

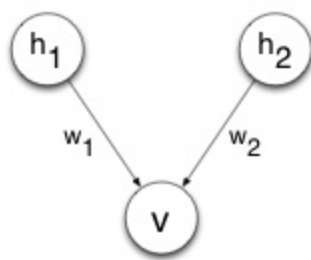


1 / 1 points

1. This quiz is going to take you through the details of Sigmoid Belief Networks (SBNs). The most relevant videos are the second video ("Belief Nets", especially from 11:44) and third video ("Learning sigmoid belief nets") of lecture 13.

See also the extra resources in the Lecture Slides reading.

We'll be working with this network:



The network has no biases (or equivalently, the biases are always zero), so it has only two parameters:  $w_1$  (the weight on the connection from  $h_1$  to  $v$ ) and  $w_2$  (the weight on the connection from  $h_2$  to  $v$ ).

Remember, the units in an SBN are all binary, and the logistic function (also known as the sigmoid function) figures prominently in the definition of SBNs. These binary units, with their logistic/sigmoid probability function, are in a sense the stochastic equivalent of the deterministic logistic hidden units that we've seen often in earlier lectures.

Let's start with  $w_1 = -6.90675478$  and  $w_2 = 0.40546511$ . These numbers were chosen to ensure that the answer to many questions is a very simple answer, which might make it easier to understand more of what's going on. Let's also pick a complete configuration to focus on:  $h_1 = 0, h_2 = 1, v = 1$  (we'll call that configuration  $C_{011}$ ).

Ready to Begin? (Please select a response. This question is reflective and selecting a certain answer will not affect your grade.)

- ☒ Yes
- ☐ No



1 / 1 points

2. What is  $P(v = 1 | h_1 = 0, h_2 = 1)$ ? Write your answer with four digits after the decimal point. Hint: the last three of

those four digits are zeros. (If you're lost on this question, then I strongly recommend that you do whatever you need to do to figure it out, before

proceeding with the rest of this quiz.)

0.6000

**Correct Response**

Pretend that this is a feed-forward neural network with two hidden units and a logistic output neuron. You're now calculating the output of the network given that the hidden units have taken on the values  $h_1 = 0$  and  $h_2 = 1$ .



1 / 1 points

3. What is the probability of that full configuration, i.e.  $P(h_1 = 0, h_2 = 1, v = 1)$ , which we called  $P(C_{011})$ ? Write your answer with four digits

after the decimal point. Hint: it's less than a half, and the last two of those four digits are zeros.

0.1500

**Correct Response**

We can use the rule of multiplication in order to obtain  $P(h_1 = 0, h_2 = 1, v = 1) = P(v = 1 | h_1 = 0, h_2 = 1)P(h_1 = 0, h_2 = 1)$ . Question 1 deals with finding  $P(v = 1 | h_1 = 0, h_2 = 1)$ , now you need to find  $P(h_1 = 0, h_2 = 1)$ . What does the picture given in the preamble tell you about the **marginal** independence of  $h_1$  and  $h_2$  (when we have not observed  $v$ )? Also, remember that  $h_1$  and  $h_2$  both have 0 total input, and that they are logistic neurons.



1 / 1 points

4. What is  $\frac{\partial \log P(C_{011})}{\partial w_1}$ ? Write your answer with at least three digits after the decimal point, and don't be too

surprised if it's a very simple answer.

0.000

**Correct Response**



1 / 1 points

5. What is  $\frac{\partial \log P(C_{011})}{\partial w_2}$ ? Write your answer with at least three digits after the decimal point, and don't be too

surprised if it's a very simple answer.

0.400

**Correct Response**



1 / 1 points

6. What is  $P(h_2 = 1 | v = 1, h_1 = 0)$ ? Give your answer with at least four digits after the decimal point. Hint: it's a fairly small number (and not a round number like for the earlier questions); try to intuitively understand why it's small. Second hint: you might find Bayes' rule useful, but even with that rule, this still requires some thought.

Let's explore it with new weights: for the remainder of this quiz,  **$w_1 = 10$** , and  **$w_2 = -4$** .

0.03472

**Correct Response**

We can use Baye's rule to determine:

$$P(h_2 = 1 | v = 1, h_1 = 0) = \frac{P(v=1|h_1=0,h_2=1)P(h_2=1)}{P(v=1|h_1=0,h_2=1)P(h_2=1)+P(v=1|h_1=0,h_2=0)P(h_2=0)}.$$



1 / 1 points

7. What is  $P(h_2 = 1 | v = 1, h_1 = 1)$ ? Give your answer with at least four digits after the decimal point. Hint: it's quite different from the answer to the previous question; try to understand why. The fact that those two are different shows that, conditional on the state of the visible units, the hidden units have a strong effect on each other, i.e. they're not independent. That is what we call explaining away, and the earthquake vs. truck network is another example of that.

0.4994

**Correct Response**