

Read each question carefully and be sure to SHOW ALL WORK. Correct answer without proper justification will not receive a “Complete” grade. Pac fat! Good luck!

Name: _____

LO 12. Series Challenge. I can work with series and power series creatively in new situations that require a deep understanding of them.

Criteria for Success: I can solve conceptual questions related to series and power series that lie on the top half of Bloom’s Taxonomy (analyze, evaluate, and create).

Question: Let $f(x) = \sum_{n=1}^{\infty} \frac{(-1)^{n+1} 2^n}{n} x^{2n}$ be a power series. Answer the following questions:

- (a) Find the function representation of the series $f(x)$. You may assume the Taylor series expansion of the most common functions and start from there, or derive it from scratch by taking derivatives or integrals of known power series.
- (b) Find the radius of convergence of $f(x)$.
- (c) Finally, combine the two parts above to find the exact value of $f(0.1) = \sum_{n=1}^{\infty} \frac{(-1)^{n+1} 2^n}{n} (0.1)^{2n}$, or conclude the series is divergent.