

ÖGOR Summer-Workshop for PhD-candidates and Post-Docs

An introduction to Julia and JuMP for Operations Research

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August 2023

Short bio



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1. Teaching areas

- ▶ Optimization: operations research; discrete and combinatorial optimization; multi-objective optimization.
- ▶ Artificial intelligence: metaheuristics; multi-objective metaheuristics.
- ▶ Computer science: Introduction to computer concepts; Julia programming language.

2. Research areas

- ▶ Optimization: operations research; multi-objective optimization.
- ▶ Artificial intelligence: metaheuristics.
- ▶ Scientific computing: MIP solvers.
- ▶ Applications: railway transportation, autonomous vehicles.

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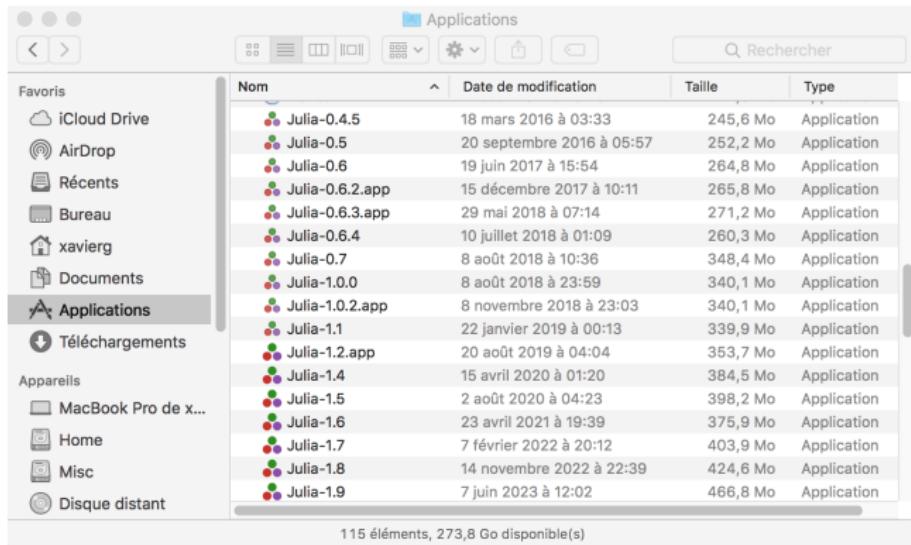
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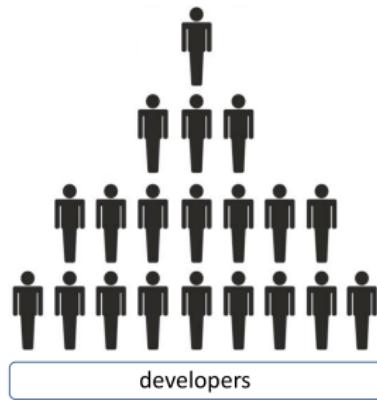
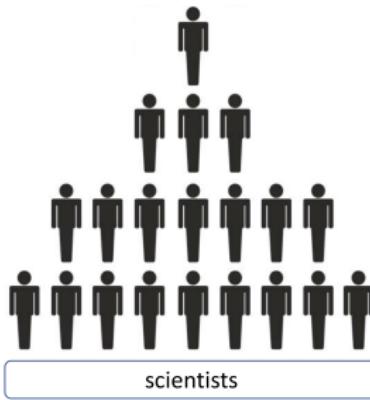
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My story with Julia and JuMP: ROADEF'2016 (Feb 2016)



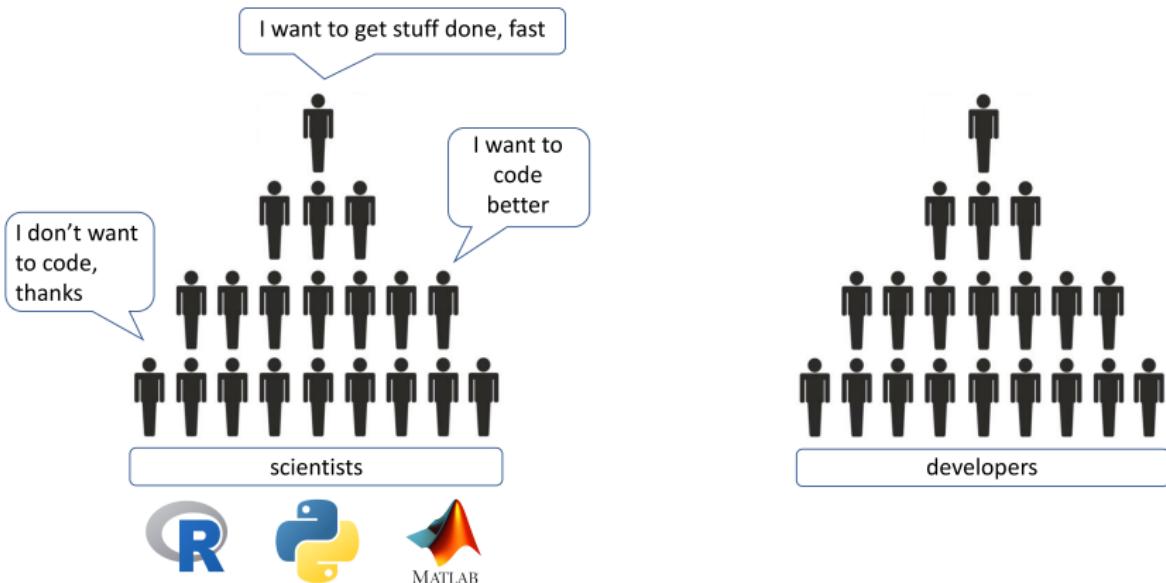
Julia

A programming language for optimization?



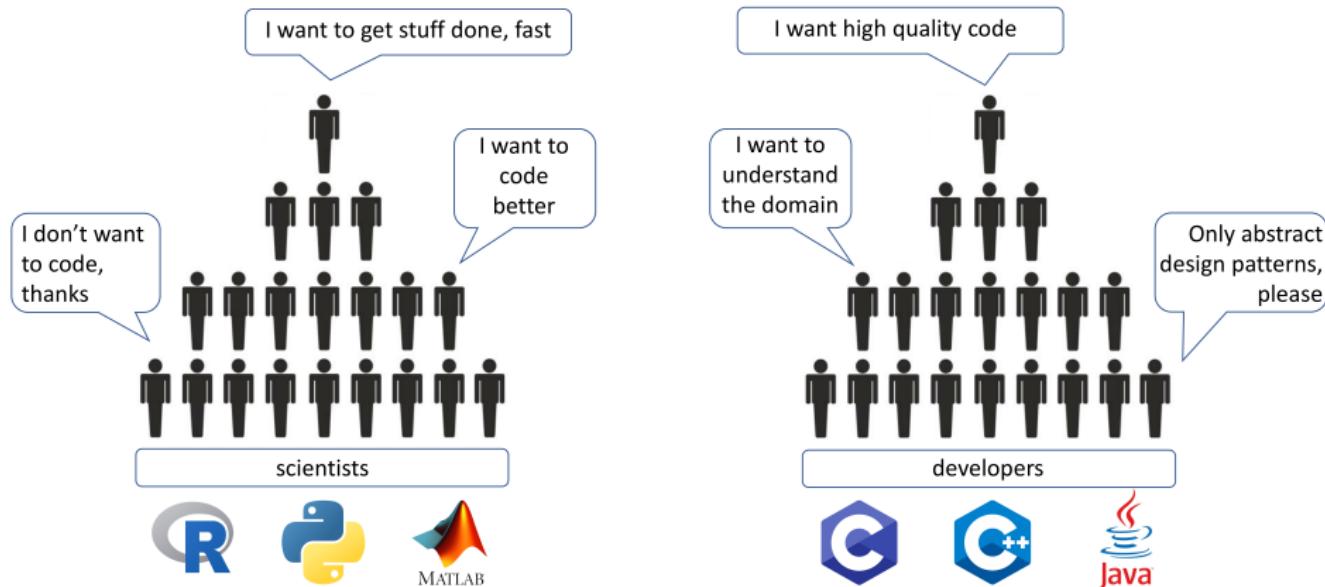
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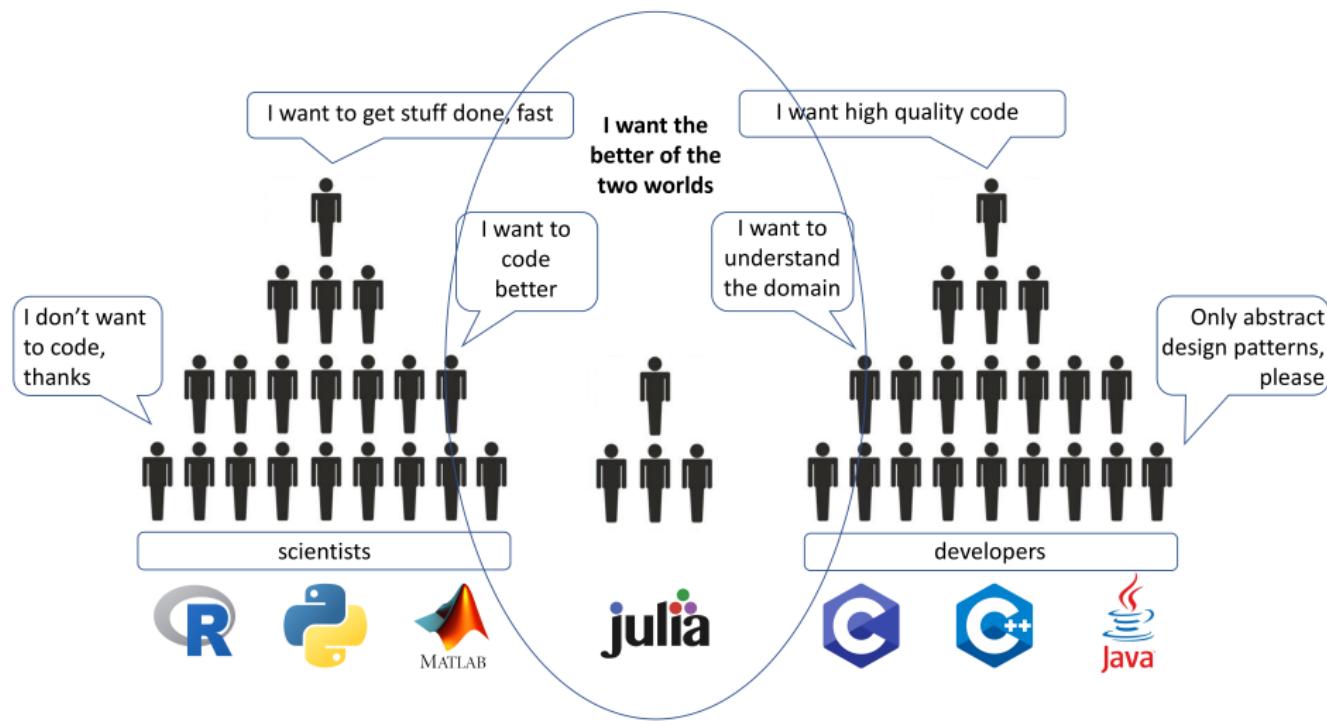
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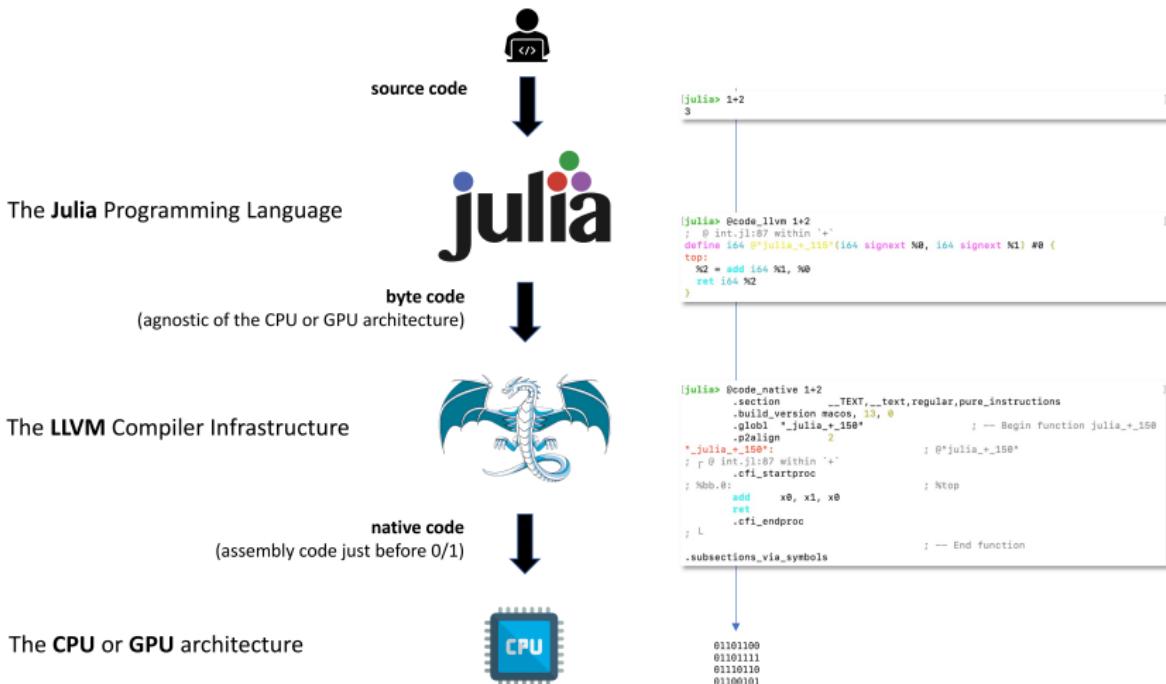
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Julia

LLVM: middleman between source code and compiled native code



Julia

Example: how to get the column sums of a matrix ...

$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$$



$$V = \begin{pmatrix} 4 & 6 \end{pmatrix}$$

... in C/C++ ?

Julia

Example: how to get the column sums of a matrix?

Assembler

C/C++

Julia

```
1 #include <stdio.h>
2 #define nLin 2
3 #define nCol 2
4
5 int main(void)
6 {
7     int A[nLin][nCol] = {{1,2} , 
8     | | | | | {3,4}};
9     int V[nCol];
10    int i, j;
11
12    for (j = 0; j < nCol; j++)
13    {
14        V[j] = 0;
15        for (i = 0; i < nLin; i++)
16            V[j] += A[i][j];
17        printf("%3d ", V[j]);
18    }
19    printf("\n");
20    return 0;
21 }
22 }
```

Julia

Example: how to get the column sums of a matrix?

Assembler

```
26    str  x8, [sp]
27    ldr  x8, [x0]
28    str  x8, [sp, #8]
29    mov  x8, sp
30    str  x8, [x0]
31
32    ldr  x1, [x20]
33    mov  x0, x19
34    mov  x2, #0
35    bl   _jl_reducedim_initarray
36    mov  x20, x0
37    str  x0, [sp, #16]
38    mov  x8, #16720
39    movk x8, #6110, lsl #16
40    movk x8, #1, lsl #32
41    mov  x9, #38880
42    movk x9, #6109, lsl #16
43    movk x9, #1, lsl #32
44
45    stp  x8, x9, [sp, #32]
46    stp  x0, x19, [sp, #48]
47    add  x1, sp, #32
48    mov  x0, #13456
49    movk x0, #6286, lsl #16
50    movk x0, #1, lsl #32
51    mov  w2, #4
52    bl   "jl_mapreducedim!_1977"
53    ldr  x8, [sp, #8]
54    str  x8, [x21]
55
56    mov  x0, x20
57    ldp  x20, x30, [sp, #96]
58    ldp  x20, x19, [sp, #80]
59    ldp  x22, x21, [sp, #64]
60    add  sp, sp, #112
61    ret
```

C/C++

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12     for (j = 0; j < nCol; j++)
13     {
14         V[j] = 0;
15         for (i = 0; i < nLin; i++)
16             V[j] += A[i][j];
17         printf("%d ", V[j]);
18     }
19     printf("\n");
20     return 0;
21 }
22 }
```

Julia

```
1  A = [1 2; 3 4]
2  V = sum(A, dims=1)
3  println(V)
4
```



version 1.9.x and later

Why Julia?

1. Runs like C, walks like Python, talks like Lisp

- ▶ Same speed as C or FORTRAN code
- ▶ Development dynamic like writing python code
- ▶ Less object-oriented more function-oriented (like Lisp)

⇒ High-level and high-performance!

⇒ Extremely good ratio between coding time and running time.

⇒ Familiar for the users of Matlab, Fortran, Python, C/C++, etc.

2. Additional value

- ▶ Open source: MIT license, source code available on GitHub
- ▶ Multi-platform (x86, ARM, Apple Silicon, etc.)
- ▶ Cross-language support: C, FORTRAN, python, R ... from Julia
- ▶ Rich set of packages: Optimisation, Plotting, Visualisation, Statistics, Data science, GPU, etc.

⇒ Ideal for the development of efficient open-source app

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A high-level, high-performance programming language for scientific computing

<https://julialang.org/>

- ▶ Timeline:
2009...2012 @ MIT, USA
version 1.0.0 in 2018; version 1.9.1 (June 7, 2023)
- ▶ Communities:
Over 9,100 Julia packages <https://julialang.org/packages/>
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Key concepts

- ▶ Julia has an LLVM-based Just-in-time compilation (JIT)
- ▶ Compilation down to native code (running on CPU and GPU, ...)
- ▶ Julia is dynamically typed, provides multiple dispatch
- ▶ Julia has many built-in mathematical functions
- ▶ A built-in package manager
- ▶ Designed for parallelism and distributed computation

Resources

Some URL to know:

- ▶ Official website

<https://julialang.org/>

- ▶ Official documentation (online and pdf)

<https://docs.julialang.org/>

- ▶ Julia channel on *youtube*

https://www.youtube.com/channel/UC9IuUwwE2xdjQUT_LMLONoA/featured

- ▶ Questions and discussion on *discourse*

<https://discourse.julialang.org/>

- ▶ Book online « Think Julia: How to Think Like a Computer Scientist »

<https://benlauwens.github.io/ThinkJulia.jl/latest/book.html>

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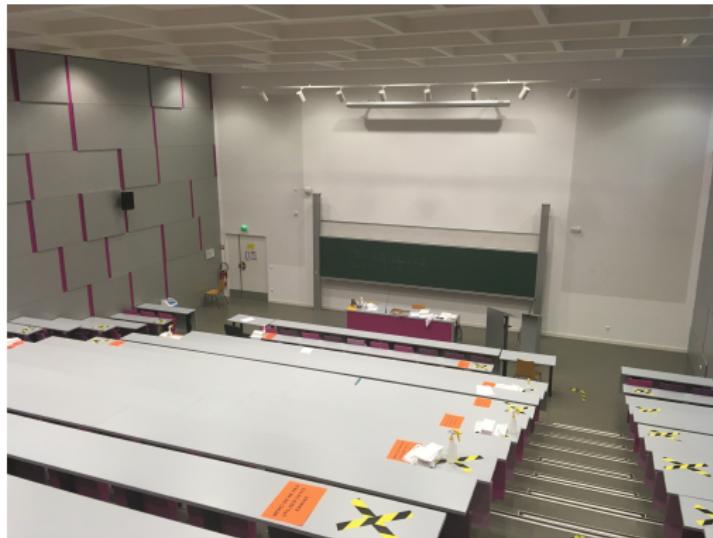
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An introduction to Julia and JuMP for OR

Planning, organisation



Planning, organisation

Planning:

- ▶ 2 days, notions and practices
- ▶ AM: 09h00 → 12h00
- ▶ PM: 13h30 → 16h30

Content of the course:

- ▶ Day 1: **Julia**
Crash course in Julia, optimization algorithms with Julia
- ▶ Day 2: **JuMP**
Optimization models and algorithms with JuMP

Profile of the public for this course

Level of fluency with

- a programming language..... ★ ★ ★ ☆ ☆
- data structures..... ★ ★ ☆ ☆ ☆
- LP/IP/MIP optimisation..... ★ ★ ★ ☆ ☆
- an algebraic modeling language... ★ ★ ★ ☆ ☆

