

Especificación formal das funcións

A especificación farase en función da lóxica de Hoare, usando o triplete $\{P\} S \{Q\}$.

Funcións:

- `bignum str2bignum (char *str)`
- `bignum add (bignum a, bignum b)`
- `bignum sub (bignum a, bignum b)`
- `bignum mult (bignum a, bignum b)`
- `bignum remainder1 (bignum a, bignum n)`
- `bignum fact (bignum n)`
- `bignum multmod (bignum a, bignum b, bignum n)`
- `int comparar (bignum a, bignum b)`
- `void imprimir(bignum resultado)`

1. `bignum str2bignum (char *str);`

`bignum totmult;`

`char *str;`

$\{P\} \equiv \{a.val \neq \text{NULL} \text{ AND } b.val \neq \text{NULL} \text{ AND } b.tam > 0 \text{ AND } a.tam > 0 \text{ AND } 0 \leq a.sign \leq 1 \text{ AND } 0 \leq b.sign \leq 1 \text{ AND } (\forall i: 0 \leq i < a.tam: 0 \leq a.val[i] \leq 9) \text{ AND } (\forall i: 0 \leq i < b.tam: 0 \leq b.val[i] \leq 9)\}$

$S \equiv \text{mult}$

$\{Q\} \equiv \{totmult.tam > 0 \text{ AND } 0 \leq totmult.sign \leq 1 \text{ AND } totmult.val \neq \text{NULL} \text{ AND } (\forall i: 0 \leq i < totmult.tam: 0 \leq totmult.val[i] \leq 9) \text{ AND } totmult == a * b\}$

2. `bignum add (bignum a, bignum b);`

`bignum a, b, totsum;`

$\{P\} \equiv \{a.val \neq \text{NULL} \text{ AND } b.val \neq \text{NULL} \text{ AND } b.tam > 0 \text{ AND } a.tam > 0 \text{ AND } 0 \leq a.sign \leq 1 \text{ AND } 0 \leq b.sign \leq 1 \text{ AND } (\forall i: 0 \leq i < a.tam: 0 \leq a.val[i] \leq 9) \text{ AND } (\forall i: 0 \leq i < b.tam: 0 \leq b.val[i] \leq 9)\}$

$S \equiv \text{add}$

{Q} \equiv {totsum.tam>0 AND 0<=totsum.sign<=1 AND totsum.val != NULL AND
($\forall i$: 0<=i<num.tam: 0<=num.val[i]=9) AND totsum==a+b}

3. bignum sub (bignum a, bignum b);

bignum a, b, totrest;

{P} \equiv {a.val != NULL AND b.val != NULL AND b.tam>0 AND a.tam>0 AND
0<=a.sign<=1 AND 0<=b.sign<=1 AND ($\forall i$: 0<=i<a.tam: 0<=a.val[i]<=9) AND
($\forall i$: 0<=i<b.tam: 0<=b.val[i]<=9)}

S \equiv sub

{Q} \equiv {totrest.tam>0 AND 0<=totrest.sign<=1 AND totrest.val != NULL AND
($\forall i$: 0<=i<totrest.tam: 0<=totrest.val[i]=9) AND totrest==a-b}

4. bignum mult (bignum a, bignum b);

bignum a, b, totmult;

{P} \equiv {a.val != NULL AND b.val != NULL AND b.tam>0 AND a.tam>0 AND
0<=a.sign<=1 AND 0<=b.sign<=1 AND ($\forall i$: 0<=i<a.tam: 0<=a.val[i]<=9) AND
($\forall i$: 0<=i<b.tam: 0<=b.val[i]<=9)}

S \equiv mult

{Q} \equiv {totmult.tam>0 AND 0<=totmult.sign<=1 AND totmult.val!=NULL AND
($\forall i$: 0<=i<totmult.tam: 0<=totmult.val[i]=9) AND totmult==a*b}

5. bignum remainder (bignum a, bignum b);

bignum a, b, remainder;

{P} \equiv {a.val != NULL AND n.val != NULL AND n.tam>0 AND a.tam>0 AND
0<=a.sign<=1 AND 0<=n.sign<=1 AND ($\forall i$: 0<=i<a.tam: 0<=a.val[i]<=9) AND
($\forall i$: 0<=i<n.tam: 0<=b.val[i]<=9) AND (n.tam != 1 OR n.val[0] != 0)}

S \equiv remainder1

{Q} \equiv {remainder.tam>0 AND 0<=remainder.sign<=1 AND remainder.val!=NULL AND
($\forall i$: 0<=i<remainder.tam: 0<=remainder.val[i]=9) AND remainder==a%n}

6. bignum fact (bignum n);

bignum n, factorial;

{P} $\equiv \{n.val \neq \text{NULL} \text{ AND } n.tam > 0 \text{ AND } n.sign == 0 \text{ AND}$
 $(\forall i: 0 \leq i < n.tam: 0 \leq n.val[i] < 9)\}$

S $\equiv \text{fact}$

{Q} $\equiv \{\text{factorial.tam} > 0 \text{ AND } \text{factorial.sign} == 0 \text{ AND } \text{factorial.val} \neq \text{NULL} \text{ AND}$
 $(\forall i: 0 \leq i < \text{factorial.tam}: 0 \leq \text{factorial.val}[i] < 9) \text{ AND } \text{factorial} == n!\}$

7. bignum multmod (bignum a, bignum b, bignum n);

bignum a, b, n, result;

{P} $\equiv \{a.val \neq \text{NULL} \text{ AND } b.val \neq \text{NULL} \text{ AND } n.val \neq \text{NULL} \text{ AND}$
 $a.tam > 0 \text{ AND } b.tam > 0 \text{ AND } n.tam > 0 \text{ AND } 0 \leq a.sign \leq 1 \text{ AND } 0 \leq b.sign \leq 1 \text{ AND}$
 $n.sign == 0 \text{ AND } (\forall i: 0 \leq i < a.tam: 0 \leq a.val[i] < 9) \text{ AND}$
 $(\forall i: 0 \leq i < b.tam: 0 \leq b.val[i] < 9) \text{ AND } (\forall i: 0 \leq i < n.tam: 0 \leq n.val[i] < 9) \text{ AND}$
 $(n.tam \neq 1 \text{ OR } n.val[0] \neq 0)\}$

S $\equiv \text{multmod}$

{Q} $\equiv \{\text{result.tam} > 0 \text{ AND } 0 \leq \text{result.sign} \leq 1 \text{ AND } \text{result.val} \neq \text{NULL} \text{ AND}$
 $(\forall i: 0 \leq i < \text{result.tam}: 0 \leq \text{result.val}[i] < 9) \text{ AND } \text{result} == (a*b)\%n\}$

8. int comparar (bignum a, bignum b);

bignum a, b;

int mayor;

{P} $\equiv \{a.val \neq \text{NULL} \text{ AND } b.val \neq \text{NULL} \text{ AND } b.tam > 0 \text{ AND } a.tam > 0 \text{ AND}$
 $0 \leq a.sign \leq 1 \text{ AND } 0 \leq b.sign \leq 1 \text{ AND } (\forall i: 0 \leq i < a.tam: 0 \leq a.val[i] < 9) \text{ AND}$
 $(\forall i: 0 \leq i < b.tam: 0 \leq b.val[i] < 9)\}$

S $\equiv \text{comparer}$

{Q} $\equiv \{\text{mayor} == -1 \text{ OR } \text{mayor} == 0 \text{ OR } \text{mayor} == 1 \text{ AND } (a < b \Rightarrow \text{mayor} == -1) \text{ AND}$
 $(a == b \Rightarrow \text{mayor} == 0) \text{ AND } (a > b \Rightarrow \text{mayor} == 1)\}$

9. void imprimir (bignum resultado);

bignum resultado;

{P} \equiv {resultado.val != NULL AND resultado.tam>0 AND 0<=resultado.sign<=1 AND
($\forall i: 0 \leq i < \text{resultado.tam}: 0 \leq \text{resultado.val}[i] \leq 9$)}

S \equiv imprimir

{Q} \equiv {TRUE}