#### Elements Of Data Science - F2020

# Week 9: Dimensionality Reduction, Feature Selection and Feature Extraction

11/16/2020

### **TODOs**

- Readings:
  - PML Chapter 6, first 3 sections on Pipelines
  - PML Chapter 8
- HW3, Out this week

• Answer and submit Quiz 9, Sunday Nov 22nd, 11:59pm ET

## **Today**

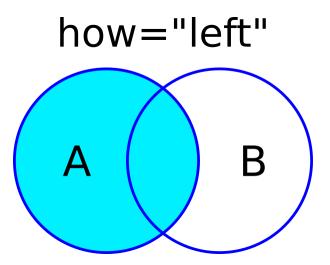
- Joining Datasets
- Dimensionality Reduction
  - Feature Selection
    - LASSO
    - Tree Based Models Feature Importance
    - Univariate Tests
    - Recursive Feature Selection
  - Feature Extraction
    - o PCA
- Image Recognition Using PCA

# Questions?

# Simple Joins: Sharing An Index

```
In [2]: df1 = pd.DataFrame(\{'A': ['A0', 'A1', 'A2']\})
        df1
Out[2]:
         0 A0
         1 A1
         2 A2
In [3]: df2 = pd.DataFrame({'B': ['B0', 'B1', 'B2']})
        df2
Out[3]:
         0 B0
         1 B1
         2 B2
In [4]: df1.join(df2)
Out[4]:
         0 A0 B0
         1 A1 B1
         2 A2 B2
```

## Simple Joins: Left Join



```
In [5]: df3 = pd.DataFrame({'C': ['C1', 'C2', 'C3']}, index=[1,2,3])

Out[5]:

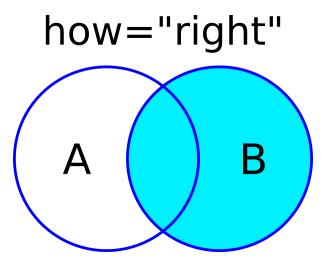
C
1 C1
2 C2
3 C3

In [6]: df1.join(df3, how="left") # default is left join

Out[6]:

A C
0 AO NaN
1 A1 C1
2 A2 C2
```

# Simple Joins: Right Join



```
In [7]: df1.join(df3,how="right")

Out[7]:

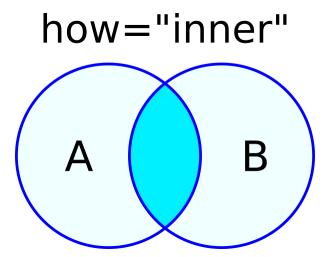
A C

1 A1 C1

2 A2 C2

3 NaN C3
```

# Simple Joins: Inner Join



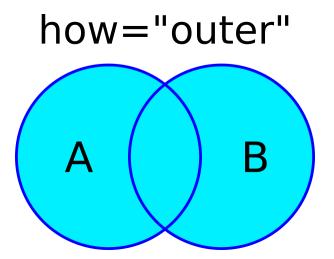
```
In [8]: df1.join(df3,how="inner")

Out[8]:

A C

1 A1 C1
2 A2 C2
```

# Simple Joins: Outer Join



```
In [9]: df1.join(df3,how="outer")

Out[9]:

A C

O AO NAN

1 A1 C1

2 A2 C2

3 NAN C3
```

# **Dimensionality Reduction**

# **Avoiding Overfitting**

- Collect additional examples
- Use a simpler model
- Regularization
- Reduce the dimensions of our data: Dimensionality Reduction

### **Dimensionality Reduction**

- Reasons to reduce the number of features
  - improve model performance (reducing complexity reducing chance of overfitting)
  - improve speed performance (reducing number of calculations)
  - interpretation (which features are most important?)
- Feature Selection
  - choose a subset of original features
- Feature Extraction
  - combine features to generate a new feature space

### Load Binary Wine Classification

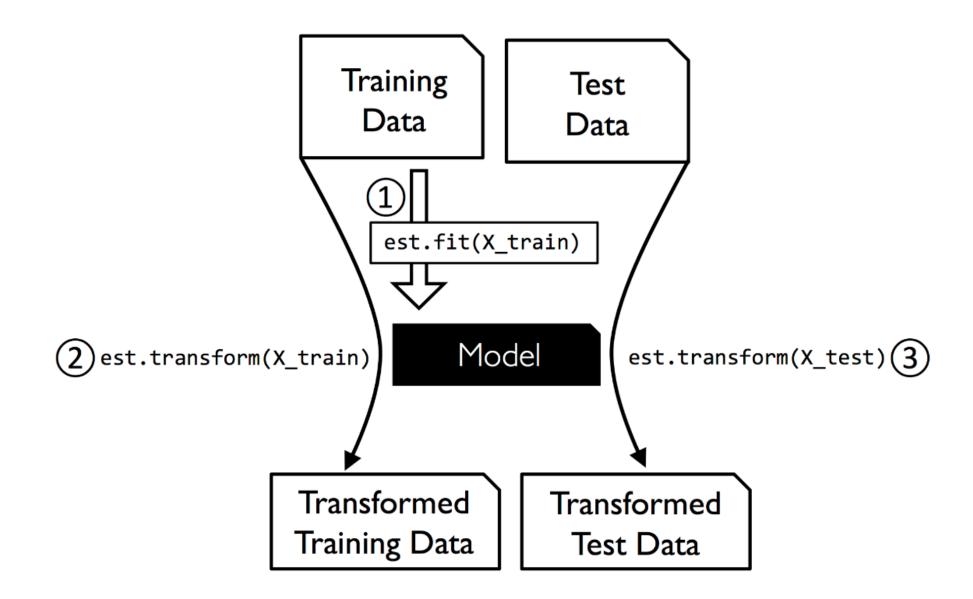
```
In [10]: from sklearn import datasets
         from sklearn.model_selection import train_test_split
         wine = datasets.load_wine()
         X_wine = pd.DataFrame(wine.data,columns=wine.feature_names)
         y_wine = wine.target
         X_{wine} = X_{wine.iloc}[y_{wine} < 2]
         y_wine = y_wine[y_wine < 2]</pre>
         feature_names = X_wine.columns.values
         X_train, X_test, y_train, y_test = train_test_split(X_wine, y_wine, random_state=0)
         X_train = pd.DataFrame(X_train,columns=X_wine.columns)
         feature_names
Out[10]: array(['alcohol', 'malic_acid', 'ash', 'alcalinity_of_ash', 'magnesium',
                 'total_phenols', 'flavanoids', 'nonflavanoid_phenols',
                 'proanthocyanins', 'color_intensity', 'hue',
                 'od280/od315_of_diluted_wines', 'proline'], dtype=object)
```

#### **Standardize Features**

```
In [11]: from sklearn.preprocessing import StandardScaler
         ss = StandardScaler()
         X_train = pd.DataFrame(ss.fit_transform(X_train), columns=X_train.columns)
         X_test = ss.transform(X_test)
In [12]: X_train.agg(['mean','std']).round(1).T.head()
Out[12]:
                       mean std
          alcohol
                       0.0
                            1.0
                       -0.0 1.0
          malic_acid
                       -0.0 1.0
          ash
          alcalinity_of_ash 0.0
                            1.0
                       0.0 1.0
          magnesium
```

# Aside: Predicting vs Transforming with Train/Test Split

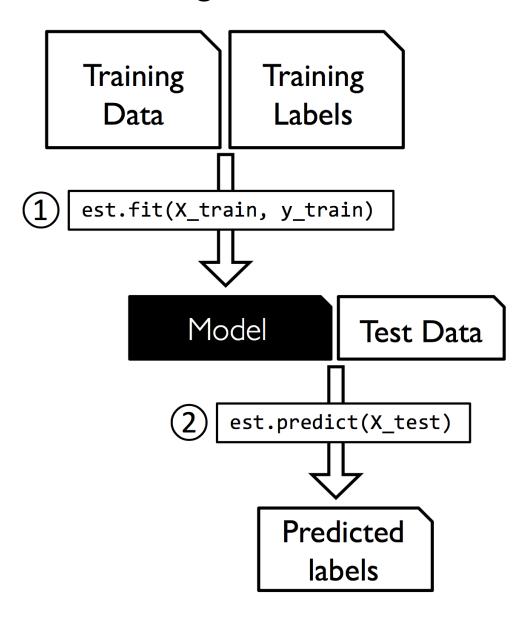
- When transforming data, fit on the training set, transform both train and test



From PML

# Aside: Predicting vs Transforming with Train/Test Split

- When performing prediction, train on the training set, evaluate on the test set



From PML

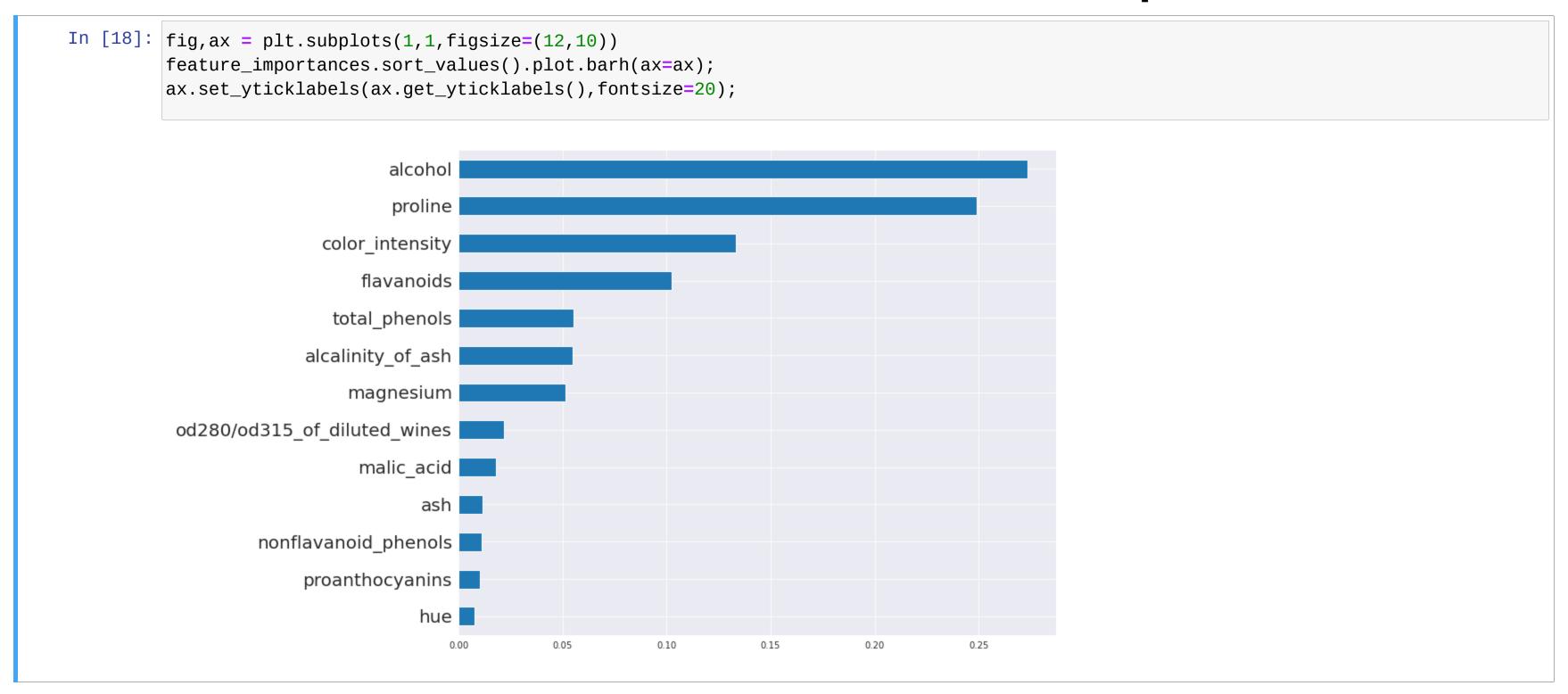
### Feature Selection: LASSO (L1)

```
In [13]: from sklearn.linear_model import LogisticRegression
        logr = LogisticRegression(C=100, penalty="l1", solver="liblinear", random_state=123)
        logr.fit(X_train, y_train)
        logr.coef_
Out[13]: array([[-5.74709641, -1.20824931, -2.70057811, 2.47398434, -0.28304842,
                -0.14584941, -0.37559551, 0. , 1.14394581, -0.63815798,
                 1.06926936, -0.86036347, -7.567675 ]])
In [14]: logr = LogisticRegression(C=0.1, penalty="l1", solver="liblinear", random_state=123)
        logr.fit(X_train, y_train)
        logr.coef_
Out[14]: array([[-0.98231183, 0. , 0.
                                                               , 0.
                          , -0.00652705, 0. , 0.
                                                               , 0.
                          , 0. , -1.10166563]])
In [15]: feature_names[logr.coef_[0] != 0]
Out[15]: array(['alcohol', 'flavanoids', 'proline'], dtype=object)
```

### Feature Selection: Tree Based Model Feature Importance

```
In [16]: from sklearn.ensemble import RandomForestClassifier
         rf = RandomForestClassifier(random_state=123).fit(X_train,y_train)
         rf.feature_importances_ # (normalized) total reduction of function measuring impurity
Out[16]: array([0.27332426, 0.01783127, 0.01145411, 0.05480187, 0.05158374,
                0.05521824, 0.10260545, 0.01117794, 0.01033494, 0.13339066,
                0.00759636, 0.0216486 , 0.24903258])
In [17]: feature_importances = pd.Series(rf.feature_importances_,index=feature_names)
         feature_importances.sort_values(ascending=False).round(3)
Out[17]: alcohol
                                          0.273
                                          0.249
         proline
         color intensity
                                          0.133
         flavanoids
                                          0.103
         total_phenols
                                          0.055
         alcalinity_of_ash
                                          0.055
         magnesium
                                          0.052
         od280/od315 of diluted wines
                                          0.022
         malic acid
                                          0.018
         ash
                                          0.011
         nonflavanoid_phenols
                                          0.011
         proanthocyanins
                                          0.010
         hue
                                          0.008
         dtype: float64
```

### Feature Selection: Tree Based Model Feature Importance



#### Feature Selection: SelectFromModel

```
In [19]: from sklearn.feature_selection import SelectFromModel
         sfm = SelectFromModel(logr,
                               threshold=None, # if model uses 11 regularization, anythin greater than 1e-5
                               prefit=True
                                              # do not need to re-fit
         sfm.get_support()
Out[19]: array([ True, False, False, False, False, False, True, False, False,
                False, False, True])
In [20]: feature_names[sfm.get_support()]
Out[20]: array(['alcohol', 'flavanoids', 'proline'], dtype=object)
In [21]: X_train_subset = sfm.transform(X_train)
        X train subset.shape
Out[21]: (97, 3)
In [22]: |sfm_rf = SelectFromModel(RandomForestClassifier(),
                                  threshold='mean', # return all features with value greater than the mean
                                                     # need to refit
                                  prefit=False
                                ).fit(X_train,y_train)
         feature_names[sfm_rf.get_support()]
Out[22]: array(['alcohol', 'flavanoids', 'color_intensity', 'proline'],
               dtype=object)
```

#### Feature Selection: Univariate Tests

- Perform statistical test on each feature independent of all others
  - Rank and select top k features
  - sklearn: SelectKBest
  - requires a scoring function
- Example: f\_classif
  - F-test
  - estimates the degree of linear dependency between feature x and target y

#### Feature Selection: Recursive Feature Elimination

- Would like to test all possible combinations of features
- Likely prohibitively expensive/time-consuming
- Instead recursively select smaller subsets of features
- Requires a model that assigns weights or importance to features

#### Feature Selection: Other Methods

- by Variance
  - eliminate columns where all rows have the same (or almost all the same) value
- Sequential Feature Selection
  - greedy algorithm similar to Recursive Feature Elimination
  - uses performance metric (eg accuracy) instead of weights, importances
  - via mlxtend
- Exaustive Feature Selection
  - evaluate all possible feature combinations
  - uses performance metric (eg accuracy) instead of weights, importances
  - via mlxtend
- Other Univariate tests
  - f\_regression, F-test for regression task
  - mutual\_info\_classif and \_regression
  - chi2, for classification, requires non-negative values

#### **Feature Extraction**

- Transform original features into new feature space
- Can be thought of as compression while maintaining relevant information
- Often used for:
  - visualization (multi-dimensional to 2-D)
  - compression (storage)
  - dimensionality reduction
- Popular methods:
  - Principal Component Analysis: Unsupervised data compression
  - Linear Discriminant Analysis: Supervised method to maximize class separation
  - Kernel PCA, etc.

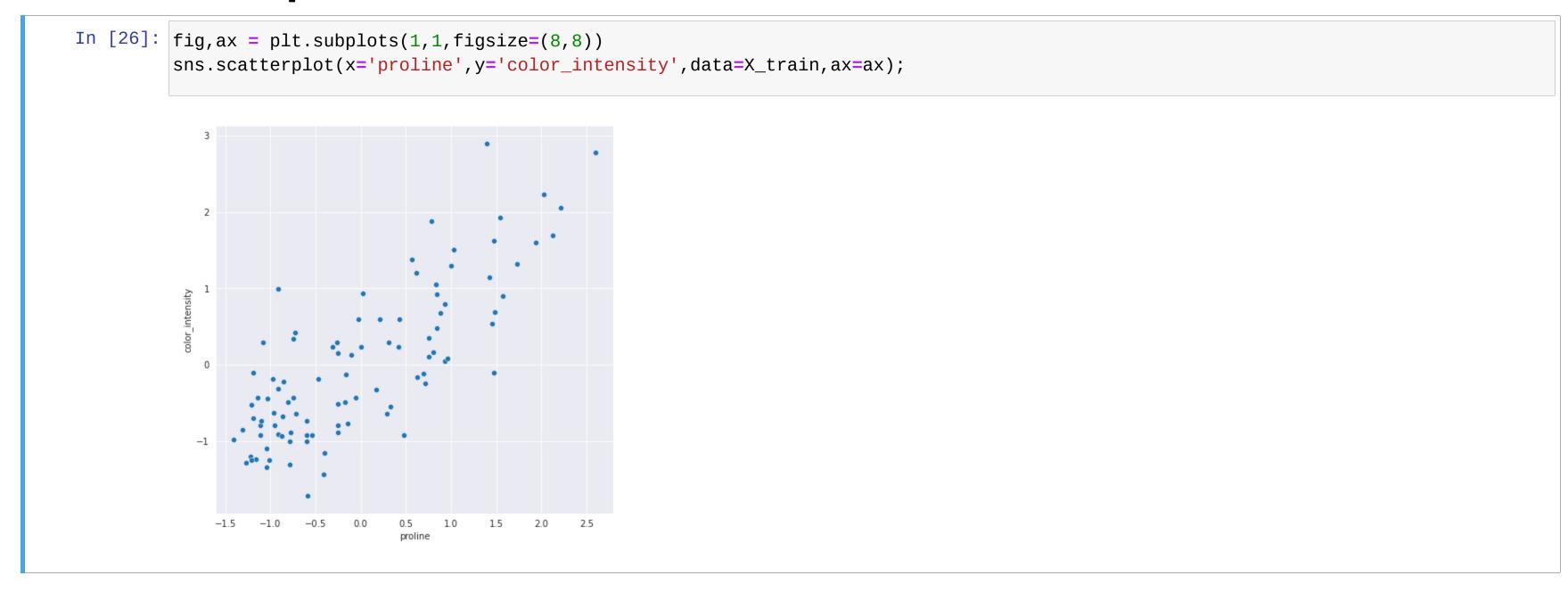
### Principal Component Analysis (PCA)

- Unsupervised Learning method (ignores label)
- Idea:
  - Directions of high variance in the data contain important information
  - Colinear features can be combined
  - Find directions of maximum variance
  - Project onto subspace with same or fewer dimensions

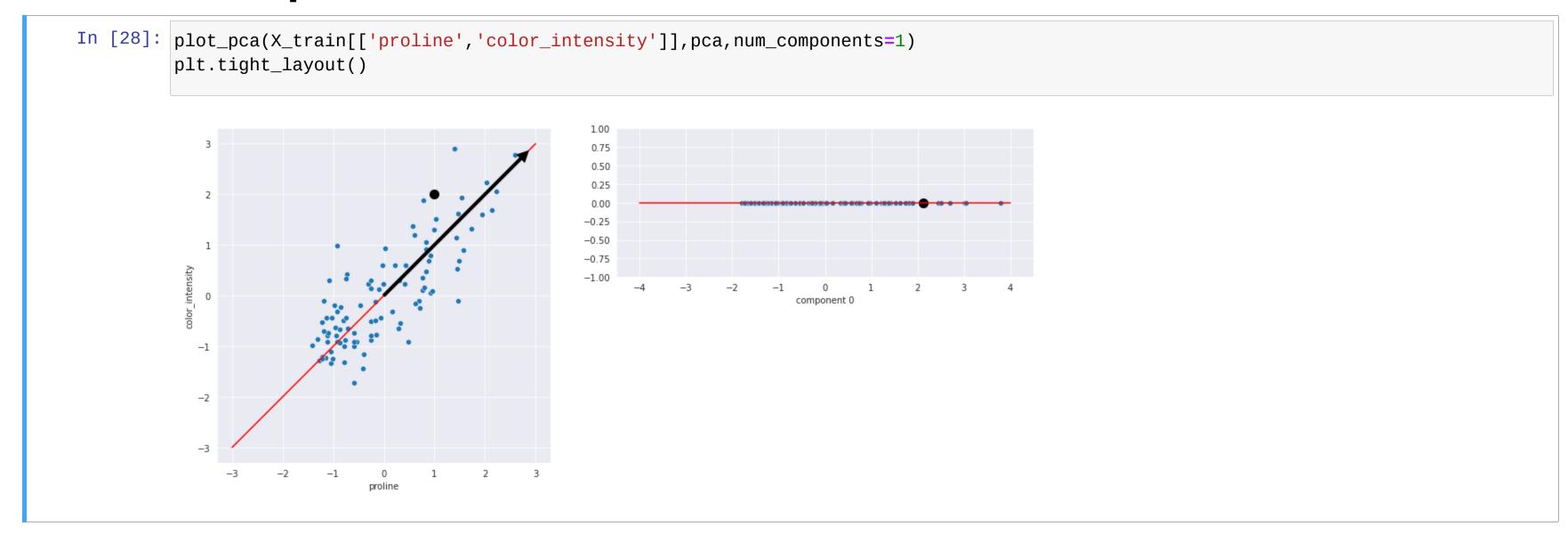
# Principal Component Analysis (PCA)

- How it works:
  - O. first center the data (subtract the means)
  - 1. first component:
    - direction (combination of features)
    - explains maximum variance
  - 2. next component:
    - direction, orthogonal to the first (linearly independent)
    - explains max remaining variance
  - 3. repeat:
    - max number of possible components equals number of original dimensions

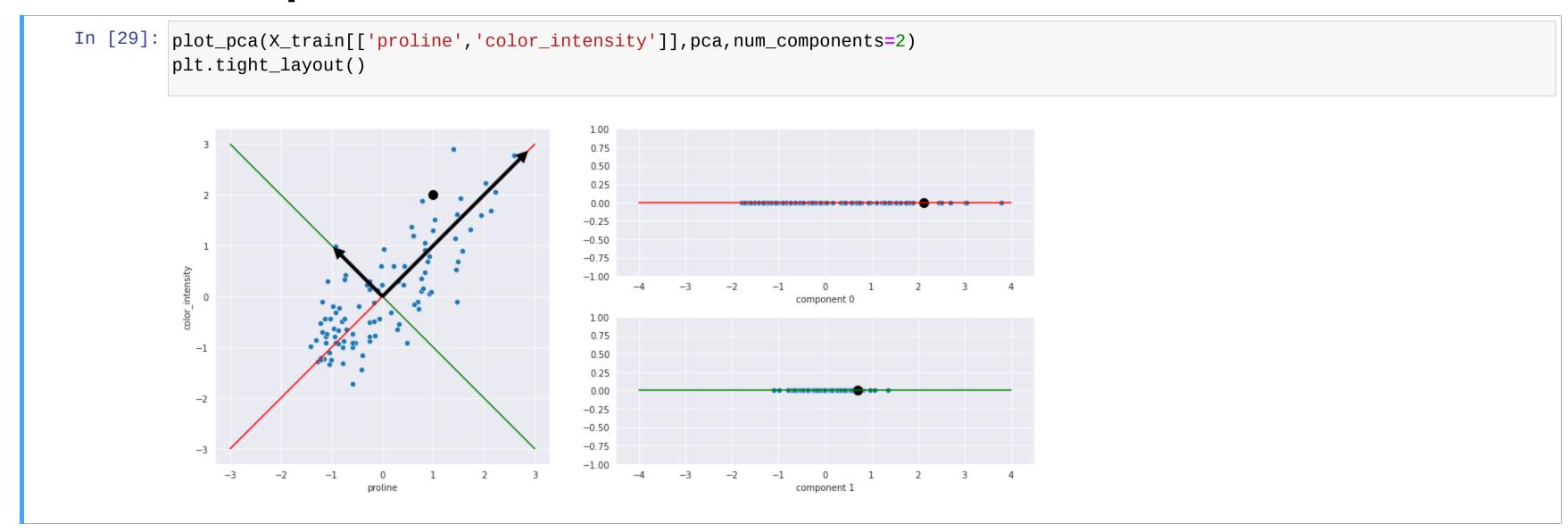
# **PCA Example**



# PCA Example Cont.



# PCA Example Cont.



#### PCA in sklearn

```
In [30]: from sklearn.decomposition import PCA
         # extract the first 2 principle compenents
         pca = PCA(n_components=2)
        X_pca = pca.fit_transform(X_train[['proline','color_intensity']])
         X_pca = pd.DataFrame(X_pca,columns=['component1','component2'])
         fig, ax=plt.subplots(1,2,figsize=(14,6))
         sns.scatterplot(x='proline',y='color_intensity',data=X_train,ax=ax[0]);
         sns.scatterplot(x='component1',y='component2',data=X_pca,ax=ax[1]);
         ax[0].axis('equal');ax[1].axis('equal');
```

# PCA: Explained Variance

• How much of the variance is explained by each component?

```
In [31]: pca.explained_variance_ratio_
Out[31]: array([0.89808764, 0.10191236])
```

### **PCA: Principle Components**

What does the first component (vector) look like?

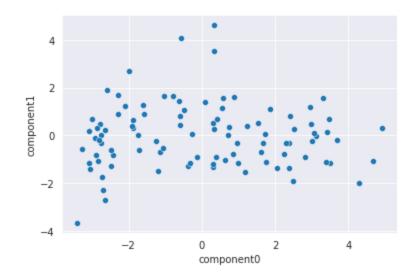
```
In [32]: pca.components_[0]
Out[32]: array([0.70710678, 0.70710678])
```

• And the second?

```
In [33]: pca.components_[1]
Out[33]: array([-0.70710678, 0.70710678])
```

### Dimensionality Reduction with PCA

```
In [34]: pca_2d = PCA(n_components=2)
X_2d = pca_2d.fit_transform(X_train, y_train)
X_2d = pd.DataFrame(X_2d, columns=["component"+str(i) for i in range(2)])
sns.scatterplot(x='component0', y='component1', data=X_2d);
```



```
In [35]: print(' + \n'.join([f'{w: 0.2f}*{f}' for f,w in sorted(zip(X_train.columns,pca_2d.components_[0]), key=lambda x:x[1])]))

-0.28*nonflavanoid_phenols +
-0.26*alcalinity_of_ash +
-0.03*hue +
0.01*malic_acid +
0.11*ash +
0.21*proanthocyanins +
0.23*magnesium +
0.25*od280/od315_of_diluted_wines +
0.36*proline +
0.36*color_intensity +
0.36*color_intensity +
0.36*total_phenols +
0.37*alcohol +
0.39*flavanoids
```

### PCA and Image Recognition

- Generally, image is represented by a grid of pixels
- Each pixel is a square that takes a value representing a shade (usually a value between 0 and 255)
- 1024 x 1024 pixels = 1,048,576 pixels = 1 megapixel
- iPhone X11 Pro: 12 megapixels
- Color images contain three layers: red, green, blue
- ~36 million pixel values
- A very high dimensional space!

- Image classification using PCA?
  - Example based on <u>Faces recognition example using eigenfaces and SVMs</u>

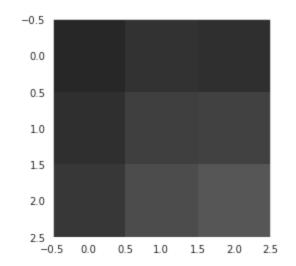
### **Example Dataset: LFW**

#### Labeled Faces in the Wild

```
In [36]: from sklearn.datasets import fetch_lfw_people
         lfw_people = fetch_lfw_people(min_faces_per_person=70, resize=0.4)
In [37]: sns.set_style('dark')
         plt.imshow(lfw_people.images[1], cmap=plt.cm.gray, vmin=0, vmax=255)
         plt.title(lfw_people.target_names[lfw_people.target[1]], size=12);
                Tony Blair
```

# **Example Pixel Values**

```
In [38]: # first 3x3 set of pixels
plt.imshow(lfw_people.images[1][:3,:3],cmap=plt.cm.gray,vmin=0, vmax=255);
```



### Representing each Image: Flatten

• Grid as a fixed length feature vector?

What information do we lose when we do this?

#### Create a Dataset

```
In [43]: # get the shape of images for plotting the
         n_samples, h, w = lfw_people.images.shape
         # use actual pixel values, ignoring relative position
        X_{faces} = lfw_{people.data}
         n_features = X_faces.shape[1]
         # the label to predict is the id of the person
        y_faces = lfw_people.target
         target_names = lfw_people.target_names
        n_classes = target_names.shape[0]
        # create train/test split
        X_train_faces, X_test_faces, y_train_faces, y_test_faces = train_test_split(X_faces, y_faces,
                                                                                    test_size=0.25,
                                                                                    stratify=y_faces,
                                                                                    random_state=123)
         print(f"image_size: {h}x{w}")
         print("n_features: %d" % n_features)
         print("n_classes : %d" % n_classes)
         print(f"n_train : {len(X_train_faces)}")
         print(f"n_test : {len(X_test_faces)}")
         image_size: 50x37
         n_features: 1850
         n classes : 7
         n train : 966
         n_test : 322
```

#### Compute PCA and Transform

## Eigenfaces

• What if we plot the top 12 components (eigenfaces) using .reshape(h,w)?



#### Train and Tune SVC

#### **Evaluate on the test set**

```
In [49]: y_pred = clf_faces.predict(X_test_pca_faces)
         from sklearn.metrics import classification_report
         print(classification_report(y_test_faces, y_pred, target_names=target_names))
                                         recall f1-score
                            precision
                                                            support
              Ariel Sharon
                                 0.70
                                           0.74
                                                     0.72
                                                                 19
              Colin Powell
                                 0.77
                                           0.86
                                                     0.82
                                                                 59
           Donald Rumsfeld
                                 0.83
                                                     0.83
                                                                 30
                                           0.83
             George W Bush
                                 0.87
                                           0.89
                                                     0.88
                                                                133
         Gerhard Schroeder
                                 0.81
                                           0.48
                                                     0.60
                                                                 27
               Hugo Chavez
                                 0.92
                                           0.67
                                                     0.77
                                                                 18
                Tony Blair
                                 0.78
                                           0.86
                                                     0.82
                                                                 36
                                                     0.82
                                                                322
                  accuracy
                                 0.81
                                                     0.78
                                                                322
                 macro avg
                                           0.76
              weighted avg
                                 0.83
                                           0.82
                                                     0.82
                                                                322
```

### **Prediction Examples**

```
In [50]: prediction_titles = [title(y_pred, y_test_faces, target_names, i)
                                       for i in range(y_pred.shape[0])]
            plot_gallery(X_test_faces, prediction_titles, h, w)
            plt.tight_layout()
             predicted: Rumsfeld predicted: Blair
                                          predicted: Bush
              true: Rumsfeld true: Schroeder
                                                        true: Bush
             predicted: Rumsfeldpredicted: Schroeder predicted: Powell
              true: Rumsfeld true: Schroeder true: Powell
                            predicted: Sharon predicted: Sharon
                            true: Sharon
                                         true: Sharon
                                                       true: Powell
```

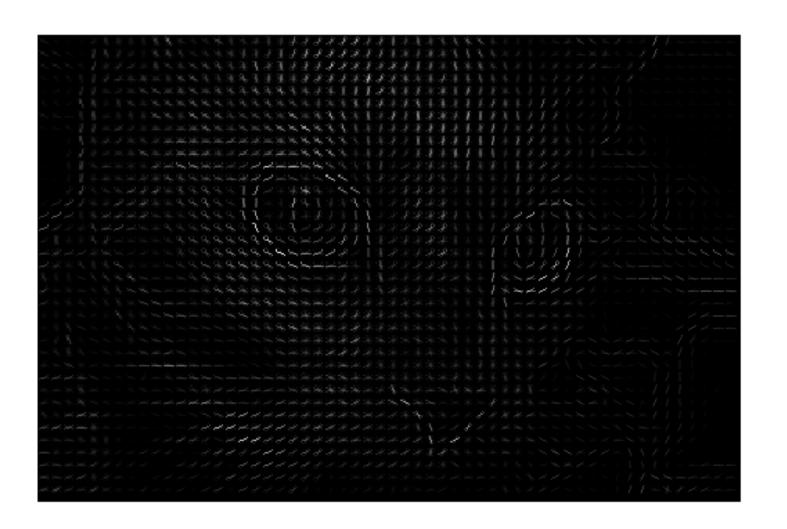
#### Performance without PCA

```
%%time
# Warning: this cell takes up to 2 minutes to execute on an Intel i7 1.8Ghz w/ 8 cores
params = \{'C': [1e3, 5e3, 1e4, 5e4, 1e5],
          'gamma': [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.1], }
clf_faces = GridSearchCV(SVC(kernel='rbf', class_weight='balanced'),
                         params, cv=3, n_jobs=-1)
clf_faces = clf_faces.fit(X_train_faces, y_train_faces)
# CPU times: user 9.57 s, sys: 72.1 ms, total: 9.64 s
# Wall time: 1min 18s
print(f"best_params : {clf_faces.best_params_}")
print(f"best_score : {clf_faces.best_score_:0.2f}")
# best_params : {'C': 1000.0, 'gamma': 0.0001}
# best_score : 0.41
```

## Other Image Recognition Methods

- With Feature Engineering and general models
  - ex: Histogram of Oriented Gradients or HOG (See PDSH Chap 5)
  - many more (See <u>scikit-image</u>)

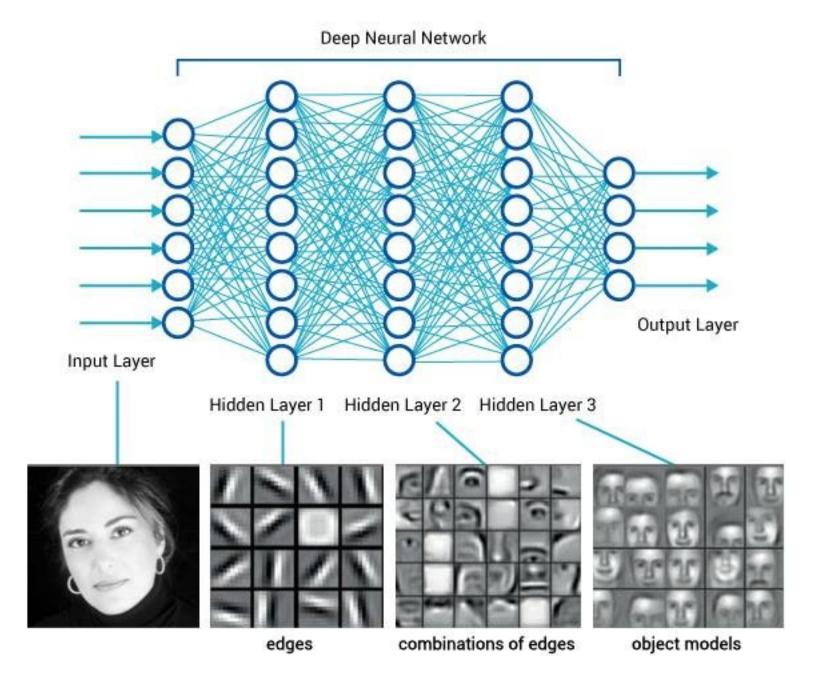




From PDSH 45/4

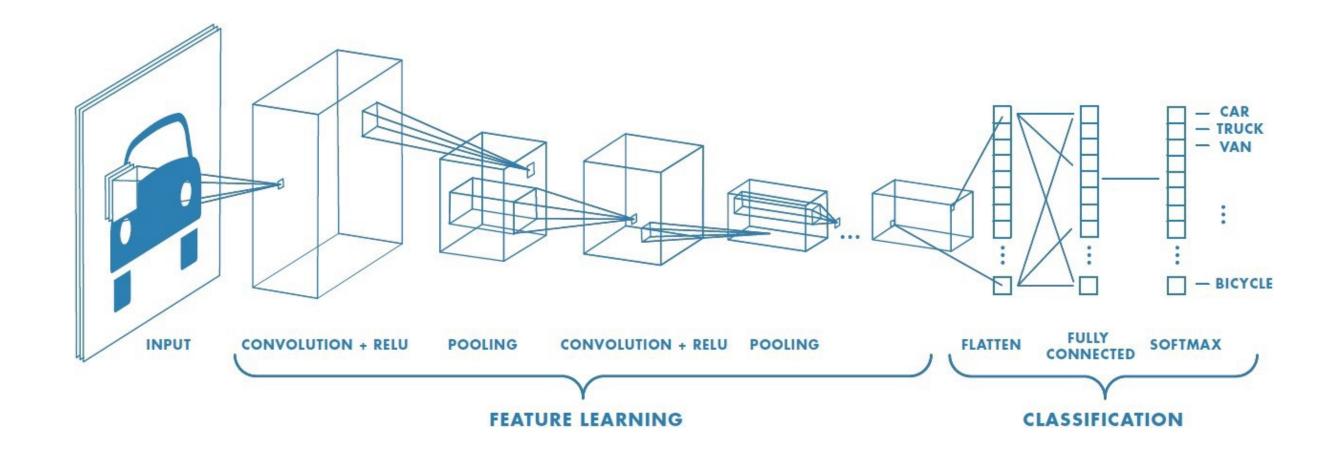
### Other Image Recognition Methods: Deep Neural Networks

With Deep Neural Nets



### Other Image Recognition Methods: Deep Neural Networks

• With Convolutional Neural Networks <u>Good Example</u>



# Questions?