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# ANNUAL MEETING

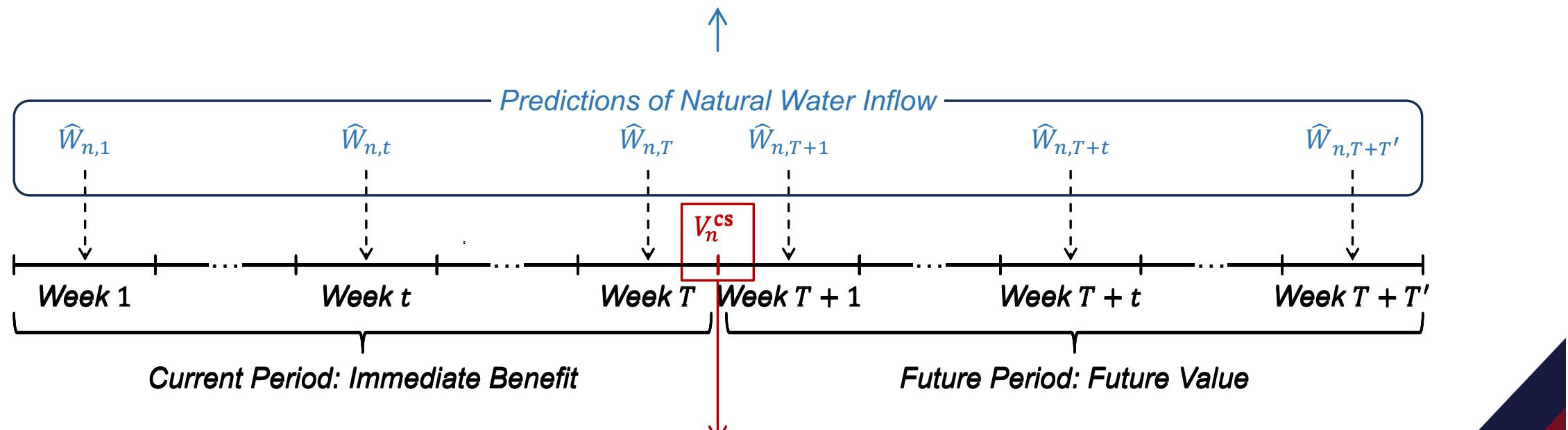


***Towards Mid-Term  
Scheduling of Cascaded  
Hydropower Systems: A  
Decision-Making Framework  
Driven by Uncertainty-Aware  
Water Inflow Predictor***

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# Background: Mid-Term Scheduling of Cascaded Hydropower Systems

Water inflow to the system: Target to be **predicted**



Carryover storage at the end of the current period:  
Target to be **optimized**

# Challenges

## On Prediction

1. How to capture the aleatoric uncertainty and epistemic uncertainty of water inflow?

Aleatoric uncertainty: Whether predictions are accurate enough?

Epistemic uncertainty: Whether predictors are well trained enough?

## On Optimization

1. How to leverage the predictions properly?
2. How to quantify the future value in an interpretable, hydrologically adaptive, and easy-to-use way?

# A Decision-Making Framework Driven by Uncertainty-Aware Predictor

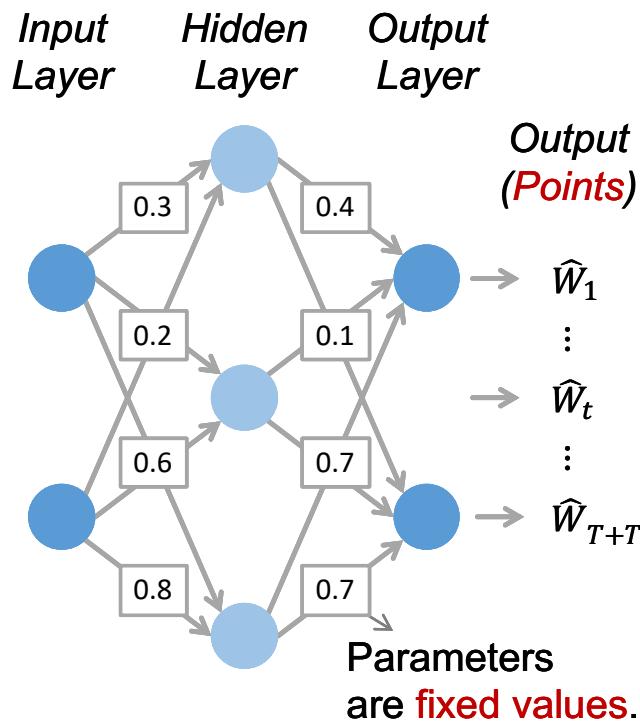
## Prediction Module

1. Uncertainty-aware predictor based on Bayesian mixture density network;
2. Prediction in the form of Gaussian mixture model.

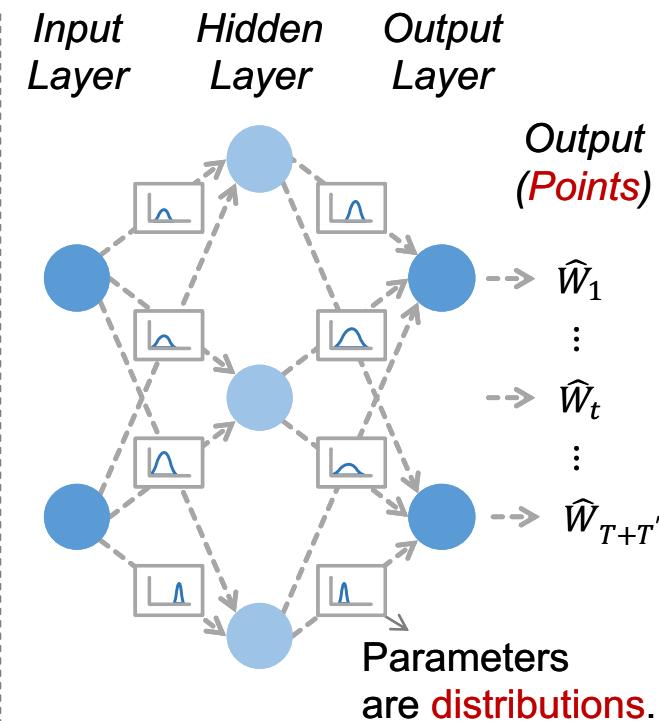
## Optimization Module

1. Chance-constrained model for the current period;
2. Multi-parametric mixed-integer linear programming to refine locational marginal water value.

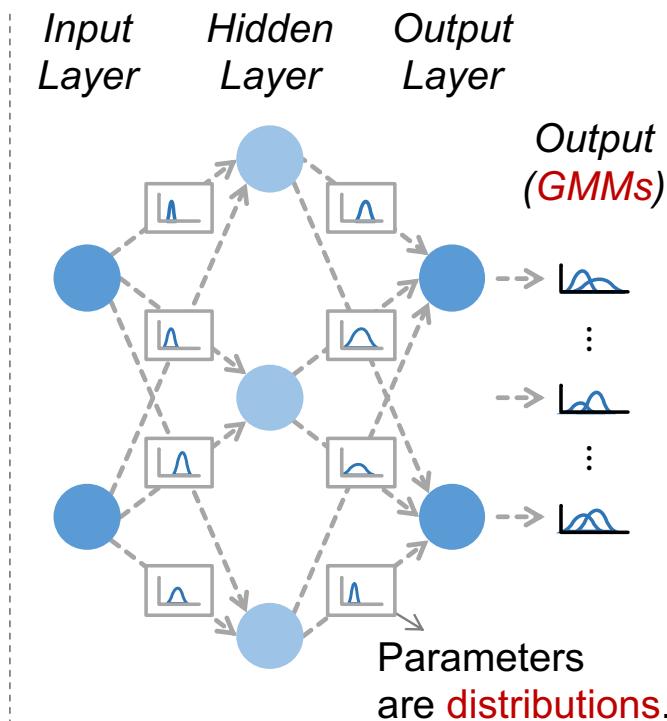
# Prediction Module



**Deep neural network:** Cannot capture uncertainty.



**Bayesian neural network:** Capture only epistemic uncertainty.



**Bayesian mixture density network:** Capture both epistemic uncertainty and aleatoric uncertainty.

# Optimization Module: Conceptual Model

Objective: max Immediate Benefit + Future Value



Generation  
of Current Period      Generation  
of Future Period

GMM-based  
Water Inflow  
Predictions

→ Constraints of the current period  
(Mimic current-period operations considering **uncertainties**)

→ Constraints of the future period  
(Represent future value with an **acceptable complexity**)

# Optimization Module: Constraints of Current Period

## Joint Chance Constraints for Storage Limit

$$\mathbb{P} \left\{ V_n^{min} \leq V_{n,1}^{bc} + \sum_{k=1}^t (\hat{W}_{nk} + W_{nk}^\Delta) \leq V_n^{max}, n = 1, \dots, N \right\} \geq 1 - \alpha_t, \\ t = 1, \dots, T$$

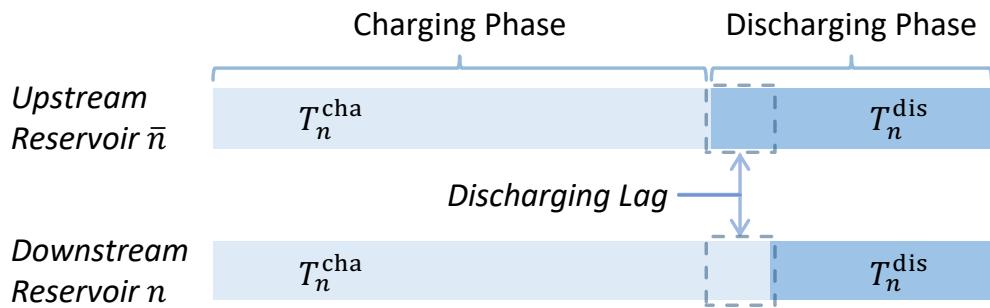
## Solving Method

1. Use Boole's inequality to decompose each joint chance constraint into individual chance constraints;
2. Convert the individual chance constraints into deterministic constraints based on the affine invariance of GMM.

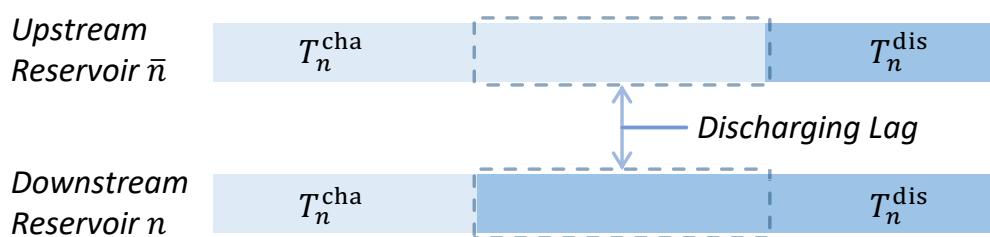
# Optimization Module: Constraints of Future Period

## A MILP Model to Quantify the Future Value

*Case 1: Reservoir  $n$  Discharges Later than Its Direct Upstream  $\bar{n}$*



*Case 2: Reservoir  $n$  Discharges Earlier than Its Direct Upstream  $\bar{n}$*



Use multi-parametric mixed-integer linear programming to refine the locational marginal water value

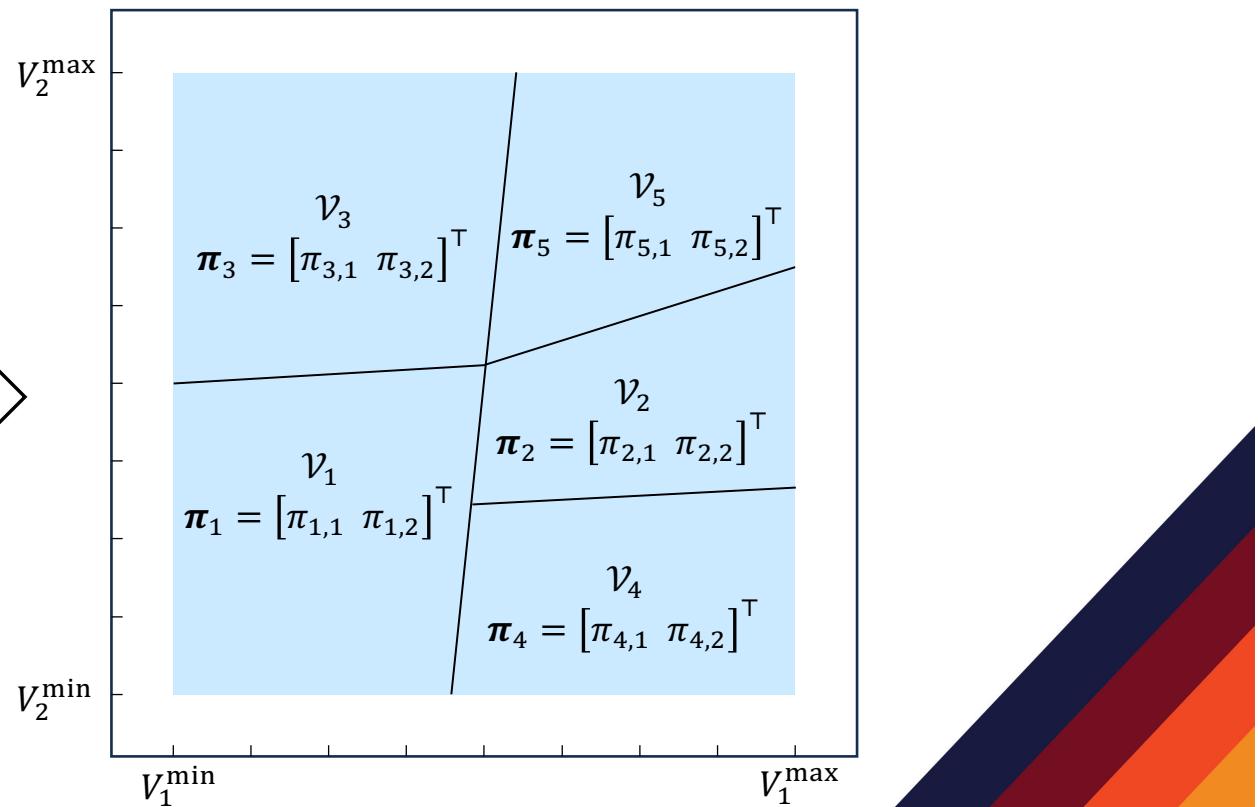
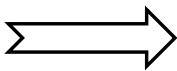
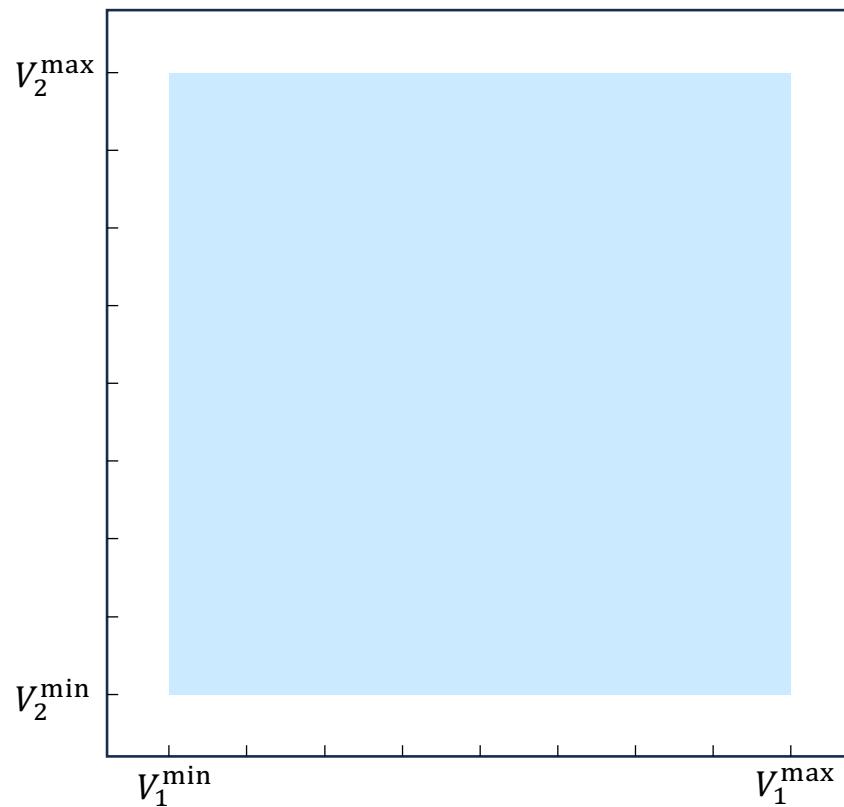


Amount of hydrogeneration that one-unit storage water can bring to the system

Not as comprehensive as the current-period part but enough for quantifying the future value.

# Optimization Module: Constraints of Future Period

Refining locational marginal water value  $\pi$  via multi-parametric mixed-integer linear programming



# Optimization Module: Constraints of Future Period

Representing the future value as “If-Then” constraints

$$\text{Future Value}(\mathbf{V}^{cs}) = \begin{cases} \sum_{n=1}^N \pi_{1,n}(V_n^{cs} - V_n^{min}) & \text{if } \mathbf{V}^{cs} \in \mathcal{V}_1 \\ \vdots \\ \sum_{n=1}^N \pi_{R,n}(V_n^{cs} - V_n^{min}) & \text{if } \mathbf{V}^{cs} \in \mathcal{V}_R \end{cases}$$

Easy-to-understand and computationally easy!

# Optimization Module: Final Model

A MILP model that is directly solvable by solvers:

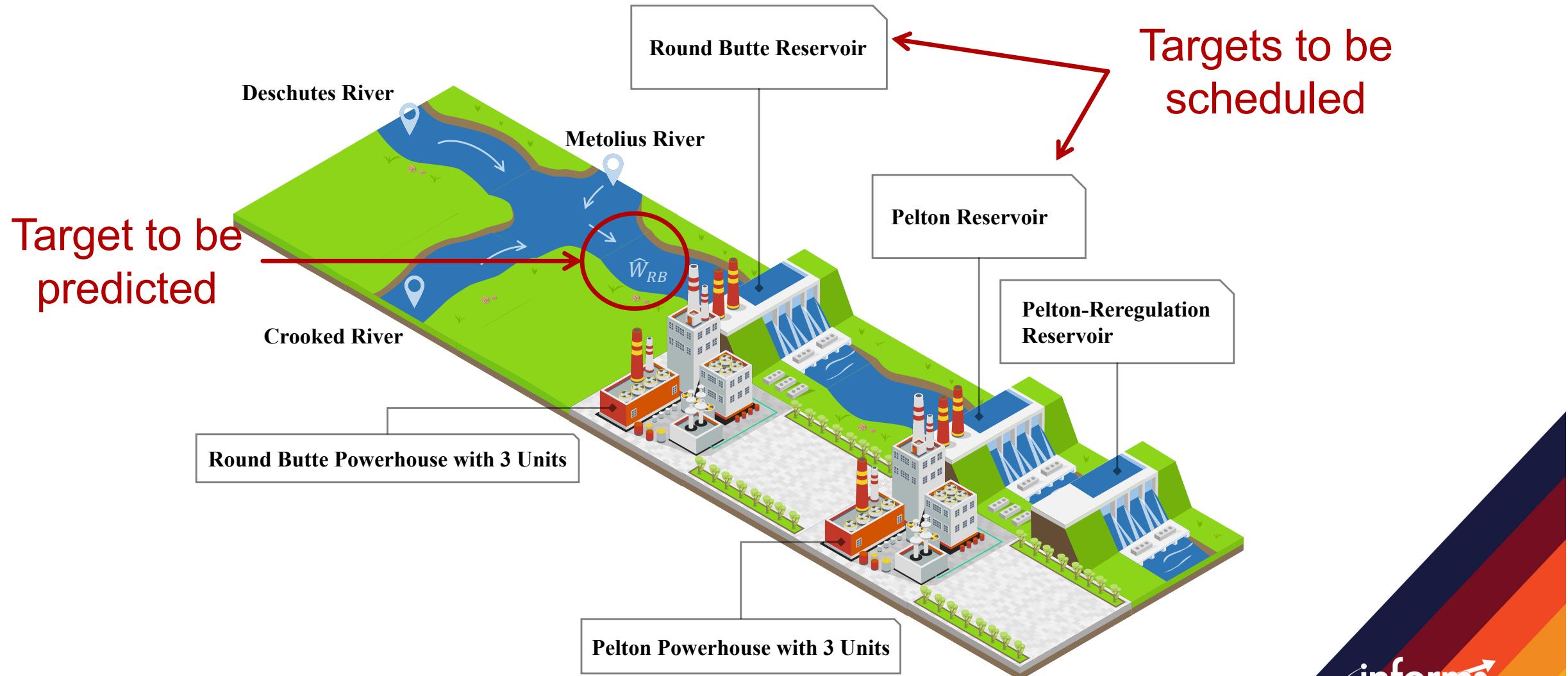
$$\begin{array}{ll} \max_{x,y} & \overbrace{\underbrace{a^\top x + b^\top y}_{\text{--- --- --- --- ---}}}^{\text{Immediate Benefit}} \\ \text{s. t. } & \underbrace{x \in \{0,1\}, y \geq 0}_{\text{--- --- --- --- ---}} \quad \& \text{Future Value} \\ & \underbrace{Ax + By \leq c}_{\text{--- --- --- --- ---}} \end{array}$$


Deterministic  
constraints for  
base-case operations

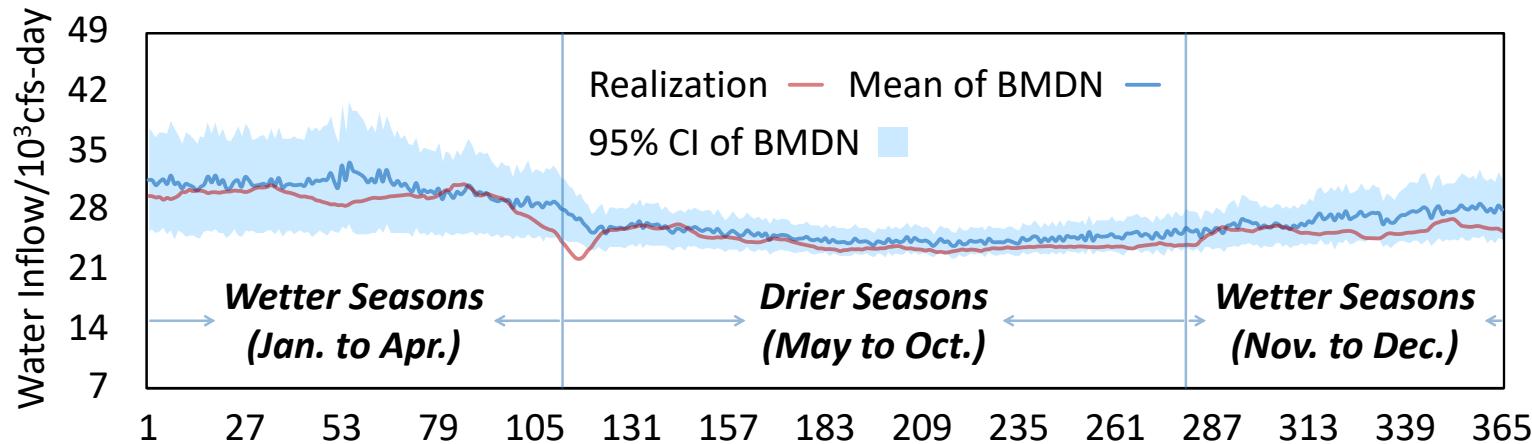
Reformulation  
of joint chance  
constraints

Linear  
constraints of  
“If-Then” logic

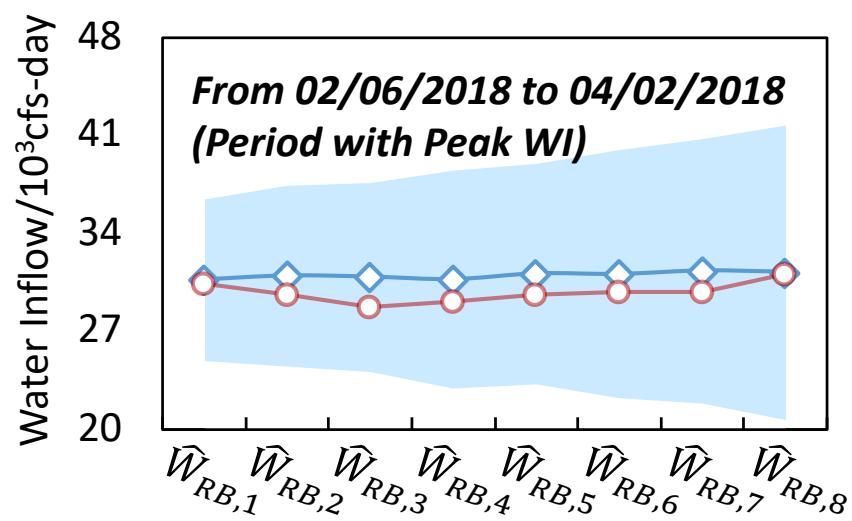
# Case Studies: Portland General Electric's System



# Case Studies: Prediction Performance



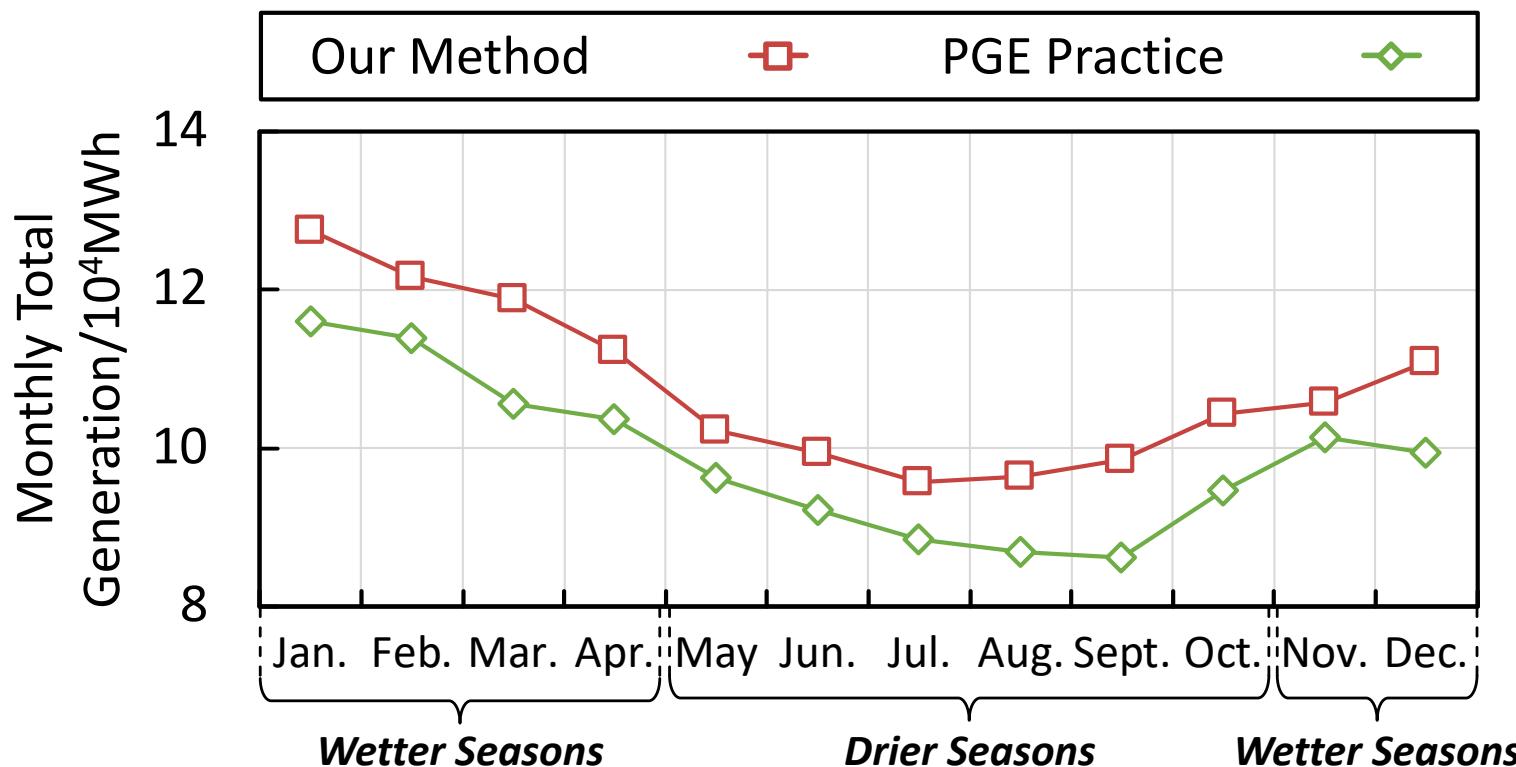
- The confidence interval can cover most realizations. (Tight)



- A shape of trumpet (Confident on next week but not confident for the weeks far from now)



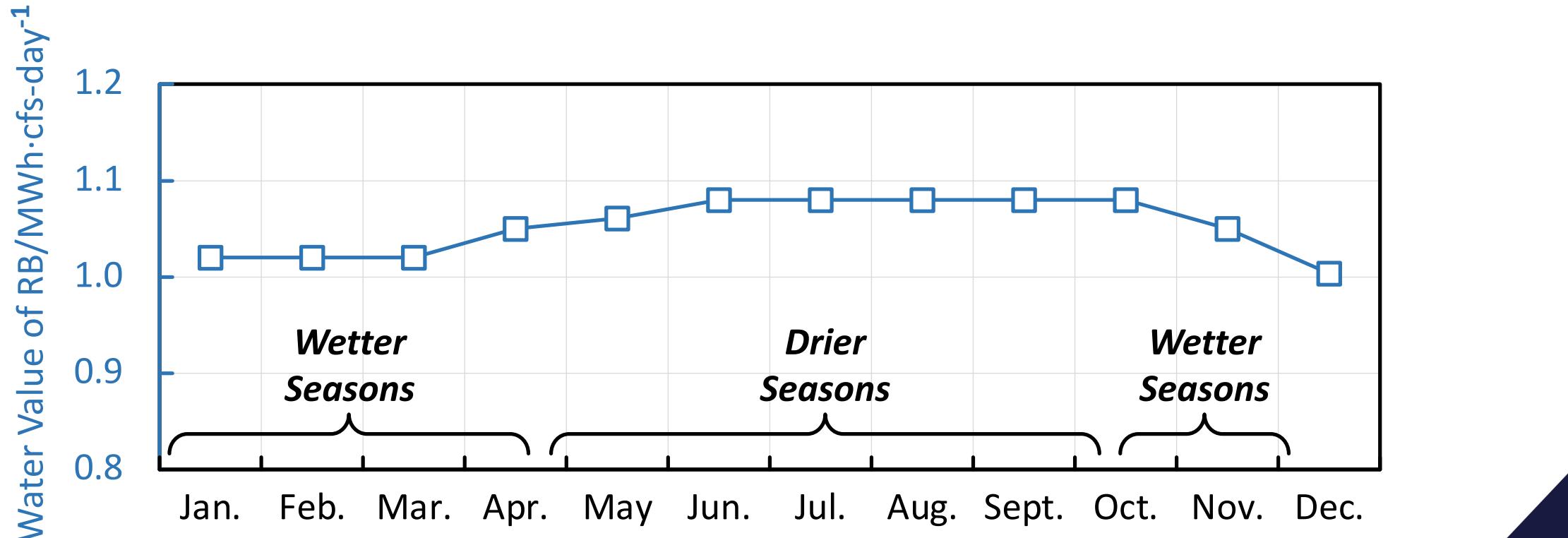
# Case Studies: Scheduling Results



- Our method outperforms the PGE practice in the generation results.

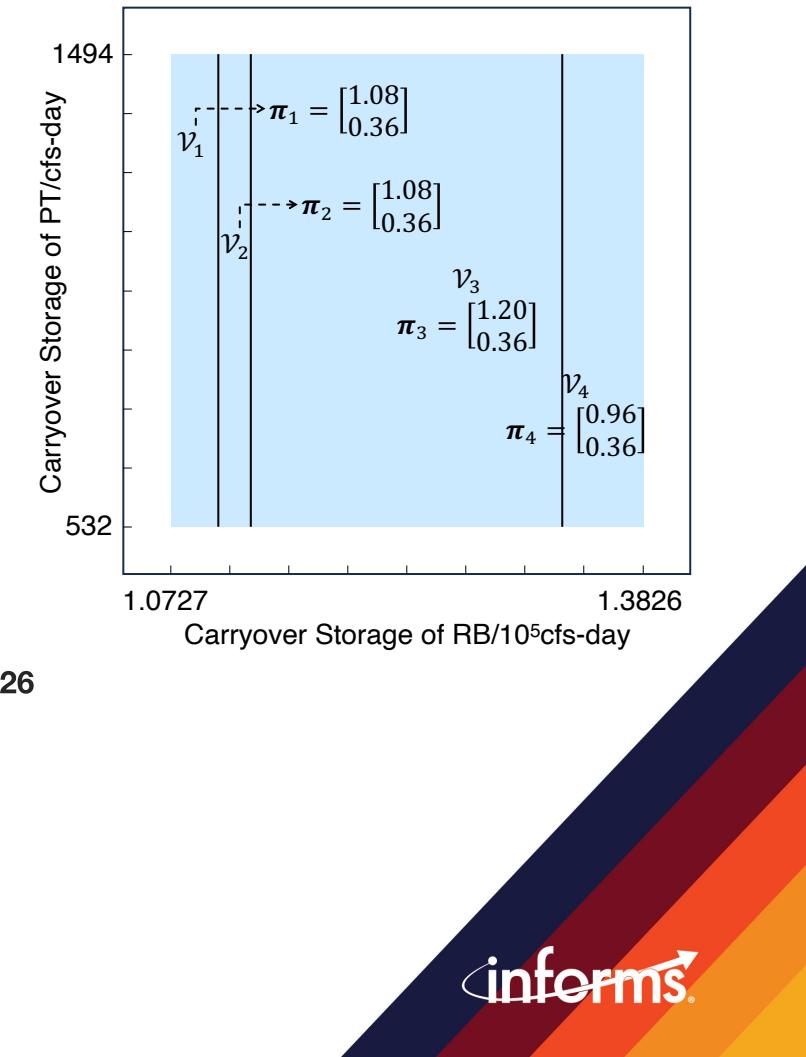
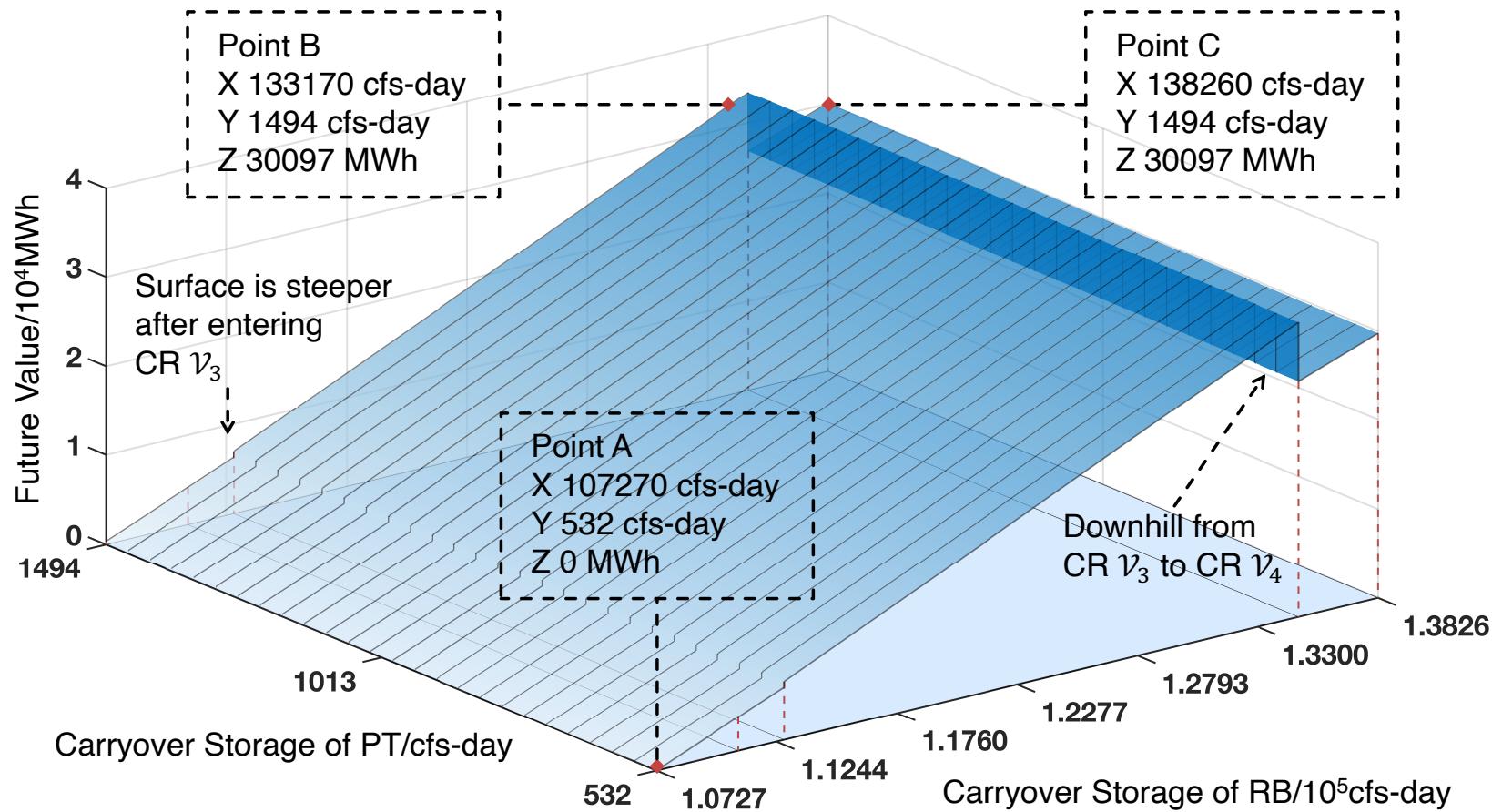


# Case Studies: Water Value



- Locational marginal water values are hydrologically adaptive.

# Case Studies: Visualization of Future Value



# Summary

1. The presented uncertainty-aware predictor can provide high-quality predictions of water inflow;
2. The presented model can leverage the water inflow to improve the hydropower generation;
3. The presented method provides an interpretable, hydrologically adaptive, and easy-to-use way to quantify the future value.