

**Read each question carefully and be sure to SHOW ALL WORK. Correct answer without proper justification will not receive a “Complete” grade. Pac fat! Good luck!**

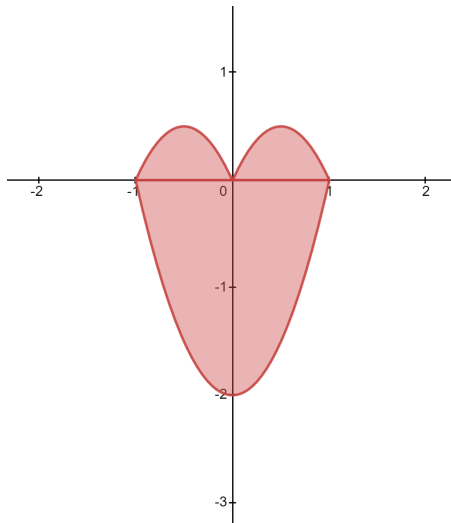
Name: \_\_\_\_\_

**LO 6. Area [CORE].** I can use the “divide and conquer strategy” to find areas.

**Criteria for Success:** I can

- use the divide and conquer method to slice a region vertically or horizontally, find the area of a general slice, and setup the corresponding Riemann sum and definite integral
- solve questions related to computing areas or average values of functions

**Question:** A student came up with the following graph of a heart for Valentine’s day: <https://www.desmos.com/calculator/17sj2ribee>, given by the equations  $y = -2x(x + 1)$  on the interval  $[-1, 0]$  and  $y = -2x(x - 1)$  on the interval  $[0, 1]$  for the top part of the heart and  $y = 2(x^2 - 1)$  on the interval  $[-1, 1]$  for the bottom part of the heart. Find the exact area of the heart using two different methods. Check to make sure the answers match and are reasonable.



**LO 9. Volume and Mass/Weight [CORE].** I can use the divide and conquer strategy to find the volume, mass or weight of an object.

**Criteria for Success:** I can

- use the divide and conquer method to slice a shape, find the volume or mass/weight of a general slice using similar figures, or the Pythagorean Theorem, and setup the corresponding Riemann sum and definite integral
- use the divide and conquer method to slice a shape of revolution, find the volume of a general slice by discs/washers or tubes/shells, and setup the corresponding Riemann sum and definite integral

**Question:** What is the volume of the shape created by rotating the heart in the previous question about the  $y$ -axis. Show the application of Divide and Conquer method by filling out the following blanks. **Setup but do not solve the definite integral.**

Volume of slice:

Riemann Sum:

Sketch of slice:

Definite Integral: