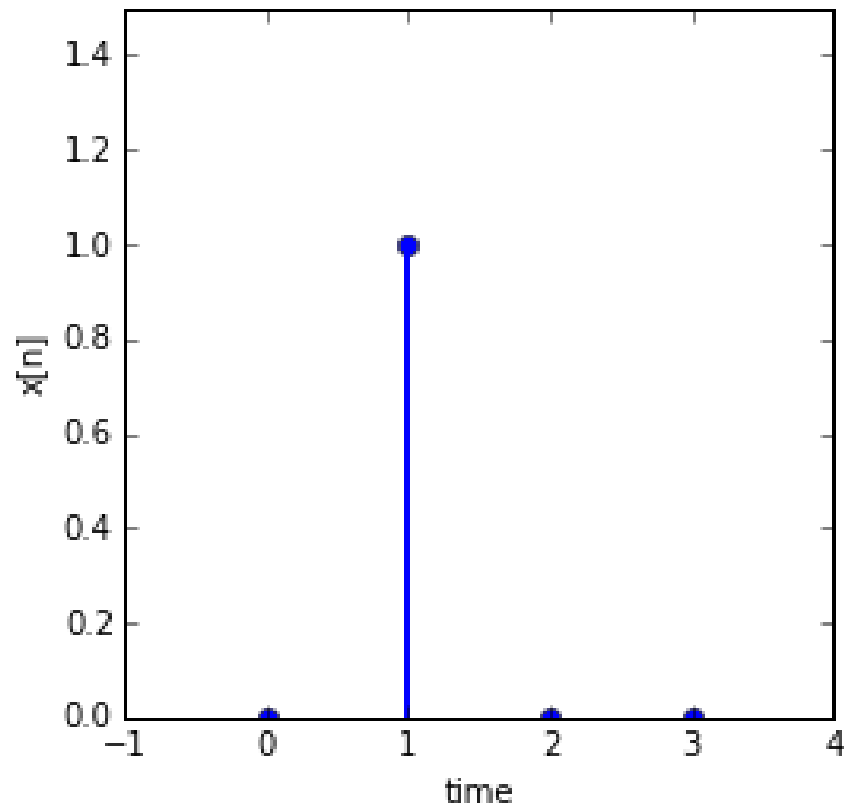
If we know the response of an LTI system for the signal below, we can compute the response to any signal whatsoever!

$$d[n] = [1, 0, 0, 0, \dots] = [1]$$


The unit impulse signal

*This special signal is called
the unit impulse*

$$d[n] = [1, 0, 0, 0, \dots] = [1]$$



The unit impulse signal

$d[n]$

1 at time 0, 0 everywhere
else

—