



# Statistical analysis (II)

## -- complex experimental designs

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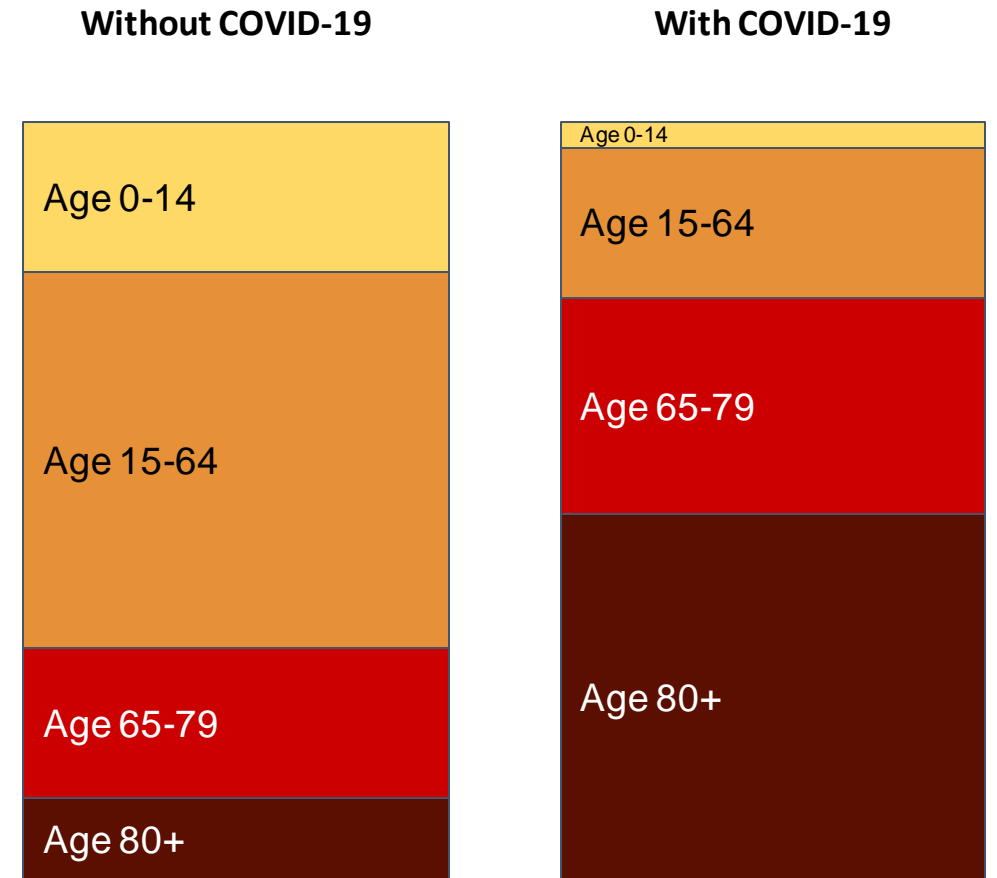
# Why complex meta-data?

- More studies are collecting samples from the “real world”:
  - Epidemiology
  - Field studies
- These samples have many uncontrolled variables (covariates):
  - Biological: sex, age, disease status
  - Environmental: location, lifestyle, temperature
- Taking covariates into account can increase statistical power and reduce confounding relationships between primary variable of interest and ‘omics data



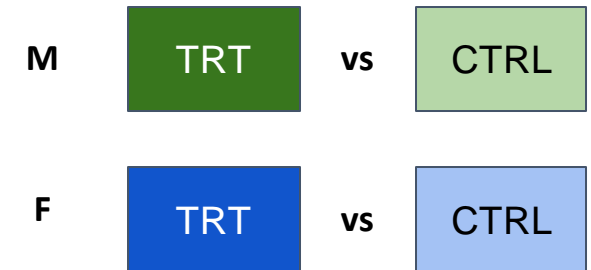
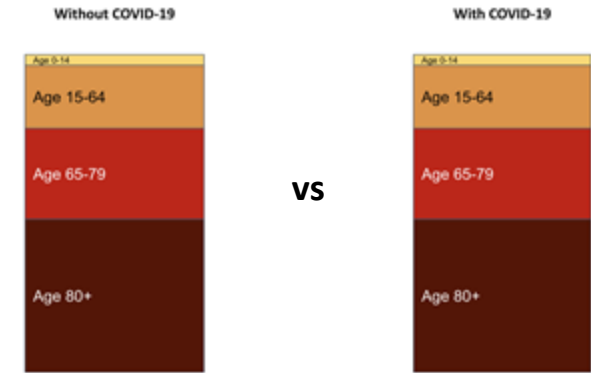
# Confounding factors: example

- Objective: identify metabolites associated with COVID-19
- Data: blood samples from subjects with and without COVID-19
  - Not a controlled experiment
  - Early in pandemic, more COVID-19 diagnoses in older subjects
- Problem: difficult to distinguish metabolites related to age vs. related to COVID-19



# Strategies for dealing with meta-data

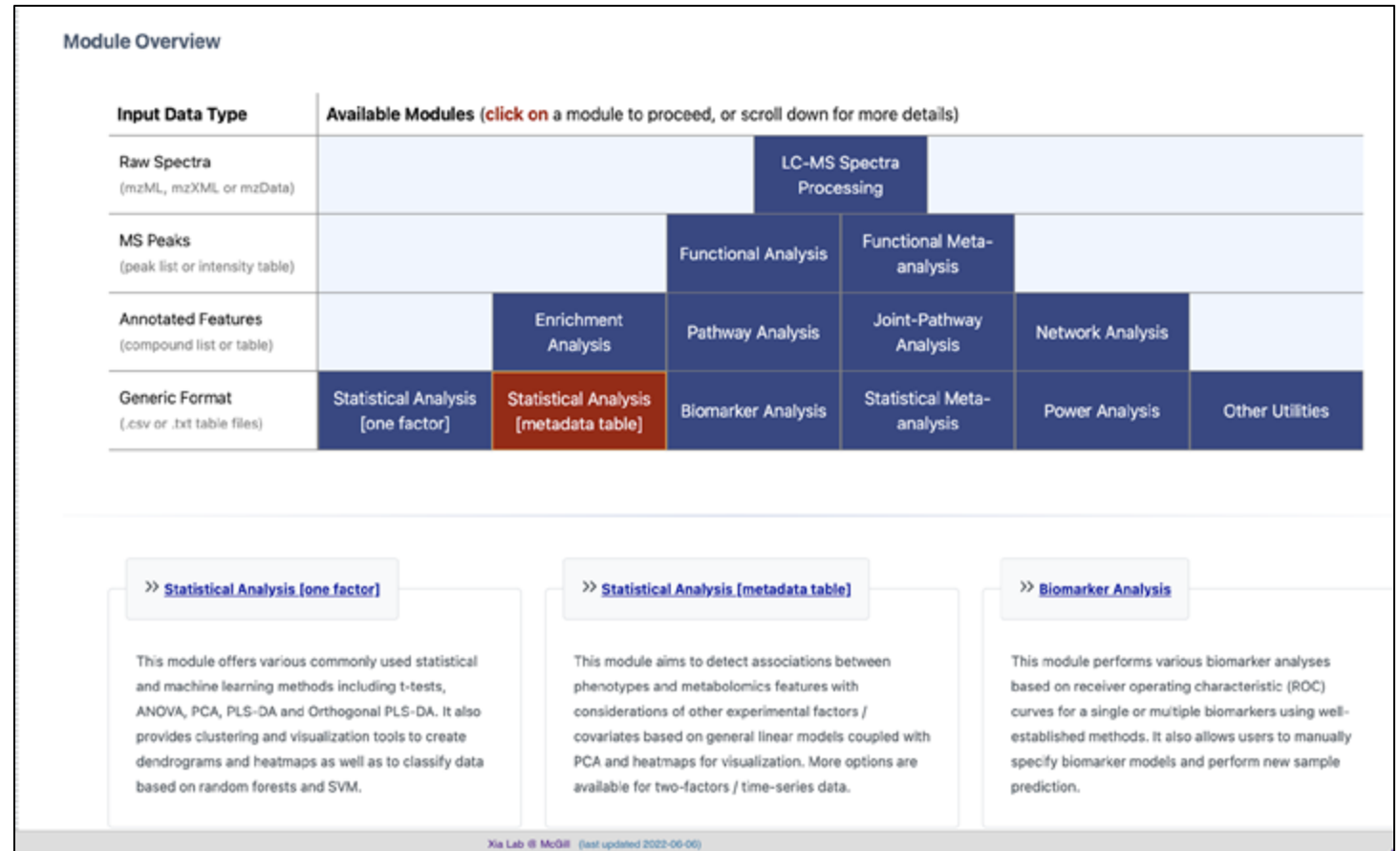
- Experimental design:
  - **Control** group that 'matches' your group of interest
- Data analysis (often limited by sample size):
  - **Stratification** - for factors with few classes, split up the data and analyze separately
  - **Take into account** - statistical Analysis [metadata table] module in MetaboAnalyst



$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * x_n$$

# Complex meta-data with MetaboAnalyst
















- We will cover how to:
  - Format meta-data
  - Analyze relationships between meta-data
  - Covariate adjustment with linear model
  - Supervised analysis with Random Forest



# Formatting meta-data

- Essential for downstream analysis
- Categorize as “Categorical” or “Continuous”
  - For categorical, must have at least 2 groups with at least 3 replicates each
- Missing values will be filtered out during analysis
- First meta-data column will be considered primary variable by default

Sample	TCE_Exp_Category	TCE_Exp_Conc	Age	Sex	Smoking_Status	Alcohol_Use	BMI	Batch
X1014	Low	0.025	28	Male	Yes	Yes	20.3	10
X1049	Low	0.025	34	Female	No	No	33.7	1
X1068	Low	0.025	30	Male	Yes	No	25.6	7
X1070	Low	0.025	42	Male	Yes	No	21.6	1
X1071	Low	0.025	41	Female	No	No	20.7	4
X1073	Low	0.025	22	Male	No	Yes	20.6	4
X1074	Low	0.025	26	Female	No	No	18.7	13
X1075	Low	0.025	26	Male	Yes	Yes	23.1	12
X1076	Low	0.025	16	Male	Yes	Yes	18.4	11
X1078	Low	0.025	32	Female	No	No	19.2	7
X1079	Low	0.025	22	Male	Yes	No	20.3	9
X1080	Low	0.025	25	Female	No	No	21.3	7
X1089	Low	0.025	30	Male	No	No	22.8	3
X1090	Low	0.025	33	Male	No	No	25.5	10
X1091	Low	0.025	27	Male	No	Yes	18.8	12
X1092	Low	0.025	29	Male	No	No	23.6	2
X1094	Low	0.025	35	Male	Yes	No	24	5
X1095	Low	0.025	33	Male	Yes	No	21	12
X1097	Low	0.025	27	Male	No	No	18.4	5
X1098	Low	0.025	32	Male	No	Yes	23.2	6
X1099	Low	0.025	20	Male	No	No	16.9	8
X1100	Low	0.025	23	Male	Yes	Yes	19	12
X1101	Low	0.025	25	Male	Yes	Yes	21.1	3
X1106	Low	0.025	40	Male	No	No	30.5	2
X1110	Low	0.025	18	Male	No	Yes	21	2
X1112	Low	0.025	28	Male	No	Yes	21.3	5

Name	Status	Type	Edit	Remove
TCE_Exp_Category	OK	Categorical 	<a href="#">Edit</a>	
TCE_Exp_Conc	OK	Categorical	<a href="#">Edit</a>	
		Continuous		
Age	OK	Continuous 	<a href="#">Edit</a>	
Sex	OK	Categorical 	<a href="#">Edit</a>	
Smoking_Status	OK	Categorical 	<a href="#">Edit</a>	
Alcohol_Use	OK	Categorical 	<a href="#">Edit</a>	
BMI	OK	Continuous 	<a href="#">Edit</a>	
Batch	OK	Categorical 	<a href="#">Edit</a>	

# Method overview

Overview to understand  
structure of data & metadata

Simple yet effective univariate  
statistical analysis

Advanced multivariate statistics  
& machine learning

## Data and Metadata Overview

### [Metadata Visualization](#)

Users can explore the metadata patterns and correlations through intuitive graphics. It is very useful for users to identify highly dependent metadata and quickly assess the overall patterns of the metadata.

### [Interactive PCA Visualization](#)

Users can visualize data using different colors or shapes based on selected metadata in an 2D and 3D (interactive) PCA plots. It is very useful to detect overall patterns of data with regard to different metadata.

### [Hierarchical Clustering and Heatmap Visualization](#)

This method displays data and metadata in the form of colored cells. It provides direct visualization of feature abundances across different samples and metadata.

## Univariate Analysis

### [Linear Models with Covariate Adjustment](#)

This approach uses linear models (limma or lm) to perform significance testing with covariate adjustments. Users can choose different metadata to be included in the analysis.

### [Correlation and Partial Correlation Analysis](#)

This approach allows users to explore the correlations or partial correlations (with covariate adjustments) between metabolomics features and different metadata of interest.

### [Two-way ANOVA \(ANOVA2\)](#)

This approach provides classical two-way ANOVA based on the two factors selected by users. For time-series data, users should choose within-subjects ANOVA.

## Multivariate Analysis

### [ANOVA Simultaneous Component Analysis \(ASCA\)](#)

This approach is designed to identify major patterns with regard to the two given factors and their interaction. The implementation was based on the algorithm described by [AK Smilde, et al.](#) with additional improvements on feature selection and model validation.

### Multivariate Empirical Bayes Analysis of Variance (MEBA) for Time Series

This approach is designed to compare temporal profiles across different biological conditions. It is based on the timecourse method described by [YC Tai, et al.](#)

## Supervised Classification

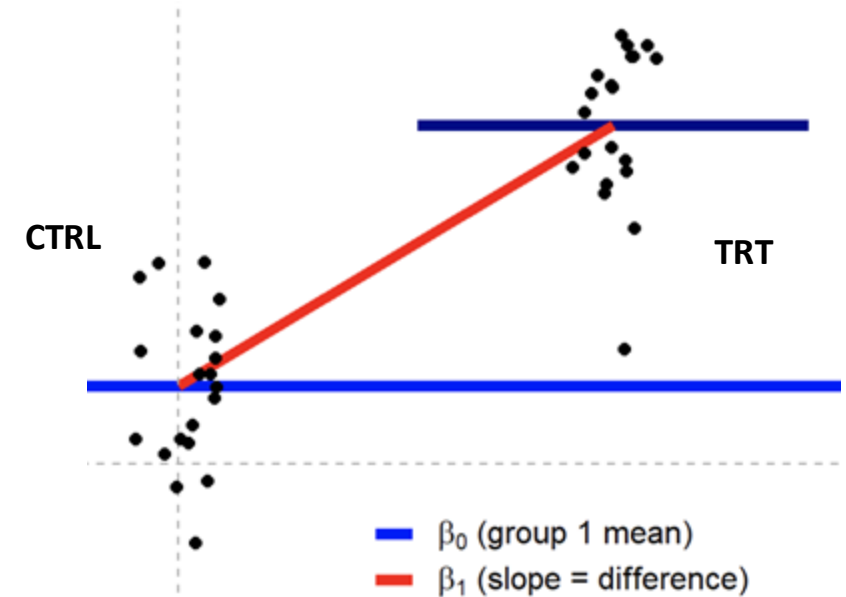
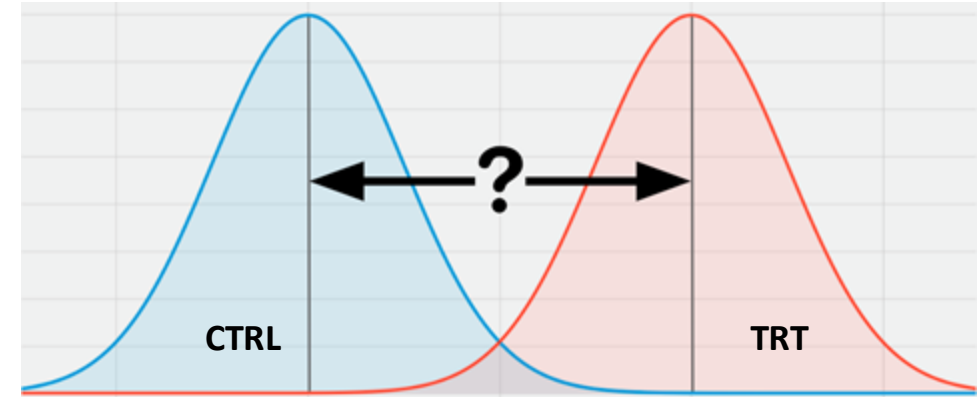
### [Random Forest](#)

This machine learning approach is designed to perform classification and feature selection analysis. Users can also test contribution of meta-data to class prediction.



# T-test vs. linear regression

- You can do t-test with linear regression:
- $y = B_0 + B_1 * x$ 
  - $y$ : level of metabolite A
  - $x$ : variable of interest





# More complex experimental design

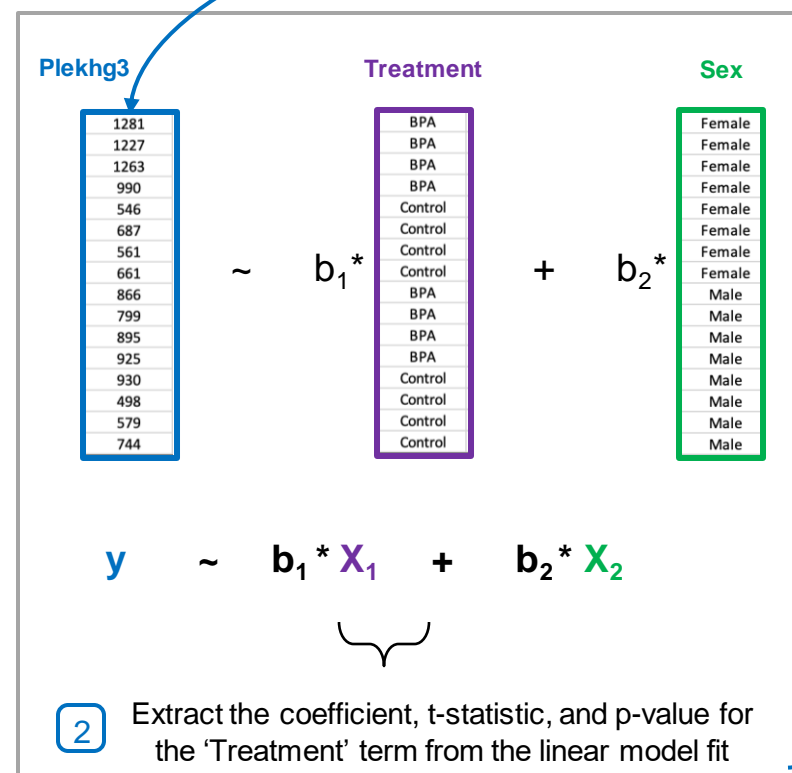
- Treatment (Control/BPA)
- Sex (male/female)
- Features associated with ***treatment*** while considering **sex**
- Treatment = primary
- Sex = covariate
- Can include many covariates
- Primary/covariate can be continuous or discrete

[illegible]

```
-- all ~15k transcripts --
```

[Feb2]	129	220	155	144	65	126	95	117	87	67	106	128	109	77	80
[Feb3]	3	4	2	0	0	0	4	0	2	0	0	0	0	4	0
[Anno1]	468	446	560	487	304	446	316	303	253	267	383	361	279	358	326

1 Perform linear regression for each transcript



3 Compile all results in a table

Symbols	BPA-Control t	P.Value	adj.P.Val
Maz	0.18999	2.7563	0.015091
Slc11a2	0.27426	2.7561	0.015096
Cyhr1	0.1355	2.7557	0.01511
Tbc1d2b	0.26692	2.7554	0.015117
Sat1	0.61953	2.7552	0.015124
Cers2	0.16232	2.7549	0.015131
Cox11	0.31729	2.7549	0.015133
Ccdc117	0.49021	2.7548	0.015136
Plekhh3	0.31496	2.754	0.01516
Lmo2	-0.44288	-2.754	0.015161
Pgam2	1.7962	2.7534	0.015178
Ublcp1	-0.16546	-2.7534	0.015178
Polr2g	0.20745	2.7533	0.015181
Nrxn1	-0.22709	-2.7523	0.015212
Uap111	0.49729	2.7521	0.015217
Mgst1	0.24975	2.7518	0.015226
Zfp93	0.24983	2.7517	0.015229
Bola2	-0.23162	-2.7513	0.015242
Eif2d	0.17861	2.7507	0.01526
Nadk	0.18645	2.7506	0.015263
Csnk1g1	-0.24522	-2.75	0.015281
Marveld2	0.32542	2.7496	0.015292
Grb7	0.21623	2.7487	0.015321
Cdk20	0.4224	2.748	0.015342
Akt1s1	0.15424	2.7468	0.015378
Ppm1g	-0.22411	-2.7463	0.015394
Sudc3	0.16652	2.7462	0.015395

```
-- all ~15k transcripts --
```

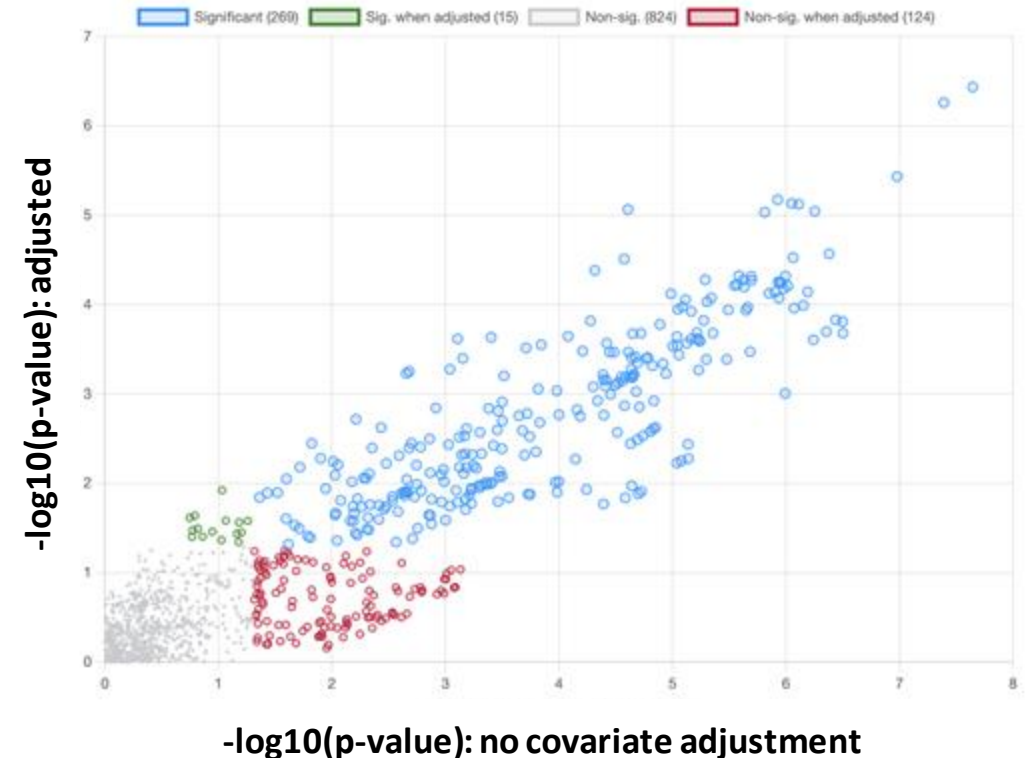
Cep97	0.35979	2.7449	0.015436	0.0528
Slc35a1	0.20103	2.7448	0.015438	0.0528
Aifm3	0.90739	2.7433	0.015484	0.052

# Interpretation of coefficient results

Multiple linear regression example:

- $y = B_0 + B_1 * x_{\text{treatment}} + B_2 * x_{\text{sex}}$

- By including  $B_2 * x_{\text{sex}}$  in the model, we account for effects of sex
- Extract  $B_1$  from the model:
  - $B_1$  value = magnitude & direction of relationship between metabolite 'y' and  $x_{\text{treatment}}$
  - $B_1$  p-value = statistical significance of relationship

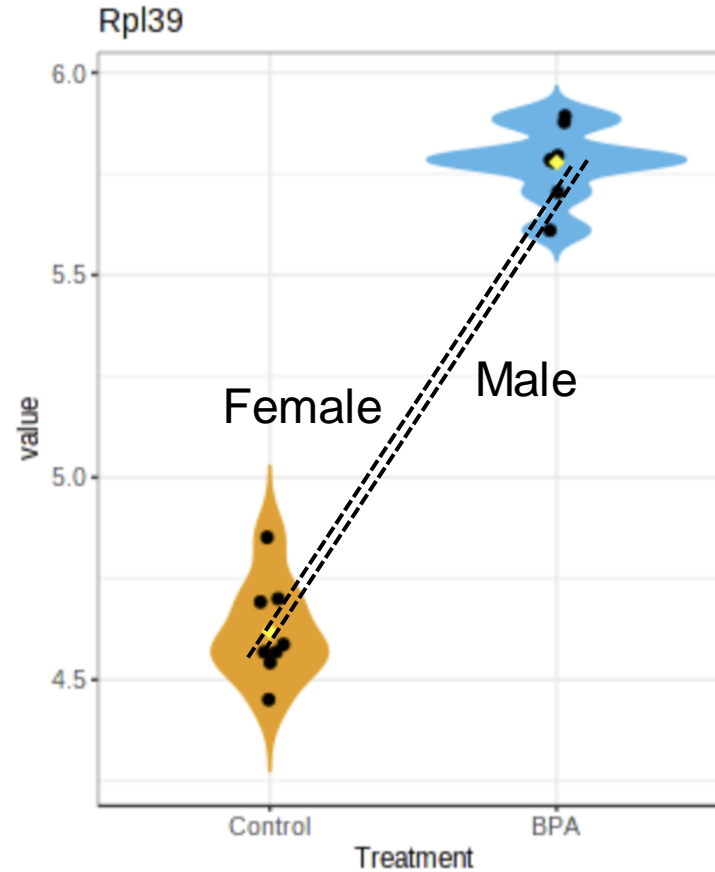


# Impact of controlling for sex

## Linear Model

Y ~ Treatment

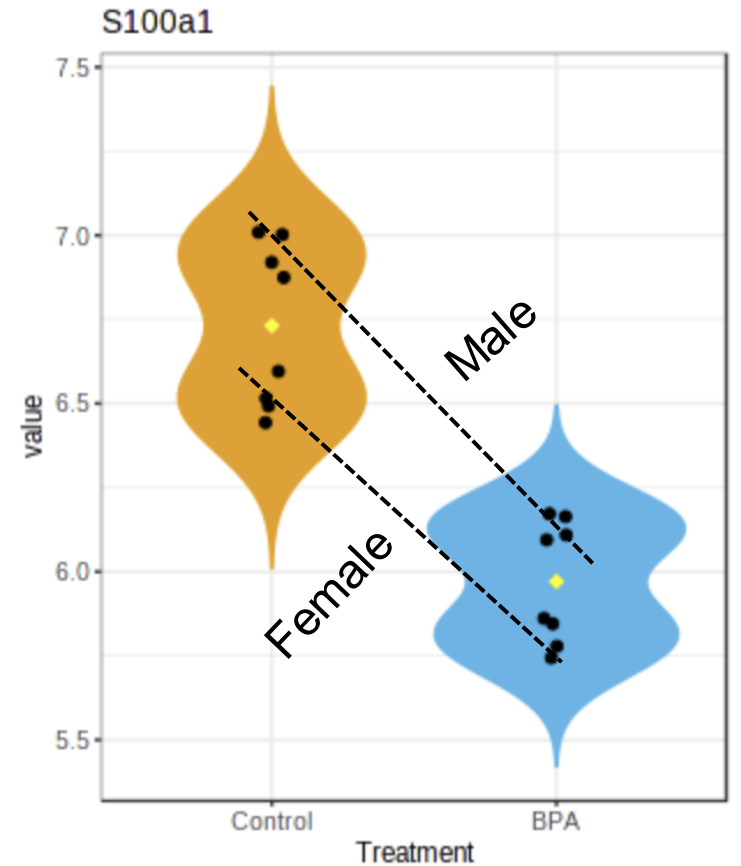
Y ~ Treatment + Sex



## Rpl39 Treatment P-value

$3.7 \times 10^{-12}$

$9.9 \times 10^{-12}$



## S100a1 Treatment P-value

$2.9 \times 10^{-6}$

$2.1 \times 10^{-11}$

# Functional Analysis

**Feature Details Table**

Click a feature name to edit its name and then click the next column to save the change. Click the view link to visualize a graphical summary of the distribution. The bar plots on the left show the original values (mean +/- SD). The box and whisker plots on the right summarize the normalized values. Note, positive infinite numbers are represented as 999999, and negative infinite numbers -999999.

To update a name suitable for graphical display, **click the name** to edit and then click the next column to save

 Download

Name ↑↓	logFC ↑↓	AveExpr ↑↓	t ↑↓	P.Value ↑↓	adj.P.Val ↑↓	B ↑↓	
<input type="text"/>							
319.227@344.95	0.73798	0.30435	6.9298	4.2134E-9	8.6544E-6	10.605	<a href="#">View</a>
347.2582@379.62	0.59923	-0.76139	6.6574	1.1944E-8	1.2266E-5	9.6281	<a href="#">View</a>
173.9855@96.75	-1.793	-2.1814	-6.2058	6.6605E-8	4.5602E-5	8.0165	<a href="#">View</a>
343.2271@340.17	0.50703	-0.45557	5.9527	1.7321E-7	8.8942E-5	7.1202	<a href="#">View</a>
357.1785@488.19	0.25935	-0.70776	5.5101	9.0415E-7	3.2343E-4	5.5712	<a href="#">View</a>
335.2944@537.41	0.39263	-0.40041	5.426	1.2334E-6	3.2343E-4	5.2803	<a href="#">View</a>
309.2794@532.6	0.34348	1.3126	5.4032	1.3415E-6	3.2343E-4	5.2017	<a href="#">View</a>
310.2826@532.64	0.34901	0.65576	5.3926	1.3946E-6	3.2343E-4	5.1653	<a href="#">View</a>
303.2328@438.79	0.29848	1.6434	5.3883	1.4172E-6	3.2343E-4	5.1503	<a href="#">View</a>
385.2345@438.71	0.26685	-0.49809	5.3122	1.8737E-6	3.8486E-4	4.8889	<a href="#">View</a>
304.2362@438.81	0.30433	0.99595	5.2773	2.129E-6	3.9629E-4	4.7693	<a href="#">View</a>

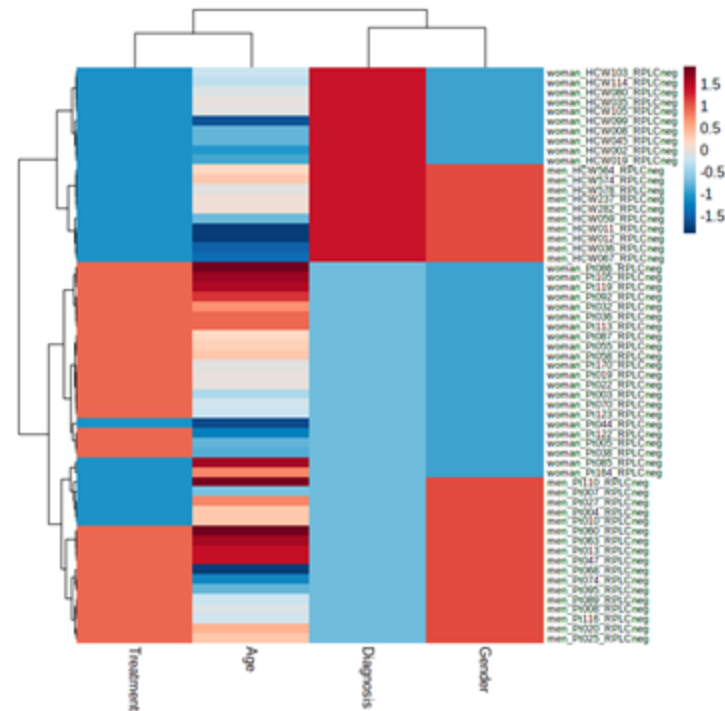
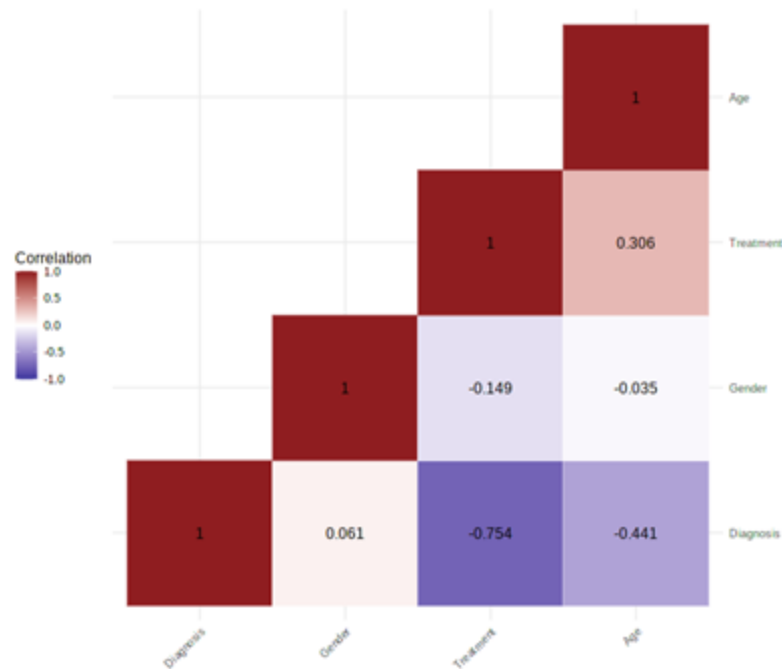
Use for functional analysis

# Important considerations

- Adding more variables into the model decreases statistical power
- Be strategic:
  - Do not include variables that have no impact on your data
  - Do not include correlated metadata
- Assess this with PCA, linear models, and metadata overview
  - We will go over this in the demo

# Relationships between metadata

- Must understand relationships between predictors
  - Know which to include in model (sample size)
  - Guide interpretation of the results



# Non-linear Strategies

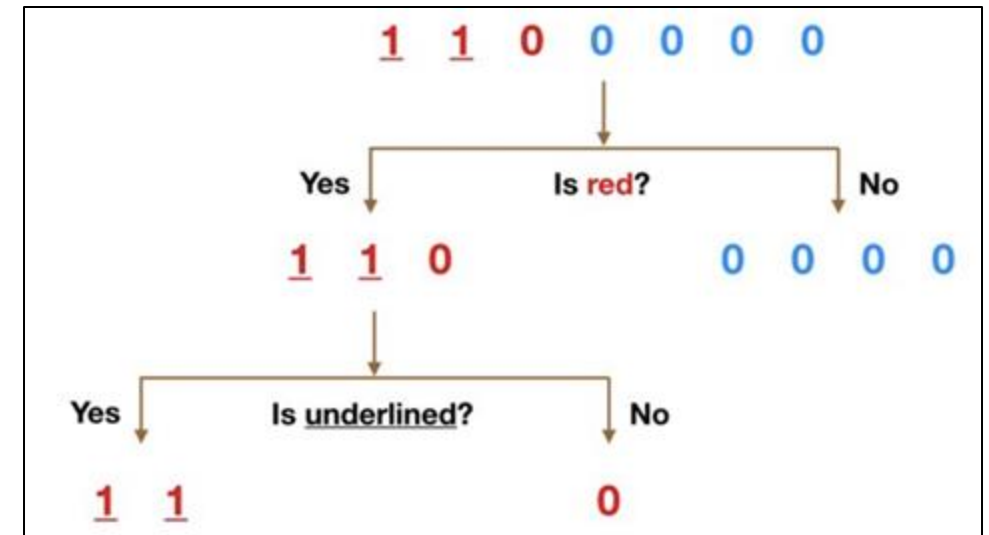
- All methods so far rely on linear relationships
  - Very stable, robust against overfitting
  - Only option with small sample size
- Many non-linear relationships in complex data
- Random forest is one approach
  - Uses decision trees

## Example Decision Tree

Predict whether digit is a “1” or a “0”

Two variables:

- Color (red, blue)
- Underlined (yes, no)





# Random Forest Classification

- In Random Forest, we build 1000s of trees
- For each tree, randomly select:
  - Random subset of metabolites + metadata
  - Random subset of samples
- Then, build a tree
- Use the rules from each tree to predict the class label for all samples (ie. COVID, healthy)
- Final prediction: majority wins

Figures from:

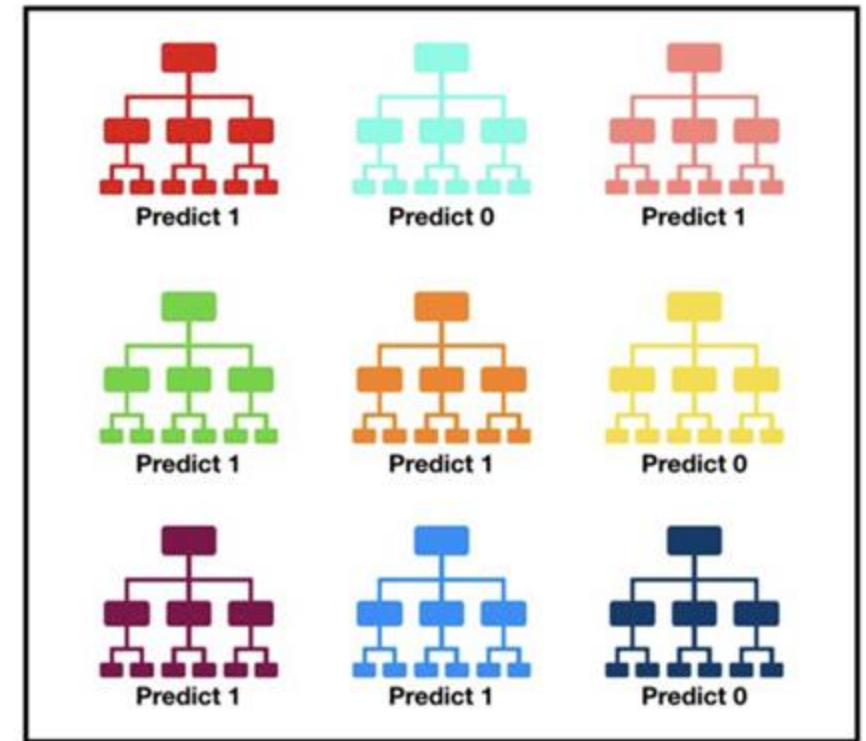
**Understanding Random Forest**

How the Algorithm Works and Why it Is So Effective



Tony Yiu

Example forest of trees



Tally: Six 1s and Three 0s

**Prediction: 1**

# Example Classification Results

Primary metadata:

Diagnosis ▼

Choose metadata for predictors:

Gender ✕

Age ✕

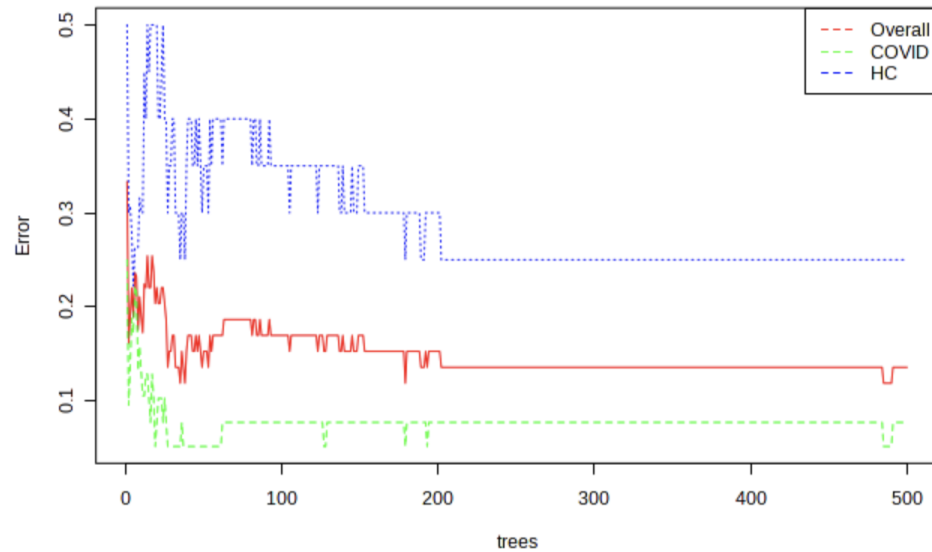
▼

Update

Randomness:

On ▼

Random Forest classification



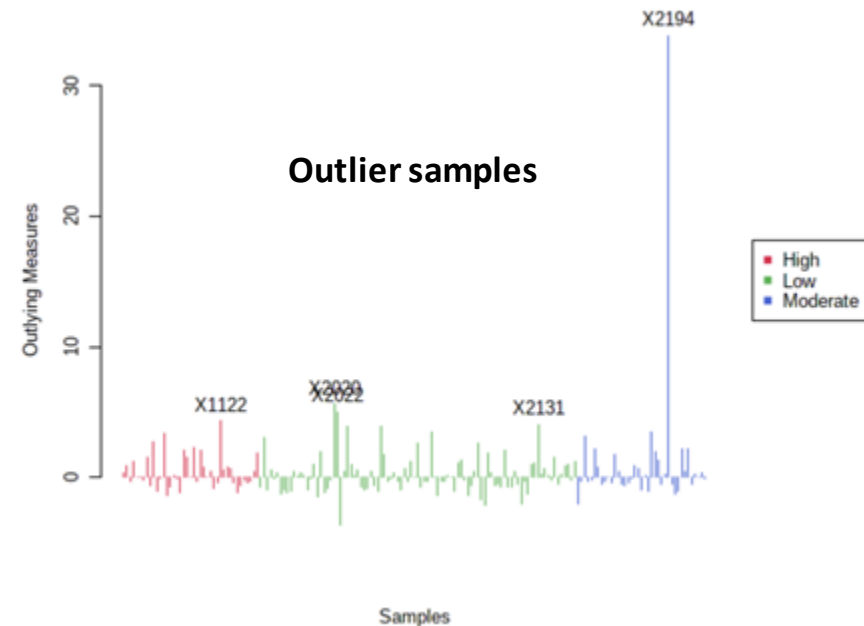
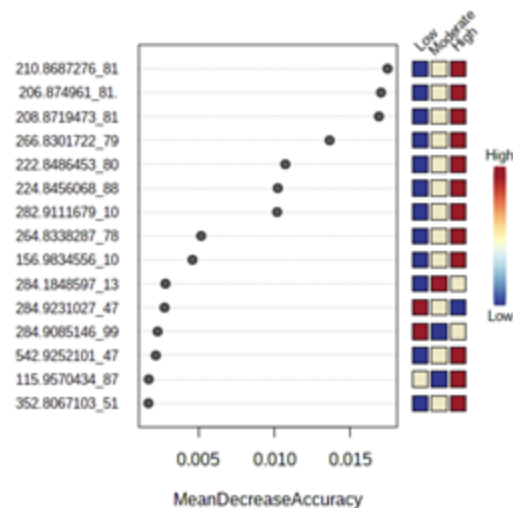
The OOB error is 0.136

	COVID	HC	class.error
COVID	36	3	0.0769
HC	5	15	0.25

# Using Random Forest in MetaboAnalyst

- Using model in real life requires extensive validation & careful design
- Most MetaboAnalyst users: use as form of exploratory statistics
- Understand which variables have high predictive power
  - Var. Importance tab
- Identify potential outlier observations
  - “Outlier Detection” tab

Most important variables



# Hands-On Demo