



# *Integrating Machine Learning and Operation Research for Improving Unit Commitment: A Closed-Loop Predict-and-Optimize Framework*

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*For OR Talk*



# Content

*Integrating  
Machine Learning (ML)  
and Operation  
Research(OR) for  
Unit Commitment (UC)*

I

*Preliminaries and Motivations*

II

*Presented Closed-Loop Predict-and-Optimize Framework*

III

*References and Q&A*



## Preliminaries and Motivations

- *Preliminaries: UC Based on Mixed-Integer Linear Programming*

- **Objective**

Minimizing operation costs including start-up and shut-down costs ( $c^T x$ ), and generation cost ( $d^T y$ ).

- **Unit constraints**

Ramping limits;

Generation limits;

...

- **System constraints**

Power balance;

Network constraints;

...



$$\begin{aligned} z(\hat{w}) = \min_{x,y} & [c^T x + d^T y] && \text{Binary decision} \\ \text{s.t. } & Ax + By \leq g && \text{Continue decision} \\ & Fy \leq \hat{w} && \begin{array}{l} \text{Prediction vector of uncertainty} \\ \text{Such as renewable energy source (RES)} \end{array} \\ & x \in \{0,1\}^M \end{aligned}$$



## Preliminaries and Motivations

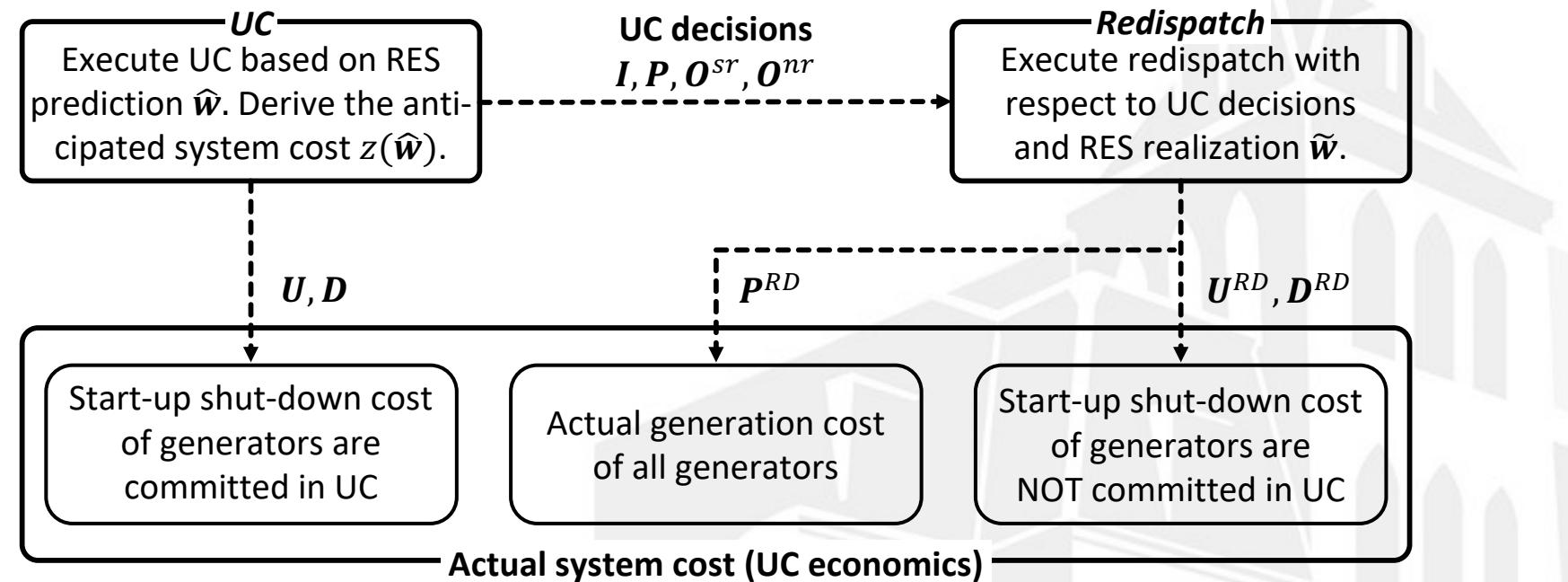
- *Preliminaries: Some Basic ML*
  - **Unsupervised learning**  
K-means
  - **Supervised learning**  
KNN  
 Linear regression  
Neural networks  
Decision trees  
Support vector machines
  - **Reinforcement learning**  
Q-learning  
Deep Q network
- *Preliminaries: Goals for ML-based UC<sup>1</sup>*
  - **Improving UC economics**  

  - **Improving UC reliability**
  - **Accelerating UC computation**
  - **Enhancing UC models**
  - **Predicting uncertainty (RES and load)**  




## Preliminaries and Motivations

- Preliminaries: Evaluation of UC Economics (Actual System Cost)**



**$I$**  Commitment

**$U$**  Start-up

**$D$**  Shut-down

**$P$**  Set-point generation

**$O^{sr}$**  Spinning reserve

**$O^{nr}$**  Non-spinning reserve

**$P^{RD}$**  Actual generation

**$U^{RD}$**  Start-up of quick generator

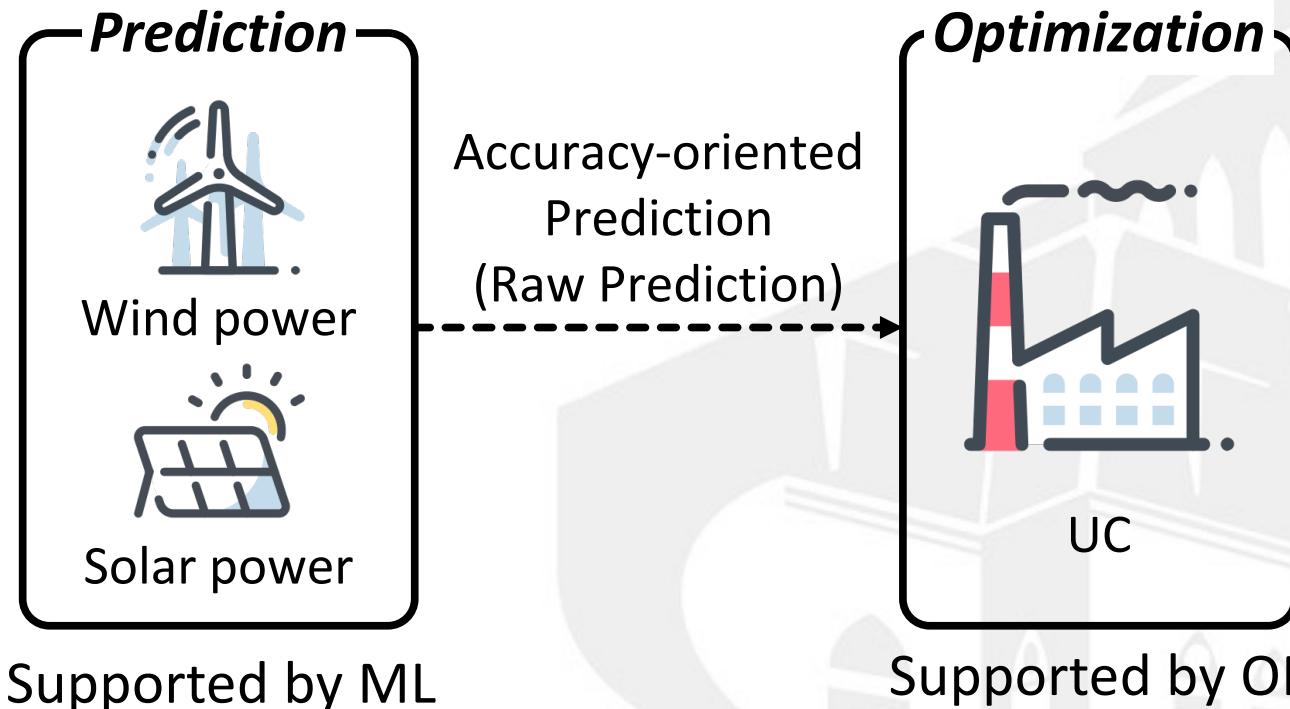
**$D^{RD}$**  Shut-down of quick generator



## Preliminaries and Motivations

- **Motivations: Flaws in Traditional Open-Loop Predict-then-Optimize Framework**

An open-loop predict-then-optimize (O-PO) framework for UC



Statistically more accurate prediction  $\not\Rightarrow$  Higher UC economics



## Preliminaries and Motivations

- *Motivations: Flaws in Traditional Open-Loop Predict-then-Optimize Framework*

- **A 2-Bus Example**

**G1:** [5MW, 100MW]

No-load cost: \$100

Generation cost: \$15/MWh

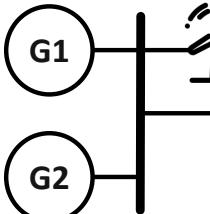
Start-up cost: \$120

**G2:** [5MW, 80MW]

No-load cost: \$60

Generation cost: \$20/MWh

Start-up cost: \$100



RES plant #1

Power realization: 100MW

Transmission capacity: 180MW

System Load: 200MW

**G3:** [5MW, 33MW]

No-load cost: \$30

Generation cost: \$40/MWh

Start-up cost: \$50

- **Prediction term**  
RES power with 100MW realization
  - **Measurement of Prediction Quality**  
Mean absolute error (Statistically)



## Preliminaries and Motivations

- **Motivations: Flaws in Traditional Open-Loop Predict-then-Optimize Framework**
  - **Case 1: Our method over-predicts and O-PO under-predicts**

Case 1		
	Method	Our method
	<b>RES power prediction/MW</b>	130
	<b>Mean absolute error/MW</b>	30 (Worse)
UC	G1 Set-point generation/MW	50
	Reserve/MW	±6
	G2 Set-point generation/MW	OFF
	Reserve/MW	+40
	G3 Set-point generation/MW	20
	Reserve/MW	±0
Re-dispatch	Dispatch of RES/MW	130
	Anticipated system cost/\$	1,850
	Actual generation of G1/MW	56
	Actual generation of G2/MW	24
	Actual generation of G3/MW	20
	Actual utilized RES/MW	100
<b>Actual system cost/\$</b>		2,580 (Better)
“±”: Bi-directional spinning reserve. “+”: Upward only non-spinning reserve.		



## Preliminaries and Motivations

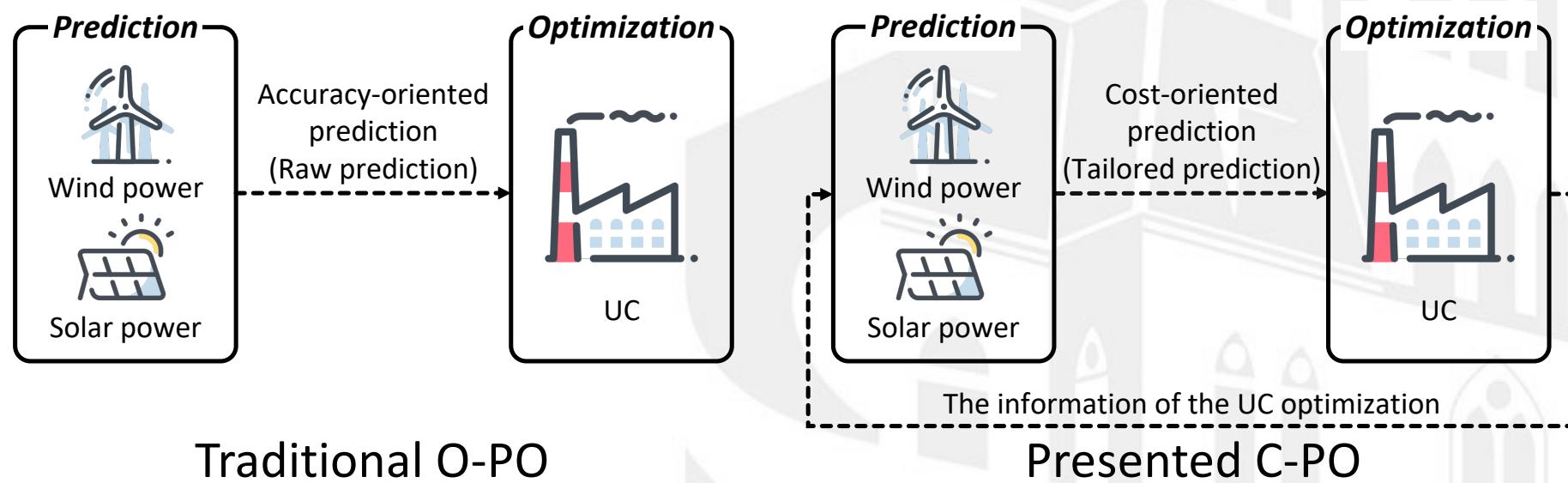
- **Motivations: Flaws in Traditional Open-Loop Predict-then-Optimize Framework**
  - **Case 2: Our method under-predicts and O-PO over-predicts**

Case 1		
	Method	Our method
	<b>RES power prediction/MW</b>	90
	<b>Mean absolute error/MW</b>	10 (Worse)
UC	G1 Set-point generation/MW	90
	Reserve/MW	±6
	G2 Set-point generation/MW	OFF
	Reserve/MW	+40
G3	Set-point generation/MW	20
	Reserve/MW	±0
	Dispatch of RES/MW	90
	Anticipated system cost/\$	2,450
Re-dispatch	Actual generation of G1/MW	84
	Actual generation of G2/MW	OFF
	Actual generation of G3/MW	20
	Actual utilized RES/MW	96
	<b>Actual system cost/\$</b>	2,360 (Better)
“±”: Bi-directional spinning reserve. “+”: Upward only non-spinning reserve.		



## Preliminaries and Motivations

- **Motivations: Flaws in Traditional Open-Loop Predict-then-Optimize Framework**
  - **Statistically more accurate prediction  $\not\Rightarrow$  Higher UC economics**
  - **To improve the UC economics, we shall close the loop:**  
Consider the downstream UC optimization when using ML for the upstream RES prediction.





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## ***Presented Closed-Loop Predict-and-Optimize Framework***

- ***Features of the Closed-Loop Predict-and-Optimize (C-PO) Framework***
  - ***Take advantage of available feature data. (Data-driven)***
  - ***Ability to delivery cost-oriented RES predictions for improving UC economics. (Economics benefits)***
  - ***Potential for large-scale MILP-based UC problems. (Practicality)***
  - ***Extendable to prediction tasks in other fields. (Expansibility)***



# ***Presented Closed-Loop Predict-and-Optimize Framework***

- ***Data-Driven C-PO Framework: Overview***
  - ***Data-processing module***
    1. Feature selection
    2. Selection of training scenarios
  - ***Cost-oriented modeling-and-training module***
    1. Cost-oriented empirical risk minimization (ERM) problem modeling
    2. Cost-oriented ERM problem solving (Predictor training)
  - ***Closed-loop predict-and-optimize module***
    1. Predict RES and optimize UC.



# *Presented Closed-Loop Predict-and-Optimize Framework*

- *Data-Driven C-PO Framework: Data-Processing Module*

***Data-processing module***



***Feature selection based on historical scenarios in past years:*** Based on historical scenarios in past years, identify the most relevant feature types using standard regression coefficient.

***Training scenarios selection from the latest historical scenarios:*** Among the latest historical scenarios, select the most representative scenarios as training scenarios using Wasserstein distance.

***Goal***

- ***Feature selection:*** Avoid overfitting and underfitting issues for the prediction model.
- ***Selection of training scenarios:*** Ensure the effectiveness of the prediction model on upcoming dispatch days.

- ***Standard regression coefficient for feature selection***

- ***Wasserstein distance for training scenario selection***



# Presented Closed-Loop Predict-and-Optimize Framework

- **Data-Driven C-PO Framework: Cost-Oriented Modeling-and-Training Module**

- **Smart “predict-then-optimize” (SPO) loss**  $\ell^{SPO}(\hat{w}, \tilde{w}) := |z^*(\hat{w}) - z^*(\tilde{w})|$   
SPO: Measuring prediction quality with *UC cost loss* instead of *statistical accuracy loss*, so that the open-loop is closed.

- **Recalling the UC model**

$$\begin{aligned} z(\hat{w}) &= \min_{x,y} [c^\top x + d^\top y] \\ \text{s.t. } &Ax + By \leq g \\ &Fy \leq \hat{w}, x \in \{0,1\}^M \end{aligned}$$

- **Cost-oriented ERM problem of  $|\mathcal{S}|$  scenarios**

$$\begin{aligned} \min_{x,y,H} & \frac{1}{|\mathcal{S}|} \sum_{s \in \mathcal{S}} [\ell_s^{SPO}(\hat{w}_s, \tilde{w}_s)] + \lambda \|H\|_1 \\ \text{s.t. } &Ax_s + By_s \leq g \\ &Fy_s \leq Hf_s, x_s \in \{0,1\}^M \end{aligned}$$

Feature data such as raw RES predictions and regional load



## *Presented Closed-Loop Predict-and-Optimize Framework*

- *Data-Driven C-PO Framework: Cost-Oriented Modeling-and-Training Module*

- **Cost-oriented ERM problem of  $|\mathcal{S}|$  scenarios**

Regression-based problem:  $\mathbf{H}$  linearly maps feature  $f_s$  to RES predictions.

Simple and interpretable.

$$\begin{aligned} \min_{\mathbf{x}, \mathbf{y}, \mathbf{H}} & \frac{1}{|\mathcal{S}|} \sum_{s \in \mathcal{S}} [\ell_s^{SPO}(\hat{\mathbf{w}}_s, \tilde{\mathbf{w}}_s)] + \boxed{\lambda} \|\mathbf{H}\|_1 \\ \text{s. t. } & \mathbf{A}\mathbf{x}_s + \mathbf{B}\mathbf{y}_s \leq \mathbf{g} \\ & \mathbf{F}\mathbf{y}_s \leq \mathbf{H}\mathbf{f}_s, \mathbf{x}_s \in \{0,1\}^M \end{aligned}$$

The only hyper-parameter  
to be tuned

- **Lagrangian-relaxation (LR) decomposition for solving the ERM**

Solving ERM is essentially training the predictors.

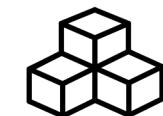
- **Training result: Cost-oriented RES predictor tailored for UC.**

$$\mathbf{H}^*$$



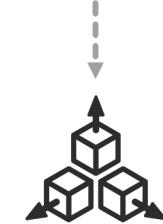
# *Presented Closed-Loop Predict-and-Optimize Framework*

- *Data-Driven C-PO Framework: Cost-Oriented Modeling-and-Training Module*



## ***Cost-oriented modeling-and-training module***

***Modeling cost-oriented ERM problem:*** Given the selected feature types of the training scenarios, model a cost-oriented ERM problem based on SPO loss function, which considers objective and constraints of UC.



***Solving cost-oriented ERM problem:*** Solve the cost-oriented ERM problem using LR-based decomposition, so that a cost-oriented RES power prediction model can be trained.

## ***Goal***

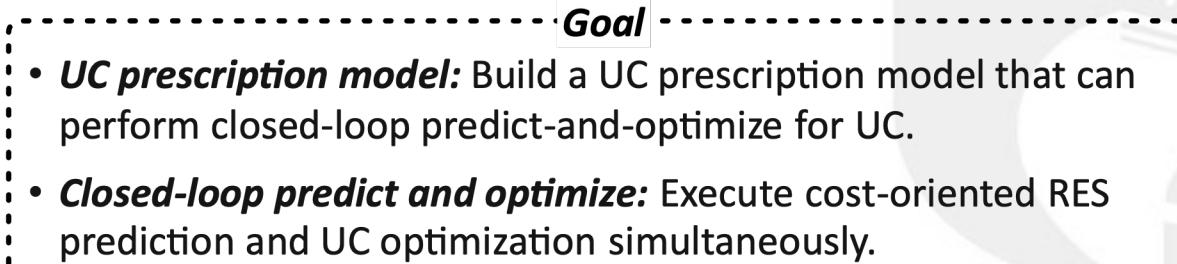
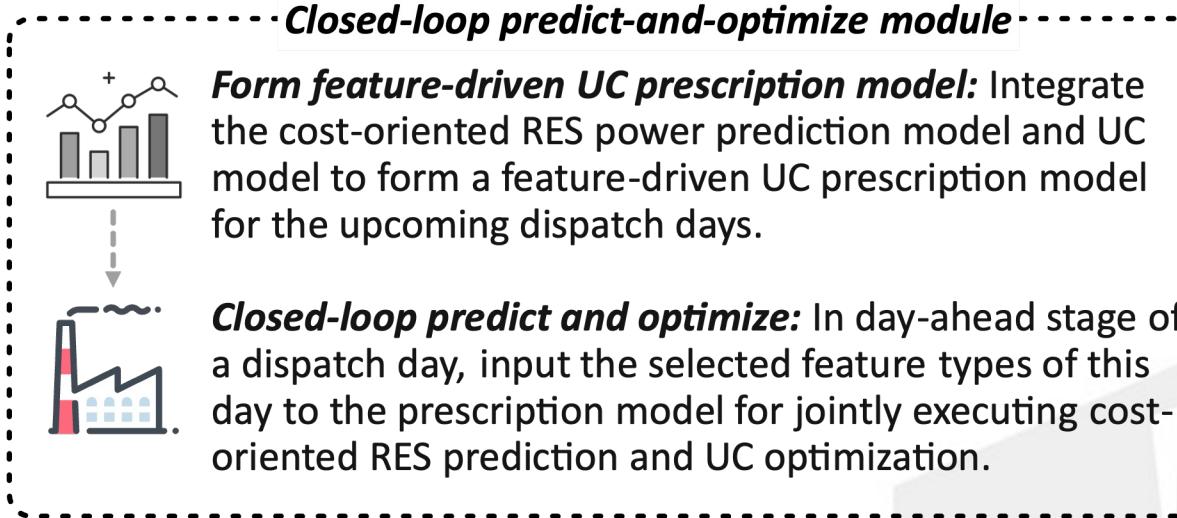
- ***ERM problem modeling:*** Feed the UC information (i.e., the induced costs, objective, and constraints) back to the ERM.
- ***ERM problem solving:*** Training a prediction model that can deliver cost-oriented RES predictions for UC.

- ***Modeling ERM based on SPO loss***
- ***Solving ERM via LR-based decomposition***
- ***Get a cost-oriented predictor for UC***



# *Presented Closed-Loop Predict-and-Optimize Framework*

- *Data-Driven C-PO Framework: Closed-Loop Predict-and-Optimize Module*



- **Data-driven UC prescription model:**  
$$z(f) = \min_{x,y} [c^T x + d^T y]$$
$$s.t. Ax + By \leq g$$
$$Fy \leq H^*f, x \in \{0,1\}^M$$
- **Prescription: Combining prediction and decision.**
- **Regression property:**  $H^*f$  is essentially a weighted sum of the features  $f$ .



## ***Presented Closed-Loop Predict-and-Optimize Framework***

- ***Comparing Original UC Model and UC Prescription Model***

- ***Original UC model***

$$z(\hat{\mathbf{w}}) = \min_{x,y} [\mathbf{c}^\top \mathbf{x} + \mathbf{d}^\top \mathbf{y}]$$

$$\text{s.t. } \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{y} \leq \mathbf{g}$$

$$\mathbf{F}\mathbf{y} \leq \hat{\mathbf{w}}, \mathbf{x} \in \{0,1\}^M$$

- Predict-**then**-optimize

- Use **accuracy**-oriented prediction

- The loop between RES prediction and UC optimization is **wide-open**

- ***Data-driven UC prescription model***

$$z(\mathbf{f}) = \min_{x,y} [\mathbf{c}^\top \mathbf{x} + \mathbf{d}^\top \mathbf{y}]$$

$$\text{s.t. } \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{y} \leq \mathbf{g}$$

$$\mathbf{F}\mathbf{y} \leq \mathbf{H}^* \mathbf{f}, \mathbf{x} \in \{0,1\}^M$$

- Predict-**and**-optimize (Prescription)

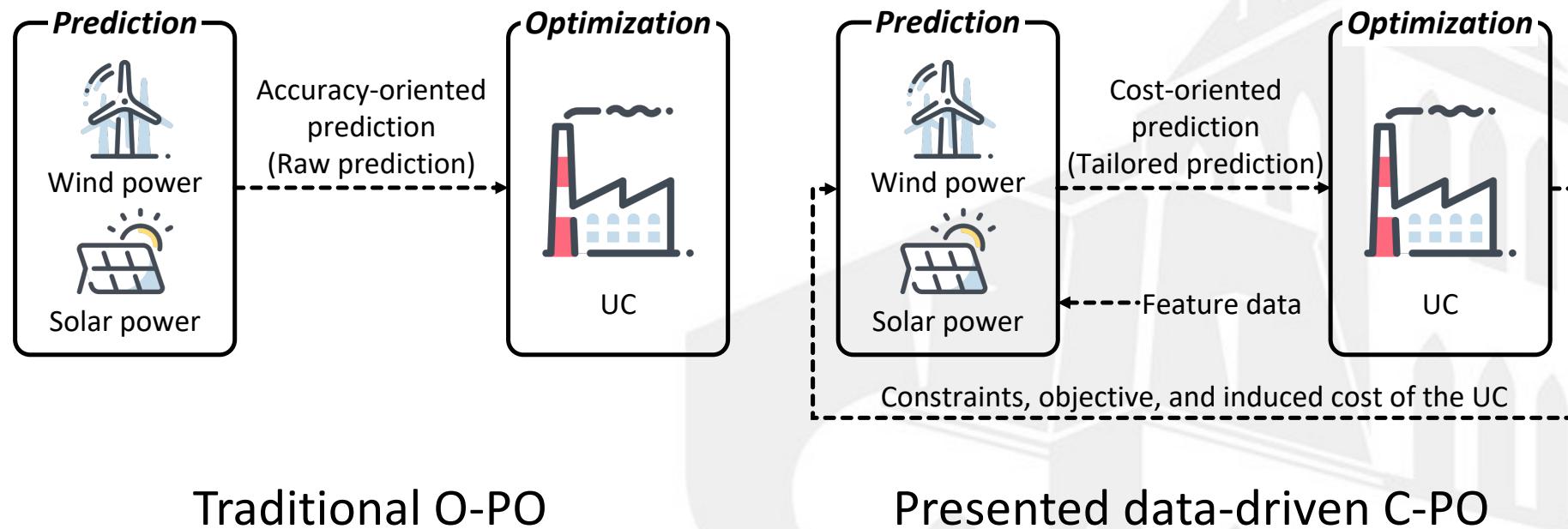
- Use **Cost**-oriented prediction  
(Driven by feature data  $\mathbf{f}$ )

- The loop between RES prediction and UC optimization is **closed**



# *Presented Closed-Loop Predict-and-Optimize Framework*

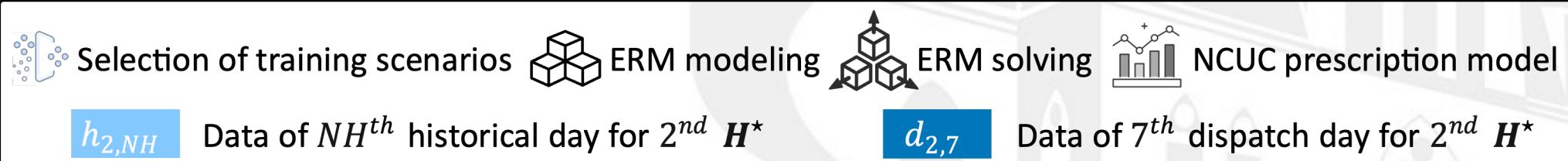
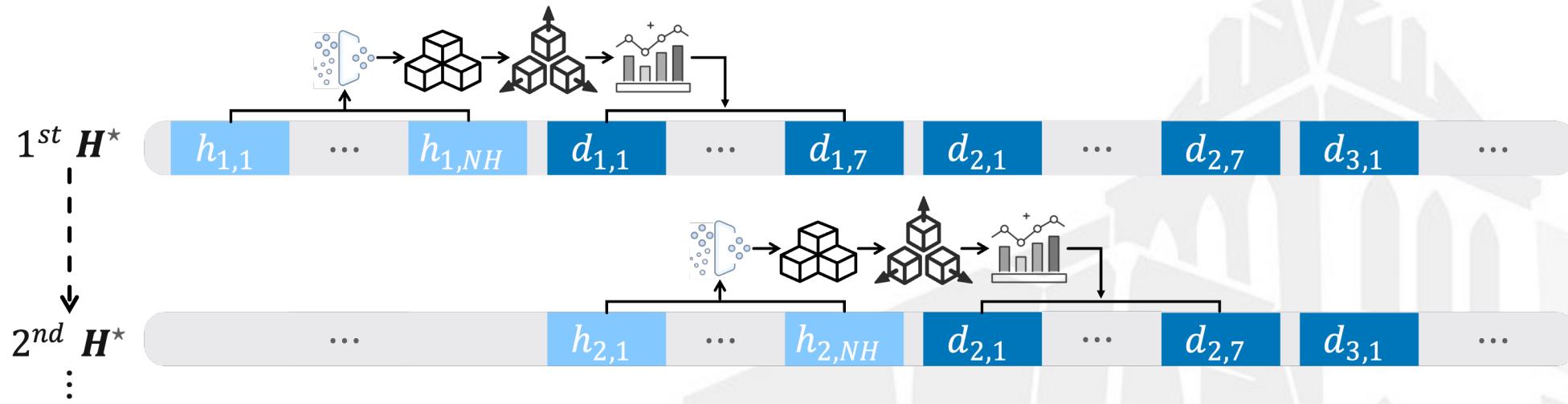
- *Comparing Traditional O-PO and Presented C-PO*





# Presented Closed-Loop Predict-and-Optimize Framework

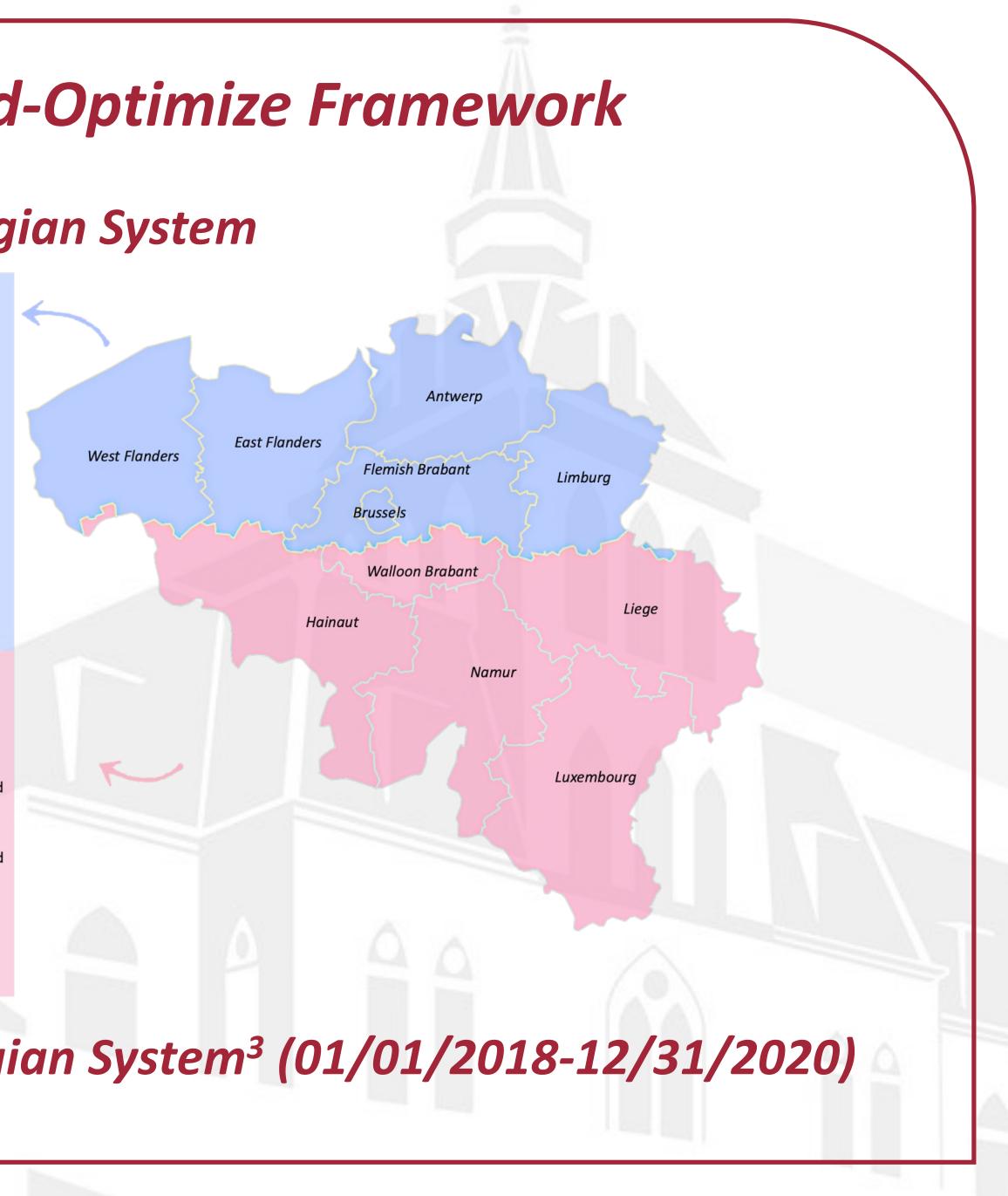
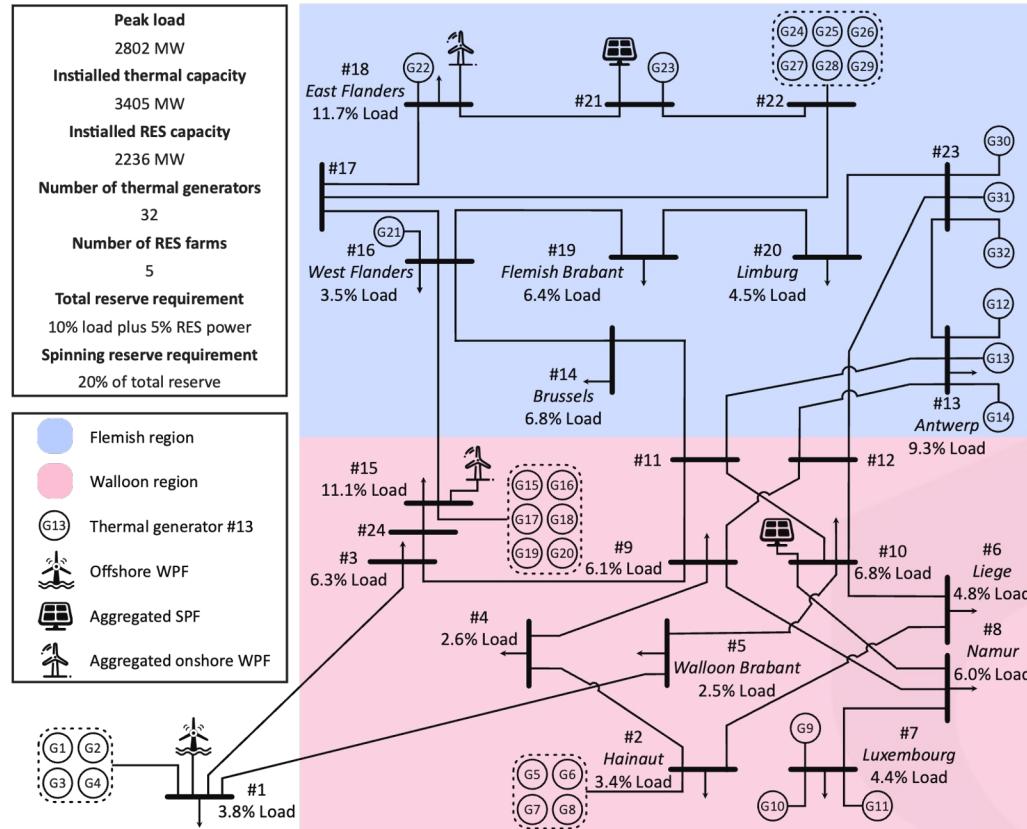
- Rolling-based C-PO Implementation for Daily UC





# *Presented Closed-Loop Predict-and-Optimize Framework*

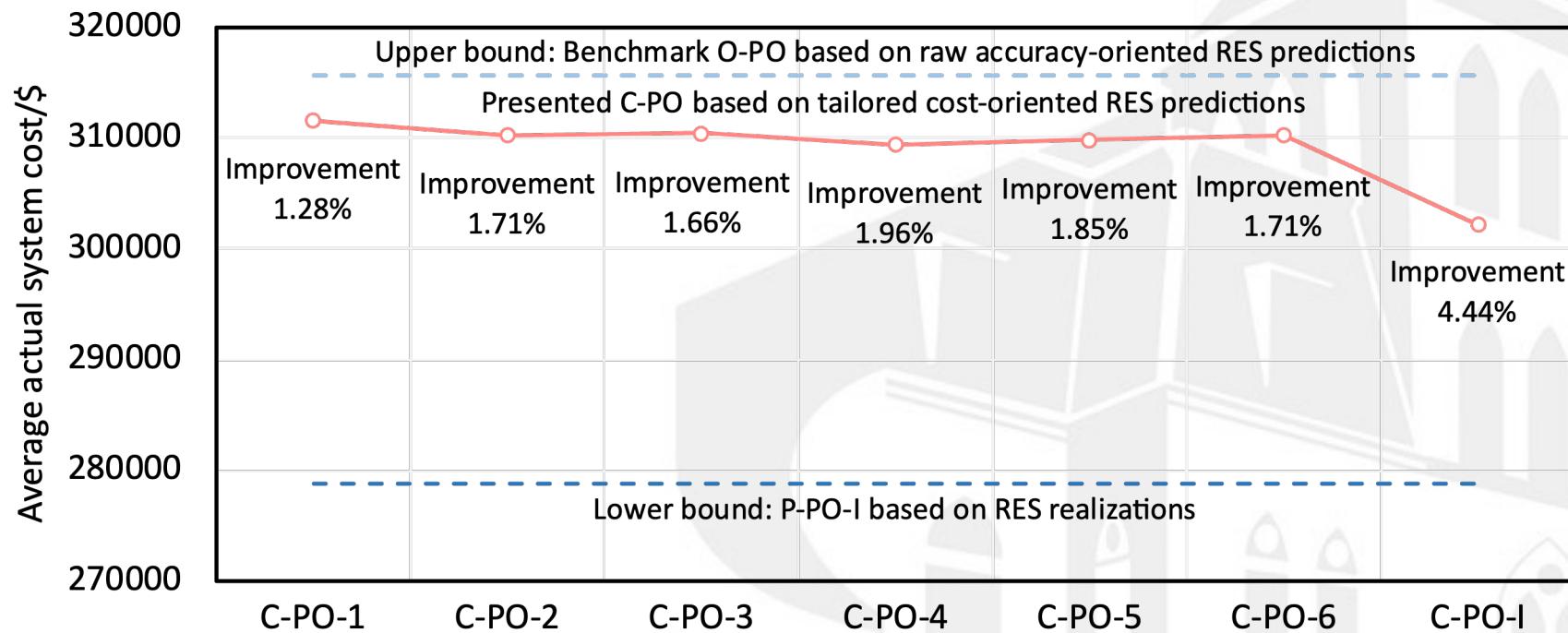
- *Cases on 24-Bus System: Simulating Belgian System*





## *Presented Closed-Loop Predict-and-Optimize Framework*

- *Cases on 24-Bus System: Results of Economics Improvements*
  - **C-PO enables noticeable economics improvements (1.28%-4.44%) over the daily UCs over entire 2020.**





## *Presented Closed-Loop Predict-and-Optimize Framework*

- *Cases on 5655-Bus System: Whether LR-based Decomposition Works?*
  - **C-PO-LR computationally outperforms C-PO-SD without optimality loss.**

Case	Training time/s		Optimality gap	
	C-PO-SD	C-PO-LR	C-PO-SD	C-PO-LR
1	1273.6	593.2	0.32%	0.62% (4 Iterations)
2	1111.7	1029.2	0.59%	0.89% (3 Iterations)
3	1655.8	927.5	0.51%	0.69% (3 Iterations)
4	828.6	619.2	0.86%	0.64% (4 Iterations)
5	685.9	512.3	0.81%	0.69% (4 Iterations)
6	3686.1	1364.1	0.93%	0.77% (4 Iterations)
7	1581.5	1312.6	0.33%	0.35% (4 Iterations)
8	1803.8	1215.9	0.74%	0.99% (4 Iterations)
9	1266.1	1211.8	0.67%	0.17% (4 Iterations)
10	1140.8	1086.3	0.36%	0.73% (4 Iterations)
11	2632.4	1089.1	0.49%	0.82% (3 Iterations)
12	1462.7	1321.3	0.31%	0.76% (4 Iterations)
13	1436.4	834.7	0.72%	0.74% (4 Iterations)
14	1138.9	714.8	0.98%	0.89% (4 Iterations)
15	1810.2	767.6	0.87%	0.99% (4 Iterations)
16	2146.1	290.8	0.92%	0.88% (1 Iteration)



## ***Presented Closed-Loop Predict-and-Optimize Framework***

- ***Conclusions***

- ***The data-driven (or feature-driven) C-PO can improve UC economics by generating cost-oriented RES predictions tailored for UC.***
- ***The LR-based decomposition method enables C-PO to be applicable to the practical system.***
- ***From perspective of machine learning, the C-PO essentially utilizes the linear regression: simple yet effective.***



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## References and Q&A

- **References**

- [1] Yafei Yang and Lei Wu, “Machine Learning Approaches to the Unit Commitment Problem: Current Trends, Emerging Challenges, and New Strategies,” *The Electricity Journal*, 2020.
- [2] Xianbang Chen, Yafei Yang, Yikui Liu, and Lei Wu, “Feature-Driven Economic Improvement for Network-Constrained Unit Commitment: A Closed-loop Predict-and-optimize Framework ,” *IEEE Transactions on Power Systems*, 2021.
- [3] Dataset of Closed-loop Predict-and-Optimize NCUC. [Online]. Available: [github.com/asxadf/Closed\\_Loop\\_NCUC\\_Dataset](https://github.com/asxadf/Closed_Loop_NCUC_Dataset).

- **Open-Access Dataset and Codes**

Our dataset and codes have been uploaded at [3], including RES, load, feature, and system data. Please feel free to use them.



## References and Q&A

- ***Opening: Join Us!***

Professor Lei Wu is looking for **highly motivated Post Doc and PhD students.**

If you are interested in our research areas, please feel free to send your resume to  
[Lei.Wu@stevens.edu](mailto:Lei.Wu@stevens.edu)

- ***About Professor Lei Wu***



- ***Professor in ECE Department at Stevens Institute of Technology***
- ***Fellow of IEEE (Class of 2022)***
- ***Research Focus: Applying mathematical optimization and machine learning on power system operation and planning.***
- ***Group: 4 PhDs & 4 Post Doctors***
- ***Homepage: <https://sites.google.com/site/leiwupes>***



## *References and Q&A*

- *About Stevens Institute of Technology*
  - *Nearby New York but quiet*
  - *Possess excellent views of Manhattan*
  - *Nice neighborhoods comfortable environment for living and studying*
  - *Solid environment for researching*
  - *Enjoy high security (Rank top 10 in USA)*









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