Software for modeling and solving multi-objective optimization problems in 2025

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* Speaking in personal capacity. Views and opinions expressed do not necessarily reflect those of NU&LS2N

RAMOO'2025

September 2025 — TU Munich @ Straubing, Germany https://github.com/xgandibleux/RAMOO2025

Mathematical Program Software for Multi-Objective Optimization in 2025

Seminal:

ADBASE × LP 1975

Full* open-source (LP/*,

file			Y_{SN}	2014	last rev 2017	
ZIMPL		MIP	Y_N	2016	last rev 2017	
file			Y_{SN}	2016?	last rev 2024	
	several MILP solvers	MIP/NLP	Y_N	2017	last rev 2025	
file	Gurobi/CPLEX	MIP/Q	Y_{SN}	2020?	last rev 2025	
		MIP	1	since Ve	er1.10?, 2025?	
	several MILP solvers	MIP/C	1			

Commercial (LP/MIP/*)

Oommicroidi (Er /	/ /-				
			NLP	Y_R	
				1	since Ver7.0, 2016
				1	since Ver12.7, 2016
				1	since Ver9.0, 2022
				1	since Ver12.0, 2023
				1	since 2025?
		several MILP solvers	NLP	1	
		several MILP solvers	NLP	Y_N	

Seminal:

ADBASE × LP 1975

Full* open-source (LP/*):

BENSOLVE polySCIP inner vOptSolver MOA PaMILO	file ZIMPL file JuMP file	GLPK SCIP GLPK several MILP solvers Gurobi/CPLEX	MIP MIP/NLP MIP/Q	Y_{SN} Y_{N} Y_{SN} Y_{N} Y_{SN}	2014 2016 2016? 2017 2020?	last rev 2017 last rev 2017 last rev 2024 last rev 2025 last rev 2025
			MIP	1	since Ve	r1.10?, 2025?
		soveral MILP solvers	MID/C	-1		

Commercial (LP/MIP/*

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			NLP	Y_R	
				1	since Ver7.0, 2016
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		several MILP solvers	NLP	1	
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Seminal:

ADBASE × LP 1975

Full* open-source (LP/*):

BENSOLVE	file	GLPK		Y_{SN}	2014	last rev 2017
polySCIP	ZIMPL	SCIP	MIP	Y_N	2016	last rev 2017
inner	file	GLPK	•	Y_{SN}	2016?	last rev 2024
vOptSolver MOA	JuMP	several MILP solvers	MIP/NLP	Y_N	2017	last rev 2025
PaMILO	file	Gurobi/CPLEX	MIP/Q	Y_{SN}	2020?	last rev 2025
	api	HiGHS	MIP	1	since Ve	er1.10?, 2025?
	CVXPY	several MILP solvers	MIP/C	1	?	

Commercial (LP/MIP/*

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			NLP	Y_R	
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		several MILP solvers	NLP	1	
		several MILP solvers	NLP	Y_N	

Seminal:

ADBASE × LP 1975

Full* open-source (LP/*):

BENSOLVE file GI PK Y_{SN} 2014 last rev 2017 polySCIP ZIMPL SCIP MIP Y_N 2016 last rev 2017 inner file GI PK Y_{SN} 2016? last rev 2024 vOptSolver MOA JuMP several MILP solvers MIP/NI P Y_N 2017 last rev 2025 **PaMILO** file Gurobi/CPLEX MIP/Q Y_{SN} 2020? last rev 2025 MIP api HiGHS 1 since Ver1.10?, 2025? MIP/C **CVXPY** several MILP solvers 1 ?

Commercial (LP/MIP/*):

Matlab	aml api api, OPL api	(meta)heuristics Gurobi Optimization IBM ILOG CPLEX Optimisation FICO Xpress Optimization	NLP	<i>Y_R</i> 1 1 1	? since Ver7.0, 2016 since Ver12.7, 2016 since Ver9.0, 2022
	aml api	Hexaly Optimizer Cardinal Optimizer (COPT)		1 1	since Ver12.0, 2023 since 2025?
		several MILP solvers	NLP NLP		

Seminal:

ADBASE × LP 1975

Full* open-source (LP/*):

BENSOLVE	file	GLPK	•	Y_{SN}	2014	last rev 2017
polySCIP	ZIMPL	SCIP	MIP	Y_N	2016	last rev 2017
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PaMILO	file	Gurobi/CPLEX	MIP/Q	Y_{SN}	2020?	last rev 2025
	api	HiGHS	MIP	1	since Ve	r1.10?, 2025?
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Commercial (LP/MIP/*):

Matlab	aml api api, OPL api aml api	(meta)heuristics Gurobi Optimization IBM ILOG CPLEX Optimisation FICO Xpress Optimization Hexaly Optimizer Cardinal Optimizer (COPT)	NLP	<i>Y_R</i> 1 1 1 1	? since Ver7.0, 2016 since Ver12.7, 2016 since Ver9.0, 2022 since Ver12.0, 2023 since 2025?
	AMPL	several MILP solvers	NLP	1	?
	GAMS	several MILP solvers	NLP	<i>Y</i> _N	?

JuMP
+
vOptSolver | MultiObjectiveAlgorithms
+
MP solvers

for MOLP/MOMIP

From vOptGeneric to MultiObjectiveAlgorithms

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2015: Kick-off of vOpt ANR/DFG project
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2017: Introduction of vOptSolver (vOptGeneric, vOptSpecific)

2018: Julia 1.0

2019: End of vOpt project

2019: First discussions on discourse/new design of MOO in JuMP

2022: JuMP 1.0

2023: Introduction of MultiObjectiveAlgorithms.jl

2023: End of vOptGeneric.jl

From vOptGeneric.jl:

- ▶ part concerning the MO model → JuMP.jl
- ▶ part concerning MO algorithms → MultiObjectiveAlgorithms.jl

Workflow for users for modeling and solving a MOP

Formulate a MOP problem	Julia (JuMP)
Provide the data	Julia
► Select the solver to use	Julia (*)
Select the algorithm to apply	Julia (MOA)
Solve the given MOP problem	Julia (MOA)
► Query the efficient solutions & nondominated points	Julia (MOA)
Analyze the results	Julia

^{*}among: GLPK, HiGHS, SCIP, CPLEX, Gurobi, Xpress, COPT...

Examples of algorithms currently available (v1.6.0)

 MOA.Lexicographic() [default] 	$p\geqslant 2$
2. MOA.Dichotomy()	p = 2
3. MOA.EpsilonConstraint()	p = 2
4. MOA.KirlikSayin()	<i>p</i> ≥ 2
5. MOA.DominguezRios()	<i>p</i> ≥ 2
6. MOA.TambyVanderpooten()	<i>p</i> ≥ 2

+ optimization attributes coming with a given algorithm

Discussion of two implementations

Discussion of two implementations

A detailed look at:

- 1. the Augmented Weighted Chebyshev scalarizing function
- 2. the Dächert-Gorski-Klamroth (2012) algorithm

after few words about JuMP and MultiObjectiveAlgorithms...

(switch on the notebook)

Final discussion

To...

- all users: your experiences and feedback
- advanced users: integration of (your) published MO algorithms

are welcome!

Advertisement (1/2)



European conference on the Julia programming language October 2-3, 2025 — Paris (France) https://juliacon.org/

Keynote Speakers:

Laura Grigori (EPFL, Switzerland) Ivet Galabova (HiGHS, Scotland) Tim Besard (JuliaHub, Belgium)

Venue:



Advertisement (2/2)

JuMP-Dev 2025

co-located with the 57th ORSNZ

November 17–20, 2025 — Auckland, New Zealand https://jump.dev/meetings/jumpdev2025/

Contact: Oscar Dowson

JuliaCon Global 2026

August 10-15, 2026 — Johannes Gutenberg Univ. Mainz, Germany https://juliacon.org/2026/

Contact: Valentin Churavy

Thanks!

 Jeff Bezanson, Alan Edelman, Stefan Karpinski, Viral B. Shah (2017). Julia: A Fresh Approach to Numerical Computing. SIAM Review 59, 65–98.

Julia:

```
https://julialang.org/
```

 Miles Lubin, Oscar Dowson, Joaquim Dias Garcia, Joey Huchette, Benoît Legat, Juan Pablo Vielma (2023). JuMP 1.0: Recent improvements to a modeling language for mathematical optimization. *Mathematical Programming Computation*.

JuMP:

```
https://jump.dev/
```

 Oscar Dowson, Xavier Gandibleux, Gokhan Kof (2025). MultiObjectiveAlgorithms.jl: a Julia package for solving multi-objective optimization problems. e-preprint (arXiv), https://arxiv.org/abs/2507.05501

MultiObjectiveAlgorithms:

```
https://github.com/jump-dev/MultiObjectiveAlgorithms.jl
```

Xavier Gandibleux (2023)

An introduction to Julia and JuMP for Operations Research ÖGOR Summer-Workshop for PhD-candidates and Post-Docs (Krems, Austria)

https://github.com/xgandibleux/Krems2023

 Nicolas Forget, Elizabeth Gandibleux, Xavier Gandibleux, Valentin Guy-Deroubaix, and Awen Jacq-Bodet (2024)

Analysis and discussion of single and multi-objective IP formulations for the Truck-to-dock Door Assignment Problem. e-preprint (optimization-online).

https://optimization-online.org/?p=27699

Xavier Gandibleux (2025)

Use of Julia/JuMP for Multi-Objective Optimization: a tutorial EURO2025, 22 - 25 June 2025 (Leeds, UK)

https://github.com/xgandibleux/EURO2025

Xavier Gandibleux and Andrzei Jaszkiewicz (2025)

Consistent and unbiased estimation of the hypervolume of an unknown true Pareto front. e-preprint (optimization-online).

https://optimization-online.org/?p=31635

Why this adventure with Julia and JuMP for MOO?

2015: Kick-off of the ANR/DFG research project vOpt

Sub-task 2.2: Experimental Analysis and Prototype Development.

→ The project of a multi-objective MILP solver was born!

Julia programming language: free, open source, multi-platform JuMP modeling language: expressive, efficient, evolutive

2017: Introduction of vOptSolver

Xavier Gandibleux, Gauthier Soleilhac, Anthony Przybylski, Stefan Ruzika. vOptSolver: an open source software environment for multiobjective mathematical optimization. IFORS2017: 21st Conference of the International Federation of Operational Research Societies. July 17-21, 2017. Quebec City (Canada).

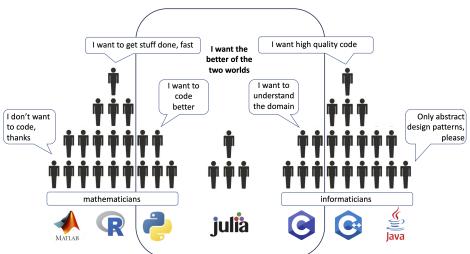
https://github.com/vOptSolver

composed of two packages:

- vOptSpecific.jl
- vOptGeneric.jl

Julia

A programming language for scientific computing



JuMP

An Algebraic Modeling Language (AML) among the existing ones . . .













... for mathematical optimization (linear, mixed-integer, conic, semidefinite, nonlinear) written in Julia.

... supporting 56 solvers; among the (MI)LP solvers: GLPK, Cbc, Clp, HiGHS, SCIP, CPLEX, Gurobi, FICO Xpress, COPT...

Example of material for optimizers

Book

Algorithms for Optimization

Mykel J. Kochenderfer, and Tim A. Wheeler

The MIT Press Cambridge, Massachusetts London, England

https://algorithmsbook.com/optimization/files/optimization.pdf