

## Xi Liu, Assignment 4

1

let the message be  $m$ , ciphertext be  $c$ , public key be  $\langle n, e \rangle$ , private key be  $\langle n, d \rangle$

$$\begin{aligned}c & \equiv m^e \pmod{n} \\ c' & \equiv (2m)^e \equiv 2^e m^e \equiv 2^e c \pmod{n}\end{aligned}$$

Trudy can send  $c' = 2^e c \pmod{n}$  to Alice

2

2 or more signatures from the signer are required to forge a signature

$$\begin{aligned}m, m_1 & \in \mathbb{Z}^* \\ m_2 & := m/m_1 \pmod{n} \\ \sigma & := \sigma_1 \sigma_2 \pmod{n} \\ \sigma^e & = (\sigma_1 \sigma_2)^e = (m_1^d m_2^d)^e = m_1^{ed} m_2^{ed} = m_1 m_2 = m \pmod{n}\end{aligned}$$

$\sigma$  is a valid signature since  $\sigma_1, \sigma_2$  are valid signatures. this is a forgery since  $m \neq m_1, m \neq m_2$

3

this is hiding since based on the Decisional Diffie Hellman assumption and hardness of discrete logarithm problem, it is hard to compute  $a, b$  from knowing only  $g$  and  $m \cdot g^{ab}$ . it is binding since  $g^{ab}$  is sent to the receiver first, the sender cannot change the copy that was sent to the receiver before sending  $a$  and  $b$

4

if Bob has a way to change his bit  $b_1$  after seeing Alice opening her  $b_0$ , then this is insecure

a better way is for Alice to send  $com(b_0)$  to Bob first, then Bob send his  $b_1$  to Alice, then Alice opens  $b_0$ , in this way the integrity of  $b_0$  is ensured