# Types and Programming Language Project Report\*

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## Introduction

Here is the introduction...

## 1 Language Design

## 1.1 Jeeves

Here we discribe Jeeves syntax in Figure 1. Totally, it contains three types

```
 \begin{array}{lll} Level & ::= & \perp \mid \top \\ Exp & ::= & v \mid Exp_1 \; (op) \; Exp_2 \\ & \mid \; \mathbf{if} \; Exp_1 \; \mathbf{then} \; Exp_t \; \mathbf{else} \; Exp_f \\ & \mid \; Exp_1 \; Exp_2 \\ & \mid \; \langle Exp_{\perp} \mid Exp_{\top} \rangle \left( \ell \right) \\ & \mid \; \mathbf{level} \; \ell \; \mathbf{in} \; Exp \\ & \mid \; \mathbf{policy} \; \ell : \; Exp_p \; \mathbf{then} \; Level \; \mathbf{in} \; Exp \\ Stmt \; ::= & \quad \mathbf{let} \; x : \tau \; = \; Exp \\ & \mid \; \mathbf{print} \; \{Exp_c\} \; Exp \end{array}
```

Figure 1: Jeeves syntax

## 1.2 Lambda J

Here we discribe the  $\lambda_{\rm J}$  language show in Figure 2.

## 2 Semantics

Here is the semantics...

<sup>\*</sup>done at June 5th, 2016

```
c ::= n \mid b \mid \lambda x : \tau.e \mid record \ x\overline{:}v
\mid \mathbf{error} \mid ()
\sigma ::= x \mid \mathbf{contex} \ \tau
\mid c_1 \ (op) \ \sigma_2 \mid \sigma_1 \ (op) \ c_2
\mid \mathbf{if} \ \sigma \ \mathbf{then} \ v_t \ \mathbf{else} \ v_f
v ::= c \mid \sigma
e ::= v \mid e_1 \ (op) \ e_2
\mid \mathbf{if} \ e_1 \ \mathbf{then} \ e_t \ \mathbf{else} \ e_f \mid e_1 \ e_2
\mid \mathbf{let} \ x : \tau = e_1 \ \mathbf{in} \ e_2
\mid \mathbf{defer} \ x : \tau \{e\} \ \mathbf{defaut} \ v_d
\mid \mathbf{assert} \ e
\mid \mathbf{concretize} \ e \ \mathbf{with} \ v_c
```

Figure 2:  $\lambda_{\rm J}$  syntax

## 3 Properties

**Lemma 1.** (ConcreteFunction). if v is a value of type  $\tau_1 \to \tau_2$ , then  $v = \lambda x : \tau_1.e$ , where e has type  $\tau_2$ .

*Proof.* According to the  $\lambda_{\rm J}$  syntax, we can get Lemma 1 immediately.

**Theorem 1.** (Progress). Suppose e is a closed, well-typed expression. Then e is either a value v or there is some e' such that  $\vdash \langle \phi, \phi, e \rangle \to \langle \Sigma', \Delta', e' \rangle$ .

```
Proof. we can ... \Box
```

**Theorem 2.** (Preservision). If  $\Gamma \vdash e : \tau \delta$  and  $e \rightarrow e'$ , then  $\Gamma \vdash e' : \tau \delta$ .

```
Proof. we can ... \Box
```

## 4 Evaluation

Here is the example area.

```
\mathscr{G} \vdash \langle \Sigma, \Delta, e \rangle \rightarrow \left\langle \Sigma', \Delta', e' \right\rangle
                                                                  \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_1 \rangle \rightarrow \left\langle \Sigma', \Delta', e_1' \right\rangle}{\mathscr{G} \vdash \langle \Sigma, \Delta, e_1 \ e_2 \rangle \rightarrow \left\langle \Sigma', \Delta', e_1' \ e_2 \right\rangle} \quad \text{E-APP1} \quad \frac{\mathscr{G} \vdash \left\langle \Sigma, \Delta, e_2 \right\rangle \rightarrow \left\langle \Sigma', \Delta', e_2' \right\rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, v \ e_2 \right\rangle \rightarrow \left\langle \Sigma', \Delta', v \ e_2 \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                                                       E-APP2
                                                                                                                                                                       E-APPLAMBDA \frac{c' = c_1 \ (op) \ c_2}{\mathscr{G} \vdash \langle \Sigma, \Delta, c_1 \ (op) \ c_2 \rangle \rightarrow \langle \Sigma', \Delta', c' \rangle}
                                                                                                                                                                                                                                                                                                                                                                                                               E-OP
                    \overline{\mathscr{G} \vdash \langle \Sigma, \Delta, \lambda x. e \ \upsilon \rangle \rightarrow \langle \Sigma', \Delta', e[x \mapsto \upsilon] \rangle}
\frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_1 \rangle \rightarrow \left\langle \Sigma', \Delta', e_1' \right\rangle}{\mathscr{G} \vdash \langle \Sigma, \Delta, e_1 \ (op) \ e_2 \rangle \rightarrow \left\langle \Sigma', \Delta', e_1' \ (op) \ e_2 \right\rangle}
                                                                                                                                                                                  E-OP1 \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_2 \rangle \rightarrow \left\langle \Sigma', \Delta', e_2' \right\rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \upsilon \right. \left(op\right) \left. e_2 \right\rangle \rightarrow \left\langle \Sigma', \Delta', \upsilon \right. \left(op\right) \left. e_2' \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                                                               E-OP2
                                                                                                       \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_c \rangle \rightarrow \langle \Sigma', \Delta', e_c' \rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \text{if } e_c \text{ then } e_t \text{ else } e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', \text{if } e_c' \text{ then } e_t \text{ else } e_f \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                                                      E-COND
                                                                                                                                                        \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_t \rangle \rightarrow \langle \Sigma', \Delta', e_t' \rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \text{if true then } e_t \text{ else } e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', e_t' \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                          E-CONDTRUE
                                                                                                                                               \frac{\mathscr{G} \vdash \left\langle \Sigma, \Delta, e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', e_f' \right\rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \text{if false then } e_t \text{ else } e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', e_f' \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                        E-CONDFALSE
                                                                                 \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e_t \rangle \rightarrow \langle \Sigma', \Delta', e_t' \rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \mathbf{if} \ \sigma \ \mathbf{then} \ e_t \ \mathbf{else} \ e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', \mathbf{if} \ \sigma \ \mathbf{then} \ e_t' \ \mathbf{else} \ e_f \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                          E-CONDSYMT
                                                                                 \frac{\mathscr{G} \vdash \left\langle \Sigma, \Delta, e_f \right\rangle \rightarrow \left\langle \Sigma', \Delta', e_f' \right\rangle}{\mathscr{G} \vdash \left\langle \Sigma, \Delta, \text{if } \sigma \text{ then } v_t \text{ else } e_f' \right\rangle \rightarrow \left\langle \Sigma', \Delta', \text{if } \sigma \text{ then } v_t \text{ else } e_f' \right\rangle}
                                                                                                                                                                                                                                                                                                                                                                          E-CONDSYMF
         \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e \rangle \rightarrow \langle \Sigma', \Delta', e' \rangle}{\mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{defer} \ x : \tau\{e\} \ \mathbf{default} \ v_d \rangle \rightarrow \langle \Sigma', \Delta', \mathbf{defer} \ x : \tau\{e'\} \ \mathbf{default} \ v_d \rangle}
                                                                                                                                                                                                                                                                                                                            E-DEFERCONSTRAINT
                                                   \frac{fresh\ x'}{\mathscr{G}\vdash \langle \Sigma, \Delta, \mathbf{defer}\ x:\tau\{e\}\ \mathbf{default}\ v_d\rangle \rightarrow \langle \Sigma\cup \{\mathscr{G}\Rightarrow v_c[x\mapsto x']\}, \Delta\cup \{\mathscr{G}\Rightarrow x'=v_d\}, x'\rangle}
                                                                                                                                                                                                                                                                                                                                                                                                E-DEFER
                                                                                                                                               \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e \rangle {\rightarrow} \langle \Sigma', \Delta', e' \rangle}{\mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{assert} \ e \rangle {\rightarrow} \langle \Sigma', \Delta', \mathbf{assert} \ e' \rangle}
                                                                                                                                                                                                                                                                                                                           E-ASSERTCONSTRAINT
                                                                                                                                                                                                                                                                                                                                                                                             E-ASSERT
                                                                                                                                                                                                              \mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{assert} \ v \rangle \rightarrow \langle \Sigma \cup \{\mathscr{G} \Rightarrow v\}, \Delta, () \rangle
                                            \frac{\mathscr{G} \vdash \langle \Sigma, \Delta, e \rangle \rightarrow \langle \Sigma', \Delta', e' \rangle}{\mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{concretize} \ e \ \mathbf{with} \ \upsilon_c \rangle \rightarrow \langle \Sigma', \Delta', \mathbf{concretize} \ e' \ \mathbf{with} \ \upsilon_c \rangle}
                                                                                                                                                                                                                                                                                                                                              E-CONCRETIZEEXP
                                                                                                          \frac{\text{MODLE}(\Delta, \Sigma \cup \{\mathscr{G} \cap \mathbf{context} = v_c\}) = \mathscr{M} \quad c = \mathscr{M}[[v_{\nu}]]}{\mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{concretize} \ v_{\nu} \ \mathbf{with} \ v_c \rangle \rightarrow \langle \Sigma, \Delta, c \rangle}
                                                                                                                                                                                                                                                                                                                                                E-CONCRETIZESAT
                                                                                                                   MODLE(\Delta,\Sigma \cup \{\mathscr{G} \cap \mathbf{context} = v_c\}) = UNSAT
                                                                                                                                                                                                                                                                                                                                   E-CONCRETIZEUNSAT
                                                                                                          \mathscr{G} \vdash \langle \Sigma, \Delta, \mathbf{concretize} \ v_{\nu} \ \mathbf{with} \ v_{c} \rangle \rightarrow \langle \Sigma, \Delta, \mathbf{error} \rangle
```

Figure 3: Dynamic semantics for  $\lambda_{\rm J}$ .

```
\delta ::= \mathbf{concretize} \mid \mathbf{sym} determinism tag
\beta ::= \mathbf{int}_c \mid \mathbf{bool}_c \mid \mathbf{unit} \mid \mathbf{int} \mid \mathbf{bool} base type
\tau ::= \beta \mid \tau_1 \xrightarrow{nr} \tau_2 \mid \tau_1 \to \tau_2 type
```

Figure 4:  $\lambda_{\rm J}$  types

```
\tau_1 <: \tau_2
                                                                                                                                                                                                                                                                                                                                           S-BOOL
                                                                                                                                          S-REFLEXIVE
                                                                                                                                                                                                                                                   S-INT
                                                                                                                                                                                                                                                                                     \overline{\mathrm{bool}_c <: \mathrm{bool}}
                                                                                                                                                                                                          \overline{\mathbf{int}_c <: \mathbf{int}}
                                                                                                              \overline{\tau < : \tau}
                                                                                                                                                                                                                                                                                     \frac{\tau_1' <: \tau_1 \quad \tau_2 <: \tau_2'}{\tau_1 \rightarrow \tau_2 <: \tau_1' \rightarrow \tau_2'}
                                                                                                                                                                                                                                 S-RECFUN
                                                                                                                                                                                                                                                                                                                                                 S-FUN
                                                                                                                                                             \overline{\tau_1} \xrightarrow{nr} \tau_2 < :\tau_1 \to \tau_2
                                                                                                                                                                          rep \tau
                                                                                                                                                                                                                     OK-SUBTYPE
                                                                                                                                                                                                                                                                                                                 OK-BASETYPE
                                                                                                                                                                                                                       \frac{\mathbf{rep}\ (\tau_1 \overset{nr}{\rightarrow} \tau')\ \mathbf{rep}\ \tau_2}{\mathbf{rep}\ (\tau_1 \overset{nr}{\rightarrow} \tau') \overset{nr}{\rightarrow} \tau_2}
                                                                                     rep \tau_2
                                                                                                                                 OK-BASEFUNCTION
                                                                                                                                                                                                                                                                                                      OK-HOFUNCTION
                                                                              rep \beta_1 \rightarrow \tau_2
                                                                                                                                                                                                           \frac{\mathbf{rep}\ \tau_1{\rightarrow}\tau_2\ \mathbf{rep}\ \tau_1'{\rightarrow}\tau_2'}{\mathbf{rep}\ (\tau_1{\rightarrow}\tau_2){\rightarrow}(\tau_1'{\rightarrow}\tau_2')}
                                         rep \tau_1 \rightarrow \tau_2
                                                                                                                                                                                                                                                                                                  OK-RECFUNCTION
                                                                                                   OK-RECFUNCTIONBASE
                                rep (\tau_1 \rightarrow \tau_2) \rightarrow \beta
                                                                                                                                                          \Gamma; \gamma \vdash e : \langle \tau, \delta \rangle
                       \tfrac{x \in \Gamma}{\Gamma; \gamma \vdash x : \Gamma(x)}
                                                                          T-VAR
                                                                                                                                                            T-INT
                                                                                                                                                                                                                                                 \operatorname{T-BOOL}
                                                                                                                                                                                                                                                                                                                                             T-UNIT
                                                                                                                                                                                                                                                                                          \overline{\Gamma;\gamma\vdash():\mathbf{unit}}
                                                                                                              \overline{\Gamma; \gamma \vdash n : \mathbf{int}_c}
                                                                                                                                                                                               \Gamma; \gamma \vdash b : \mathbf{bool}_c
                                                                                                                                                                                                              \frac{\Gamma; \gamma \vdash e_1 : \tau_1 \quad \Gamma; \gamma \vdash e_2 : \tau_2 \quad \tau_1, \tau_2 < : \tau \quad \mathbf{rep} \ \tau}{\Gamma; \gamma \vdash e_1 \ (op) \ e_2 : \tau}
                                                                              \frac{\mathbf{rep} \ \tau}{\Gamma; \gamma \vdash \mathbf{context} \ \tau : \tau}
                                                                                                                                                    T-CONTEXT
                                                                                                                                        \frac{\Gamma; \gamma \vdash e : \mathbf{bool}_c \quad \Gamma; \gamma \vdash e_t : \tau_1 \quad \Gamma; \gamma \vdash e_f : \tau_2 \quad \tau_1, \tau_2 <: \tau \quad \mathbf{rep} \ \tau}{\Gamma; \gamma \vdash \mathbf{if} \ e \ \mathbf{then} \ e_t \ \mathbf{else} \ e_f : \tau}
                                                                                                                                                                                                                                                                                                                                    T-CONDC
                                                                                                 \underline{\Gamma;} \gamma \vdash e{:}\mathbf{bool} \quad \Gamma; \mathbf{sym} \vdash e_t{:}\beta_1 \quad \Gamma; \mathbf{sym} \vdash e_f{:}\beta_2 \quad \beta_1, \beta_2 < :\beta_c \quad \mathbf{rep} \ \beta_c
                                                                                                                                                                                                                                                                                                                          T-CONDSYM
                                                                                                                                                        \Gamma; \gamma \vdash \mathbf{if} \ e \ \mathbf{then} \ e_t \ \mathbf{else} \ e_f : \beta_c
                                                                                                                                                              \frac{\Gamma; \gamma \vdash e_1 : \tau_1 \xrightarrow{nr} \tau_2 \quad \Gamma, x : \tau_d; \gamma \vdash e_2 : \tau_1' \quad \tau_1' < : \tau_1 \quad \mathbf{rep} \ \tau_1 \quad \mathbf{rep} \ \tau_2}{\Gamma; \gamma \vdash (e_1 \ e_2) : \tau_2} \quad \text{T-APP}
\frac{\Gamma,\! x :\! \tau_d;\! \gamma \vdash\! e :\! \tau' \quad \mathbf{rep} \ \tau_d \quad \mathbf{rep} \ \tau'}{\Gamma;\! \gamma \vdash\! (\lambda x :\! \tau_d.e) :\! \tau_d \!\rightarrow\! \tau'}
                                                                                                       T-LAMBDA
                                                                                               \frac{\Gamma, f: \tau_1 \rightarrow \tau_2; \gamma \vdash e_1: \tau_1 \rightarrow \tau_2 \quad \Gamma, f: \tau_1 \overset{nr}{\rightarrow} \tau_2; \gamma \vdash e_2: \tau_2 \quad \mathbf{rep} \ \tau \quad \mathbf{rep} \ \tau_2}{\Gamma; \gamma \vdash \mathbf{let} \ \mathbf{rec} \ f: \tau_1 \overset{nr}{\rightarrow} \tau_2 = e_1 \ \mathbf{in} \ e_2: \tau_2}
                                                                                                                                                                                                                                                                                                                  T-APPLETREC
                                                                           \frac{\gamma{=}\mathbf{concrete} \quad \Gamma;\!\gamma{\vdash}e_1{:}\tau_1{\to}\tau_2 \quad \Gamma;\!\gamma{\vdash}e_2{:}\tau_1' \quad \tau_1'{<:}\tau_1 \quad \mathbf{rep} \ \tau_1 \quad \mathbf{rep} \ \tau_2}{\Gamma;\!\gamma{\vdash}(e_1\ e_2){:}\tau_2}
                                                                                                                                                                                                                                                                                                                 T-APPCURREC
                                                                           \frac{\Gamma{,}x{:}\beta{;}\gamma{\vdash}e_c{:}\mathbf{bool}\quad \Gamma{;}\gamma{\vdash}v{:}\beta}{\Gamma{;}\gamma{\vdash}(\mathbf{defer}x{:}\beta\{e_c\}\ \mathbf{default}\ v){:}\beta}
                                                                                                                                                                                                                                                   \frac{\Gamma; \gamma \vdash e_c \text{:bool}}{\Gamma; \gamma \vdash (\mathbf{assert} \ e_c) \text{:unit}}
                                                                                                                                                                                                    T-DEFER
                                                                                                                                                                                                                                                                                                                                   T-ASSERT
                                                                                                                                                                                         \Gamma; \gamma \vdash e_1 : \beta \quad \Gamma; \gamma \vdash^c e_1 : \beta' \quad \Gamma; \gamma \vdash v : \beta'
                                                                                                                                                                                                                                                                                                               T-CONCRETIZE
                                                                                                                                                                                         \Gamma; \gamma \vdash (\mathbf{concretize} \ e_1 \ \mathbf{with} \ v) : \beta_c
```

Figure 5: Static semantics for  $\lambda_{\rm J}$  describing simple type-checking and enforce restriction on scope of nondeterminism and recursion. Recall that  $\beta$  refers to base (non-function) types.

```
deriving (Ord, Eq)
   data Op = OP_PLUS | OP_MINUS
                     | OP_LESS | OP_GREATER
                     | OP_EQ | OP_AND | OP_OR | OP_IMPLY
                     deriving (Ord,Eq)
   data UOp = OP_NOT
                         deriving (Ord, Eq)
   data FieldName = FIELD_NAME String deriving(Ord, Eq)
   data Var = VAR String deriving (Ord, Eq)
_____
let name =
   level a in
   policy a: !(context = alice) then bottom in < "Anonymous" | "Alice" >(a)
let msg = "Author is " + name
print {alice} msg
print {bob} msg
```

## 5 Conclusion

Here is the conclusion section...

## References

- [1] J. Yang, K. Yessenov, and A. Solar-Lezama. A language for automatically enforcing privacy policies. In Proceedings of the 39th annual ACM SIGPLAN-SIGACT symposium on Principles of programming languages (POPL '12). ACM, New York, NY, USA, 85-96.
- [2] B. Pierce. Types and Programming Languages, MIT Press, 2002.