

Problem: Input  $\rightarrow$  Output

Algorithm :   
  $\rightarrow$  (I) correctness   
  $\rightarrow$  (II) efficient   
  $\rightarrow$  time efficient   
  $\rightarrow$  space efficient

Sorting Problem: Input:  $a_1, a_2, \dots, a_n$  (array of size  $n$ )

Output: reordering (permutation)

$a_{i_1}, a_{i_2}, \dots, a_{i_n}$

$a_{i_1} \leq a_{i_2} \leq \dots \leq a_{i_n}$

Example Input: 7, 10, 1, -2, 4

Output: -2, 1, 4, 7, 10

Insertion sort

Merge sort

Quick sort

linear sorting (radix sort, bucket sort, counting sort)

## Insertion sort

### Pseudo-code

Insertion-Sort (  $A[1 \dots n]$  )

for  $i=1$  to  $n$

(1)  $aux = A[i]$

(2)  $j = i-1$

(3) while (  $j > 0$  &&  $A[j] > aux$  )

$A[j+1] = A[j]$

$j = j-1$

} constant  
time

} time  
to run:  
 $t_i$

(4)  $A[j+1] = aux$

### Example

Input: 7 9 6 1 8

$i=1$ : 7 9 6 1 8  $\rightarrow A[1]$  sorted

$i=2$ : 7 9 6 1 8  $\rightarrow A[1..2]$  sorted

$i=3$ : 7 6 9 1 8

6 7 9 1 8  $\rightarrow A[1..3]$  sorted

$i=4$ : 1 6 7 9 8  $\rightarrow A[1..4]$  sorted

$i=5$     1   6   7   8   9  $\rightarrow A[1 \dots 5]$  sorted

	(1)	(2)	(3)	(4)
SC : constant in-place	constant	constant	X	X

TC	constant C	constant C	$t_1 + t_2 + \dots + t_n$	constant C
----	---------------	---------------	---------------------------	---------------

$t_i :=$  time needed to run line (3)

for-loop running time:

$$i=1: \underbrace{(1) + (2) + (4)}_{3C} + \underbrace{(3)}_{t_1} = 3C + t_1$$

$i=2:$

$3C + t_2$

$\vdots$

$\vdots$

$i=n:$

$3C + t_n$

$=$

$$\text{total TC} = \underbrace{3C + \dots + 3C}_{n \text{ times}} + (t_1 + \dots + t_n) = (3C)n + \sum_{i=1}^n t_i$$