1. transaction totals €15. On Tuesday you buy 3 apples, 2 bananas, 1 carrot, all for €28. Then on Wednesday 2 apples, 1 banana, 2 carrots, for €23. Construct a matrix and vector for this linear algebra system. That is, for

You go to the shops on Monday and buy 1 apple, 1 banana, and 1 carrot; the whole

$$A \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} s_{
m Mon} \\ s_{
m Tue} \\ s_{
m Wed} \end{bmatrix}$$
 Where  $a$ ,  $b$ ,  $c$ , are the prices of apples, bananas, and carrots. And each  $s$  is the total for that day.

Fill in the components of A and s. 1 - # Replace A and s with the correct values below: A = [[1, 1, 1],

[3, 2, 1], [2, 1, 2]]

```
Run
6 	 s = [15, 28, 23]
                                                                             Reset
Correct Response
Correct! Well done.
```

①, if we divide the whole row by 4, then the top-left element of the matrix becomes 1,

2.

①: 
$$\begin{bmatrix} 4 & 6 & 2 \\ 3 & 4 & 1 \\ 2 & 8 & 13 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9 \\ 7 \\ 2 \end{bmatrix}$$
We wish to convert this to echelon form, by using elimination. Starting with the first row,

Given another system,  $B\mathbf{r} = \mathbf{t}$ ,

Next, we need to fix the second row. This results in the following,

What steps did we take?

row, i.e., @'' = [@' - 2@'].

Correct

system?

Fix row 3 to be a linear combination of the other two. What is the echelon form of the

We've made the new second row a linear combination of previous rows.

The new second row,  $\mathfrak{D}''$  is the old second row minus two times the old first

points

$$\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 5 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ -5/2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ 1/2 \end{bmatrix}$$

From the previous question, our system is almost in echelon form.

4.

Correct

3.

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ -1/4 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ 0 \end{bmatrix}$$

What is the value of  $\begin{bmatrix} a \\ b \\ c \end{bmatrix}$ ?

 $\mathbf{r} = \begin{bmatrix} 3 \\ -1/2 \\ 0 \end{bmatrix}$ 

Correct

This system is now in echelon form.

Taking your answer from the previous part, use back substitution to solve the system.

5.

points

$$\begin{bmatrix} 1 & A'_{12} & A'_{13} \\ 0 & 1 & A'_{23} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} s'_1 \\ s'_2 \\ s'_3 \end{bmatrix}.$$

Find values for A' and s'.

A = [[1, 1, 1],3 [ 0, 1, 2], 4 [ 0, 0, 1 ]]

5 s = [15, 17, 5]

**Correct Response** Correct! Well done.

Let's return to the apples and bananas from Question 1.

1 - # Replace A and s with the correct values below:

Take your answer to Question 1 and convert the system to echelon form. I.e.,

Run

Reset

Run

Reset

Run

Reset

Run

Reset

Run

Reset

6.

Following on from the previous question; now let's solve the system using back substitution.

2 s = [3, 7, 5]

**Correct Response** Correct! Well done.

3

3

4

5

question.

3

4

3

6

4

1

8.

**Correct Response** Correct! Well done.

What is the price of apples, bananas, and carrots?

totals - then you should solve the system in general.

2 Ainv = [[-3/2, 1/2, 1/2],

[2, 0, -1],

[1/2, -1/2, 1/2]

That is, find the inverse of the matrix you used in Question 1.

1 - # Replace a, b, and c with the correct values below:

1 - # Replace the matrix elements with the correct values below:

points

A = [[1, 1, 3],4 [1, 2, 4],5 [1, 1, 2]]6 Ainv = np.linalg.inv(A)

Use this code block to see *numpy* invert a matrix.

import numpy as np

a

r = np.linalg.solve(A, s)

In general, one shouldn't calculate the inverse of a matrix unless absolutely necessary. It is more computationally efficient to solve the linear algebra system if that is all you need. Use this code block to solve the following linear system with *numpy*.  $A\mathbf{r} = \mathbf{s}$ ,

You can try to invert any matrix you like. Try it out on your answers to the previous

2 13 [ c ] 8 1 import numpy as np 2 A = [[4, 6, 2],

linear algebra routines are quicker to solve the system for each case.

**Correct Response** In cases when you don't need the inverse matrix itself,

8