

Motion Detection

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Abstract

In this project we will explore a simple technique for motion detection in image sequences captured with a stationary camera where most of the pixels belong to a stationary background and relatively small moving objects pass in front of the camera. In this case, the intensity values observed at a pixel over time is a constant or slowly varying signal, except when a moving object begins to pass through that pixel, in which case the intensity of the background is replaced by the intensity of the foreground object. Thus, we can detect a moving object by looking at large gradients in the temporal evolution of the pixel values.

1 Introduction

Motion detection is an interesting and classical topic in the computer vision community, which is a widely-used tool in video surveillance, object tracking, and *etc.* In this paper, we propose a simple implementation for it, based on several image filtering techniques and we will discuss which one is better.

2 Algorithm

Algorithm 1. *Motion Detection based on Temporal Filtering*

Input: a frame sequence I_i , $1 \leq i \leq n$, a 1D temporal filter f_T of length m , a pre-defined threshold θ

Output: a temporal derivative sequence D_i , and the segmented motion objects F_i , $1 \leq i \leq n$

Initial: for $\forall i$, $D_i = 0$

1: Set s as $s = (m - 1)/2$;

2: **for** $i = s + 1 : n - s$ **do**

3: **for** $j = 1 : s$ **do**

4: $D_i = D_i + f_T(s - j + 1)I_{i-j} + f_T(s + j + 1)I_{i+j}$;

5: **end for**

6: **end for**

7: **for** $i = 1 : n$ **do**

8: Get a mask M_i for I_i by using Eq. 1

9: Obtain F_i by $F_i = M_i \odot I_i$;

10: **end for**

3 Experiments

- 1) Read in a sequence of image frames and make them grayscale and apply a 1-D differential operator at each pixel to compute a temporal derivative.
 - (a) Derivative of Gaussian window size: $5 \cdot \text{tsigma}$



original image



simple $0.5[1, 0, 1]$ filter

1D derivative of Gaussian with $\text{tsigma}=1$



1D derivative of Gaussian with $\text{tsigma}=1.8$

1D derivative of Gaussian with $\text{tsigma}=2.6$

(b) Gaussian filter window size: $5 \cdot \sigma$



original image



simple $0.5 \begin{bmatrix} 1 & 0 & 1 \end{bmatrix}$ filter



1D derivative of Gaussian with $\sigma=1$

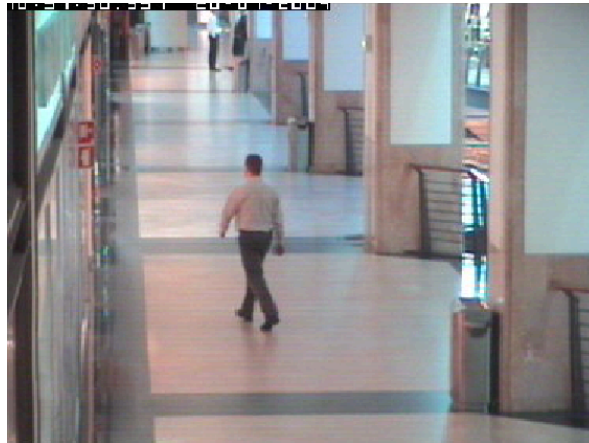


1D derivative of Gaussian with $\sigma=1.8$

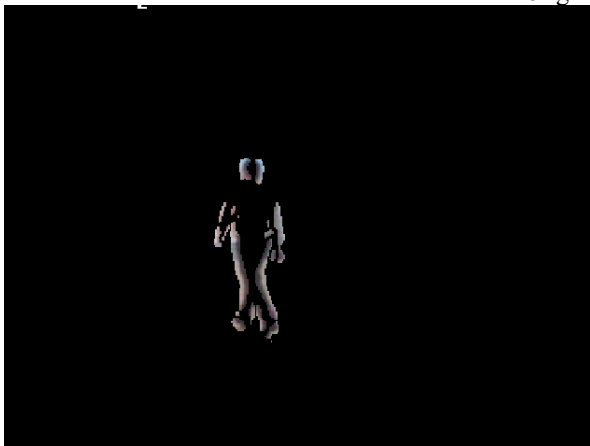


1D derivative of Gaussian with $\sigma=2.6$

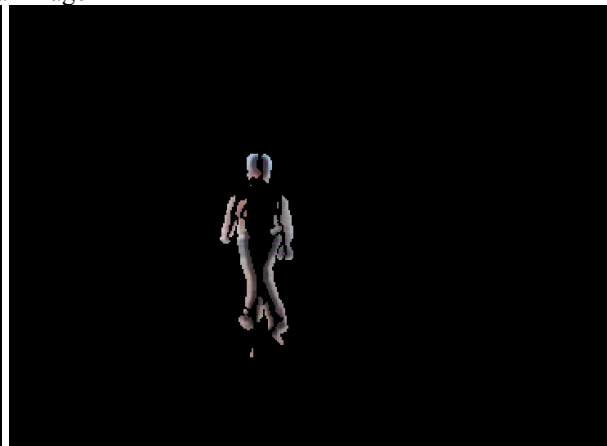
- (c) Threshold at every image, take the standard deviation of the Gaussian noise in every image to be the threshold.



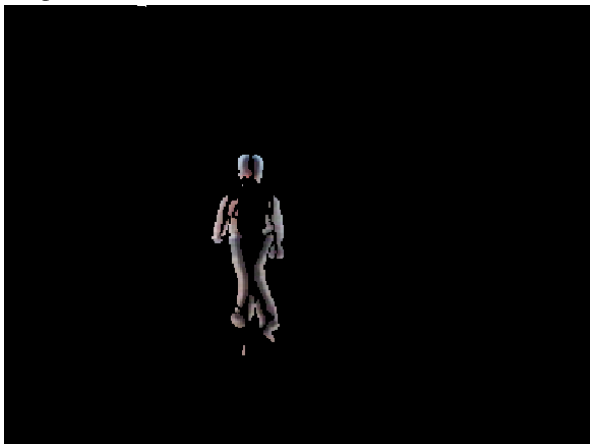
original image



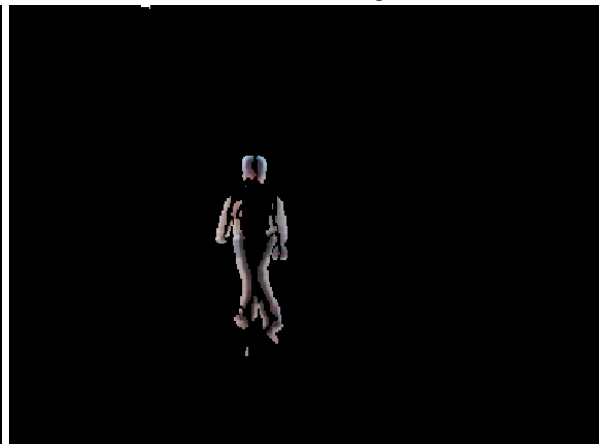
simple 0.5[1, 0, 1] filter



1D derivative of Gaussian with $\text{tsigma}=1$



1D derivative of Gaussian with $\text{tsigma}=1.8$

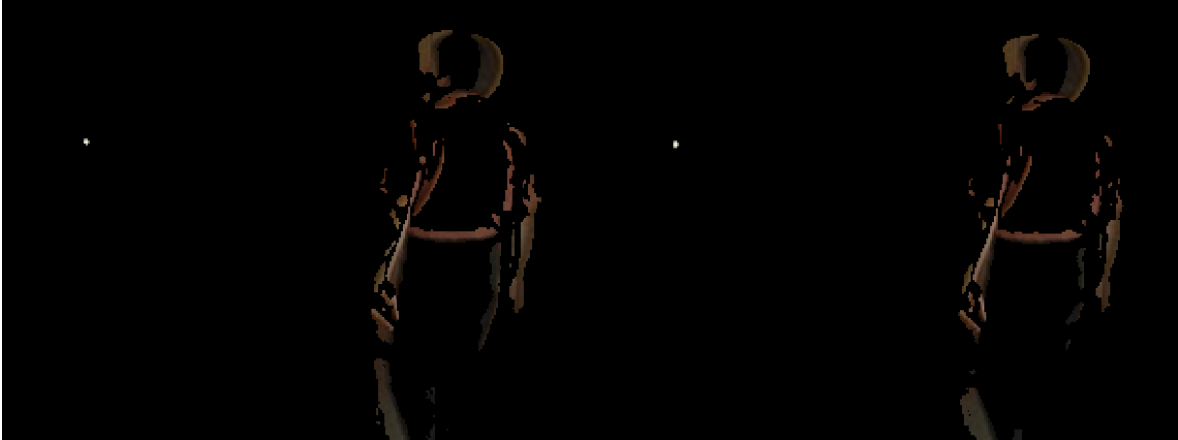


1D derivative of Gaussian with $\text{tsigma}=2.6$

We can see that under simple 0.5[1, 0, 1] filter, the boundaries are little and not complete. In Gaussian filter, the detection is better. And when tsigma equals to 1, the noise is less than tsigma equals to 1.8 or 2.6. So 1D derivative Gaussian with $\text{tsigma}=1$ is the best choice in this situation.

- 2) Applying a 2D spatial smoothing filter to the frames to reduce the noise before applying the temporal derivative filter. For the spatial smoothing filter, we try and compare 3x3, 5x5 box filters and 2D Gaussian filters with a defined standard deviation. In the report, we choose 1D derivative of Gaussian with $\sigma=1$ above in step (1) as reference.

(a)



3x3 box filter

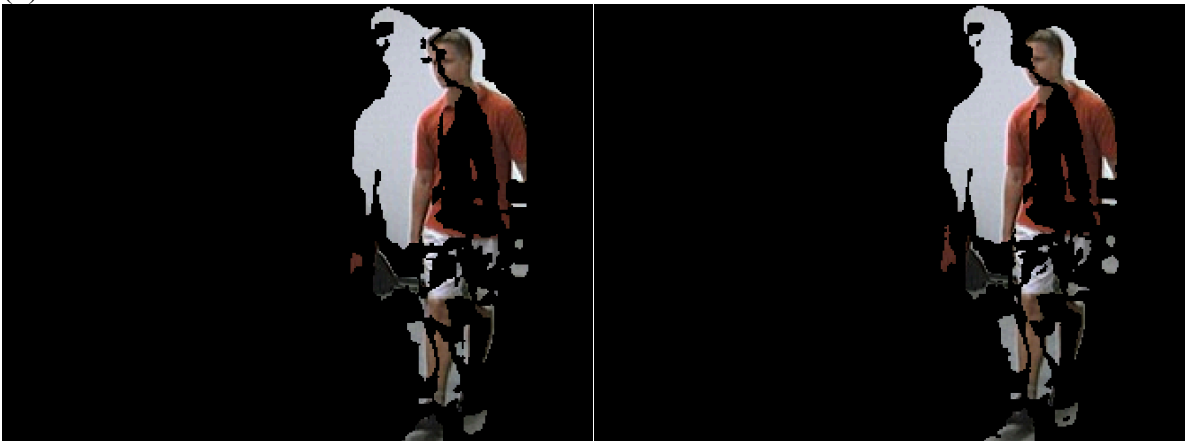
5x5 box filter



2D Gaussian filter with $\sigma=1$

2D Gaussian filter with $\sigma=1.8$

(b)



3x3 box filter



5x5 box filter



2D Gaussian filter with $\sigma=1$

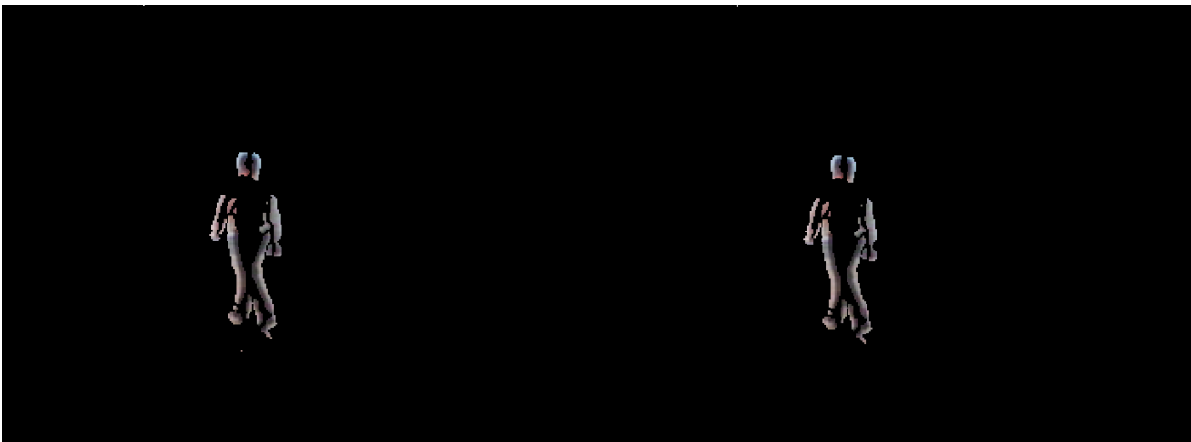
2D Gaussian filter with $\sigma=1.8$

(c)



3x3 box filter

5x5 box filter



2D Gaussian filter with $\sigma=1$

2D Gaussian filter with $\sigma=1.8$

We can see that under 5x5 box filter or 2D Gaussian filter with $\sigma=1.8$, it filters too much important information and make the detection not complete. 3x3 box filter and 1D Gaussian filter with $\sigma=1$ is both effective to make the output better.

- 3) Vary the threshold to get the mask and see what works best. Design a strategy to select a good threshold for each image. Then Combine the mask with the original frame. In this report, we choose 1D derivative of Gaussian with $\sigma=1$ above in step (1) and 2D Gaussian filter with $\sigma=1$ as reference.

(a)



threshold too high

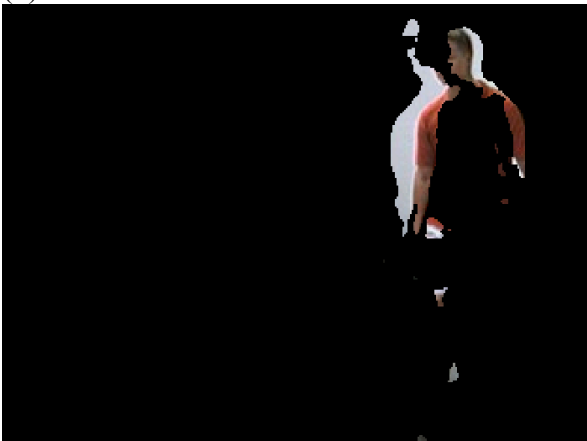


threshold too low



best threshold

(b)



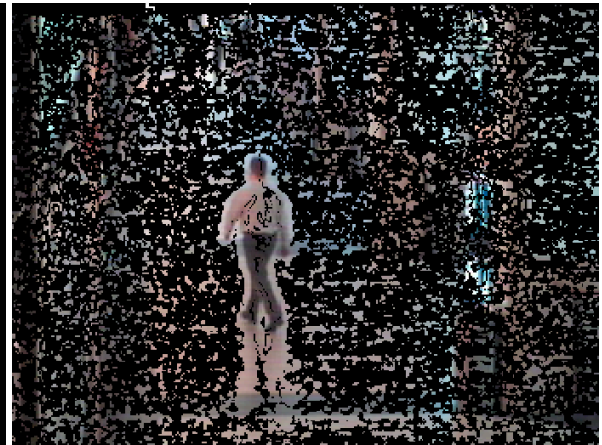
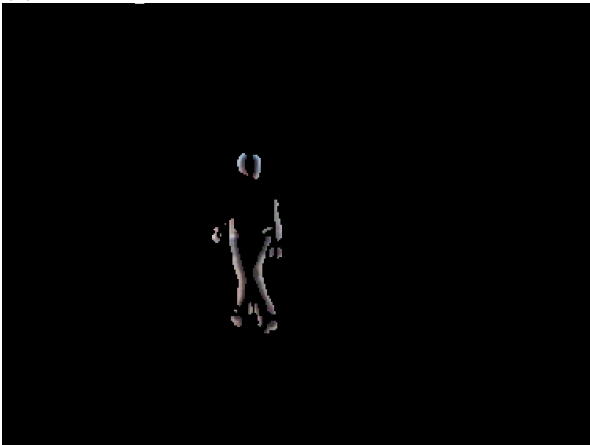
threshold too high



threshold too low

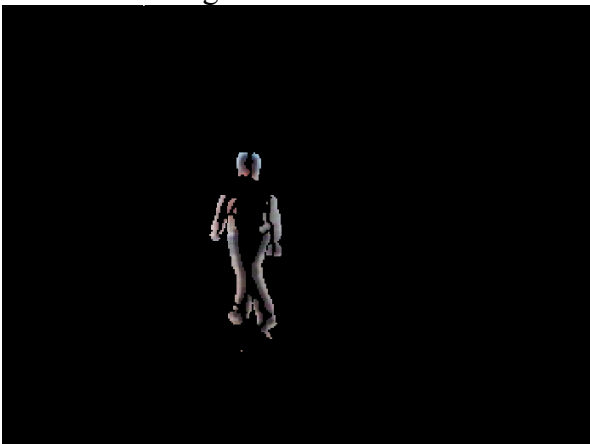
best threshold

(c)



threshold too high

threshold too low



best threshold

We can see that if the threshold is too high, then there will be more gaps. If the threshold is too low, there will be more noise. If the threshold is suitable, the detection is wonderful.

4 Conclusion

When doing the motion detection, we can first use a 2D Gaussian filter to erase noise, then apply a 1D derivative of Gaussian filter with the standard deviation of 1.0 or 1.4 at each pixel of a series of continuous frames to compute a temporal derivative. Choose a reasonable threshold and threshold the absolute values of the derivatives to create a 0 and 1 mask of the moving objects. Finally combine the mask with the original frame to display the results.

4 Appendix

```
1. clear;
2. close all;
3. clc;
4.
5. %%read and store multiple image frames
6. file_path = './EnterExitCrossingPaths2cor/';
7. img_path_list = dir(strcat(file_path, '*.jpg'));
8. %% the number of image frames
9. img_num = length(img_path_list);
10.    %% used to store original image frames
11.    img = cell(1,img_num);
12.    %%used to store gray values of image frames
13.    img_gray = cell(1,img_num);
14.    finalImageSF=cell(1,img_num);
15.    finalImageG1=cell(1,img_num);
16.    finalImageG2=cell(1,img_num);
17.    finalImageG3=cell(1,img_num);
18.    for i=1:img_num
19.        image_name=img_path_list(i).name;
20.        image_name=strcat(file_path,image_name);
21.        img{i}=imread(image_name);
22.        finalImageSF{i}=double(img{i});
23.        finalImageG1{i}=double(img{i});
24.        finalImageG2{i}=double(img{i});
25.        finalImageG3{i}=double(img{i});
26.        %% make image frames grayscale
27.        img_gray{i}=rgb2gray(img{i});
28.    end
29.
30.    h3=fspecial('average',[3,3]);
31.    h5=fspecial('average',[5,5]);
32.    G1=fspecial('Gaussian',[5,5],1.0);
33.    G2=fspecial('Gaussian',[9,9],1.8);
34.    I_G1=cell(1,img_num);
35.    for i=1:img_num
36.        I_G1{i}=imfilter(img_gray{i},G1,'replicate');
37.    end
38.
39.    %%the length value of the matrix correspond to one image frame
40.    len=size(img{1},2);
41.    %%the width value of the matrix correspond to one image frame
42.    wid=size(img{1},1);
```

```

43.     %%sf_G1 is a?wid x len?matrix,
44.     %%each entry is also a (1 x img_num) matrix
45.     gx1_G1=cell(wid,len);
46.
47.     for i=1:wid
48.         for j=1:len
49.             for k=1:img_num
50.                 gx1_G1{i,j}(k)=I_G1{k}(i,j);
51.             end
52.         end
53.     end
54.     sf_G1=gx1_G1;
55.     gx2_G1=gx1_G1;
56.     gx3_G1=gx1_G1;
57.     %%create a simple 0.5[-1, 0, 1] filter
58.     sim_f=[-0.5,0,0.5];
59.     t1=1.0; %%value of sigma t1
60.     t2=1.8; %%value of sigma t2
61.     t3=2.6; %%value of sigma t3
62.     gx1_mask=zeros(1,5);%range 5*t1
63.     gx2_mask=zeros(1,9);%range 5*t2
64.     gx3_mask=zeros(1,13);%range 5*t3
65.
66.     %%a 1D derivative of Gaussian filter with standard deviation of
1.0
67.     for x=-2:2
68.         gx1_mask(x+3)=-x/(t1*t1)*exp(-(x*x)/(2*t1*t1));
69.     end
70.     %%a 1D derivative of Gaussian filter with standard deviation of
1.8
71.     for x=-4:4
72.         gx2_mask(x+5)=-x/(t2*t2)*exp(-(x*x)/(2*t2*t2));
73.     end
74.     %%a 1D derivative of Gaussian filter with standard deviation of
2.6
75.     for x=-6:6
76.         gx3_mask(x+7)=-x/(t3*t3)*exp(-(x*x)/(2*t3*t3));
77.     end
78.
79.     for i=1:wid
80.         for j=1:len
81.             %sf_G1{i,j}=imfilter(double(sf_G1{i,j}),sim_f,'replicate'
);
82.             gx1_G1{i,j}=imfilter(double(gx1_G1{i,j}),gx1_mask,'replicate');
83.             %gx2_G1{i,j}=imfilter(double(gx2_G1{i,j}),gx2_mask,'repli
cate');
84.             %gx3_G1{i,j}=imfilter(double(gx3_G1{i,j}),gx3_mask,'repli
cate');
85.             %gx1_G1{i,j}=imfilter(gx1_G1{i,j},h3,'replicate');
86.             %gx1_G1{i,j}=imfilter(gx1_G1{i,j},h5,'replicate');
87.             gx1_G1{i,j}=imfilter(gx1_G1{i,j},G1,'replicate');
88.             %gx1_G1{i,j}=imfilter(gx1_G1{i,j},G2,'replicate');
89.         end
90.     end
91.
92.

```

```

93.     thr_sf_G1=cell(1,img_num);
94.     thr_gx1_G1=cell(1,img_num);
95.     thr_gx2_G1=cell(1,img_num);
96.     thr_gx3_G1=cell(1,img_num);
97.
98.     for k=1:img_num
99.         for i=1:wid
100.             for j=1:len
101.                 %thr_sf_G1{k}(i,j)=sf_G1{i,j}(k);
102.                 thr_gx1_G1{k}(i,j)=gx1_G1{i,j}(k);
103.                 %thr_gx2_G1{k}(i,j)=gx2_G1{i,j}(k);
104.                 %thr_gx3_G1{k}(i,j)=gx3_G1{i,j}(k);
105.             end
106.         end
107.     end
108.
109.
110.
111.     %calculate the threshold
112.     thres1=cell(1,img_num);
113.     thres2=cell(1,img_num);
114.     thres3=cell(1,img_num);
115.     thres4=cell(1,img_num);
116.     for i=1:img_num
117.         %thres1{i}=(std(double(thr_sf_G1{i}(:)))+7)*ones(wid,len);
118.         thres2{i}=(std(double(thr_gx1_G1{i}(:)))+7)*ones(wid,len);
119.         %thres3{i}=(std(double(thr_gx2_G1{i}(:)))+7)*ones(wid,len);
120.         %thres4{i}=(std(double(thr_gx3_G1{i}(:)))+7)*ones(wid,len);
121.     end
122.
123.     %Convert image to binary image by thresholding
124.     for i=1:img_num
125.         %thr_sf_G1{i}=im2bw(abs(thr_sf_G1{i})-thres1{i},1/255);
126.         thr_gx1_G1{i}=im2bw(abs(thr_gx1_G1{i})-thres2{i},1/255);
127.         %thr_gx2_G1{i}=im2bw(abs(thr_gx2_G1{i})-thres3{i},1/255);
128.         %thr_gx3_G1{i}=im2bw(abs(thr_gx3_G1{i})-thres4{i},1/255);
129.         %finalImageSF{i}(:,:,1) =
            finalImageSF{i}(:,:,1).*double(thr_sf_G1{i});
130.         %finalImageSF{i}(:,:,2) =
            finalImageSF{i}(:,:,2).*double(thr_sf_G1{i});
131.         %finalImageSF{i}(:,:,3) =
            finalImageSF{i}(:,:,3).*double(thr_sf_G1{i});
132.         finalImageG1{i}(:,:,1) =
            finalImageG1{i}(:,:,1).*double(thr_gx1_G1{i});
133.         finalImageG1{i}(:,:,2) =
            finalImageG1{i}(:,:,2).*double(thr_gx1_G1{i});
134.         finalImageG1{i}(:,:,3) =
            finalImageG1{i}(:,:,3).*double(thr_gx1_G1{i});
135.         %finalImageG2{i}(:,:,1) =
            finalImageG2{i}(:,:,1).*double(thr_gx2_G1{i});
136.         %finalImageG2{i}(:,:,2) =
            finalImageG2{i}(:,:,2).*double(thr_gx2_G1{i});
137.         %finalImageG2{i}(:,:,3) =
            finalImageG2{i}(:,:,3).*double(thr_gx2_G1{i});
138.         %finalImageG3{i}(:,:,1) =
            finalImageG3{i}(:,:,1).*double(thr_gx3_G1{i});
139.         %finalImageG3{i}(:,:,2) =

```

```

    finalImageG3{i}(:,:,2).*double(thr_gx3_G1{i});
140.    %finalImageG3{i}(:,:,3) =
    finalImageG3{i}(:,:,3).*double(thr_gx3_G1{i});
141.    end
142.
143.    %{
144.    %display the result of images filtered by a simple[-0.5 0 0.5]
    filter
145.    for i=1:img_num
146.        figure(),imshow(uint8(finalImageSF{i}));
147.        pause(0.05);
148.    end
149.    %}
150.
151.    %display the result of images filtered by a 1D derivative
152.    %of Gaussian filter with standard deviation of 1.0
153.    for i=1:img_num
154.        figure(),imshow(uint8(finalImageG1{i}));
155.        pause(0.05);
156.    end
157.
158.    %{
159.    %display the result of images filtered by a 1D derivative
160.    %of Gaussian filter with standard deviation of 1.4
161.    for i=1:img_num
162.        figure(),imshow(uint8(finalImageG2{i}));
163.        pause(0.05);
164.    end
165.
166.    %display the result of images filtered by a 1D derivative
167.    %of Gaussian filter with standard deviation of 1.8
168.    for i=1:img_num
169.        figure(),imshow(uint8(finalImageG3{i}));
170.        pause(0.05);
171.    end
172.    %}

```