points

As we have seen in the lecture videos, the dot product of vectors has a lot of applications. 1. Here, you will complete some exercises involving the dot product.

What is the size of the vector $\begin{bmatrix} 1 \\ 3 \\ 4 \\ 2 \end{bmatrix}$?

 $\sqrt{10}$

 $\sqrt{30}$

Correct

The size of the vector is the square root of the sum of the squares of the components.

10

30

points

2.

What is the dot product of the vectors $\begin{bmatrix} -5 \\ 3 \\ 2 \\ 8 \end{bmatrix}$ and $\begin{bmatrix} 1 \\ 2 \\ -1 \\ 0 \end{bmatrix}$?

-1

The dot product of two vectors is the total of the component-wise products.

points

Let $\mathbf{r} = \begin{bmatrix} 3 \\ -4 \\ 0 \end{bmatrix}$ and let $\mathbf{s} = \begin{bmatrix} 10 \\ 5 \\ -6 \end{bmatrix}$. What is the scalar projection of s onto r?

 $-\frac{1}{2}$

-2

The scalar projection of of ${\bf s}$ onto ${\bf r}$ can be calculated with the formula $\frac{r \cdot s}{|r|}$

Let $\mathbf{r} = \begin{bmatrix} 3 \\ -4 \\ 0 \end{bmatrix}$ and let $\mathbf{s} = \begin{bmatrix} 10 \\ 5 \\ -6 \end{bmatrix}$. What is the vector projection of s onto r?

 $\begin{bmatrix} 30 \\ -20 \\ 0 \end{bmatrix}$

 $\begin{bmatrix}
6/5 \\
-8/5 \\
0
\end{bmatrix}$

The vector projection of \mathbf{s} onto \mathbf{r} can be calculated with the formula $\frac{r \cdot s}{r \cdot r} r$.

 $\begin{bmatrix} 6 \\ -8 \\ 0 \end{bmatrix}$

Given Let $\mathbf{a} = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$ and let $\mathbf{b} = \begin{bmatrix} 0 \\ 5 \\ 12 \end{bmatrix}$. Which is larger, $|\mathbf{a} + \mathbf{b}|$ or $|\mathbf{a}| + |\mathbf{b}|$?

 $|\mathbf{a} + \mathbf{b}| \ge |\mathbf{a}| + |\mathbf{b}|$

 $|\mathbf{a} + \mathbf{b}| = |\mathbf{a}| + |\mathbf{b}|$

 $|\mathbf{a} + \mathbf{b}| \le |\mathbf{a}| + |\mathbf{b}|$

Correct

This is in general true for any a or b. This is called the "triangle inequality".