

HW2 - 20161595

Problem 1

2.23 value \$0 is less than \$t0

So \$t2 = 1 after slt \$t2, \$0, \$t0 statement.

value \$t2 = 1 and \$0 is not equal

So we go to ELSE: addi, \$t2, \$t2, 2 statement

After this statement, \$t2 has value 3.

∴ The value of \$t2 after the instructions = 3 (0x00000003)

2.24

0x20000000 = 0010 0000 0000 0000 0000 0000 0000 0000 ← current PC

0x40000000 = 0100 0000 0000 0000 0000 0000 0000 0000 ← wants to get

when we use jump, PC's most significant 4bit should be same. but they are different (0010, 0100). So we cannot use jump instruction to set.

And when we use beq instruction, we can get the address by currentPC + 4 + offset × 4, but offset is only 16bits. So it is too far to get 0x40000000 from 0x20000000 by using 16bits offset. So we cannot use beq instruction

∴ NO, NO

Problem 2.

2.39

lui \$t1, 8193

ori \$t1, \$t1, 18724

2.41

0000 0000 0000 0000 0000 0110 0000 0000 ← current PC

0010 0000 0000 0001 0100 1001 0010 0100 ← wants to get

when we use branch instruction, we can get the address by currentPC + 4 + offset × 4, but offset is only 16bits. So it is too far to get 0x20014924 from 0x00000600 by using 16bits offset. So we cannot use branch instruction.

∴ NO

2.42

0001 1111 1111 1111 1111 0000 0000 0000 ← Current PC
0010 0000 0000 0001 0100 1001 0010 0100 ← wants to get

when we use branch instruction, we can get the address by $\text{current PC} + 4 + \text{offset} \times 4$, but offset is only 16bits. So it is too far to get 0x20014924 from 0x1FFFF000 by using 16bits offset. So we cannot use branch instruction.

∴ NO

Problem 3

2.46.1 CPU time = Clock Cycles × clock cycle time.

$$\begin{aligned}\text{Clock Cycles}_{\text{org}} &= 5 \times 10^8 \times 1 + 3 \times 10^8 \times 10 + 1 \times 10^8 \times 3 \\ &= 3.8 \times 10^9\end{aligned}$$

$$\text{CPU time}_{\text{org}} = 3.8 \times 10^9 \times \text{Clock cycle time}_{\text{org}}$$

$$\begin{aligned}\text{Clock Cycles}_{\text{new}} &= 0.75 \times 5 \times 10^8 \times 1 + 3 \times 10^8 \times 10 + 1 \times 10^8 \times 3 \\ &= 3.675 \times 10^9\end{aligned}$$

$$\begin{aligned}\text{CPU time}_{\text{new}} &= 3.675 \times 10^9 \times 1.1 \times \text{clock cycle time}_{\text{org}} \\ &= 4.0425 \times 10^9 \times \text{clock cycle time}_{\text{org}}\end{aligned}$$

∴ It is not a good design choice, because CPU time is increased.

2.46.2

CPU time_d (double the Performance of arithmetic instructions)

CPU time₊ (improve the Performance of arithmetic instructions by 10 times)

$$\begin{aligned}\text{Clock Cycles}_d &= 5 \times 10^8 \times 0.5 + 3 \times 10^8 \times 10 + 1 \times 10^8 \times 3 \\ &= 3.55 \times 10^9\end{aligned}$$

$$\text{CPU time}_d = 3.55 \times 10^9 \times \text{clock cycle time}_{\text{org}}$$

$$\text{Clock Cycle}_+ = 5 \times 10^8 \times 0.1 + 3 \times 10^8 \times 10 + 1 \times 10^8 \times 3 = 3.35 \times 10^9$$

$$\text{CPU time}_+ = 3.35 \times 10^9 \times \text{clock cycle time}_{\text{org}}$$

$$\frac{\text{CPU time}_{\text{org}}}{\text{CPU time}_d} = \frac{3.8}{3.55} \approx 1.08$$

$$\frac{\text{CPU time}_{\text{org}}}{\text{CPU time}_+} = \frac{3.8}{3.35} \approx 1.13$$

Speed up: $\left. \begin{array}{l} 1.08 \text{ (doubled)} \\ 1.13 \text{ (10 times)} \end{array} \right\} \text{relative to original machine.}$

Problem 4.

$$\begin{array}{r} 3.6 \quad 10111001_2 \quad 185 \\ - 01111010_2 \quad -122 \\ \hline 00111111_2 \quad 63 \end{array}$$

→ no overflow and no underflow.
∴ So neither.

$$3.7 \quad 185 \rightarrow 10111001_2 \rightarrow 57 \text{ (cause it's sign-magnitude)}$$
$$-57 + 122 = 65$$

It can be stored as 8bit signed integer.

So neither.

3.18

$$74 \rightarrow 1001010_2$$

$$21 \rightarrow 0010101_2$$

∴ Starting Divisor: 00101010000000

Starting Remainder: 00000001001010

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Iteration	Step	Quotient	Divisor	Remainder
0	initial values	000 0000	0010101 000 0000	0000000 1001010
1	1: Rem = Rem - Div	000 0000	0010101 000 0000	①10 1011 1001010
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	0010101 000 0000	0000000 1001010
	3: Shift Div right	000 0000	0001010 100 0000	0000000 1001010
2	1: Rem = Rem - Div	000 0000	0001010 100 0000	①1 0110 0001010
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	0001010 100 0000	0000000 1001010
	3: Shift Div right	000 0000	000 0101 0100 0000	000 0000 1001010
3	1: Rem = Rem - Div	000 0000	000 0101 0100 0000	①11 011 0101010
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	000 0101 0100 0000	0000 0000 1001010
	3: Shift Div right	000 0000	000001010100 0000	0000 0000 1001010
4	1: Rem = Rem - Div	000 0000	0000010 1010000	①1111 01 111010
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	0000010 1010000	0000 0000 1001010
	3: Shift Div right	000 0000	0000001 0101000	0000 0000 1001010
5	1: Rem = Rem - Div	000 0000	000 0001 0101000	①11111 0100010
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	000 0001 0101000	0000 0000 1001010
	3: Shift Div right	000 0000	0000000 1010100	0000 0000 1001010
6	1: Rem = Rem - Div	000 0000	000 0000 1010100	①11111 1110110
	2b: Rem < 0 \Rightarrow +Div, sll Q, Q0=0	000 0000	000 0000 1010100	0000 0000 1001010
	3: Shift Div right	000 0000	000 0000 0101010	000 0000 1001010
7	1: Rem = Rem - Div	000 0000	000 0000 0101010	①000000 0100000
	2a: Rem \geq 0 \Rightarrow sll Q, Q0=1	000 0001	000 0000 0101010	0000 0000 0100000
	3: Shift Div right	000 0001	000 0000 0010101	0000 0000 0100000
8	1: Rem = Rem - Div	000 0001	000 0000 0010101	①000000 0001011
	2a: Rem \geq 0 \Rightarrow sll Q, Q0=1	000 0011	000 0000 0010101	0000 0000 0001011
	3: Shift Div right	000 0011	0000000 0001010	0000 0000 0001011

\therefore Quotient = $0000011_2 = 3$

Remainder = $0001011_2 = 11$

Problem 5.

3.22

$$0x0C000000 = \underbrace{0000}_{\text{sign bit: S}} \underbrace{1100}_{\text{exponent}} \underbrace{0000000000000000}_{\text{fraction}}$$

$$\text{Sign bit} = 0$$

$$\text{exponent} = 00011000_2 = 24$$

$$\text{fraction} = 0$$

$$(-1)^S \times (1 + \text{fraction}) \times 2^{(\text{exponent} - \text{bias})} = 1 \times 2^{24 - 127} = 2^{-103}$$

$$\therefore 2^{-103}$$

3.24

$$63.25 = 11111.01_2 = (1.111101) \times 2^5$$

Since we use IEEE754 double Precision format, bias is 1023.

$$S = 0$$

$$\text{exponent} = 5 + 1023 = 1028 = 10000000100_2$$

$$\text{fraction} = 1111010000000000 \dots 0000_2$$

$$\therefore 01000000010011110100000000 \dots 0000$$