

Wardrop's Principle (Equilibrium): [Also known as User Equilibrium]

↳ the costs of the used routes will be equal and less than or equal to the costs of the unused routes.

[Complementarity Problem],

Note: routes \equiv links

① Demonstrating $x_1 = 0$ and $x_2 = d$ is a UE assignment.

$$\text{when } x_1 = 0 \quad c_1(0) = 1 + \frac{1}{0} = \underline{\underline{\infty}} \text{ (infinity)}$$

$$\text{when } x_2 = d \quad c_2(d) = 3 + d = \underline{\underline{3+d}}$$

$\therefore \underline{\underline{c_1(0) \geq c_2(d)}}$ and so $x_1 = 0$ and $x_2 = d$ is a UE assignment

② Deriving a condition on d for which $x_1 = d$ and $x_2 = 0$ is also a UE assignment

$$\text{when } x_1 = d \quad c_1(d) = 1 + \frac{1}{d} = \frac{d+1}{d}$$

$$\text{when } x_2 = 0 \quad c_2(0) = 3 + 0 = 3$$

$$\therefore c_1(d) \leq c_2(0)$$

$$\text{From ①} \quad c_1(0) \geq c_2(d) \Rightarrow \infty \geq 3+d \rightarrow \text{can't use this}$$

$$\text{From ②} \quad c_1(d) \leq c_2(0) \Rightarrow \frac{d+1}{d} \geq 3$$

$$d+1 \geq 3d$$

$$1 \geq 2d$$

$$\therefore \underline{\underline{d \leq 1/2}}$$