

# Effects of a superconducting lead endcap on the magnetic field profile for the nEDM search

Aritra Biswas

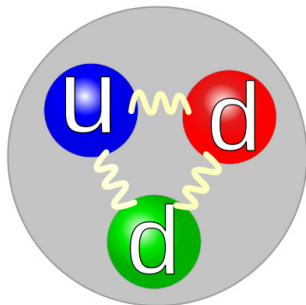
Kellogg Radiation Laboratory

Mentors: Brad Filippone, Simon Slutsky

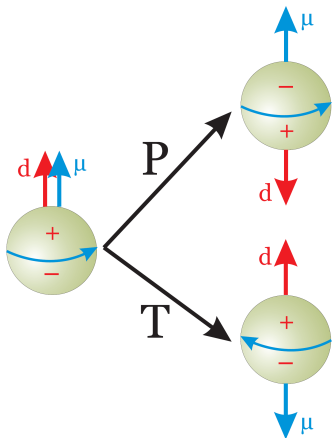
October 18, 2014

# nEDM = neutron electric dipole moment

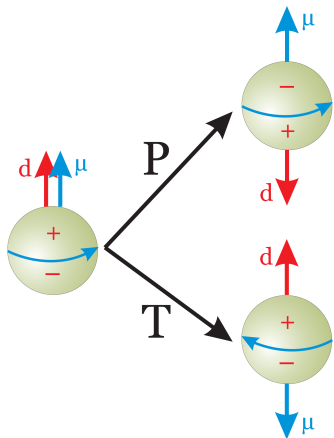
- ▶ distributed + and - charges inside neutron
- ▶ electric dipole moment (EDM) measures separation between centers of + and - charge



# why does the nEDM matter?

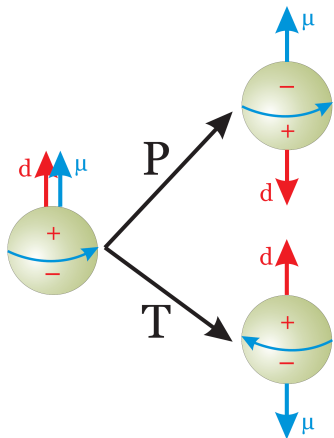


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►  $C : q \mapsto -q$

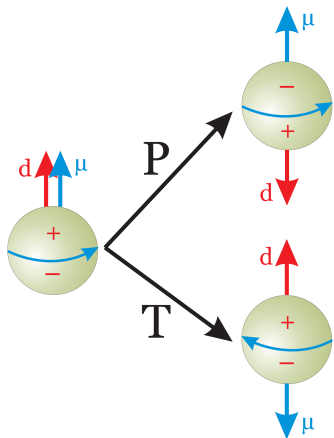
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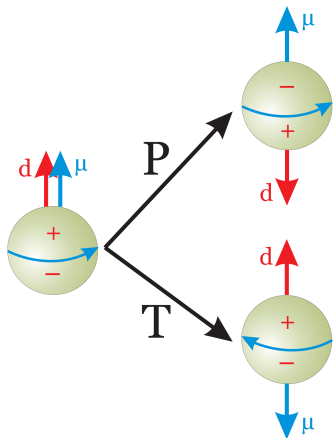
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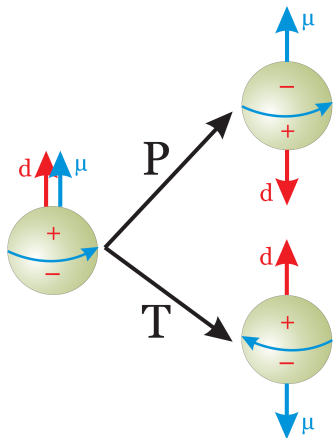
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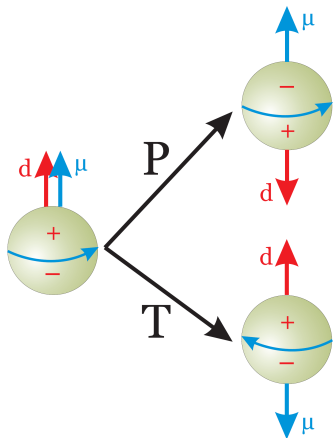
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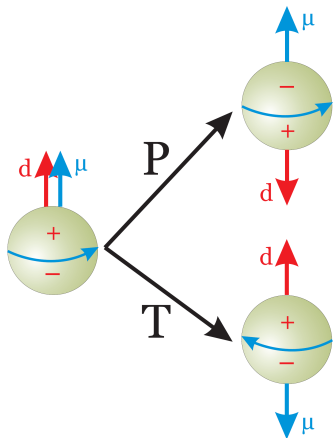


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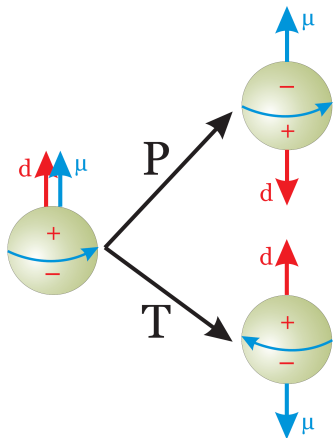
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- ▶ reformulations of Standard Model
- ▶ matter-antimatter asymmetry

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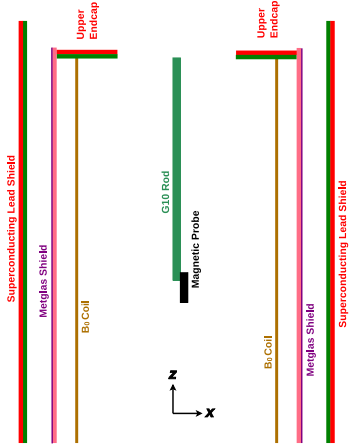
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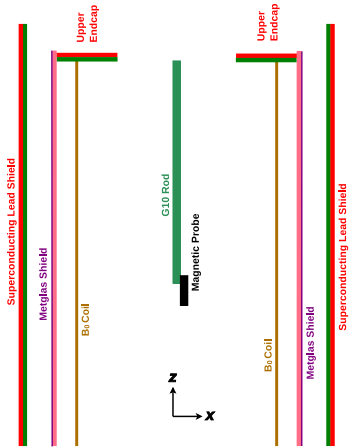
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- ▶ engineering challenge: creating an uniform magnetic field

# the half-scale model

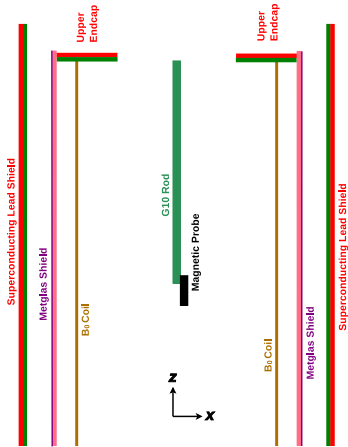


# the half-scale model



- $B_0$  coil:  $\cos \theta$  coil geometry

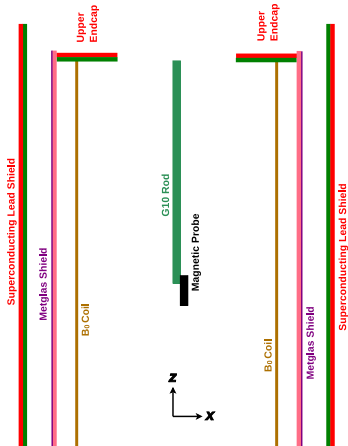
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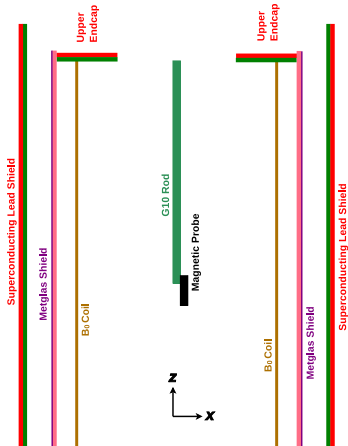


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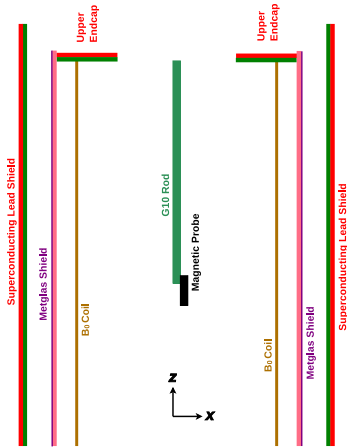
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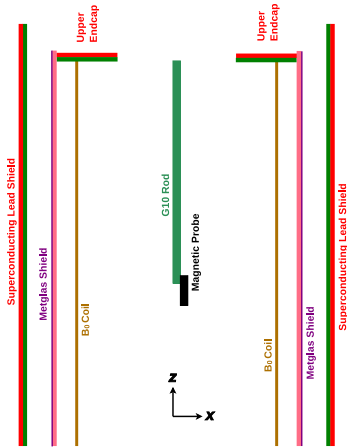
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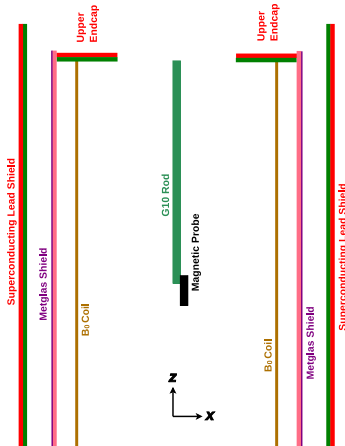
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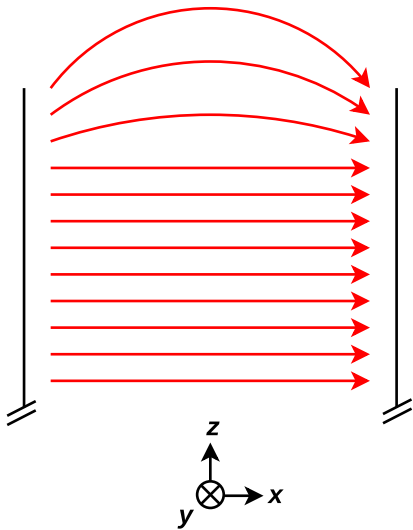
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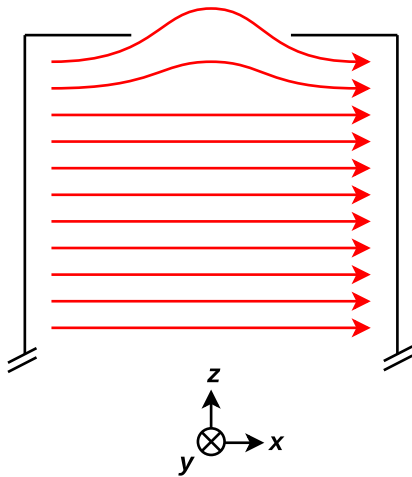
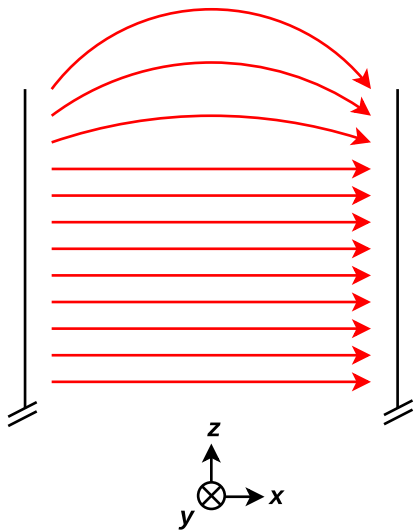


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- ▶ superconducting upper endcap

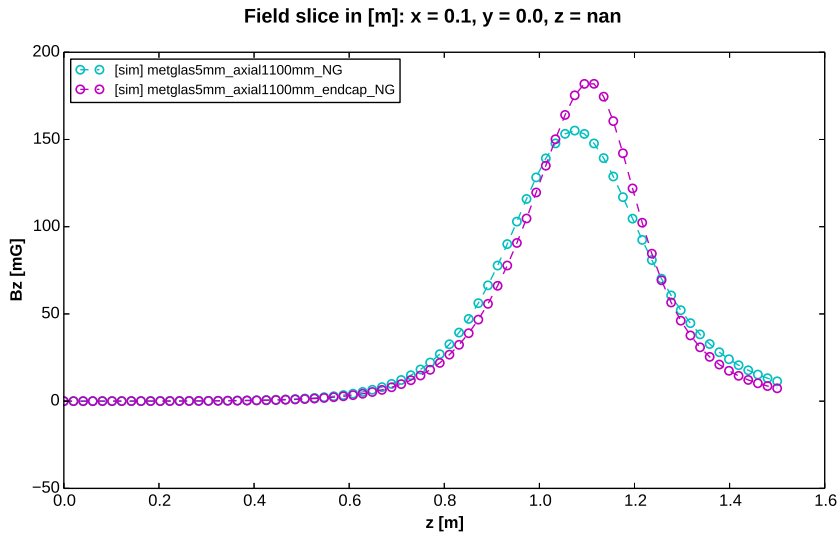
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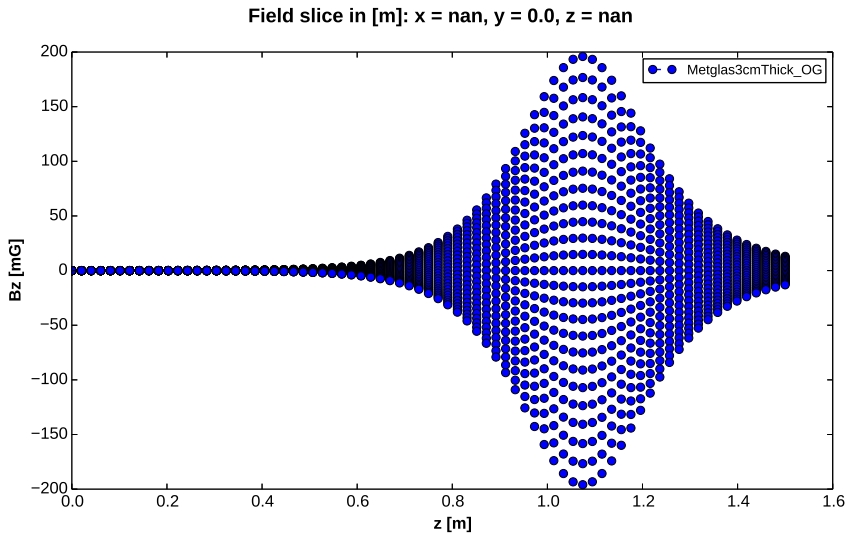


# simulations of endcap effect

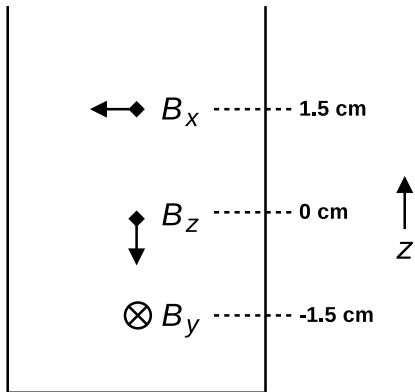




correction: probe x centering

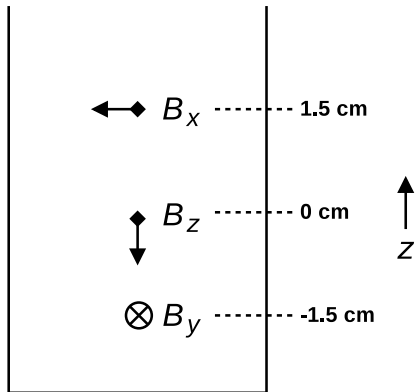


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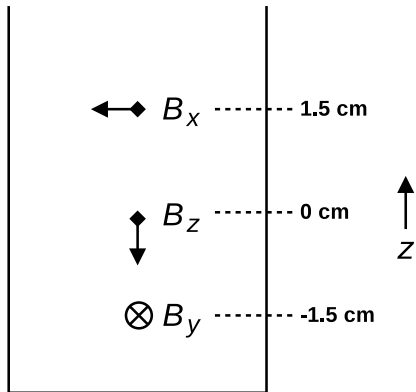
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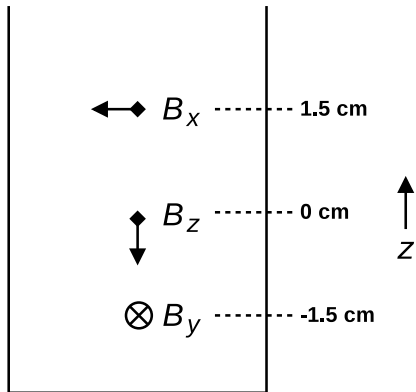
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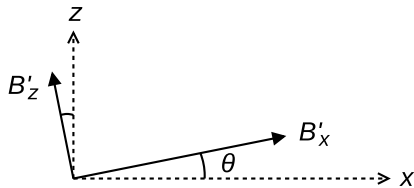
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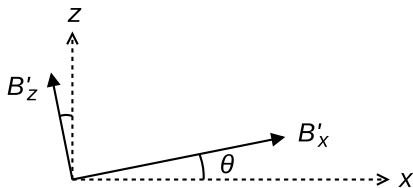


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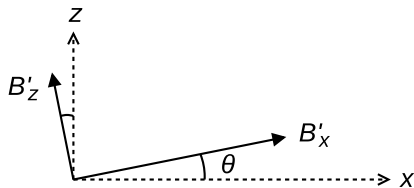


correction: probe tilt



$$B_x = B'_x \cos \theta - B'_z \sin \theta, \quad B_z = B'_z \cos \theta + B'_x \sin \theta \quad (3)$$

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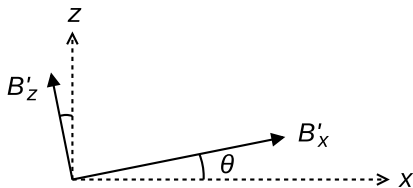


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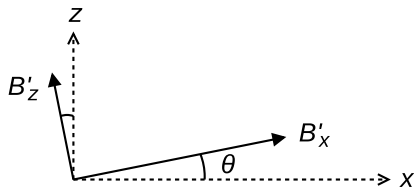


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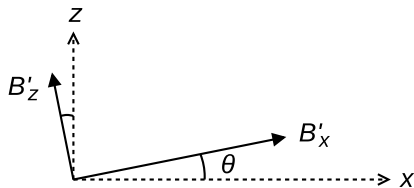
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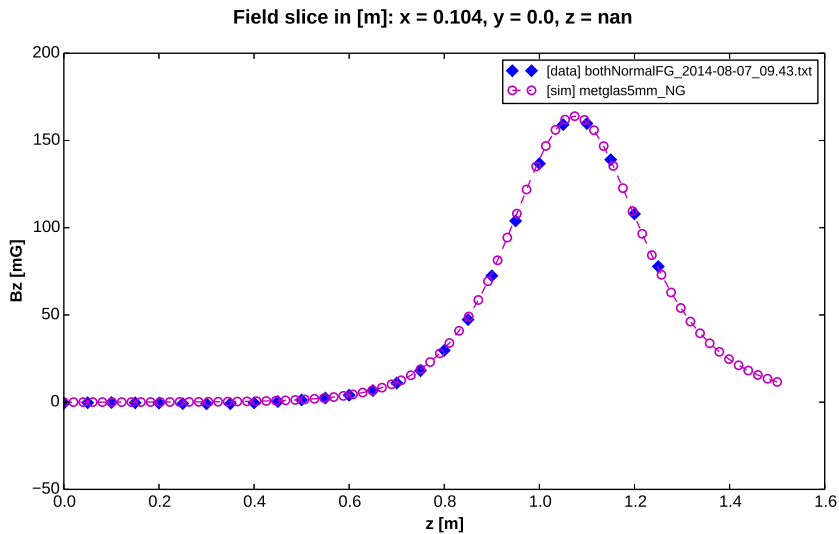
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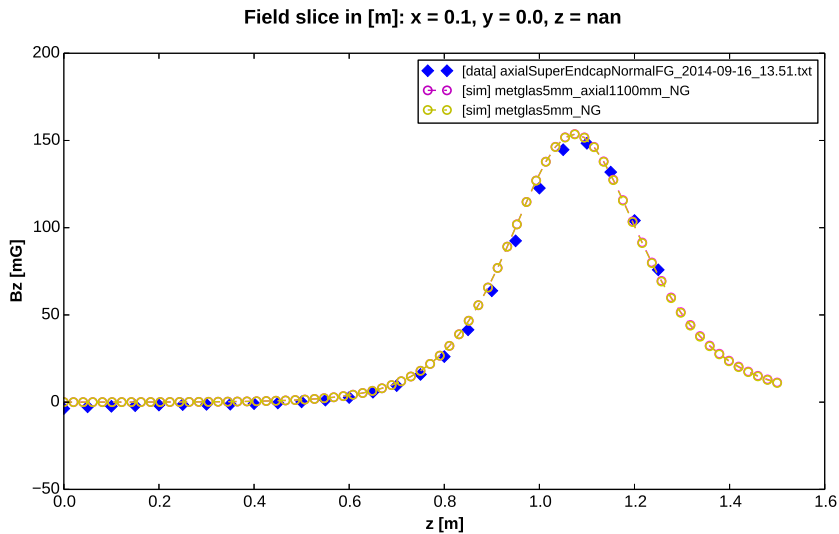
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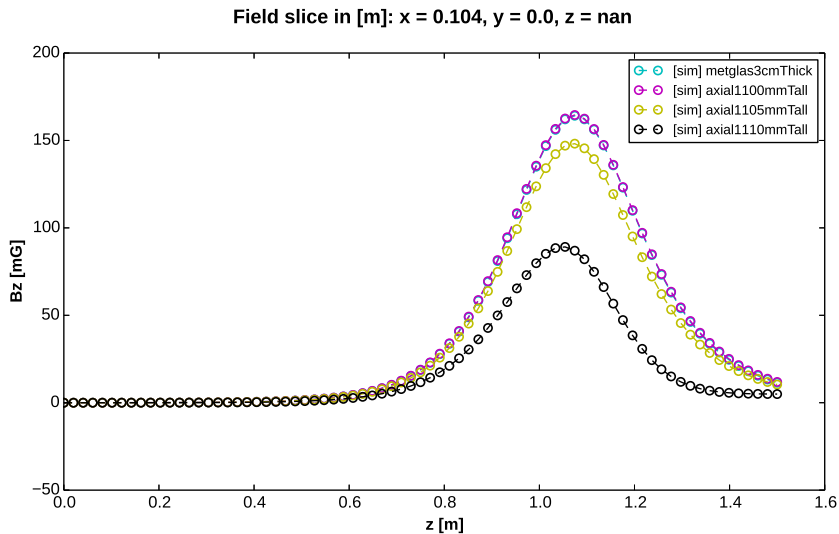
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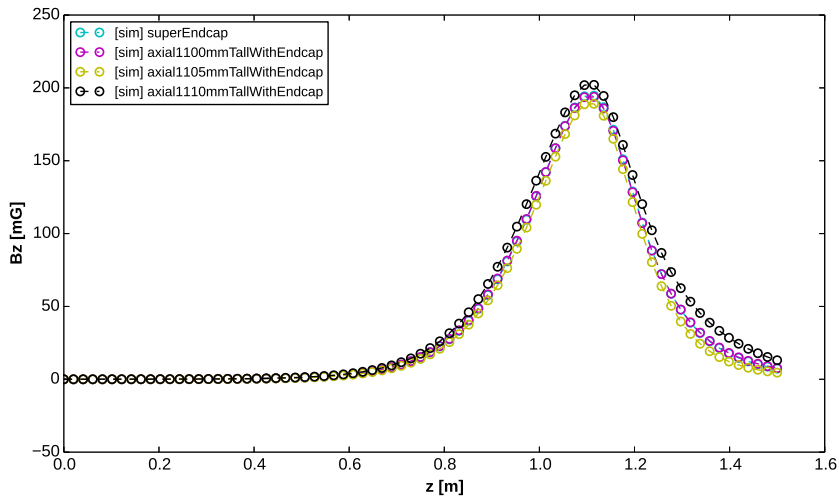


# simulation: varying axial shield height

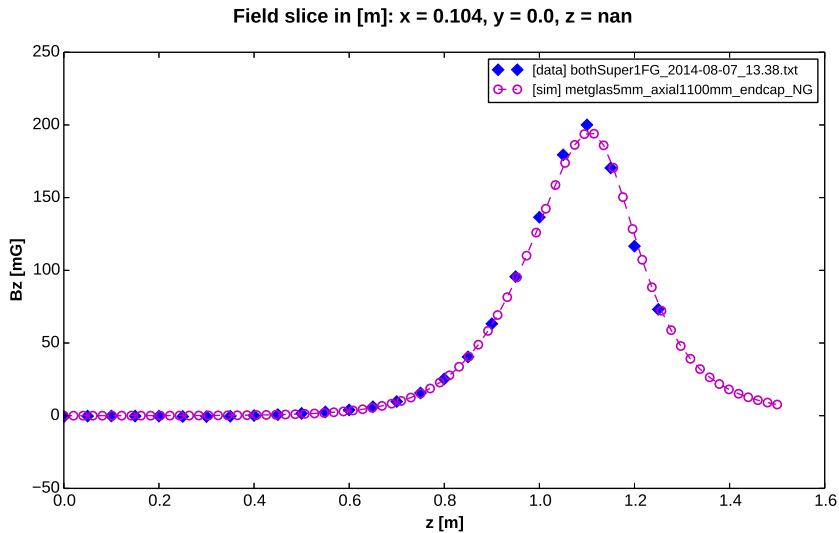


# simulation: varying axial shield height, with endcap

Field slice in [m]:  $x = 0.104$ ,  $y = 0.0$ ,  $z = \text{nan}$



# comparison: axial shield SC, endcap SC





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- ▶ our endcap seems to shift the  $B_z$  peak away from magnet center
- ▶ axial shield effect is stronger when more of it is “uncovered” by the Metglas
- ▶ SC endcap hides axial shield influence, even over small variation in height

## acknowledgments

- ▶ Mentor: Brad Filippone
- ▶ Co-mentor: Simon Slutsky
- ▶ Chris Swank, Chub Osthelder, Bob Carr
- ▶ Arthur R. Adams SFP Fellowship
- ▶ Caltech SURF Program