

# Analysis of structural damage on the struck ship under side collision scenario

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**Abstract**—The occurrence of impact needs to be predicted for various cases as it mostly delivers negative to target object and environment. In marine structure, this phenomenon has distributed numerous damages to involved objects, such as can be found in tragedy of the Estonia in 1994. This disaster led to a reassessment of the safety of passenger ships in many country. During impact both of structural and material aspects contributes to responses in form of energy, force, and damage. In present work, consideration of the both aspects would be considered in preparation, analysis, and discussion, to evaluate contribution of considered aspects on failure characteristic. A target subjected to impact load in form of collision so called struck ship which had different hull configuration would be used in analysis as structural behaviour during and after hull structure of the struck ship was penetrated by the striking ship would be observed. In material level, analyses were conducted with applying different mechanical properties on the side structure. The results indicated that the tearing of inner hull was avoided due to size of double hull structure. This condition provided better safety but lower ship capacity. In other hand, strength characteristic of material was proofed dom-in-ate difference of internal energy. Finally, the influences of material strength, failure strain, and hardening parameter were evaluated and summarized.

**Index Terms**—Collision scenario; Finite element analysis (FEA); Hull con.guration; Material properties; Internal energy; Crushing force

## I. INTRODUCTION

Impact can be described as an applied high-magnitude load in short-time period. Involved objects that undergo this load susceptible to experience failure as most of instruments are designed to withstand gradual energy and load. This statement explicitly clarify the negative effect of impact phenomenon which closely related with failures and casualties. In naval architecture field, this load was taken seriously after catastrophe of Exxon Valdez which massively contributed to destruction

of Alaska's water territory, after received impact load in form of grounding. In other case, remarkable human life losses happened as anticipation of passenger evacuation in tragedy of the Titanic could not be fulfilled in event of collision impact. Efforts to increase safety have been conducted in various ways, including in calculation method to predict casualties on involved objects. Concept of collision energy was introduced by Minorsky [1] in 1959 who concerned regarding safety of nuclear reactor on ship. His formula was followed by analytical concept of collision by Zhang [2]. Even though the concept was simplified, but it was considered useful to estimate ship positions during collision. Recent development of ship collision was expanded into collision between structure and iceberg by Liu and Amdahl [3]. The concept of contact between two entities by Stronge [4] was developed analytically and the results was compared with finite element simulation.

As other physical phenomenon, numerous influences which come from internal or external parts can affect the result of impact between two entities or even with more subjects. In this paper, influence of structural configuration and mechanical properties of material were taken into consideration as applied parameters which were included in the internal parts. Double hull size with different width represented structure configuration, while material properties took strength characteristic, strain behaviour, and hardening parameter as selected parameters. Structural responses, including energy, force, and damage were evaluated based on applied parameters. Contribution of applied parameter would be compared in order to obtain information regarding influence level to the observed responses on the struck ship.

## II. COLLISION PHENOMENON AND MATERIAL BEHAVIOUR

The impact phenomenon may occur in several forms, especially in marine and ocean engineering. As briefly described in previous section, collision is example of impact phenomenon in the mentioned field. Remarkable damages and wide range of casualties make involved parties to take collision load into calculation for their design. This condition encourages researchers to expand their study in impact engineering to marine and ocean fields with ship is main object in their

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studies. Several researches have been addressed for different ship types, including bulk carrier [5], tanker [6], [7], barge [8], and passenger vessel [9]–[12]. Researches in collision have dominated by tanker in order to reduce possibility of oil spill, for instance by Yip et al. [13], and developed by several methods. The analytical method was developed by Hong and Amdahl in 2008 to calculate crushing resistance of web girders [14]. Experiment was also conducted by Lehmann and Peschmann [15] when they conducted collision test using NEDLLOYD 34 as the striking ship and AMATHA as the struck ship with cooperation of Germanischer Lloyd in 2002. After that empirical formula was used by Ozguc et al. [5] when they used modified Minorsky formula to estimate internal energy based on damage pattern. Improvement of energy formula was taken into consideration by Bae et al. [16] as they used proposed energy formula by Zhang (Eqs. (1)–(3)). This formula is more specific than Minorsky as given in Eqs. (4) and (5) [1], and Woisin in Eq. (6) [17] as energy can be calculated based on different damage pattern. The damage modes of some basic structural element had been investigated by several authors [18]–[22], and the mean resistance is expressed in Eq. (7), and its relation with lateral indentation is described in Eq. (8). Kitamura in 2002 introduced finite element method (FEM) approach in simulating collision phenomenon [23] which was followed with verification in method and setting of FEM [24].

$$E = 0.77\varepsilon_c\sigma_0R_T \quad (1)$$

$$E = 3.50 \left( \frac{t}{d} \right)^{0.67} \sigma_0 R_T \quad (2)$$

$$E = 3.21 \left( \frac{t}{l} \right)^{0.6} \sigma_0 R_T \quad (3)$$

$$E = 47.2R_T + 32.7 \quad (4)$$

$$R_T = \sum P_N L_N T_N + \sum P_n L_n T_n \quad (5)$$

$$E = 47.2R_T + 0.5 \sum (h.t_s^2) \quad (6)$$

$$F_m = D_1\sigma_0 t^\alpha c^\beta \quad (7)$$

$$F_p = D_2\sigma_0 t\delta \quad (8)$$

These researches are classified in large-analyses as ships are used as observation object. Smaller involved objects was reviewed in crash simulation by finite element analysis [25] and oblique impact scenario of thin-walled tube [26]. In collision study, damage is evaluated which directly receives influence from applied material on its structure or construction. Formulation of material characteristic was addressed in term of hardening parameter [27] as in isotropic hardening, the center of the yield surface is fixed but the radius is a function of the plastic strain, strain rate of steel influences yield stress of mild steel which is well known very sensitive to the strain

rate [28], and failure, for example as introduced by Jones and Wierzbicki, there are three failure modes that can be experienced by material in experiencing certain load [29]. These concepts were implemented in present work to observe behaviour of the target object when encountered impact load in form of side collision with other ship.

### III. DEFINED COLLISION SCENARIO AND NUMERICAL CALCULATION

This section presented scenario model for collision simulation. Scenario was defined including involved ships and configuration during impact. Setting and instrument for numerical calculation was described in following paragraph.

#### A. Geometry of involved ships

This work considered 85 m passenger ship as the struck ship or it would be the target of penetration by other ship. In other hand, larger cargo ship with size 144 m in length was selected to be the striking ship or the ship that would penetrate the struck ship. The detail dimension for both ships are presented in Table 1. Ship models of the struck and striking ships are presented in Fig. 1. As briefly stated in previous section, the struck ship had different structural configuration on side part of its hull. Double hull spaces with 1.5 m and 3.5 m in width were used in the analyses. The illustration and scantling data of the struck ship are presented in Fig. 2 and Fig. 3.

#### B. Collision scenario

Side collision was selected to be implemented as fundamental scenario in present work. In this situation, the striking ship penetrated side hull of the struck ship with coming angle 90 degrees or in perpendicular position. Main parameters were taken from structural level as different double hull spaces of the struck ship would be the target, and mechanical characteristic and configuration, including strength magnitude, failure strain, and hardening type had been selected as parameters in material level. Detail description regarding these configurations are presented consecutively in Table 2.

#### C. Setting for numerical calculation

The numerical calculation would be conducted by ANSYS LSDYNA [30] to perform defined collision scenario and produce structural behaviour during and after collision. In this process, the struck ship was defined as deformable structure, and rigidbody characteristic was applied in the striking ship. On both of models, plastic-kinematics material which the yield criterion is presented in Eqs. (9) and ((10)), was implemented together with element formulation Belytschko-Tsay. This formulation was considered as it was evidenced by previous author that this formulation type could produce faster results than other options in simulation setting [16]. Meshing size for each ship was given different treatment. The struck ship which was defined as deformable structure, was given meshing size according to recommendation of Tornqvist and Simonsen [31] as well as Alsos and Amdahl [32], who indicated that in order to capture local deformation pattern, the size should be

## NOMENCLATURE

$\alpha$	exponent for Eq. (7) with range 1.5–1.7	$D_2$	coefficient related to the impact position and the plate size
$\beta$	exponent for Eq. (7) with range 0.3–0.5 with $\alpha + \beta = 2$	$E$	Young's modulus (Pa)
$\beta$	hardening parameter	$E$	absorbed energy (MJ)
$\delta$	lateral indentation (mm)	$E_p$	plastic hardening modulus (Pa)
$\mathcal{E}$	strain rate ( $s^{-1}$ )	$E_{tan}$	Tangent modulus (Pa)
$\mathcal{E}_c$	critical rupture strain of the material which is determined from where $\mathcal{E}_c = 0.10(\mathcal{E}_f/0.32)$ where $\mathcal{E}_f$ is the steel material ductility obtained in tensile test	$F_m$	mean resistance (N)
$\mathcal{E}_p^{eff}$	effective plastic strain	$F_p$	resistance force (N)
$\sigma_0$	flow stress of the material (MPa)	$H$	height of rupture aperture in side shell (m)
$\sigma_o$	initial yield stress (Pa)	$L$	critical tearing length (mm)
$\sigma_y$	yield stress (Pa)	$L_N$	damage length of striking ship (m)
$C$	Cowper-Symonds strain rate parameters ( $s^{-1}$ )	$L_n$	damage length of struck ship (m)
$c$	cross-sectional length of a unit or the tearing length (mm)	$P$	Cowper-Symonds strain rate parameters
$d$	average width of the plates in the crushed cross-section (mm)	$P_N$	damage depth of striking ship (m)
$D_1$	coefficient related to the actual crushing or tearing configuration	$P_n$	damage depth of struck ship (m)
		$R_T$	destroyed material volume for both struck and striking ship/resistance factor (m <sup>3</sup> )
		$t_N$	damage thickness of striking ship (m)
		$t_n$	damage thickness of struck ship (m)
		$t_s$	side shell thickness (cm)

Table I: Configurations of the struck and striking ships.

Characteristics	Struck Passenger ship	Striking Cargo ship
Length over all (m)	85.92	144.50
Breadth moulded (m)	15.00	19.80
Design draft (m)	4.30	5.60
Depth (m)	10.40	10.20
Frame spacing (m)	0.60	-

Table II: Detail of scenario models.

Parameters	Impact scenario model		
Structural	Double hull	Space width (m)	1.50
			3.50
Material	Strength	Yield - Ultimate strengths (MPa)	180 – 325
			205 – 380
			430 – 605
			480 – 800
	Failure	Failure strain	0.1
			0.2
			0.3
			0
	Yield surface	Hardening value	0
			0.5
			1

given within range of the element-length-to-thickness (ELT) ratio 5–10.

$$\sigma_y = \left[ 1 + \left( \frac{\mathcal{E}}{C} \right)^{\frac{1}{P}} \right] (\sigma_0 + \beta E_p \mathcal{E}_p^{eff}) \quad (9)$$

$$E_p = \frac{E_{tan} E}{E - E_{tan}} \quad (10)$$

The struck ship was applied with size 80–100 mm, while the striking ship which had rigid characteristic, larger mesh with 300–700 mm in size was applied on its model. Failure on the struck ship was predicted based on applied material behaviour with strain-dependent characteristic was the main influence on failure mode. The involved objects were built using steel material and on contact area friction between steels was taken into consideration. Therefore friction coefficient between mild steel was applied in the analyses. In the finite element analysis, displacement of the struck ship was set to be fixed at the centre-line, and fixation was applied on all transverse frame and longitudinal deck in the end of model. In this location, axial displacements are restrained. The striking ship, in other hand, moved to the designated target points as presented in Fig. 4 with implemented velocity 12 knots or 6.17 m/s in SI unit. All defined scenarios were processed on high-performance computer with 4th Generation Intel Core i7-4790 Processor 4.00 GHz, 16 GB RAM.

## IV. RESULTS AND DISCUSSION

In this section, calculation results by numerical simulation would be presented. Discussion was presented based on each of applied configurations. Several responses on the struck ship was described and evaluated regarding influence degree of proposed parameters to the results.

## A. Double hull size

Safety standard of a ship against various forms of impact load (e.g. collision and grounding) can be evaluated from condition of the inner hull after resisting such damage. Breach of the inner hull can be considered fatal since damage occurs

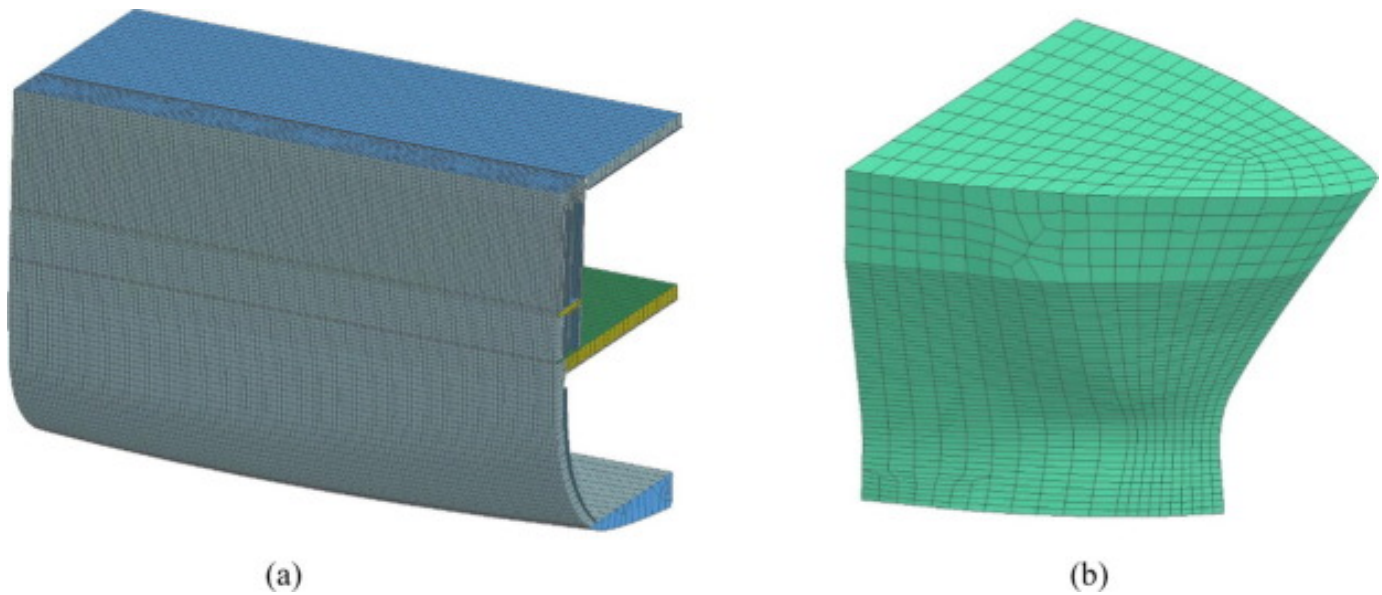


Figure 1: Involved ships for collision analysis: (a) struck ship, and (b) striking ship.

not only on ship structure, but also already reach ship cargo. Calculation results based on different hull configurations are presented in Fig. 5 and Fig. 6. Internal energy in these graphs are defined as energy that is needed to plastically deform or even destroy the involved structures in impact. In this case, the struck ship as the deformable object is observed. Energy to deform side hull with narrower space was indicated higher as both hulls (outer and inner) were significantly damaged by the striking ship during penetration. Indication of higher internal energy is not solely dictated a structural configuration has better resistance against impact load. Crushing force in the figures is defined as force fluctuation during destruction of the involved objects take place by certain impact load. The force for wider space on the struck ship was observed go down in the end of collision process as the destruction was focussed on the outer hull. Major deformation or even hole on the inner hull could be avoided as large space was provided by double hull with size

3.5 m in width. Contrast with this situation, the narrower double hull (1.5 m in width) showed rising trend line as penetration went further. This situation addressed the situation of the inner hull of this hull was slowly deformed plastically. Illustration of this phenomenon is presented in Fig. 7 and Fig. 8 for both hulls. The presented contours in these figures are von Mises stress which represent failure stress. In 1.5 m double hull, stress on the inner hull was found distributed on the area of penetrated hulls. Stress concentration was clearly indicating failure if penetration was continued on this location. Stress on inner was widely distributed on the inner hull for the larger double hull. This hull size provided adequate time during penetration to deliver the stress to other structural components. Initial conclusion based on this discussion that narrower double hull space more susceptible to failure during collision. Therefore, double hull with space 1.5 m would be used in further analyses and simulations accounting for

material configurations.

#### B. Strength characteristic

Material is inseparable element in structural analysis. In this work, this parameter is taken into consideration with deploying material with different strength magnitude. The energy results of this study indicated that the internal energy was equally perpendicular with magnitude of yield and ultimate strength. Material with higher strength needed more energy to be destroyed during penetration. Difference in yield strength between the first and second materials was found 12% and internal energy introduced 12% distinction. The third and fourth material showed difference 50 MPa in term of yield strength with energy comparison between both materials indicated 27% discrepancy. Between the first and second materials,

Difference was relative lower than the third and fourth materials, that contribution of tensile strength was taken into consideration as the third and fourth materials had bigger disparity. Behaviour of crushing force also provided good correlation since higher material strength, higher stress that would be experienced. These results are presented in Fig. 9 and Fig. 10, consecutively. Damage extents in Fig. 11 were presented by Tresca stress indicated that the higher strength would reduce casualties on the inner hull after collision process. This material was proven provide better resistance for side hull against collision by the striking ship. However, attention should be paid in term of material treatment. Higher strength tends to need more costly treatment in building and repairing processes which lead to increase of maintenance cost.

#### C. Failure strain

In analysis using strain-dependent material to predict failure pattern on the involved objects, it was considered important to evaluate how far failure strain affected calculation results.

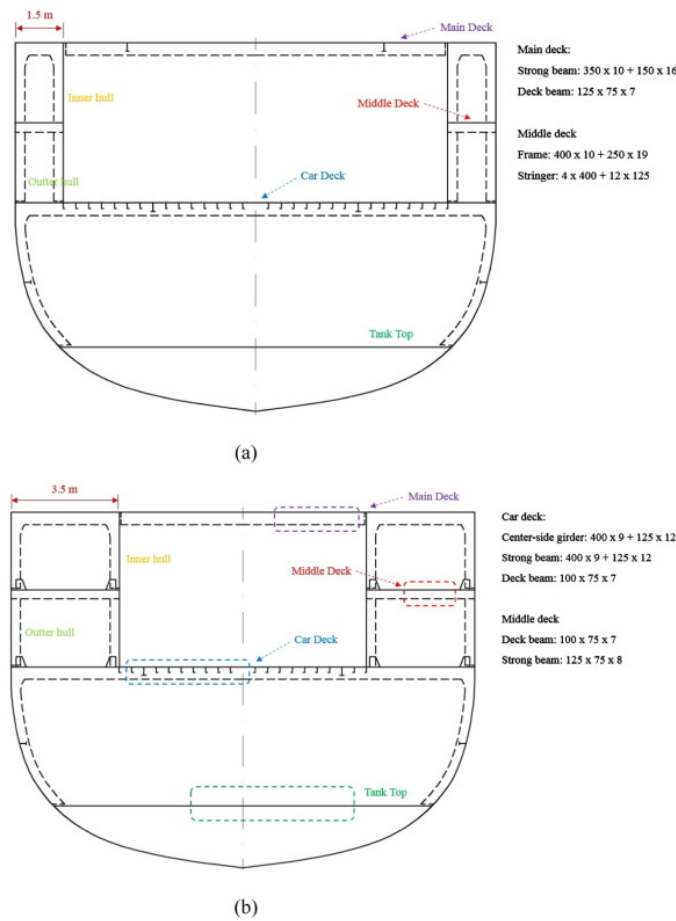


Figure 2: Configurations of double hull structure: (a) 1.5 m and (b) 3.5 m.

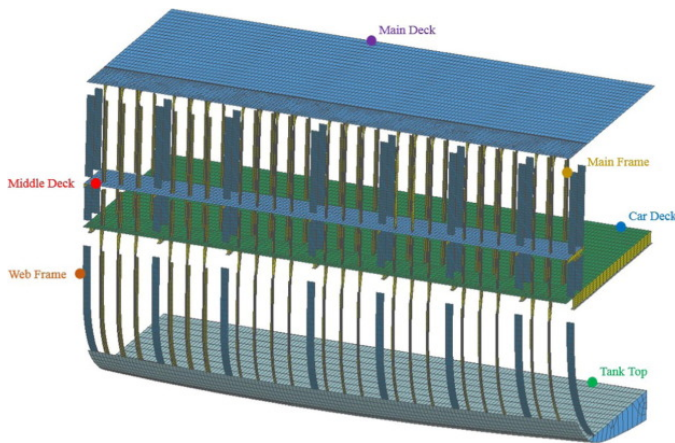


Figure 3: Structure of the struck ship. Side shell is removed to show transverse and longitudinal components.

Three different strain constants were applied on the deformable structure. Calculation results in Fig. 12 indicated that the internal energy was gradually increasing for the proposed strain constants. The target structure was shown better strain capability during penetration and made the structure was harder

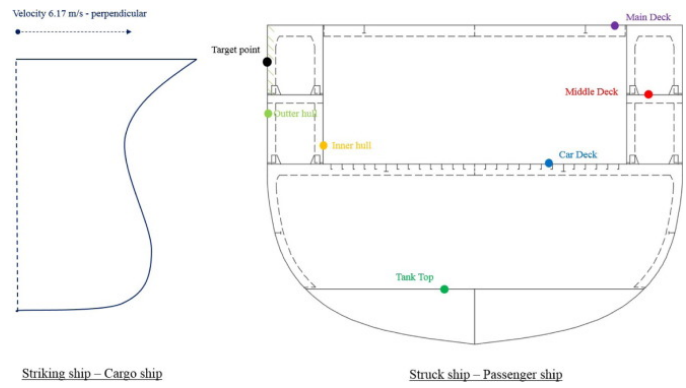


Figure 4: Illustration of side collision. Bullets highlight location of pointed components.

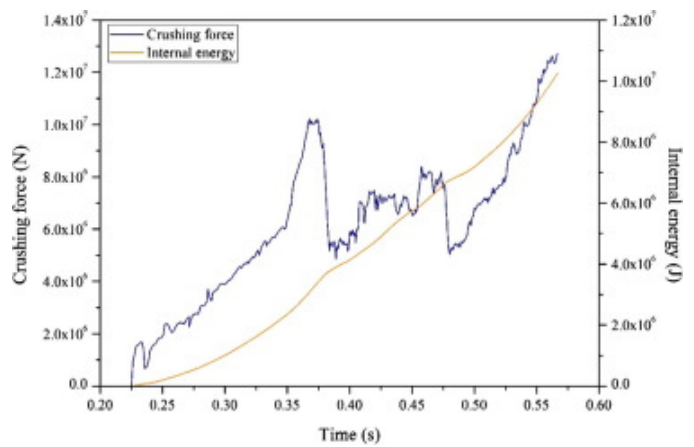


Figure 5: Crushing force and internal energy for double hull configuration 1.50m.

to experience failure. Illustration in Fig. 13 was presented wide area with was wrinkled as effect of collision load in structure with strain constant 0.3. Compared with the smallest constant which the inner hull was successfully breached and tearing was found that the striking ship clearly tore the both hulls, the strain constant 0.3 delivered better capability to resist penetration by the striking ship. Benchmarking study can be considered as good method to estimate reasonable strain constant for applied material properties in analysis.

#### D. Hardening value

Hardening was taken into consideration to observe different assumption in position of yield surface during penetration. Kinematic hardening with constant 0 indicates that the radius of the yield surface is fixed but the center translates in the direction of the plastic strain, which means it can be move as translated direction of plastic strain. In opposite of the first assumption, if the yield surface is fixed and works as function of the plastic strain, this definition is called isotropic hardening with constant 1. The transition constant 0.5 was considered in the analysis to provide intermediary comparison for kinematic and isotropic results. In term of internal energy



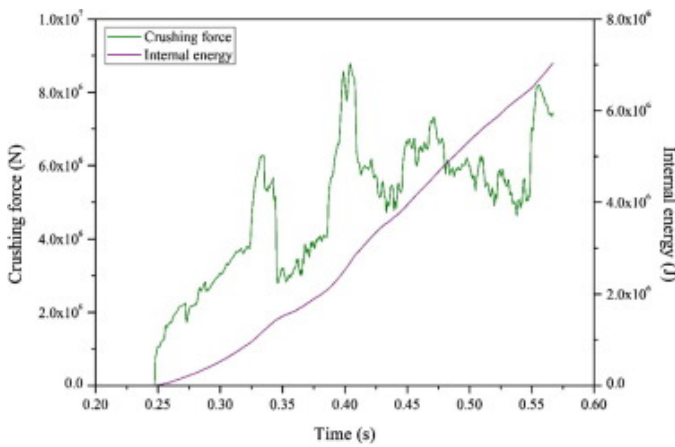


Figure 6: Crushing force and internal energy for double hull configuration 3.50m.

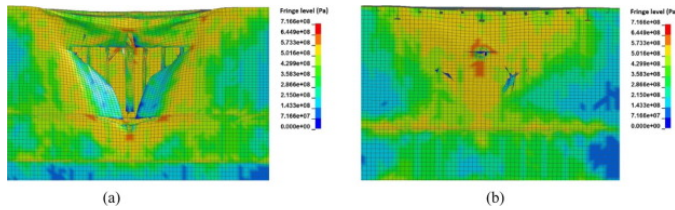


Figure 7: Damage pattern on the double hull structure with space 1.50 m: (a) outer hull, and (b) inner hull.

(Fig. 14), significant difference was unlikely found for all proposed assumptions. Trend line and value were also showing similarity in term of crushing force as presented in Fig. 15. Both responses indicated that isotropic hardening produced higher results than kinematic hardening with no remarkable characteristic. Results of the transition value 0.5 was found between kinematic and isotropic magnitudes.

## V. CONCLUSIONS

This work presented a study on structural and material aspects of double hull passenger ship as the struck ship against certain impact phenomenon. Collision with the striking ship was taken into consideration in this study with two ships involved in the proposed scenario. Discussion was initiated on structural aspect, which two different double hull sizes were compared. Results indicated that narrower the distance between the outer and inner hulls would deliver more significant effect to inner hull which could harm cargo safety. Implementation of wider double was considered good option to increase safety, but capacity of the ship would be reduced as consequences. Double hull with space 1.5 m was used in further collision analysis with different material configurations were applied. Strength characteristic was concluded deliver the most significant effect to the calculation results. Response of energy and force during collision supported this argument. Implementation of high strength material can be implemented on the side hull to give better resistance against collision load. However, treatment of this material should be given

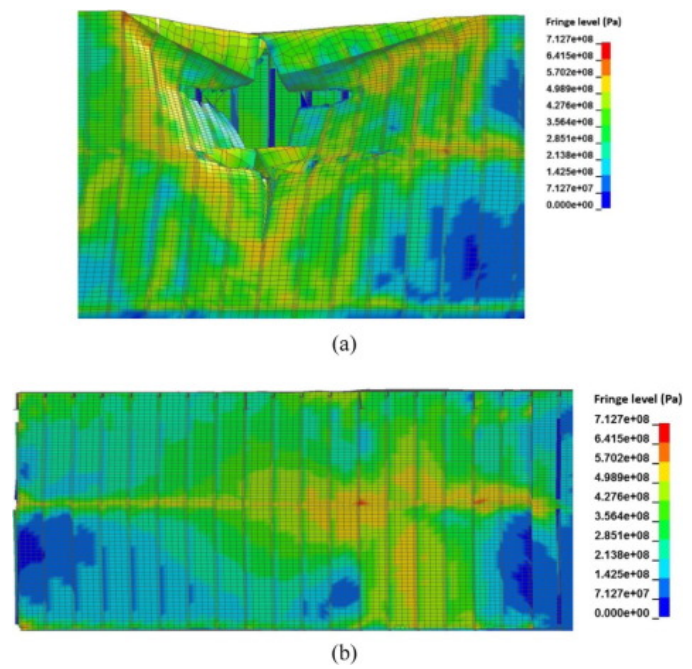


Figure 8: Damage pattern on the double hull structure with space 3.50 m: (a) outer hull, and (b) inner hull.

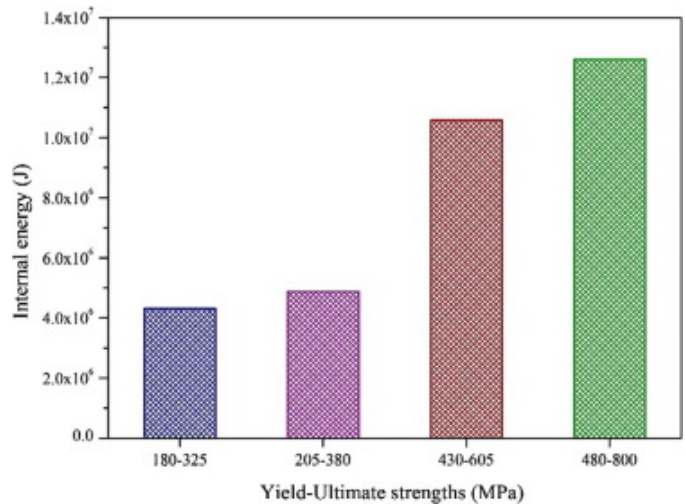


Figure 9: Internal energy for different applied material strength on the double hull structure.

serious attention as remarkable treatment cost may occur. Failure strain in other hand addressed gradual effect to internal energy as higher strain constant was used in analyses. Larger strain constant made the struck ship experienced wrinkle on the area near contact surface. The structure was also found harder to be torn by the striking ship. Assumption in yield surface was represented by hardening parameter, which was considered contribute the lowest effect to the calculation results. This study can be reasonable reference in applying material behaviour for impact analysis, especially for marine structures under collision and grounding. Further considera-

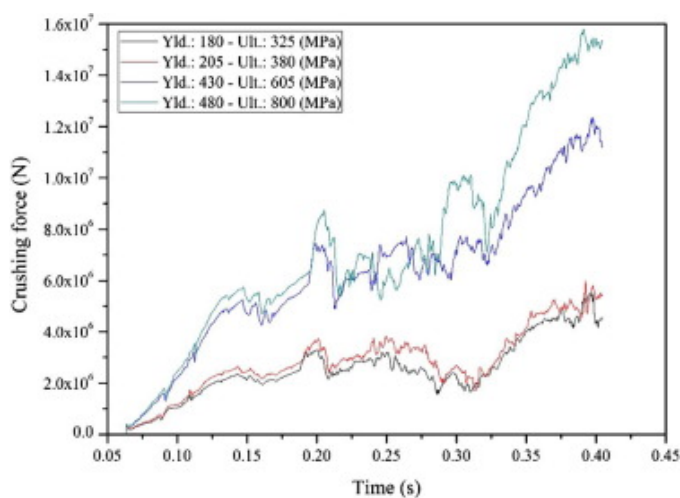


Figure 10: Characteristic of crushing force on the double hull structure with different strengths.

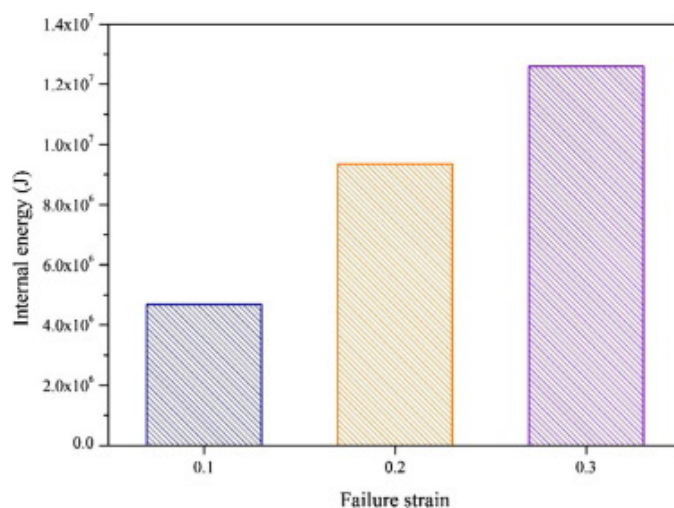


Figure 12: Effect of failure strain constant to internal energy during ship collision.

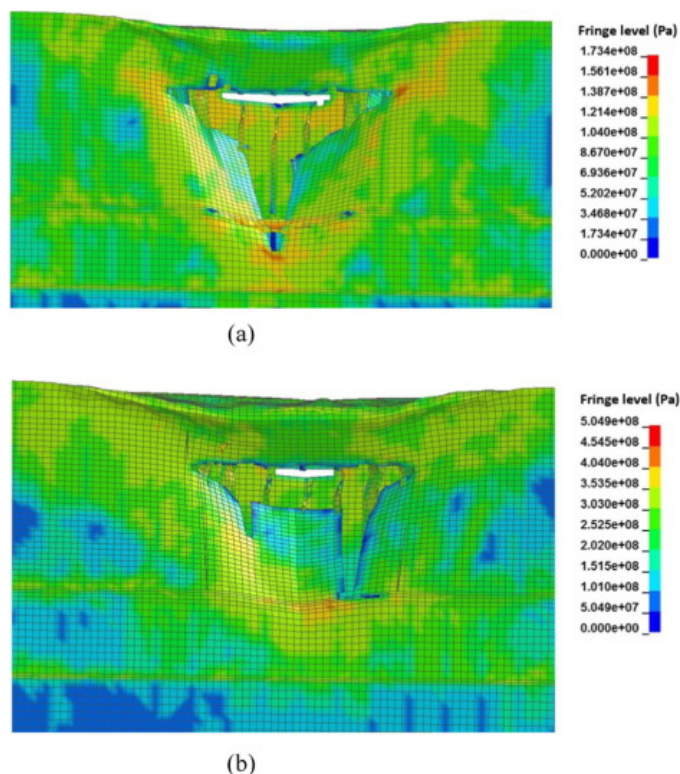


Figure 11: Damage pattern on the outer and inner hulls: (a) yield 180 MPa, and (b) yield 480 MPa.

tions in conducting material testing and laboratory experiment for nonlinear and large scale analyses can be performed to increase accuracy of material property and behaviour as they are highly encouraged by the authors.

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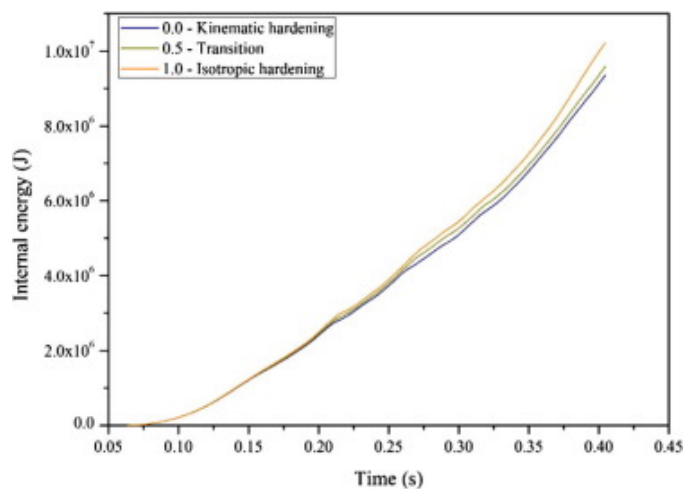


Figure 13: Internal energy for proposed assumption of yield surface. Significance is not found on the results.

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#### REFERENCES

- [1] V. Minorsky, "An analysis of ship collisions with reference to protection of nuclear power plants," Sharp (George G.) Inc., New York, Tech. Rep., 1958.
- [2] S. Zhang, "The mechanics of ship collision. technical university of denmark," Ph.D. dissertation, Doctoral Dissertation, 1999.
- [3] Z. Liu and J. Amdahl, "A new formulation of the impact mechanics of ship collisions and its application to a ship-iceberg collision," *Marine Structures*, vol. 23, no. 3, pp. 360–384, 2010.
- [4] J. Coaplen, W. Stronge, and B. Ravani, "Work equivalent composite coefficient of restitution," *International Journal of Impact Engineering*, vol. 30, no. 6, pp. 581–591, 2004.
- [5] O. Ozguc, P. K. Das, and N. Barltrop, "A comparative study on the structural integrity of single and double side skin bulk carriers under collision damage," *Marine Structures*, vol. 18, no. 7-8, pp. 511–547, 2005.

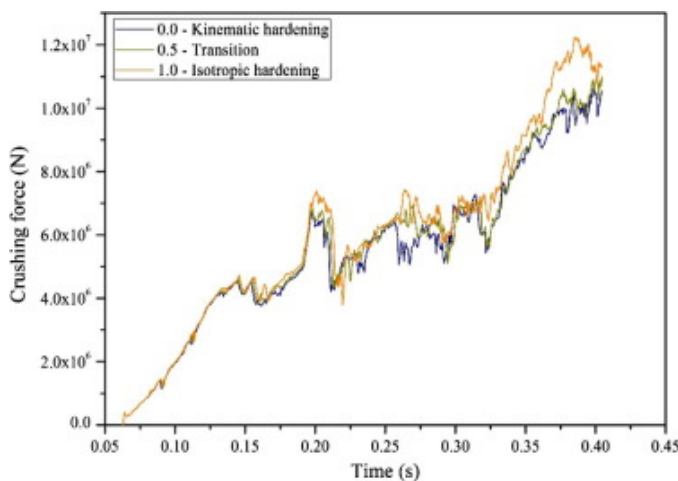


Figure 14: Crushing force during penetration by the striking ship with different assumed yield surfaces.

- [6] S. Haris and J. Amdahl, "Analysis of ship-ship collision damage accounting for bow and side deformation interaction," *Marine Structures*, vol. 32, pp. 18–48, 2013.
- [7] D. M. Bae, A. R. Prabowo, B. Cao, J. M. Sohn, A. F. Zakki, and Q. Wang, "Numerical simulation for the collision between side structure and level ice in event of side impact scenario," *Latin American Journal of Solids and Structures*, vol. 13, pp. 2991–3004, 2016.
- [8] H. Lehta, A. Elhewy, and W. E. S. Mohamed, "Finite element simulation of barge impact into a rigid wall," *Alexandria Engineering Journal*, vol. 53, no. 1, pp. 11–21, 2014.
- [9] A. R. Prabowo, D.-M. Bae, J.-M. Sohn, and A. F. Zakki, "Evaluating the parameter influence in the event of a ship collision based on the finite element method approach," *International Journal of Technology*, vol. 4, pp. 592–602, 2016.
- [10] A. R. Prabowo, D. M. Bae, J. M. Sohn, and B. Cao, "Energy behavior on side structure in event of ship collision subjected to external parameters," *Heliyon*, vol. 2, no. 11, p. e00192, 2016.
- [11] A. R. Prabowo, D. M. Bae, J. M. Sohn, A. F. Zakki, B. Cao, and Q. Wang, "Analysis of structural behavior during collision event accounting for bow and side structure interaction," *Theoretical and Applied Mechanics Letters*, vol. 7, no. 1, pp. 6–12, 2017.
- [12] A. R. Prabowo, D. M. Bae, J. M. Sohn, A. F. Zakki, B. Cao, and J. H. Cho, "Effects of the rebounding of a striking ship on structural crashworthiness during ship-ship collision," *Thin-Walled Structures*, vol. 115, pp. 225–239, 2017.
- [13] T. L. Yip, W. K. Talley, and D. Jin, "The effectiveness of double hulls in reducing vessel-accident oil spillage," *Marine Pollution Bulletin*, vol. 62, no. 11, pp. 2427–2432, 2011.
- [14] L. Hong and J. Amdahl, "Crushing resistance of web girders in ship collision and grounding," *Marine Structures*, vol. 21, no. 4, pp. 374–401, 2008.
- [15] E. Lehmann and J. Peschmann, "Energy absorption by the steel structure of ships in the event of collisions," *Marine Structures*, vol. 15, no. 4–5, pp. 429–441, 2002.
- [16] D.-M. Bae, A. R. Prabowo, B. Cao, A. F. Zakki, and G. D. Haryadi, "Study on collision between two ships using selected parameters in collision simulation," *Journal of Marine Science and Application*, vol. 15, no. 1, pp. 63–72, 2016.
- [17] G. Woisin, "Design against collision," *Advances in Marine Technology*, pp. 309–336, 1979.
- [18] J. K. Paik and P. T. Pedersen, "Ultimate and crushing strength of plated structures," *Journal of ship research*, vol. 39, no. 03, pp. 250–261, 1995.
- [19] G. Lu and C. Calladine, "On the cutting of a plate by a wedge," *International Journal of Mechanical Sciences*, vol. 32, no. 4, pp. 293–313, 1990.
- [20] T. Wierzbicki and P. Thomas, "Closed-form solution for wedge cutting force through thin metal sheets," *International Journal of Mechanical Sciences*, vol. 35, no. 3–4, pp. 209–229, 1993.
- [21] B. C. Simonsen, "Ship grounding on rock—i. theory," *marine Structures*, vol. 10, no. 7, pp. 519–562, 1997.
- [22] A. R. Prabowo, B. Cao, D. M. Bae, S. Y. Bae, A. F. Zakki, and J. M. Sohn, "Structural analysis of the double bottom structure during ship grounding by finite element approach," *Latin American Journal of Solids and Structures*, vol. 14, pp. 1106–1123, 2017.
- [23] O. Kitamura, "Fem approach to the simulation of collision and grounding damage," *Marine Structures*, vol. 15, no. 4–5, pp. 403–428, 2002.
- [24] K. Wiśniewski and P. Kołakowski, "The effect of selected parameters on ship collision results by dynamic fe simulations," *Finite elements in analysis and design*, vol. 39, no. 10, pp. 985–1006, 2003.
- [25] Y. A. Abdel-Nasser, "Frontal crash simulation of vehicles against lighting columns using fem," *Alexandria Engineering Journal*, vol. 52, no. 3, pp. 295–299, 2013.
- [26] G. Manikandaraja *et al.*, "Numerical study on energy absorbing characteristics of thin-walled tube under axial and oblique impact," *Alexandria Engineering Journal*, vol. 55, no. 1, pp. 187–192, 2016.
- [27] R. Krieg and S. Key, "Implementation of a time independent plasticity theory into structural computer programs," *Constitutive equations in viscoplasticity: Computational and engineering aspects*, pp. 125–137, 1976.
- [28] N. Jones and W. Q. Shen, "Criteria for the inelastic rupture of ductile metal beams subjected to large dynamic loads," *Structural crashworthiness and failure*, pp. 95–130, 1993.
- [29] N. Jones, *Structural impact*. Cambridge university press, 2011.
- [30] A. L.-D. ANSYS, "user guide, ansys," *Inc. version*, vol. 15, 2017.
- [31] R. Toernqvist and B. C. Simonsen, "Safety and structural crashworthiness of ship structures; modelling tools and application in design," *Society of Naval Architects of Japan*, pp. 285–294, 2004.
- [32] H. S. Alsos and J. Amdahl, "On the resistance of tanker bottom structures during stranding," *Marine Structures*, vol. 20, no. 4, pp. 218–237, 2007.