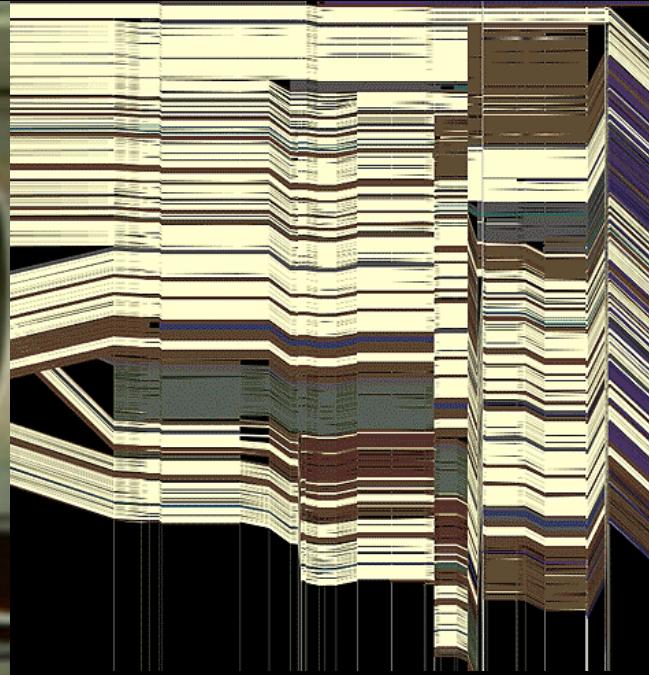
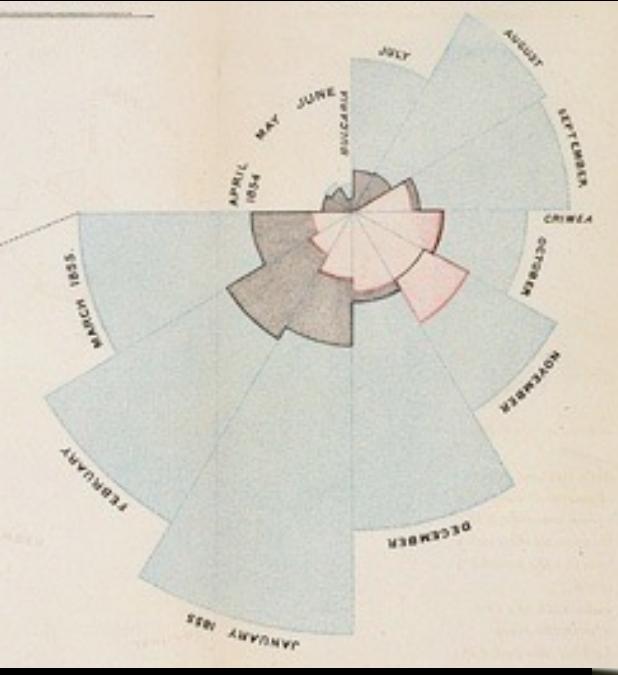


CSE 512 - Data Visualization

# Multidimensional Vis



Jeffrey Heer University of Washington

Last Time:  
Exploratory Data Analysis



**Exposure**, the effective laying open of the data to display the unanticipated, is to us a major portion of data analysis. Formal statistics has given almost no guidance to exposure; indeed, it is not clear how the **informality** and **flexibility** appropriate to the **exploratory character of exposure** can be fitted into any of the structures of formal statistics so far proposed.

# Graph Viewer

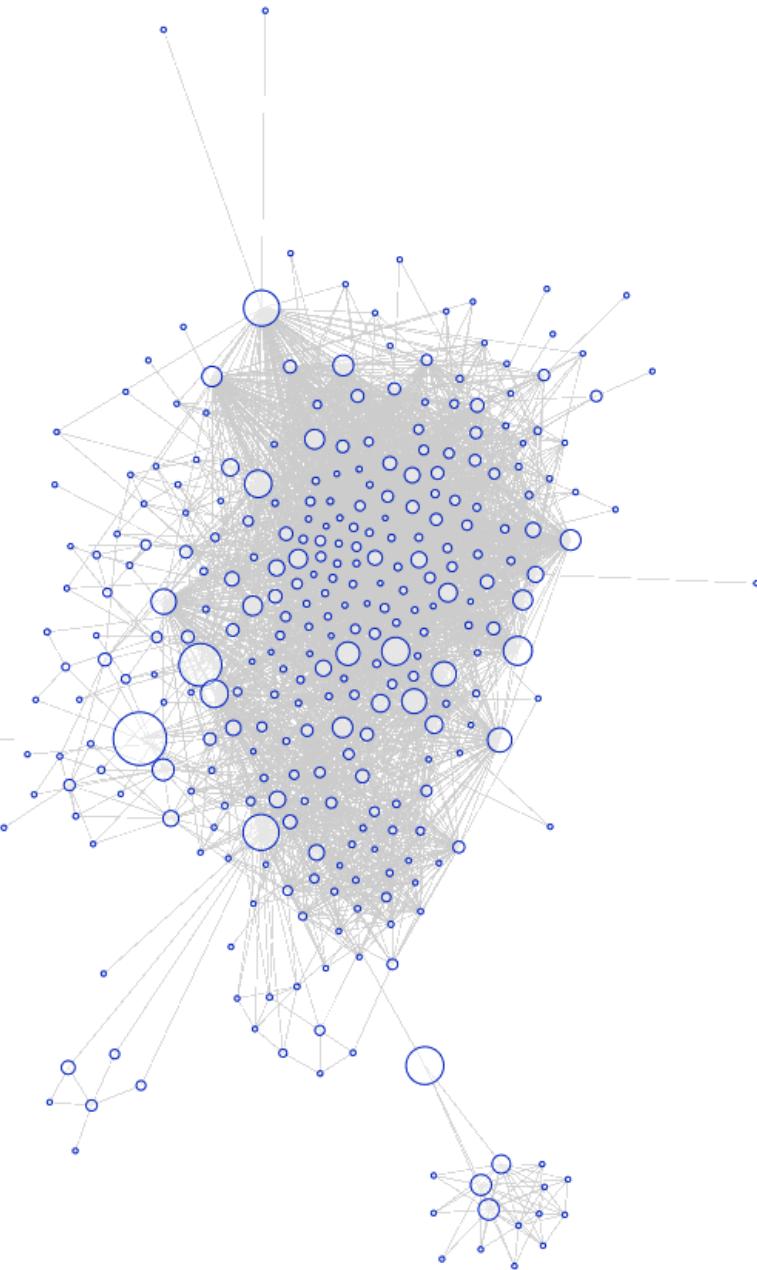
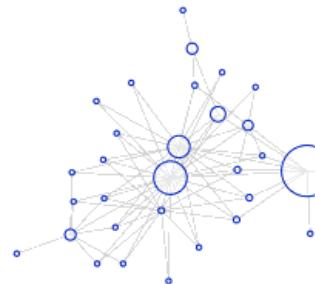
## Graph Viewer

Roll-up by:

Visualization:

Sort by:

Edge centrality filters:



Images

Animate

# Graph Viewer

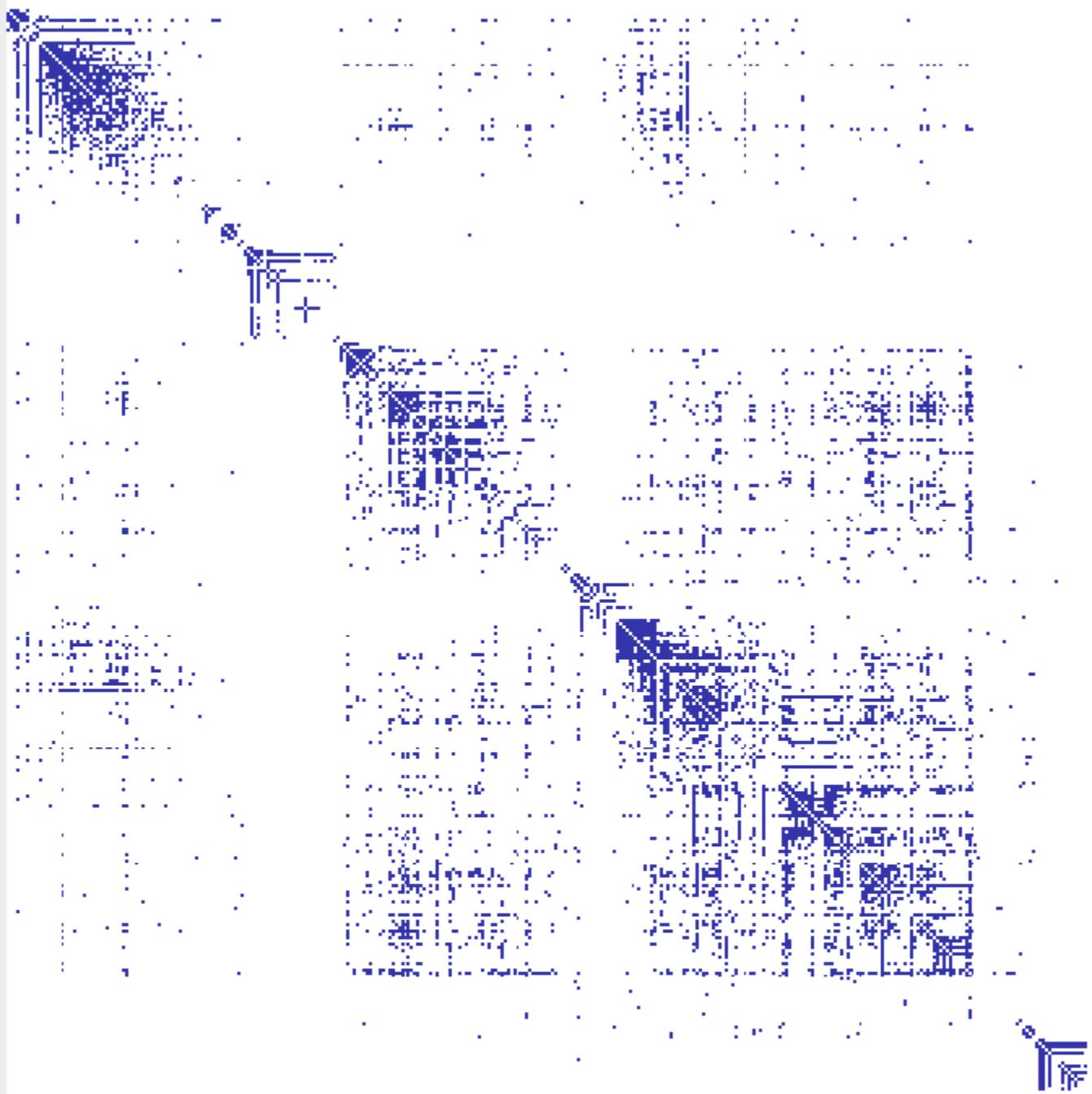
## Graph Viewer

Roll-up by:

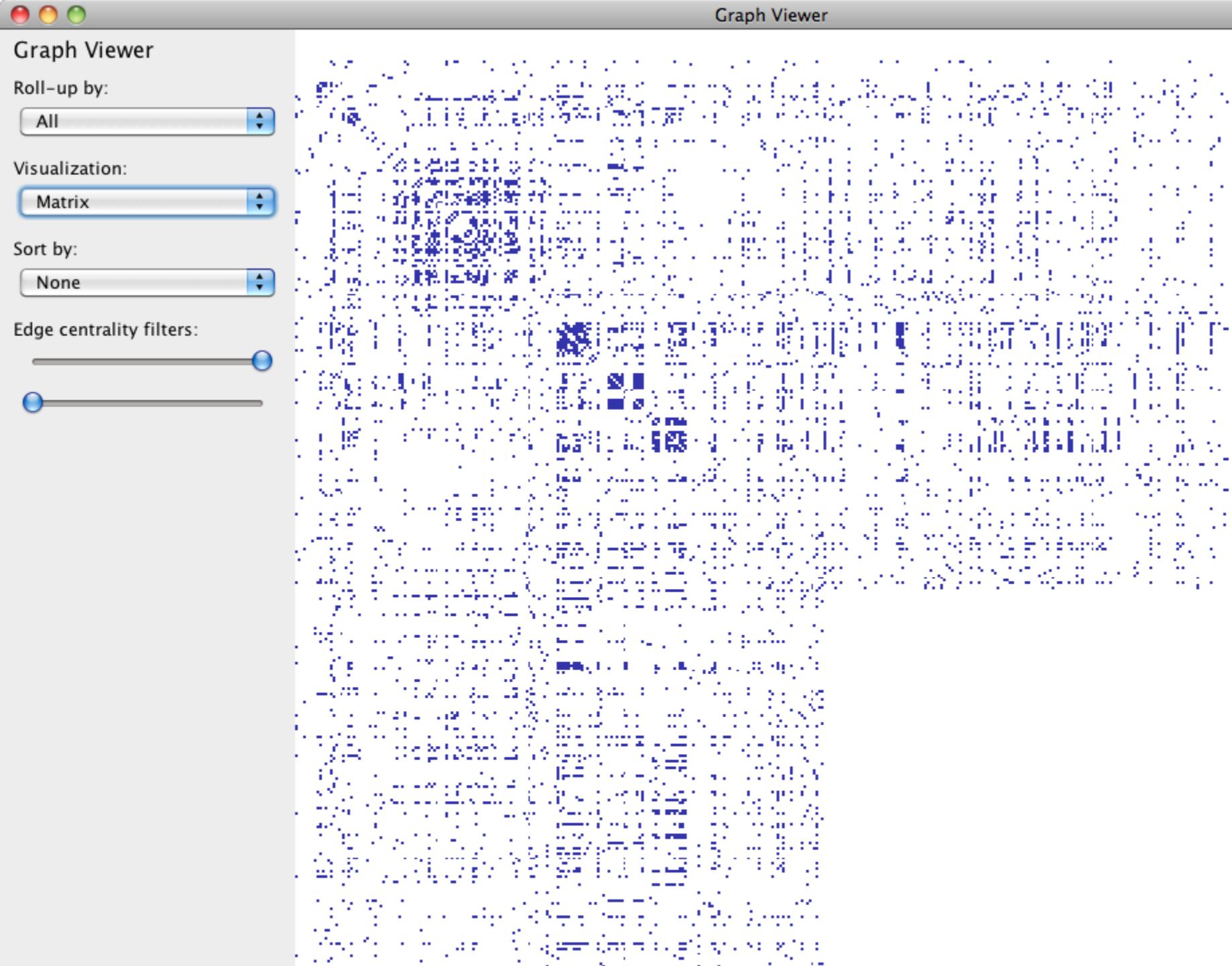
Visualization:

Sort by:

Edge centrality filters:



Graph Viewer

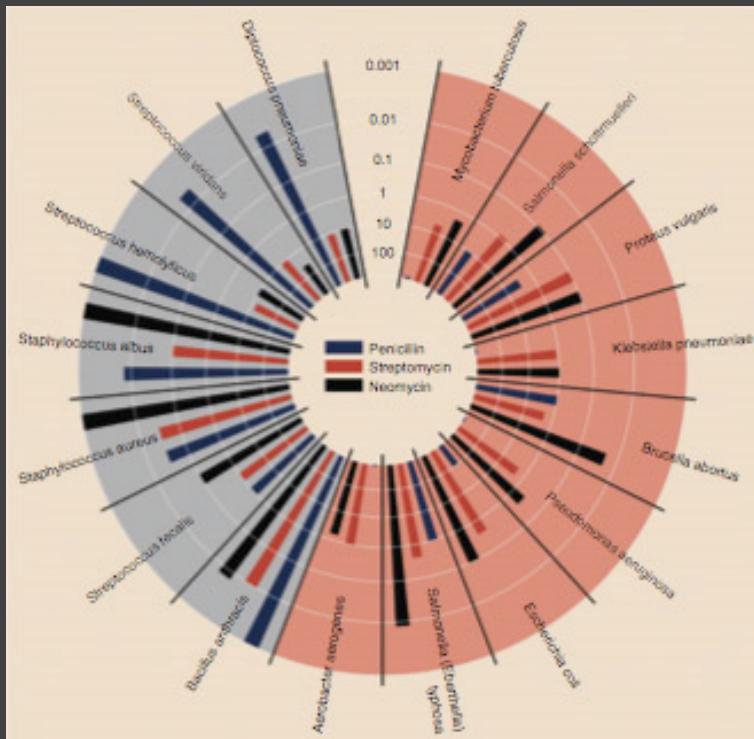


# Antibiotic Effectiveness

Table 1: Burtin's data.

Bacteria	Antibiotic			Gram Staining
	Penicillin	Streptomycin	Neomycin	
<i>Aerobacter aerogenes</i>	870	1	1.6	negative
<i>Brucella abortus</i>	1	2	0.02	negative
<i>Brucella anthracis</i>	0.001	0.01	0.007	positive
<i>Diplococcus pneumoniae</i>	0.005	11	10	positive
<i>Escherichia coli</i>	100	0.4	0.1	negative
<i>Klebsiella pneumoniae</i>	850	1.2	1	negative
<i>Mycobacterium tuberculosis</i>	800	5	2	negative
<i>Proteus vulgaris</i>	3	0.1	0.1	negative
<i>Pseudomonas aeruginosa</i>	850	2	0.4	negative
<i>Salmonella (Eberthella) typhosa</i>	1	0.4	0.008	negative
<i>Salmonella schottmuelleri</i>	10	0.8	0.09	negative
<i>Staphylococcus albus</i>	0.007	0.1	0.001	positive
<i>Staphylococcus aureus</i>	0.03	0.03	0.001	positive
<i>Streptococcus fecalis</i>	1	1	0.1	positive
<i>Streptococcus hemolyticus</i>	0.001	14	10	positive
<i>Streptococcus viridans</i>	0.005	10	40	positive

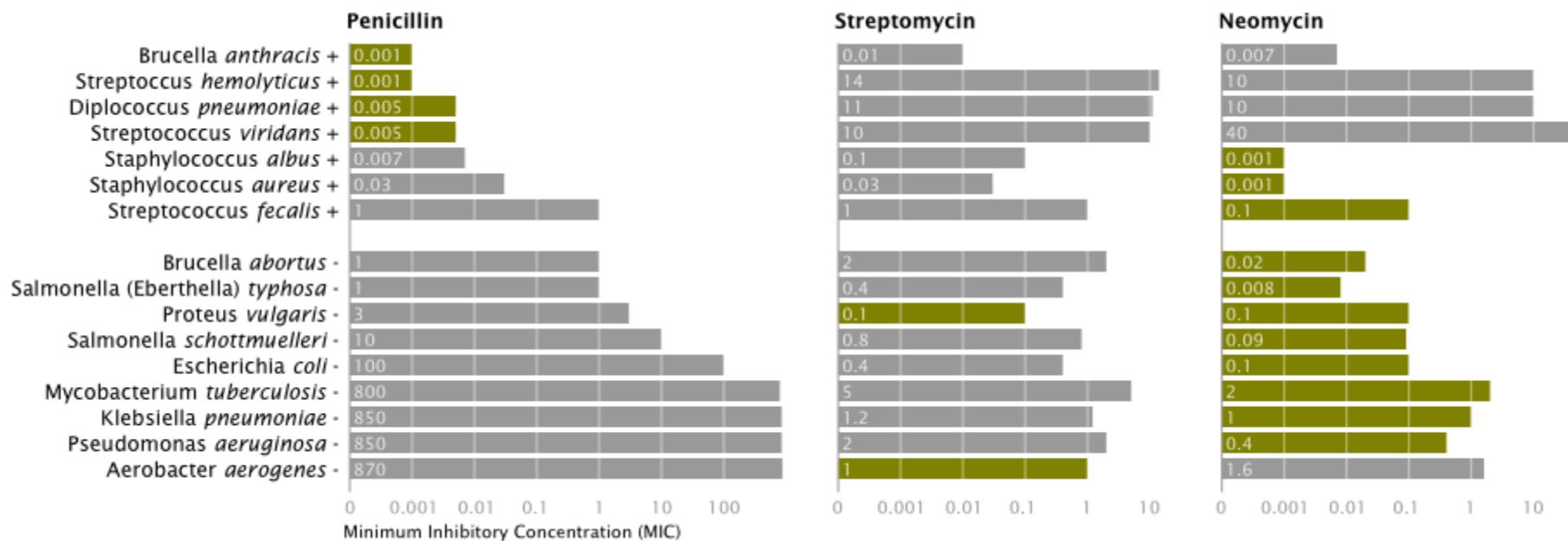
# How do the drugs compare?



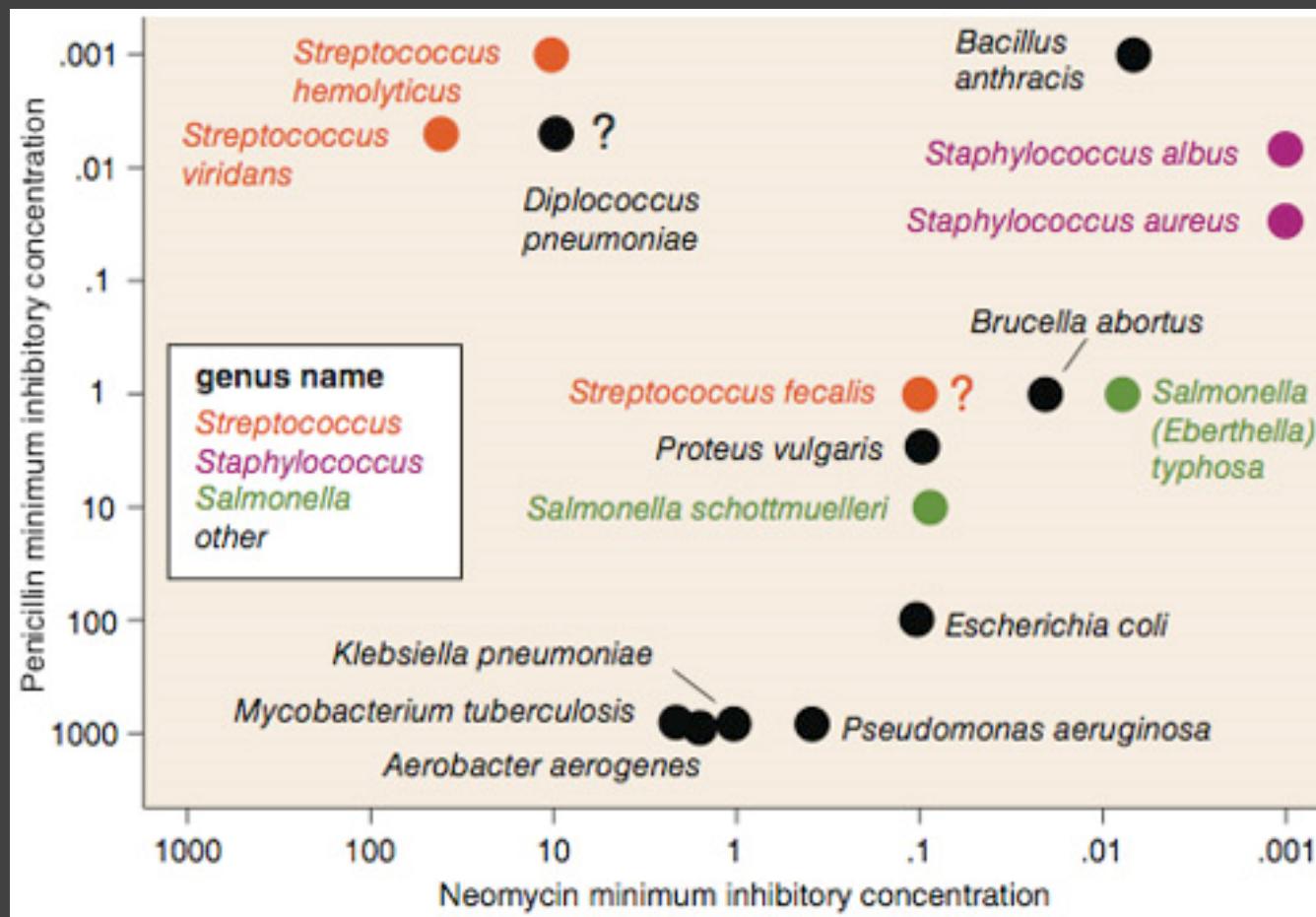
Bacteria	Penicillin	Antibiotic Streptomycin	Neomycin	Gram stain
<i>Aerobacter aerogenes</i>	870	1	1.6	-
<i>Brucella abortus</i>	1	2	0.02	-
<i>Bacillus anthracis</i>	0.001	0.01	0.007	+
<i>Diplococcus pneumoniae</i>	0.005	11	10	+
<i>Escherichia coli</i>	100	0.4	0.1	-
<i>Klebsiella pneumoniae</i>	850	1.2	1	-
<i>Mycobacterium tuberculosis</i>	800	5	2	-
<i>Proteus vulgaris</i>	3	0.1	0.1	-
<i>Pseudomonas aeruginosa</i>	850	2	0.4	-
<i>Salmonella (Eberthella) typhosa</i>	1	0.4	0.008	-
<i>Salmonella schottmuelleri</i>	10	0.8	0.09	-
<i>Staphylococcus albus</i>	0.007	0.1	0.001	+
<i>Staphylococcus aureus</i>	0.03	0.03	0.001	+
<i>Streptococcus faecalis</i>	1	1	0.1	+
<i>Streptococcus hemolyticus</i>	0.001	14	10	+
<i>Streptococcus viridans</i>	0.005	10	40	+

Original graphic by Will Burtin, 1951

# How do the drugs compare?

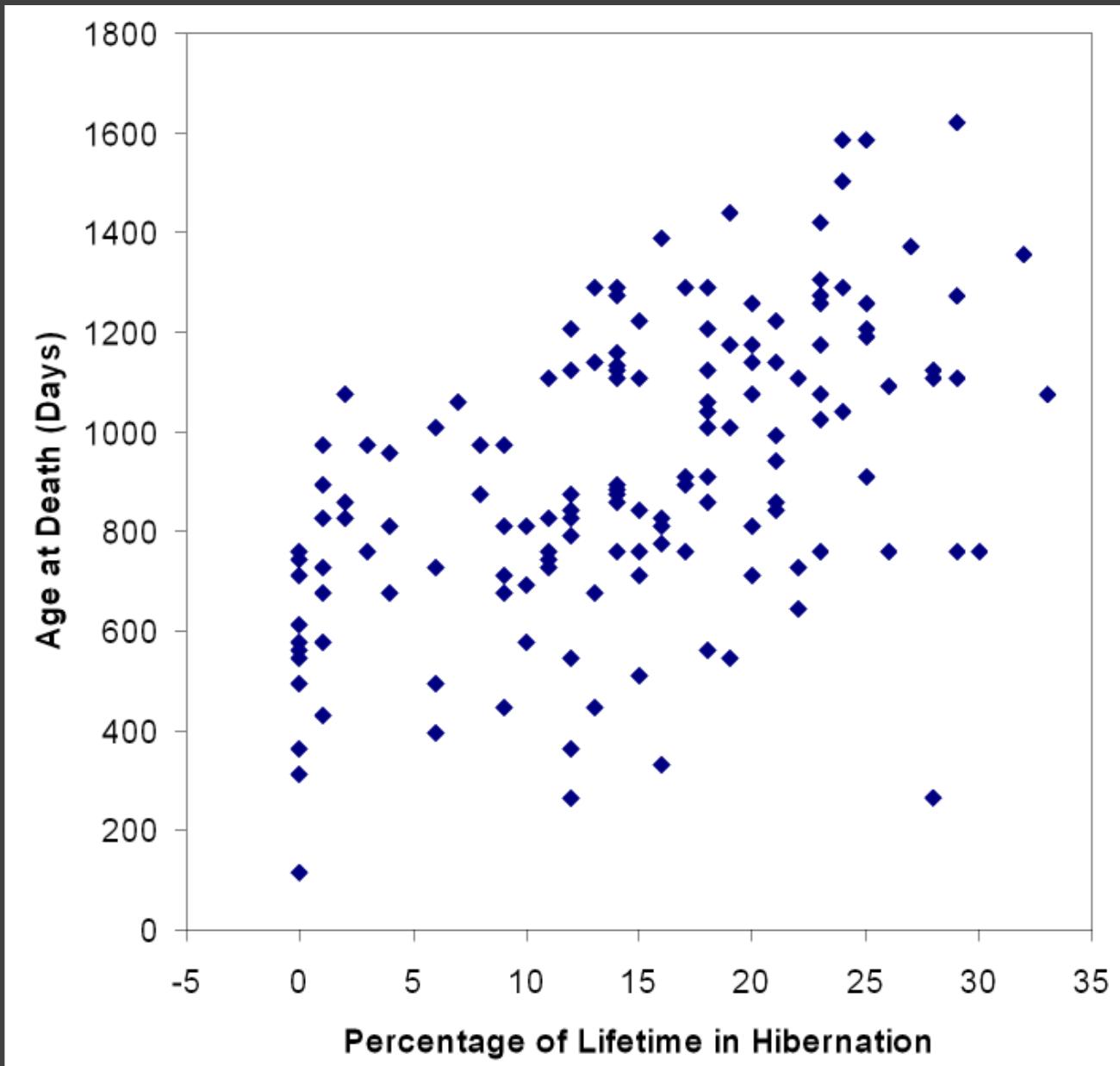


Mike Bostock  
Stanford CS448B, Winter 2009

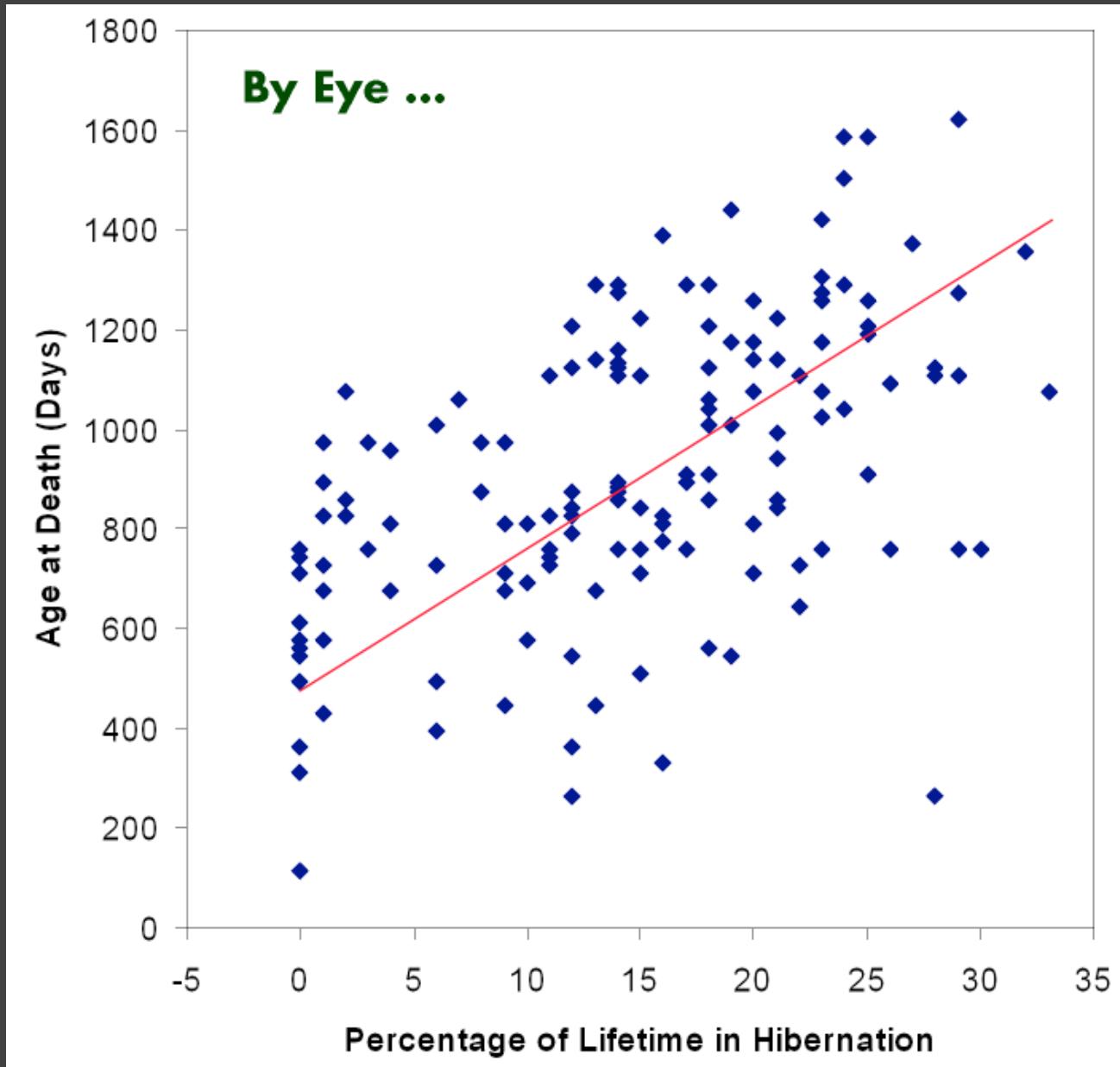


Do the bacteria group by resistance?  
Do different drugs correlate?

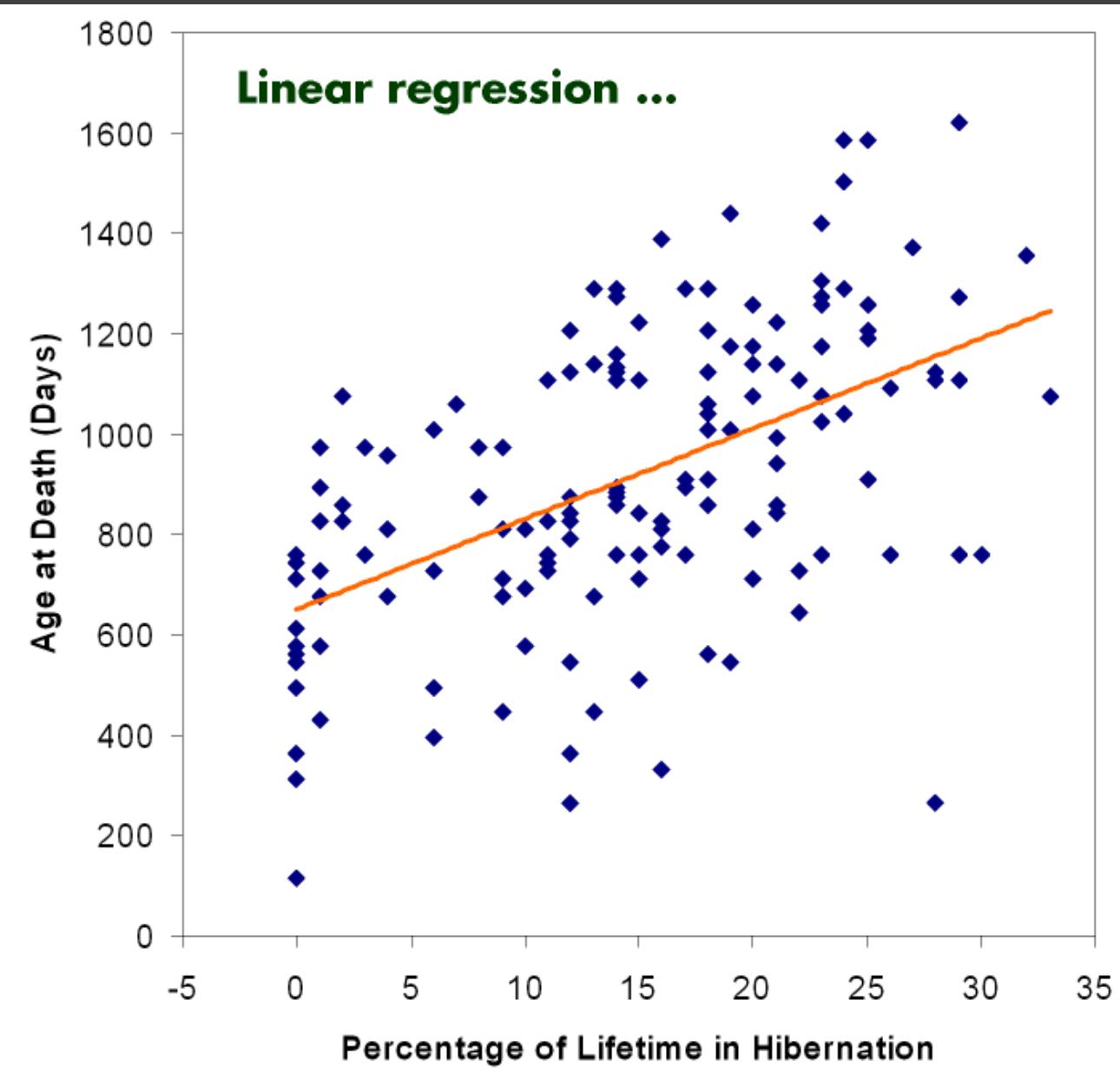
Wainer & Lysen  
*American Scientist, 2009*



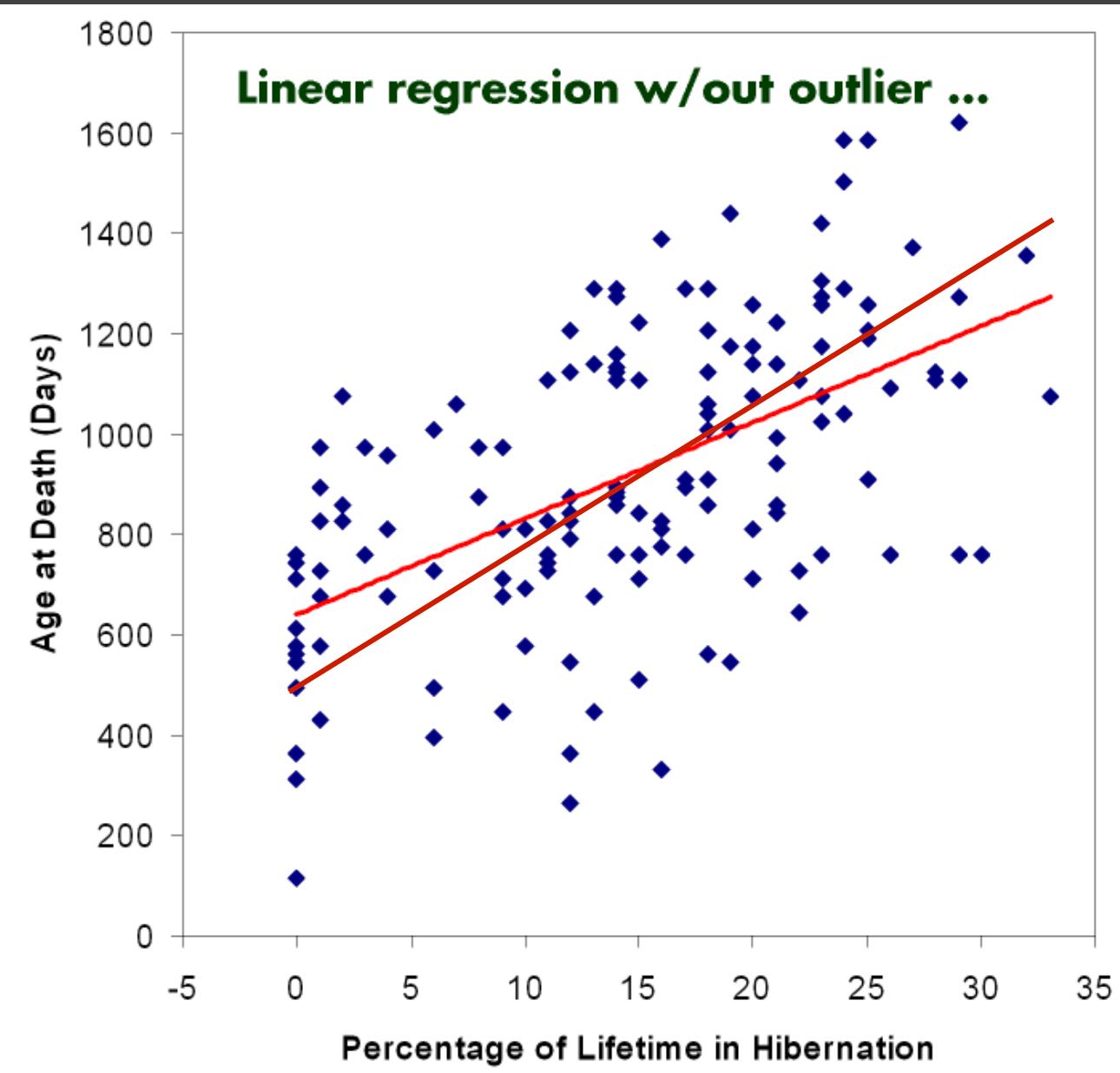
[The Elements of Graphing Data. Cleveland 94]



[The Elements of Graphing Data. Cleveland 94]



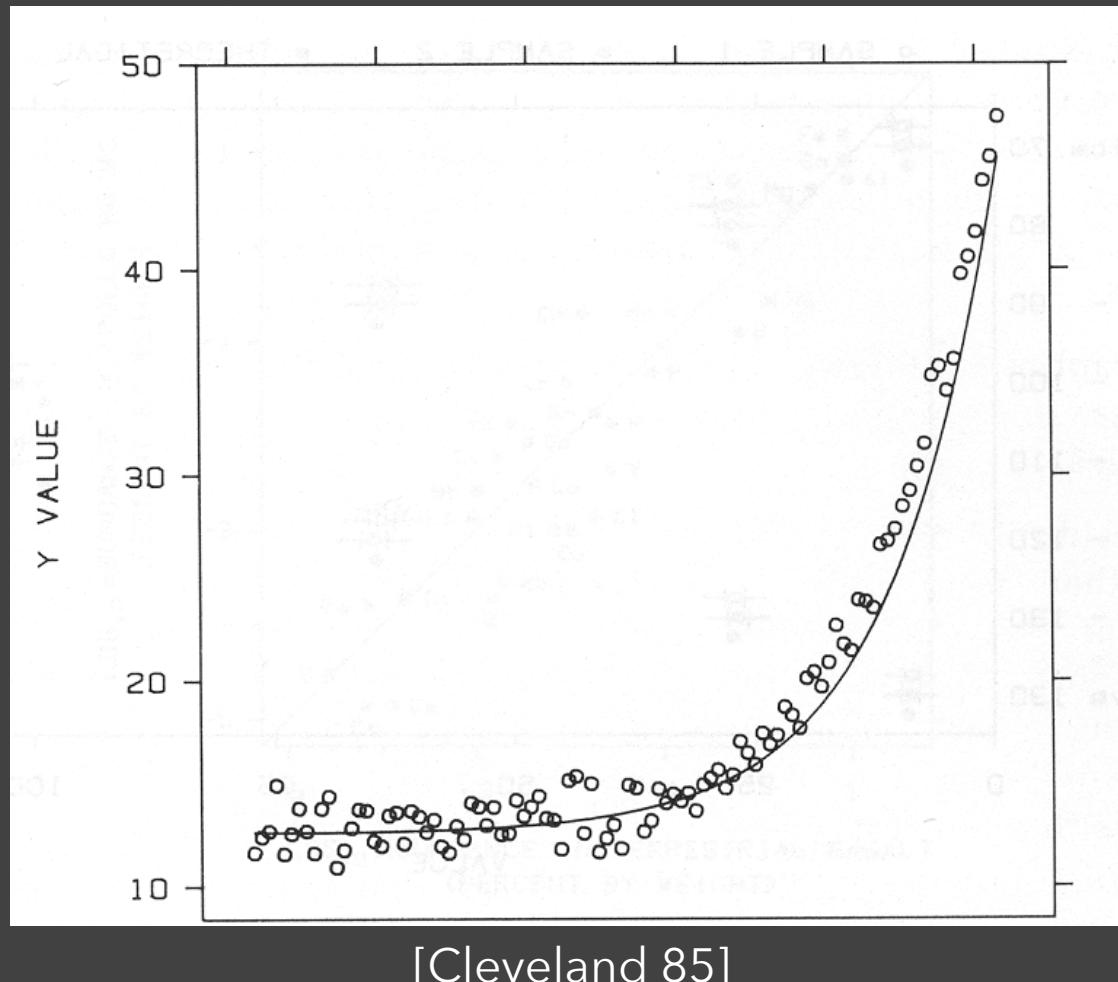
[The Elements of Graphing Data. Cleveland 94]



[The Elements of Graphing Data. Cleveland 94]

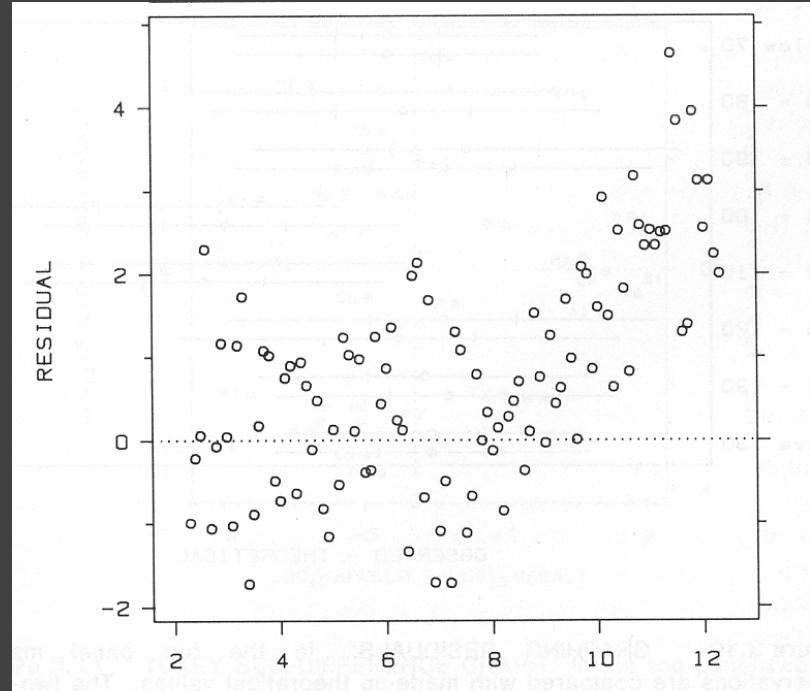
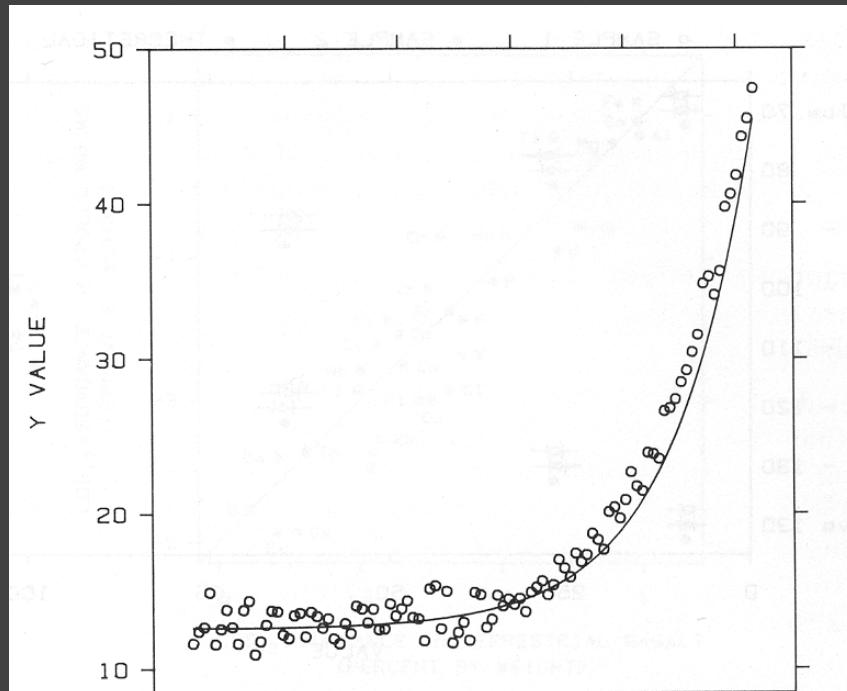
# Transforming Data

How well does the curve fit the data?



# Plot the Residuals

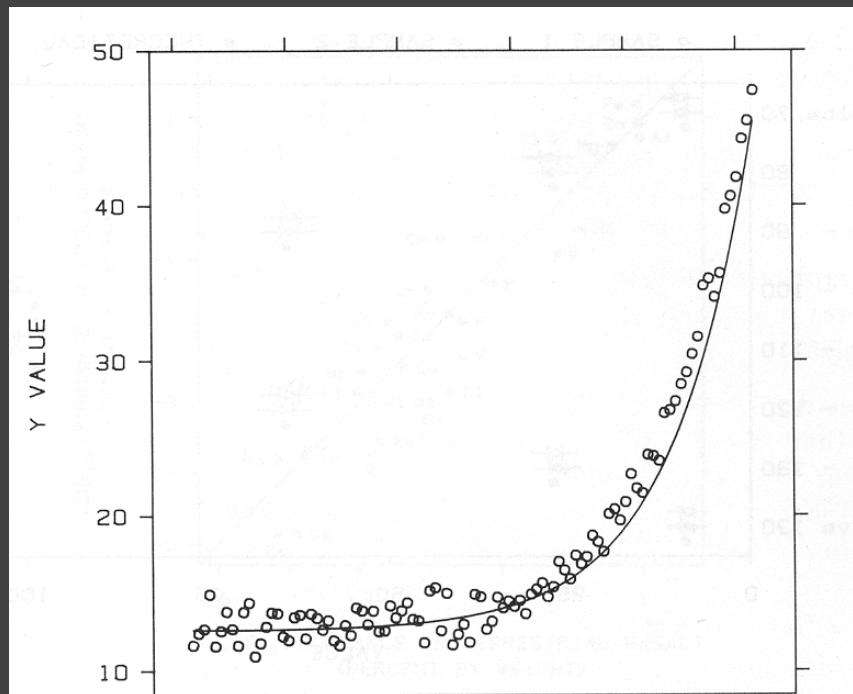
Plot vertical distance from best fit curve  
Residual graph shows accuracy of fit



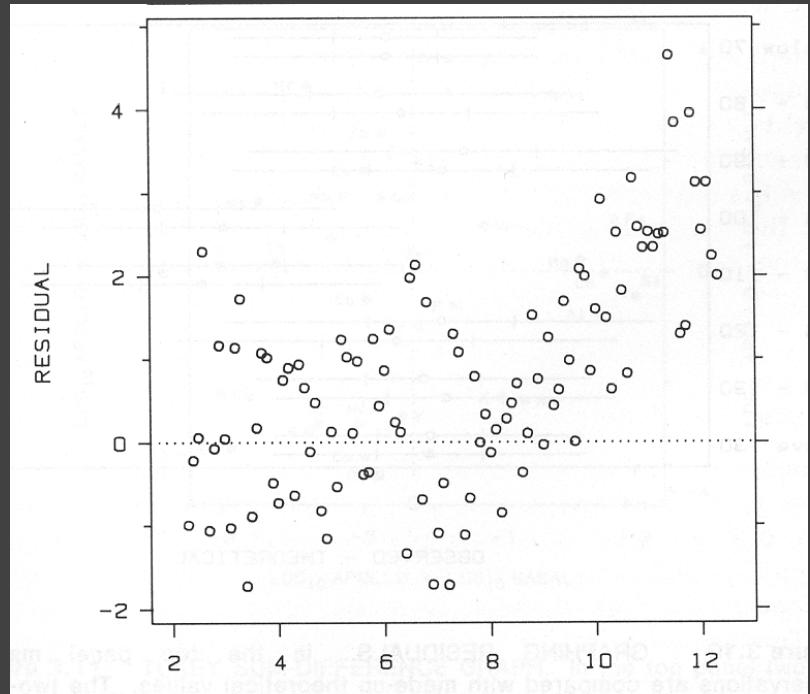
[Cleveland 85]

# Multiple Plotting Options

Plot model in data space



Plot data in model space



[Cleveland 85]

# A2: Exploratory Data Analysis

Use visualization software to form & answer questions

## First steps:

Step 1: Pick domain & data

Step 2: Pose questions

Step 3: Profile the data

Iterate as needed

## Create visualizations

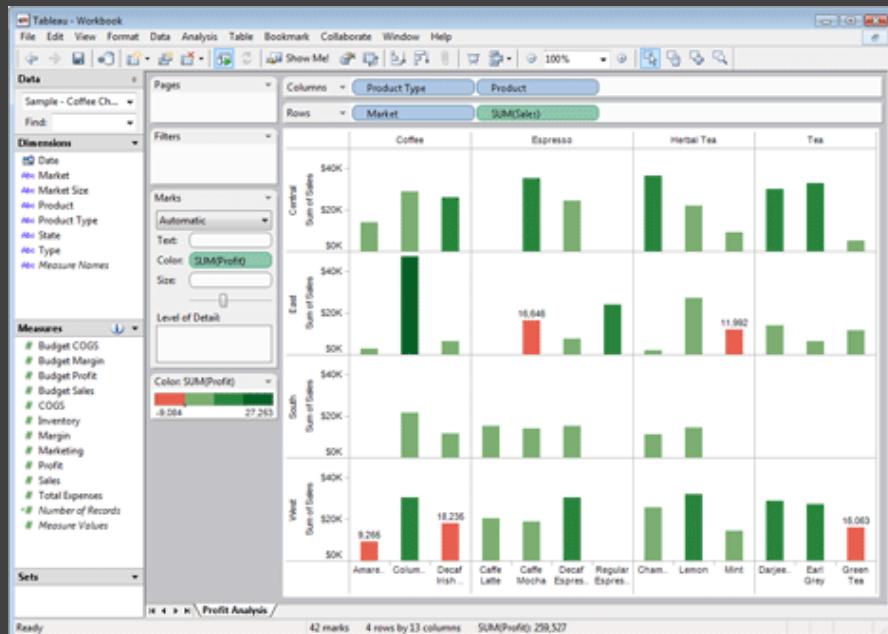
Interact with data

Refine your questions

## Make a notebook

Keep record of your analysis

Prepare a final graphic and caption



Due by 5:00pm

**Friday, April 15**

# Tutorials!

## Visualization Tools

Tue 4/12, 3:00-4:20pm PAA 114A

Introduction to Tableau, plus a few others.

## d3.js: Data-Driven Documents

Tue 4/19, 3:00-4:20pm PAA 114A

Focus on D3, touches on HTML/CSS/JS

# The Design Space of Visual Encodings

# Univariate Data



	factors			
	A	B	C	
1				

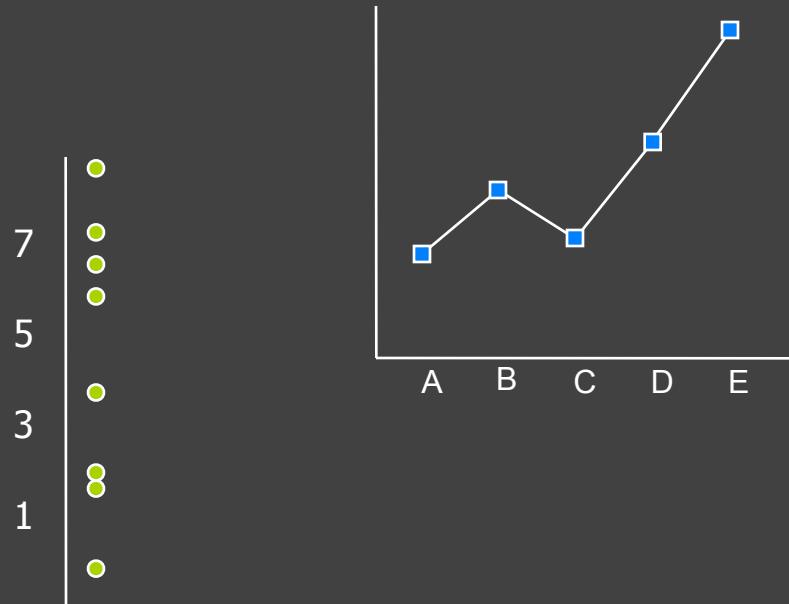
variable

# Univariate Data

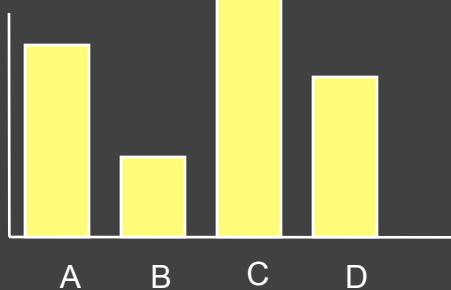
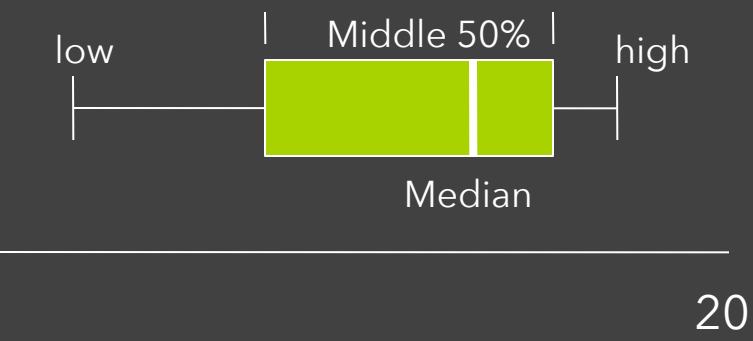
factors

1	A	B	C	

variable

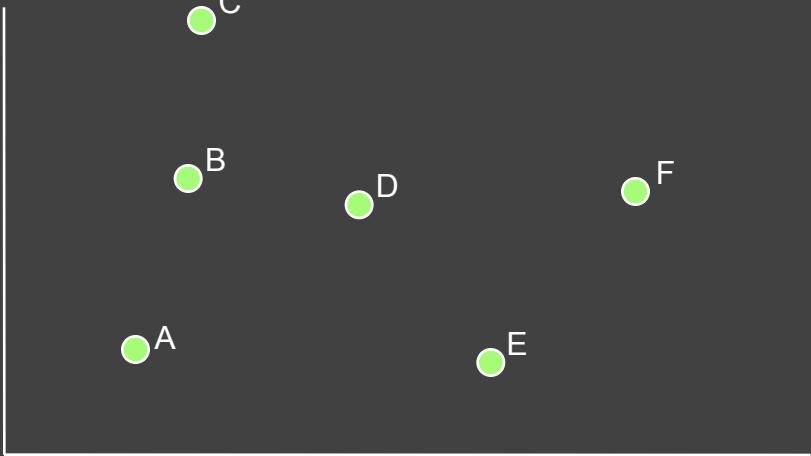


Tukey box plot



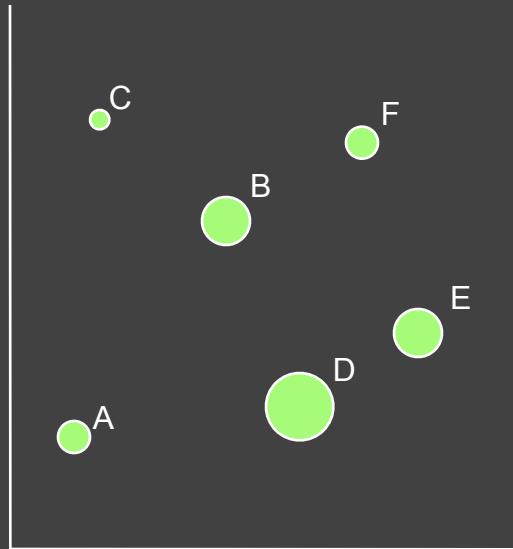
# Bivariate Data

	A	B	C
1			
2			



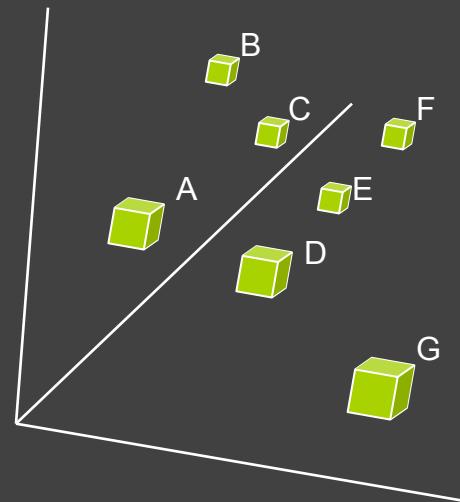
Scatter plot is common

# Trivariate Data



	A	B	C
1			
2			
3			

3D scatter plot is possible



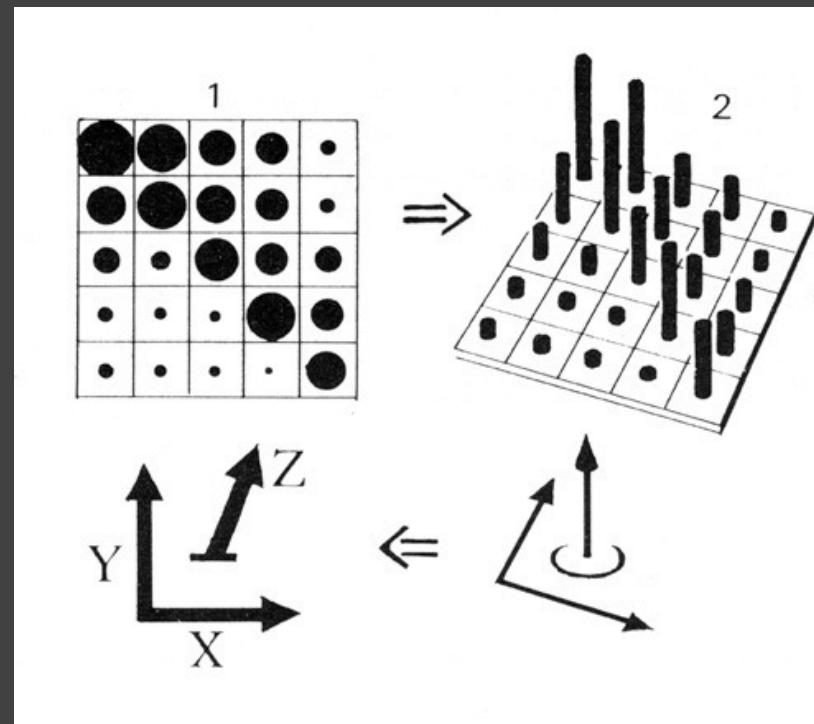
# Three Variables

**Two variables** [x,y] can map to points

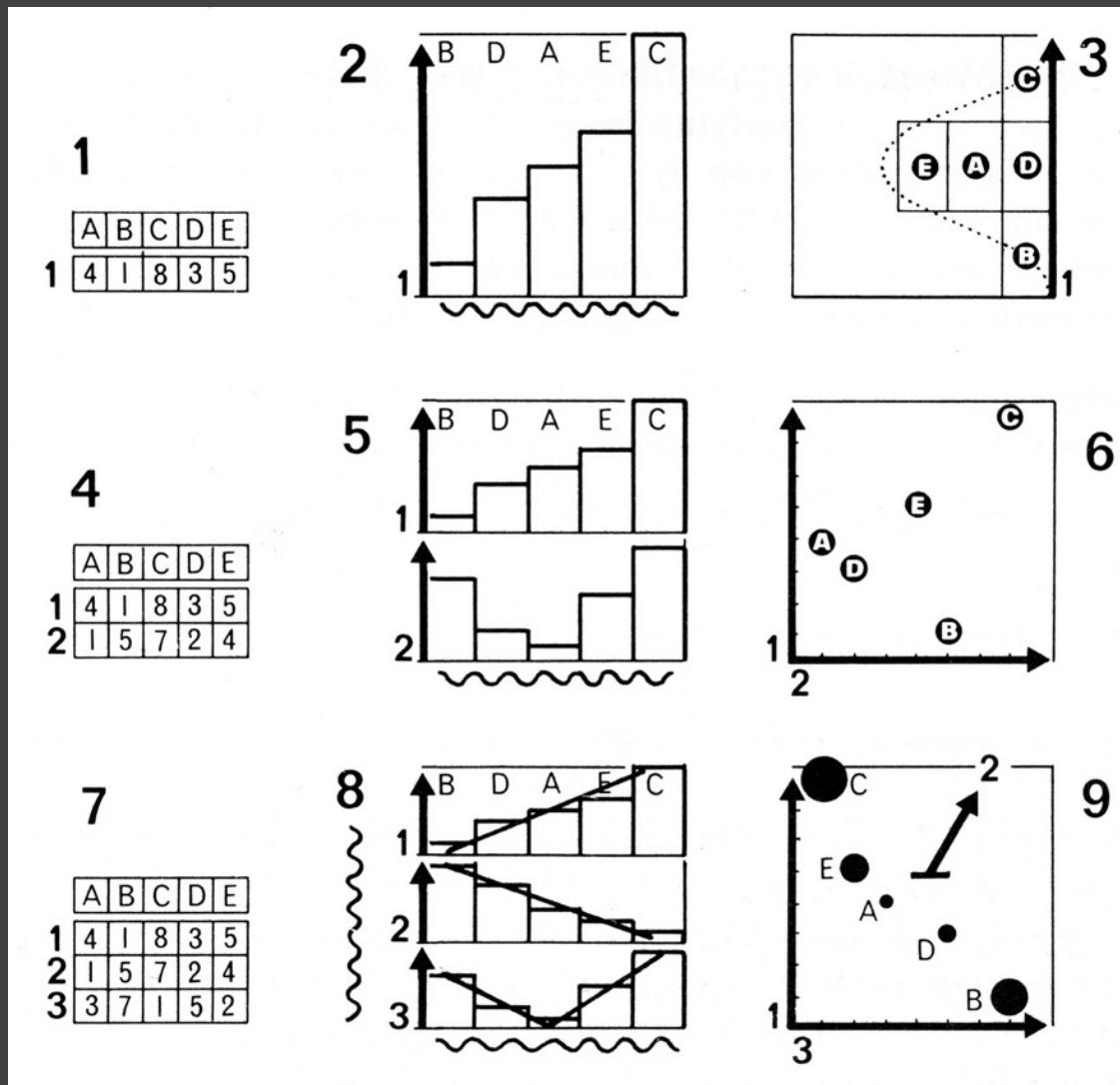
Scatterplots, maps, ...

**Third variable** [z] must use

Color, size, shape, ...



# Large Design Space



[Bertin, Graphics  
and Graphic Info.  
Processing, 1981]

# Multidimensional Data

# Visual Encoding Variables

Position (X)

Position (Y)

Size

Value

Texture

Color

Orientation

Shape

~8 dimensions?

		LES VARIABLES DE L'IMAGE				
		POINTS	LIGNES	ZONES		
XY 2 DIMENSIONS DU PLAN	Z	x	x	x	12	12
	TAILLE	■	■	■	12	12
	VALEUR	■	■	■	12	12
		LES VARIABLES DE SÉPARATION DES IMAGES				
GRAIN		■■■	■■■	■■■	12	12
COULEUR		■	■	■	12	12
ORIENTATION		■	■	■	12	12
FORME		■	▲	●	12	12

# Example: Coffee Sales

Sales figures for a fictional coffee chain

Sales	Q-Ratio
Profit	Q-Ratio
Marketing	Q-Ratio
Product Type	N {Coffee, Espresso, Herbal Tea, Tea}
Market	N {Central, East, South, West}

## Filters

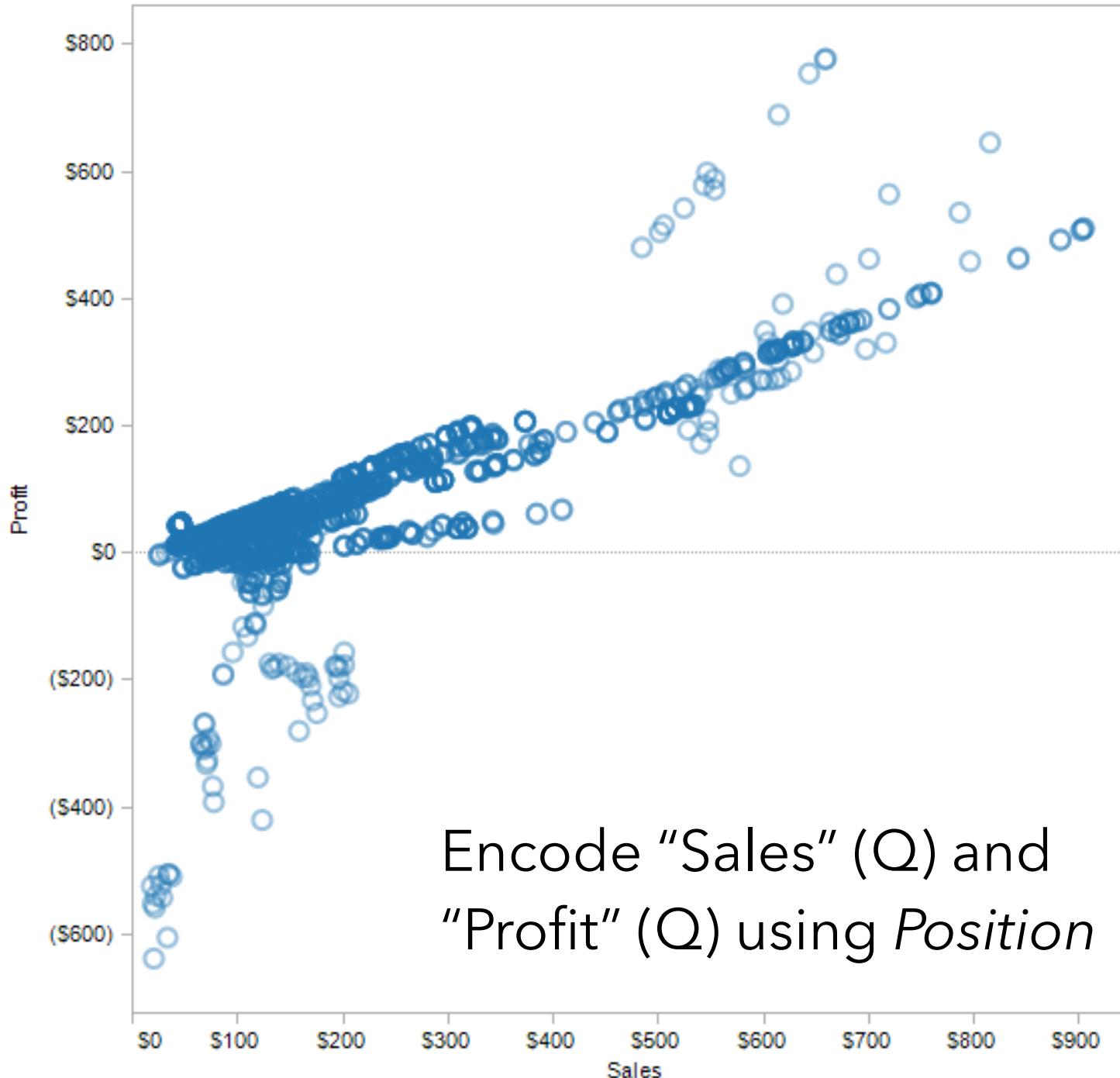
YEAR(Date): 2010

## Marks

x+ Automatic

Shape Label Color Size 

Level of Detail



## Filters

YEAR(Date): 2010

## Marks

x+ Automatic

Shape Label 

Color ▾ Product Type

Size Level of Detail 

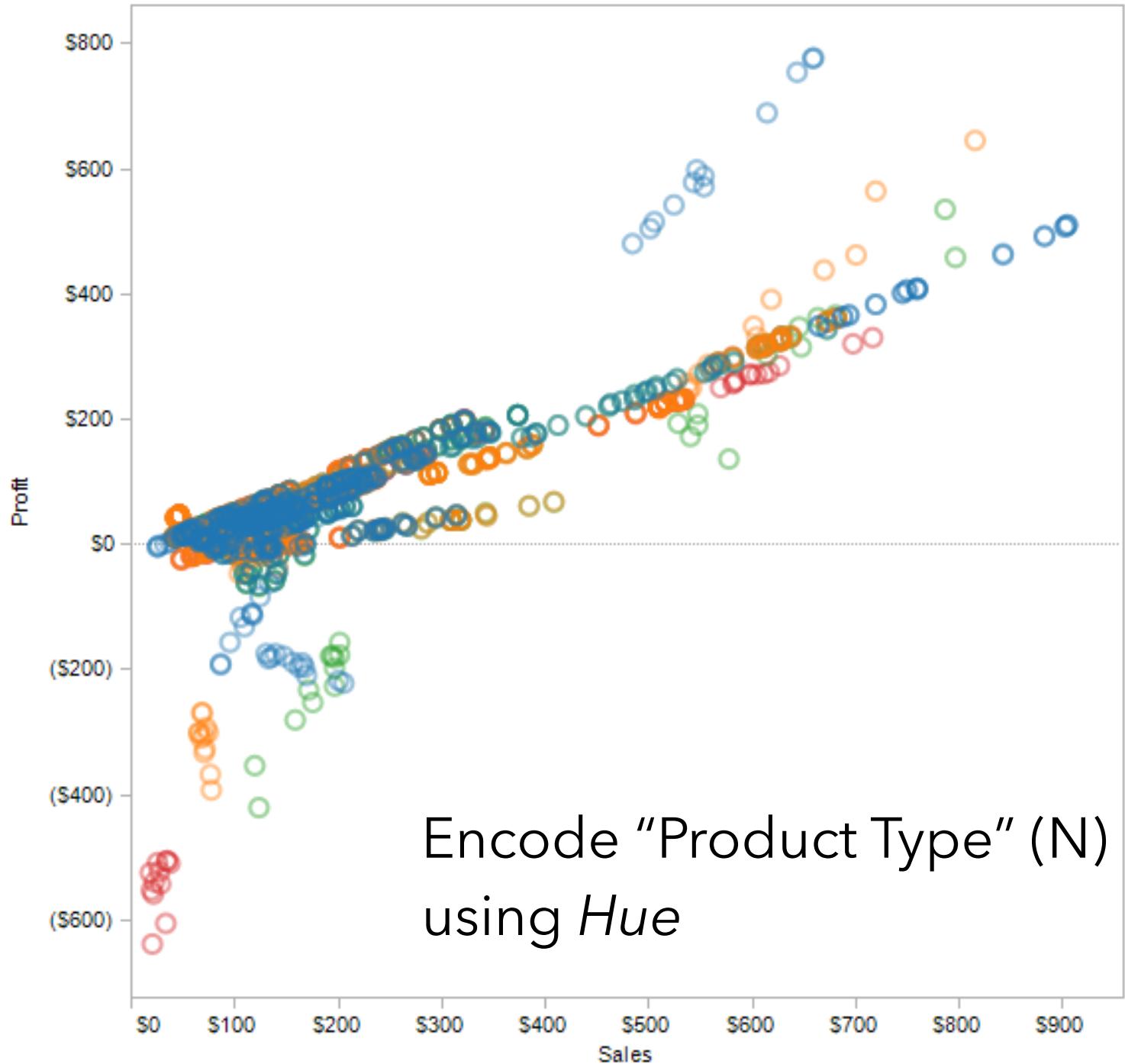
## Product Type

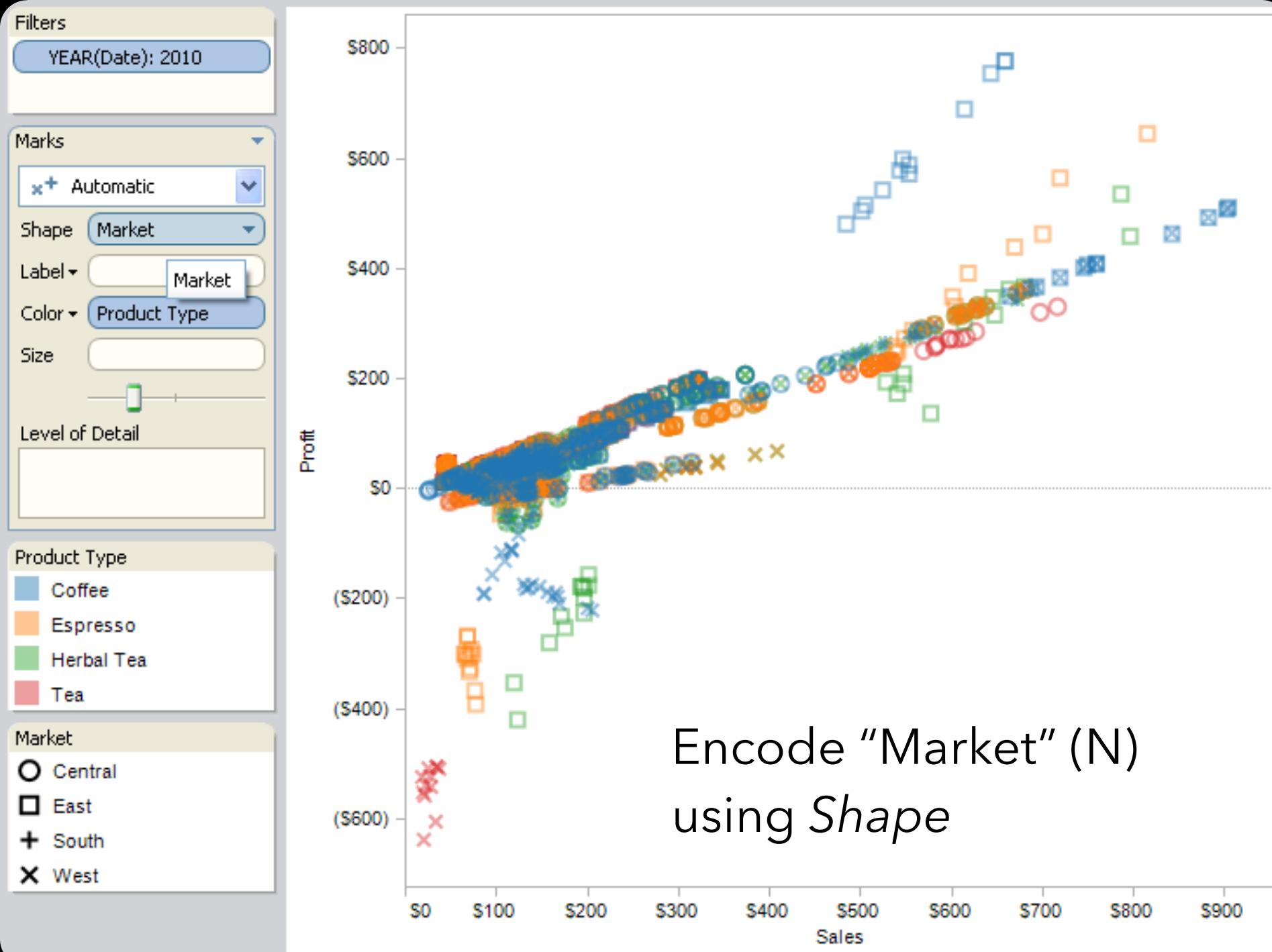
Coffee

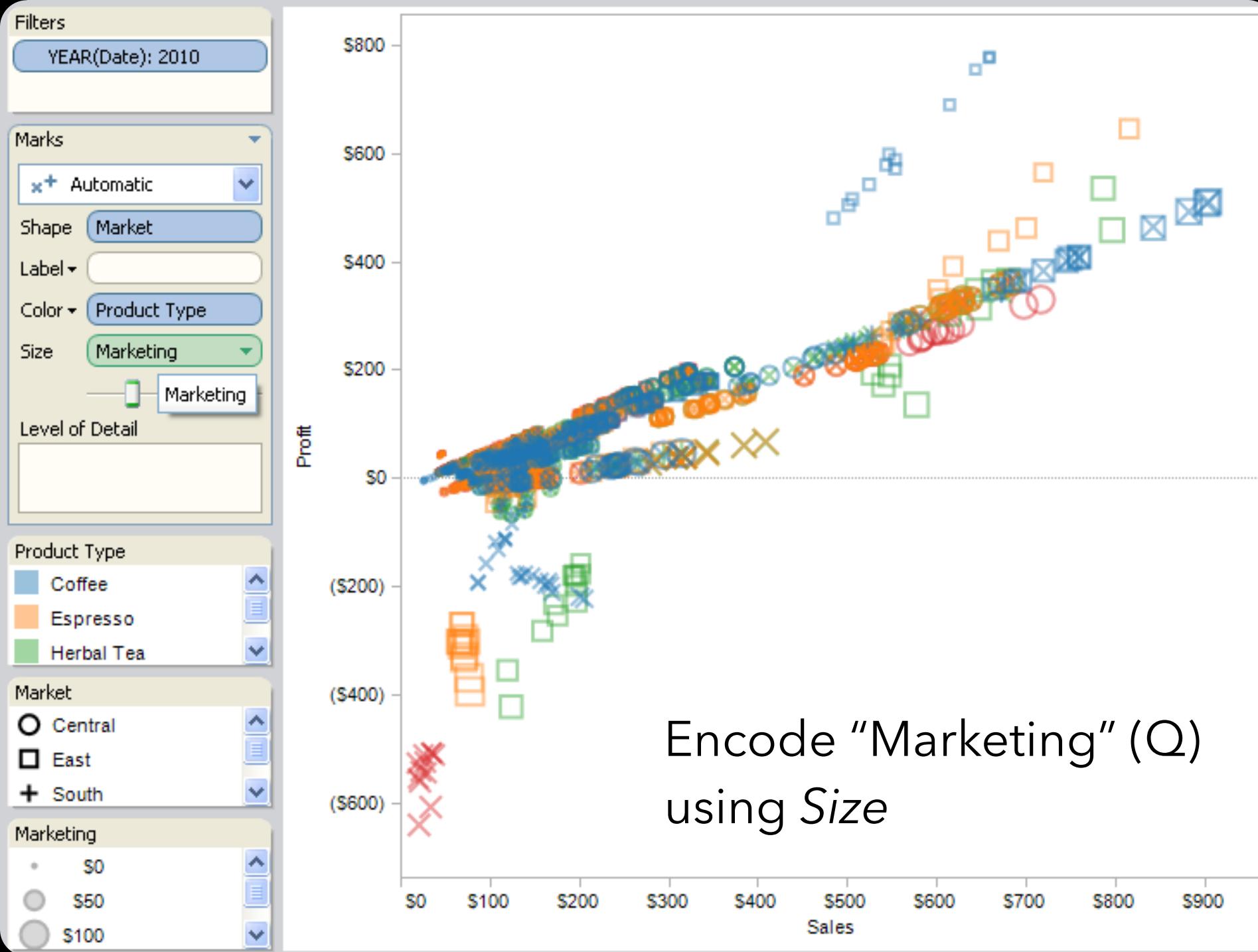
Espresso

Herbal Tea

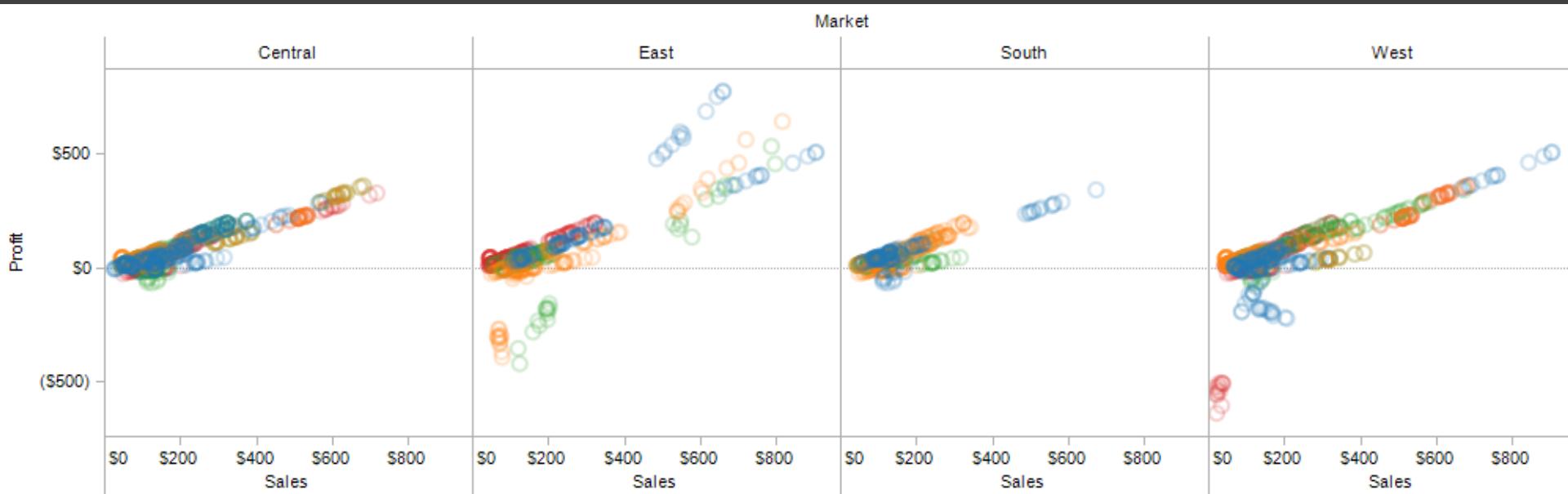
Tea







# Trellis Plots



A *trellis plot* subdivides space to enable comparison across multiple plots.

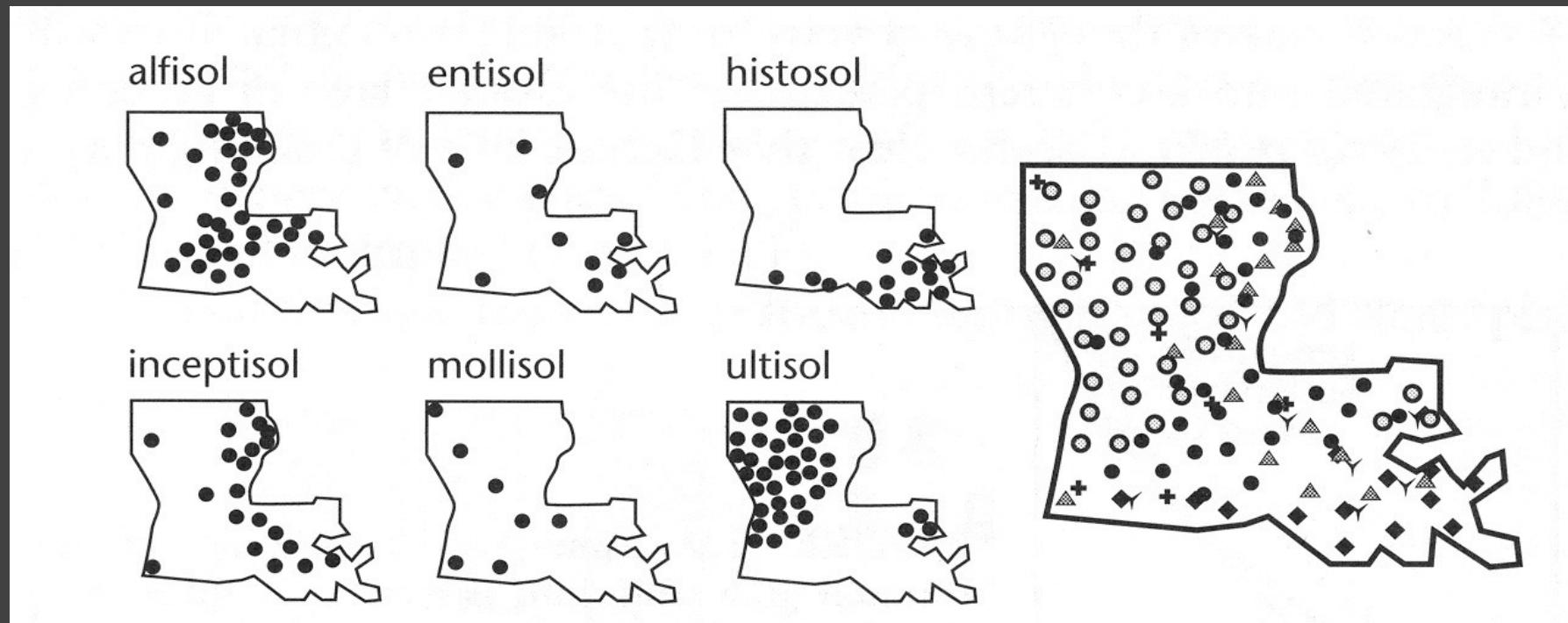
Typically nominal or ordinal variables are used as dimensions for subdivision.

# Small Multiples



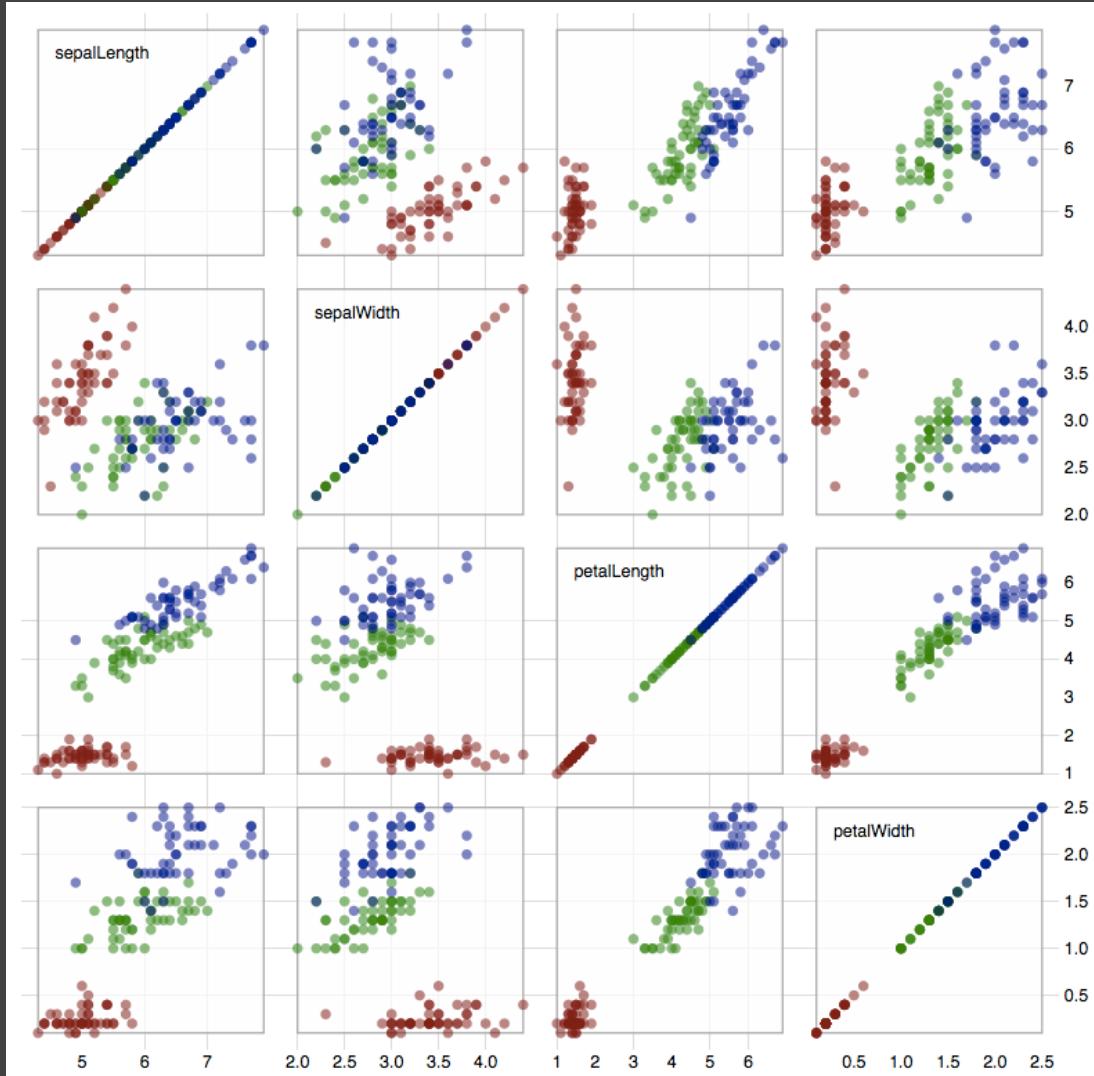
[MacEachren 95, Figure 2.11, p. 38]

# Small Multiples

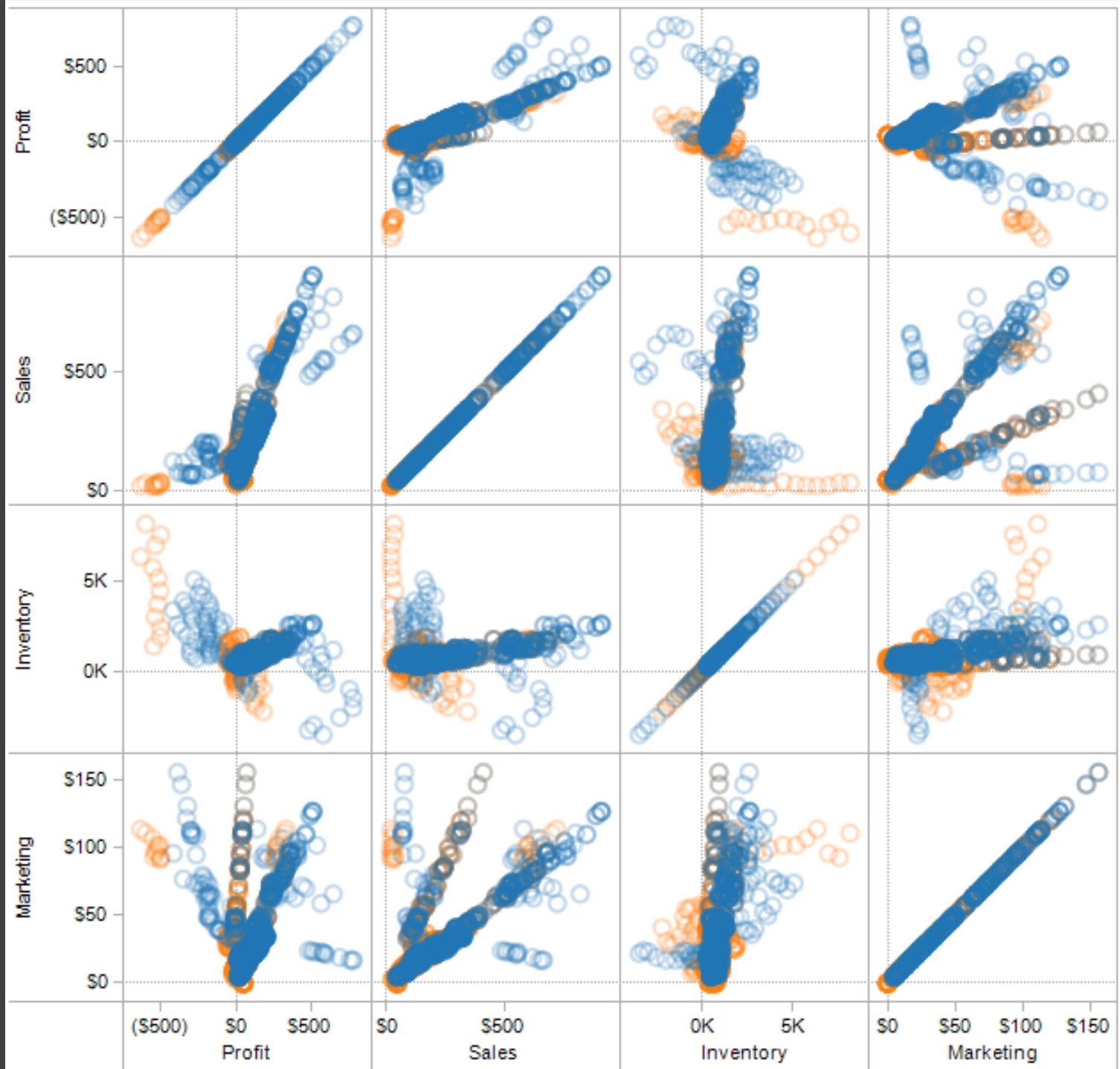


[MacEachren 95, Figure 2.11, p. 38]

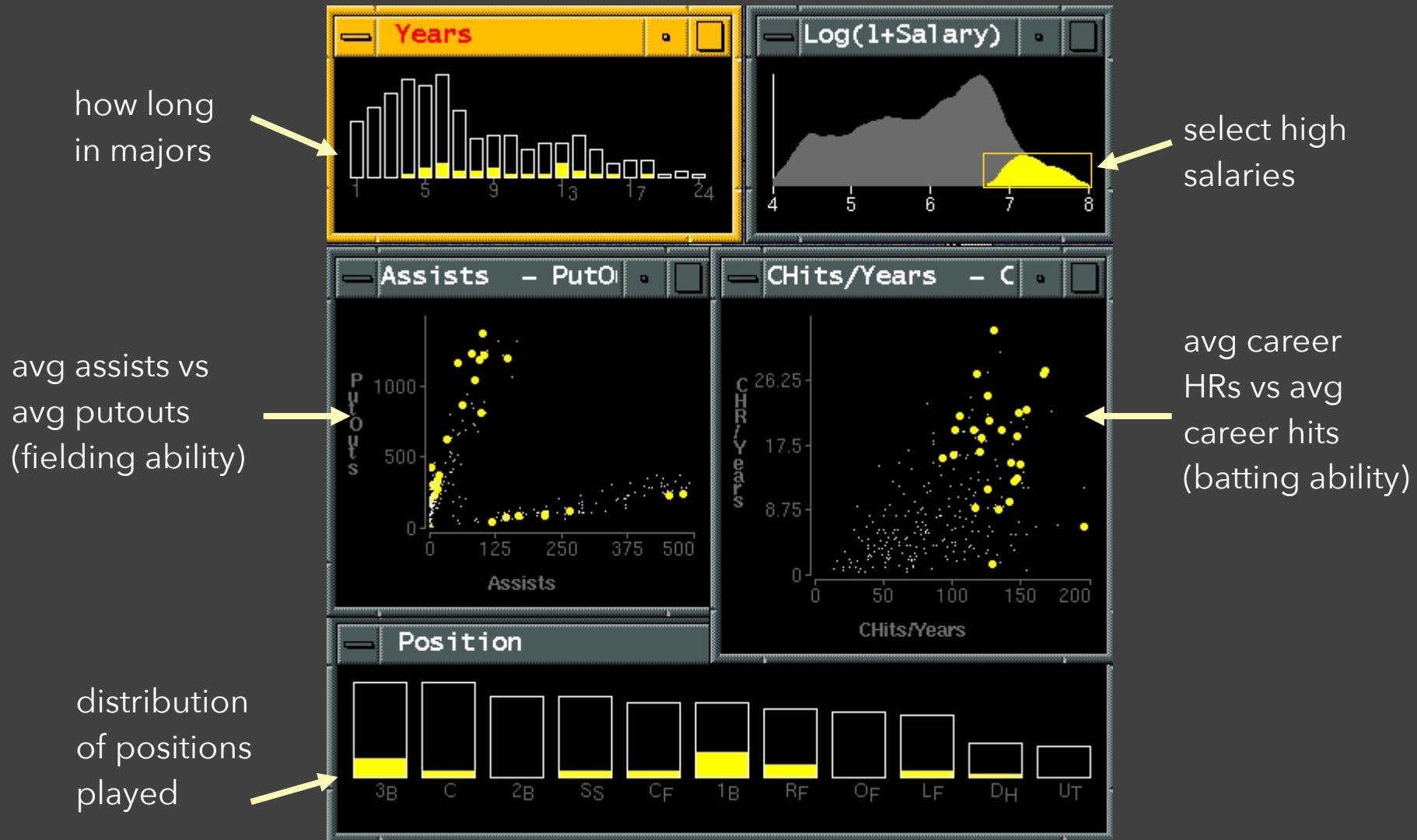
# Scatterplot Matrix (SPLOM)



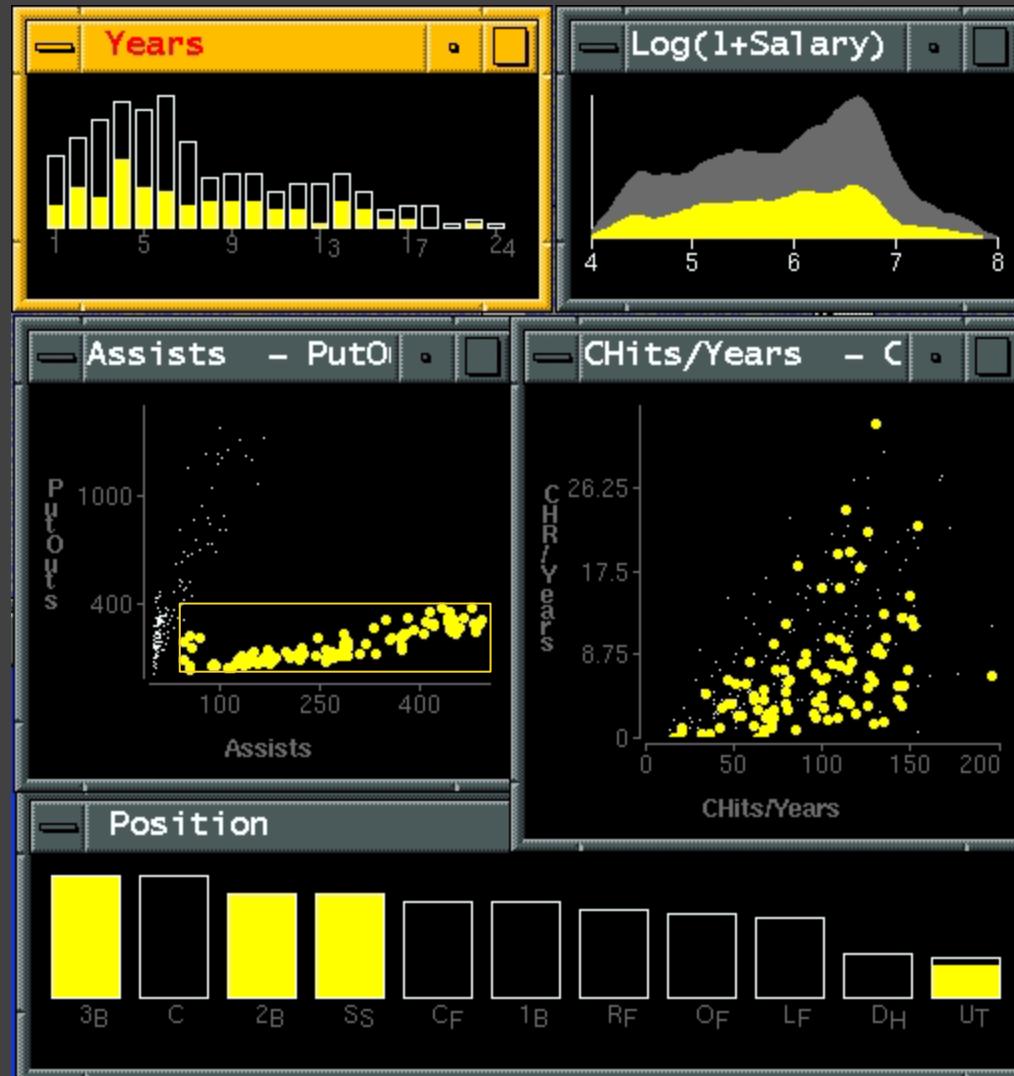
Scatter plots  
for pairwise  
comparison  
of each data  
dimension.



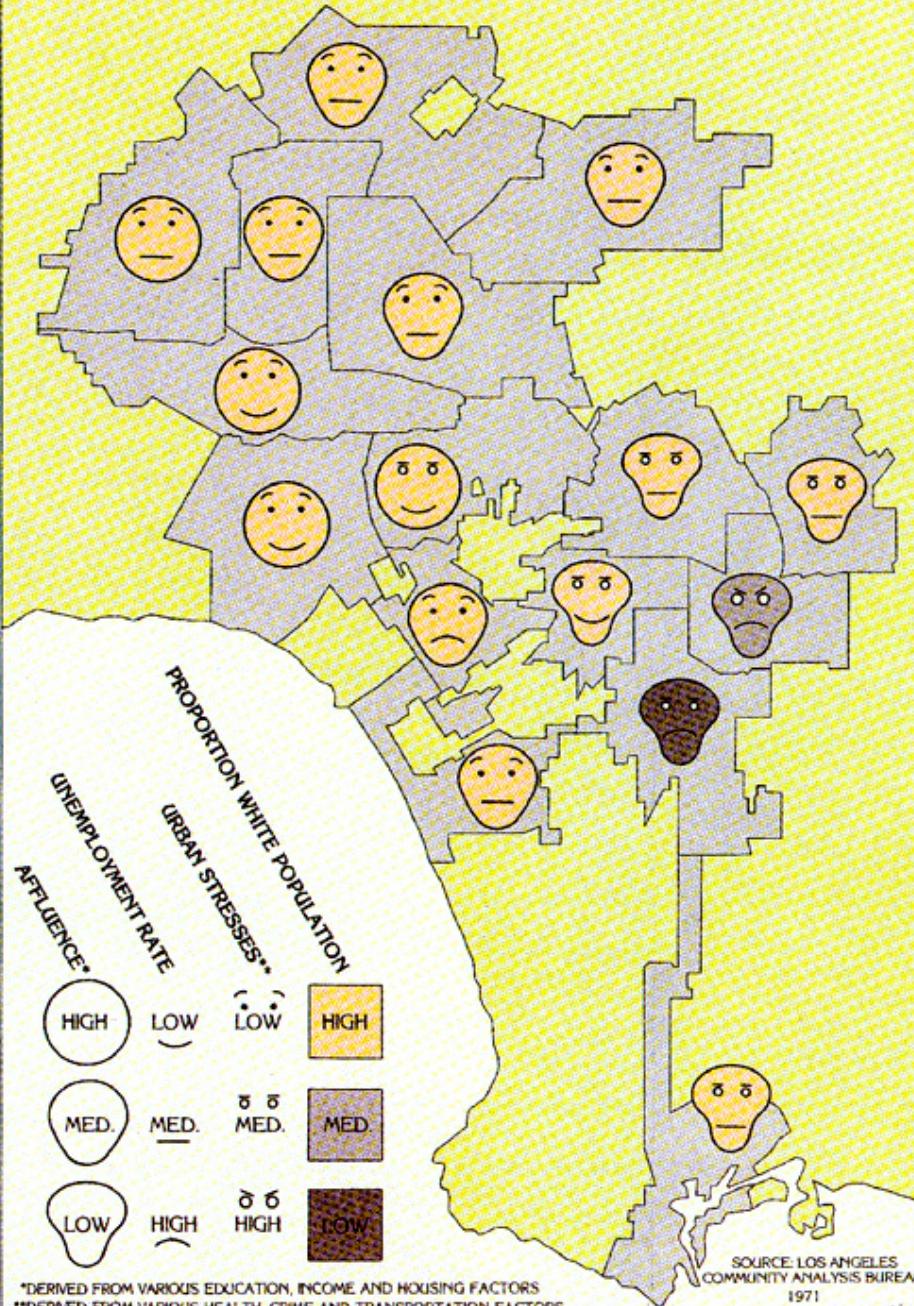
# Multiple Coordinated Views



# Linking Assists to Position



# Life in Los Angeles



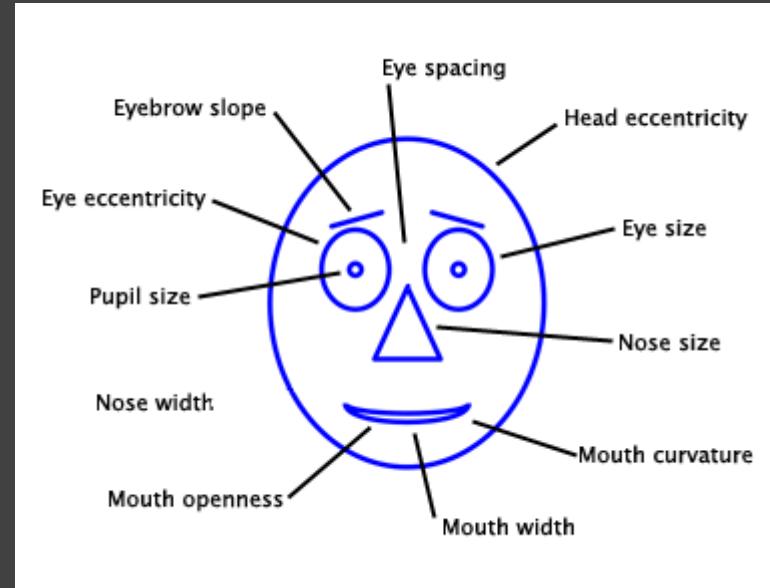
# Chernoff Faces

Observation: We have evolved a sophisticated ability to interpret faces.

Idea: Map data variables to facial features.

Question: Do we process facial features in an uncorrelated way? (i.e., are they *separable*?)

This is just one example of nD “glyphs”



# Visualizing Multiple Dimensions

## Strategies:

Avoid “over-encoding”

Use space and small multiples intelligently

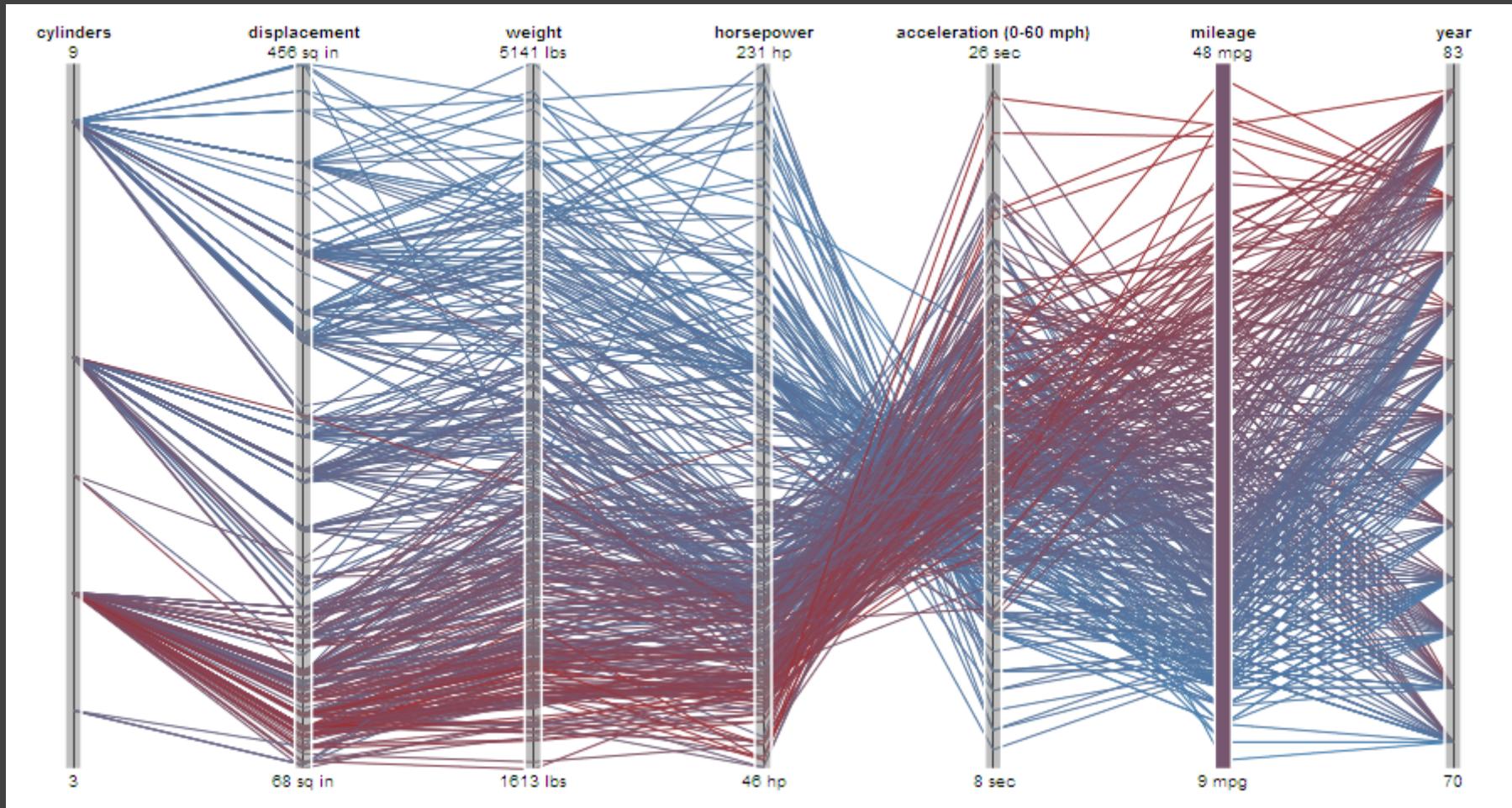
Reduce the problem space

Use interaction to generate *relevant* views

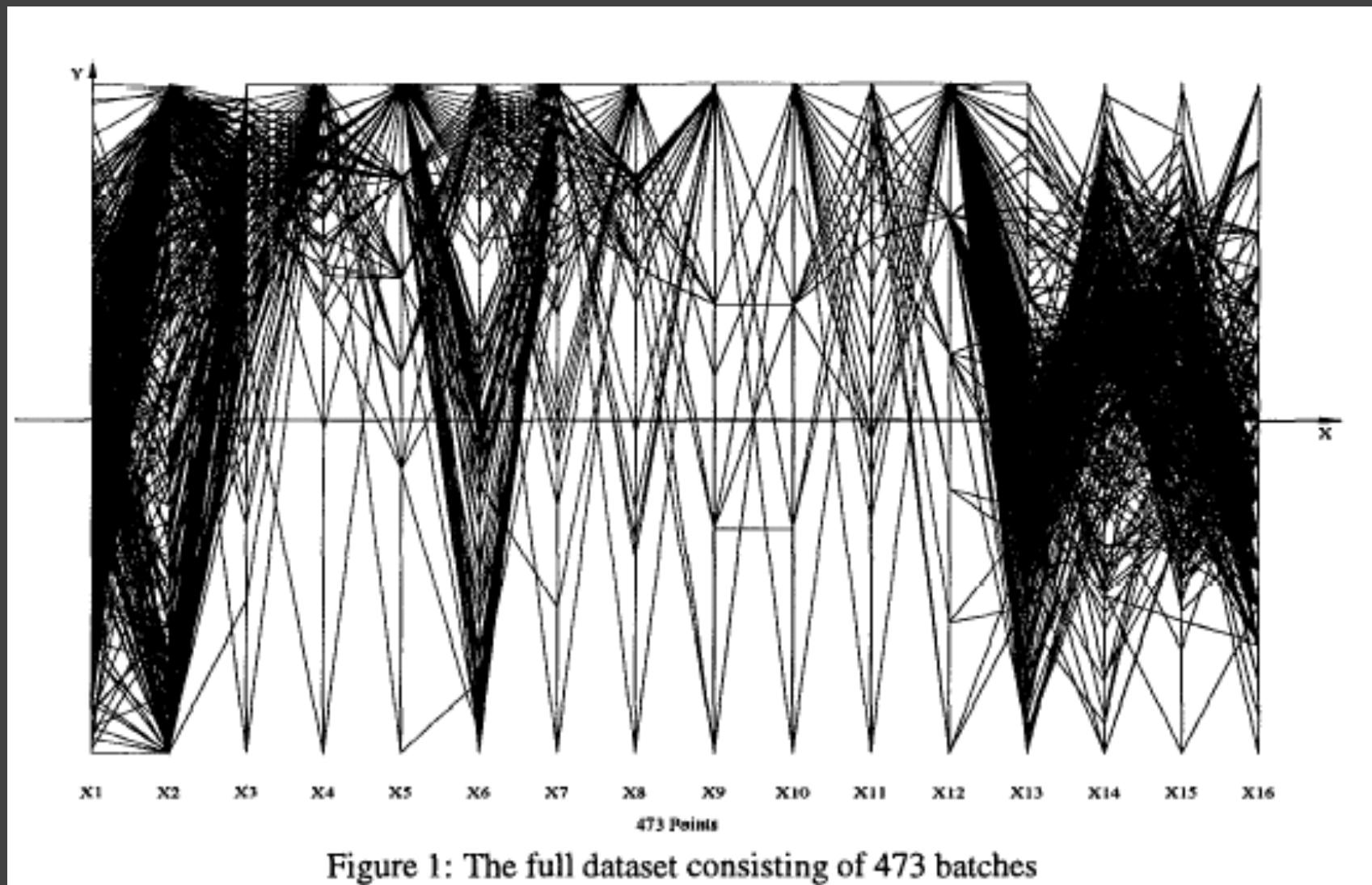
Rarely does a single visualization answer all questions. Instead, the ability to generate appropriate visualizations quickly is key.

# Parallel Coordinates

# Parallel Coordinates [Inselberg]



# Parallel Coordinates [Inselberg]



# The Multidimensional Detective

Production data for 473 batches of a VLSI chip

**16 process parameters**

X1: The yield: % of produced chips that are useful

X2: The quality of the produced chips (speed)

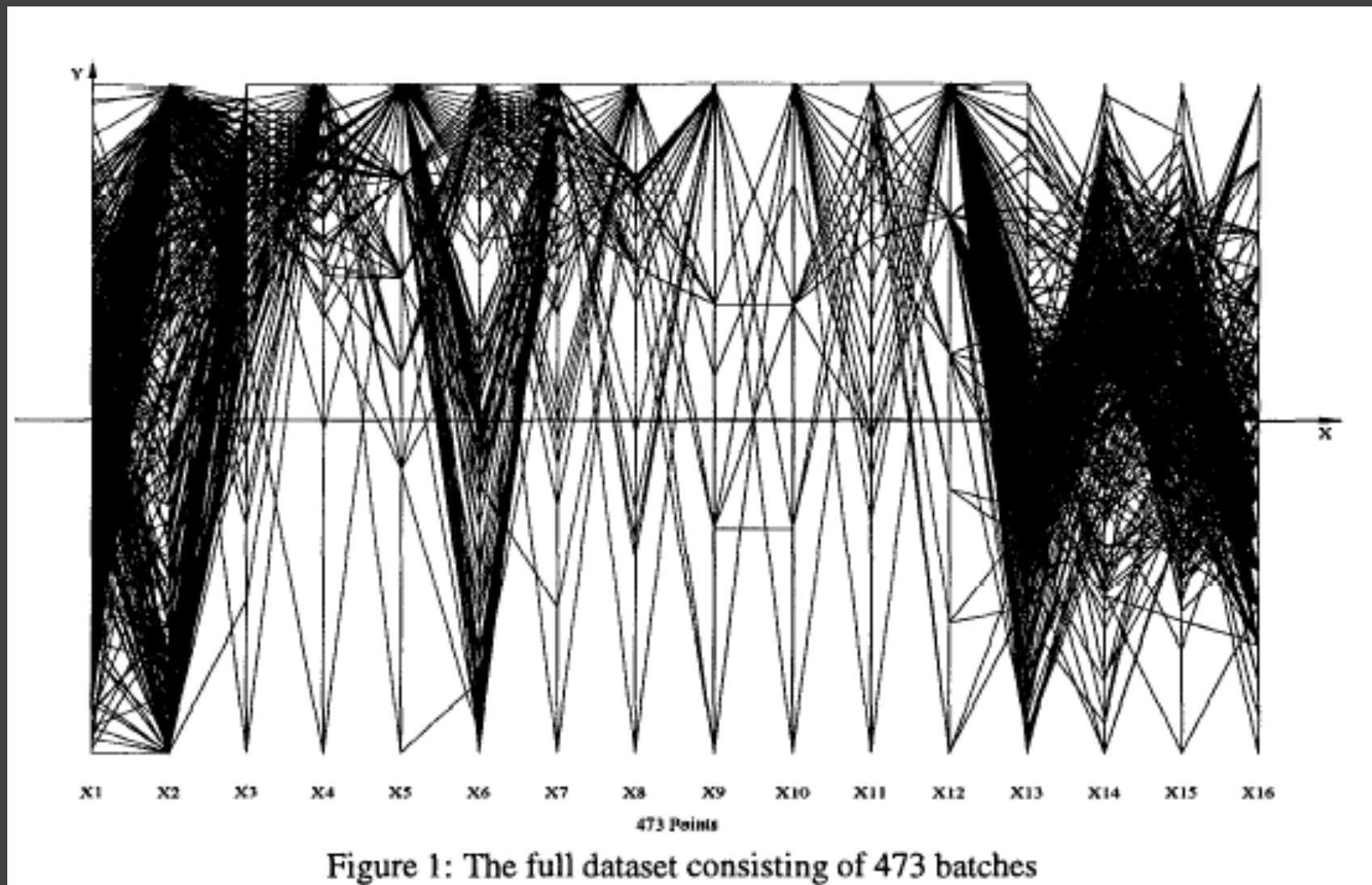
X3-12: 10 types of defects (0 defects shown at top)

X13-16: 4 physical parameters

**Objective:**

Raise the yield (X1) and maintain high quality (X2)

# Parallel Coordinates [Inselberg]



# Inselberg's Principles

1. Do not let the picture scare you.
2. Understand your objectives. Use them to obtain visual cues.
3. Carefully scrutinize the picture.
4. Test your assumptions, especially the "I am really sure of's".
5. You can't be unlucky all the time!

Each line represents a tuple (e.g., VLSI batch)

Filtered below for high values of  $X_1$  and  $X_2$

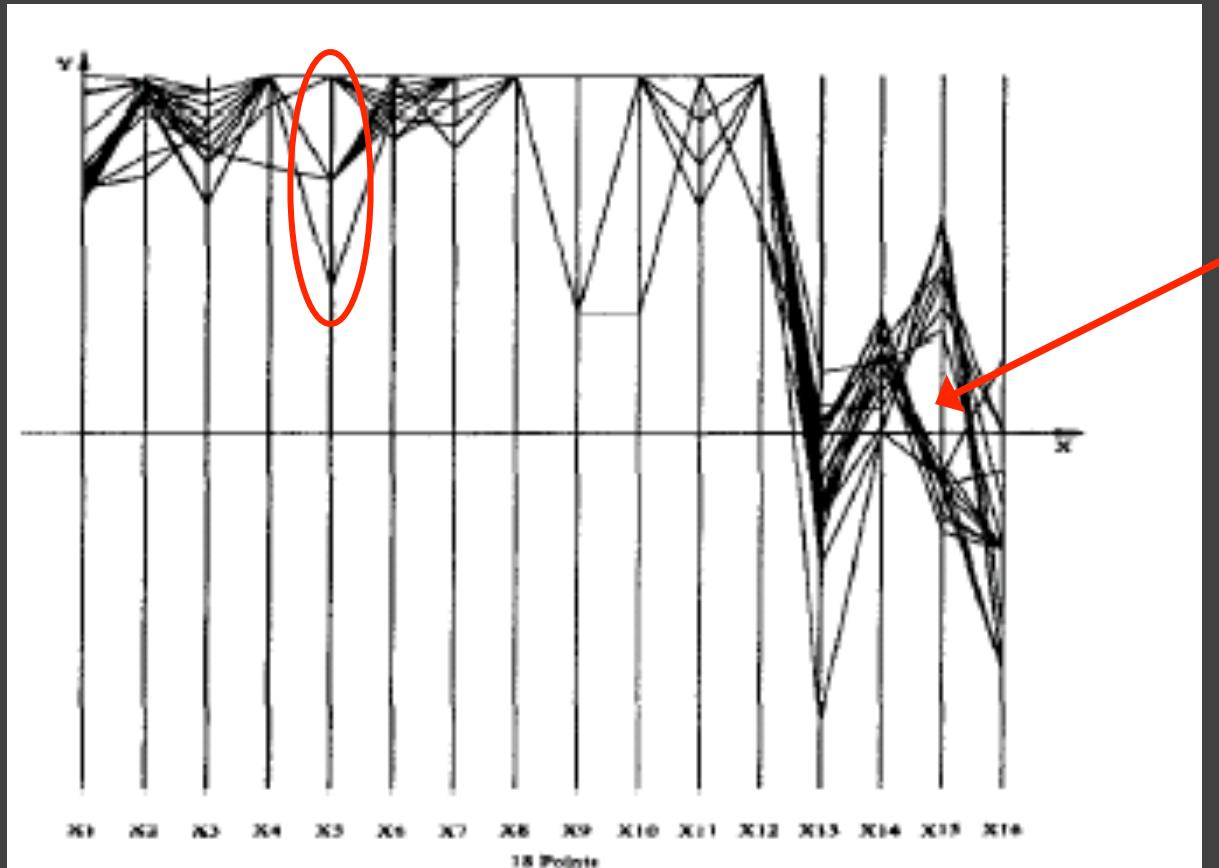
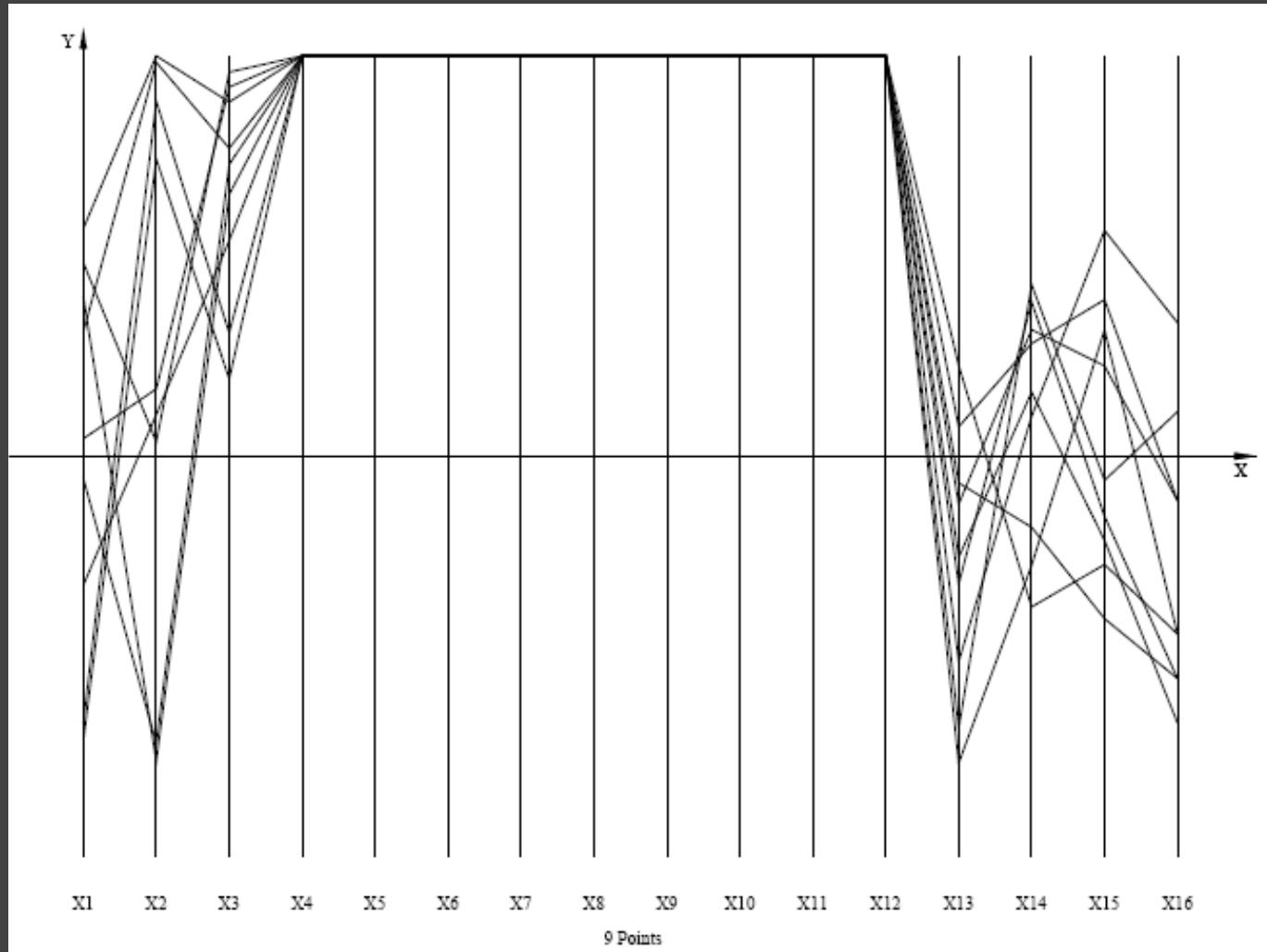


Figure 2: The batches high in Yield,  $X_1$ , and Quality,  $X_2$ .

Look for batches with *nearly* zero defects (9/10)

Most of these have low yields -> defects OK.



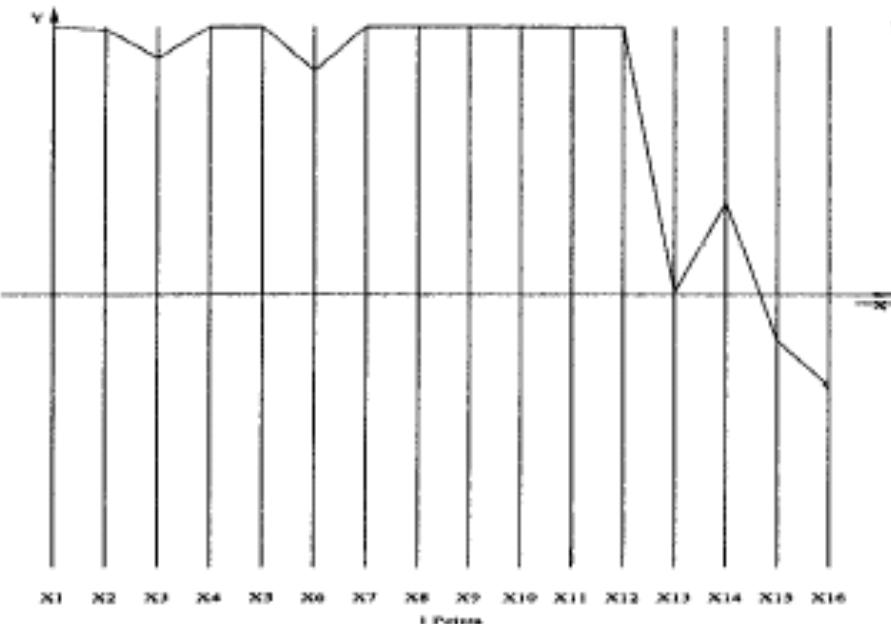


Figure 5: The best batch. Highest in Yield,  $X_1$ , and very high in Quality,  $X_2$ .

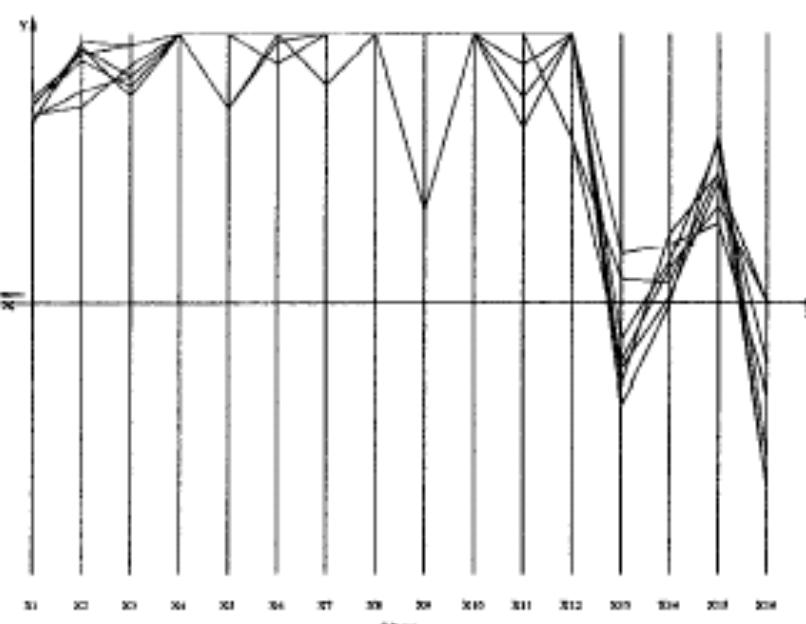
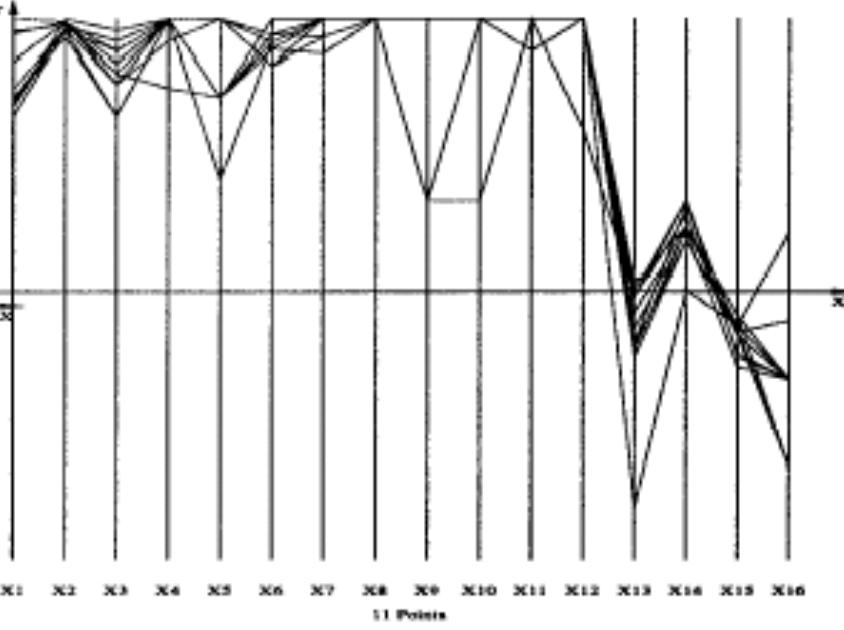
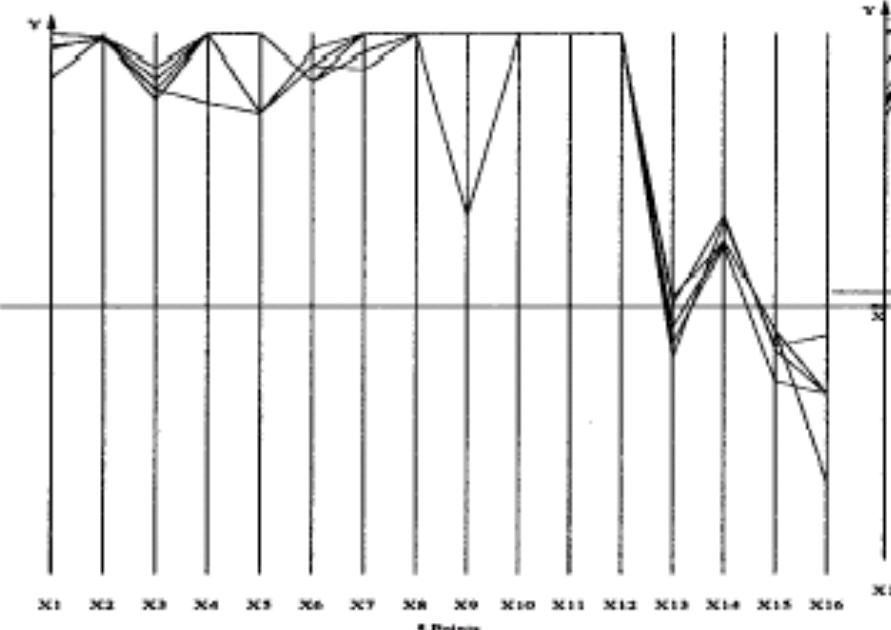
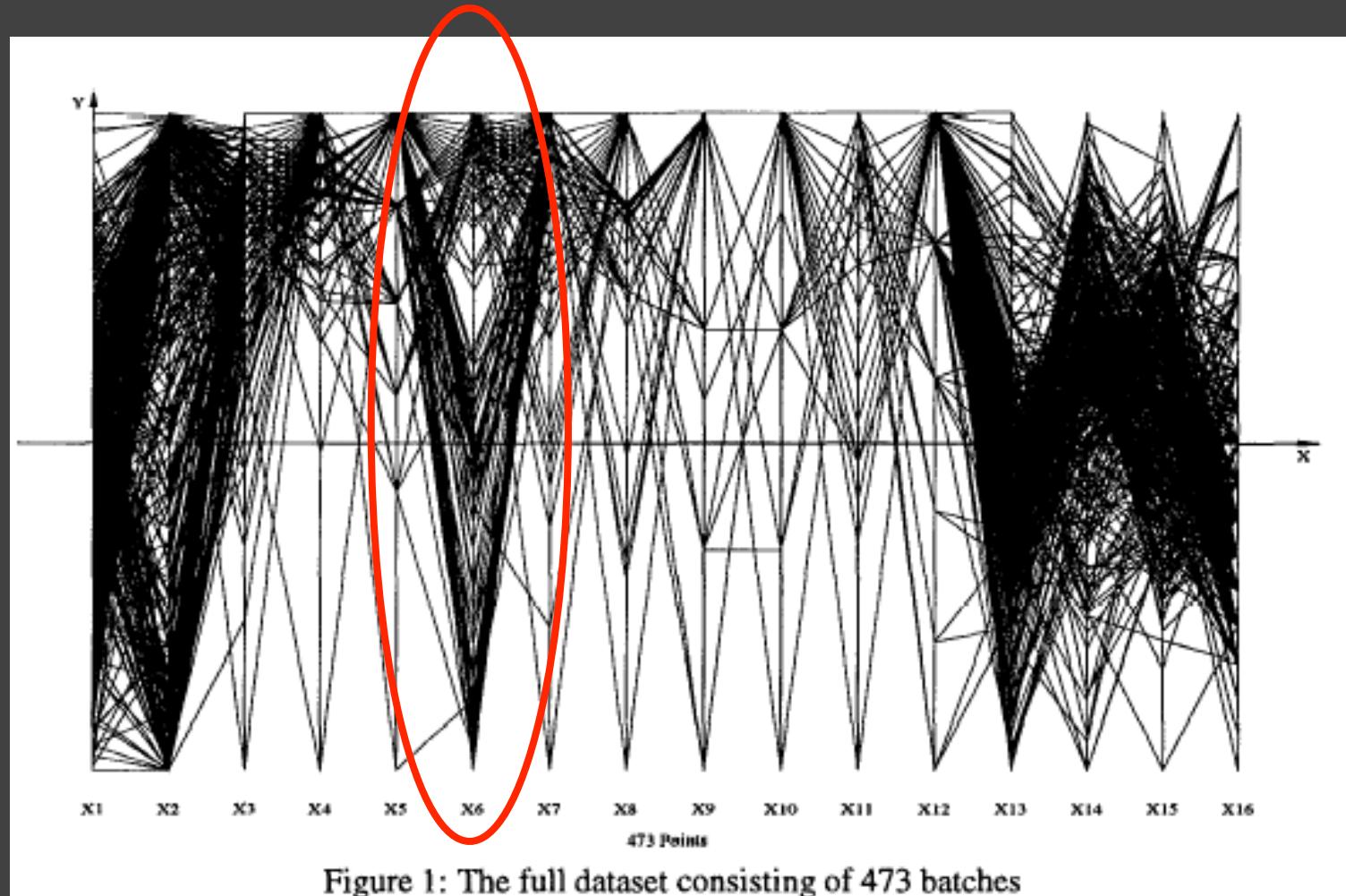


Figure 7: Upper range of split in  $X_{15}$

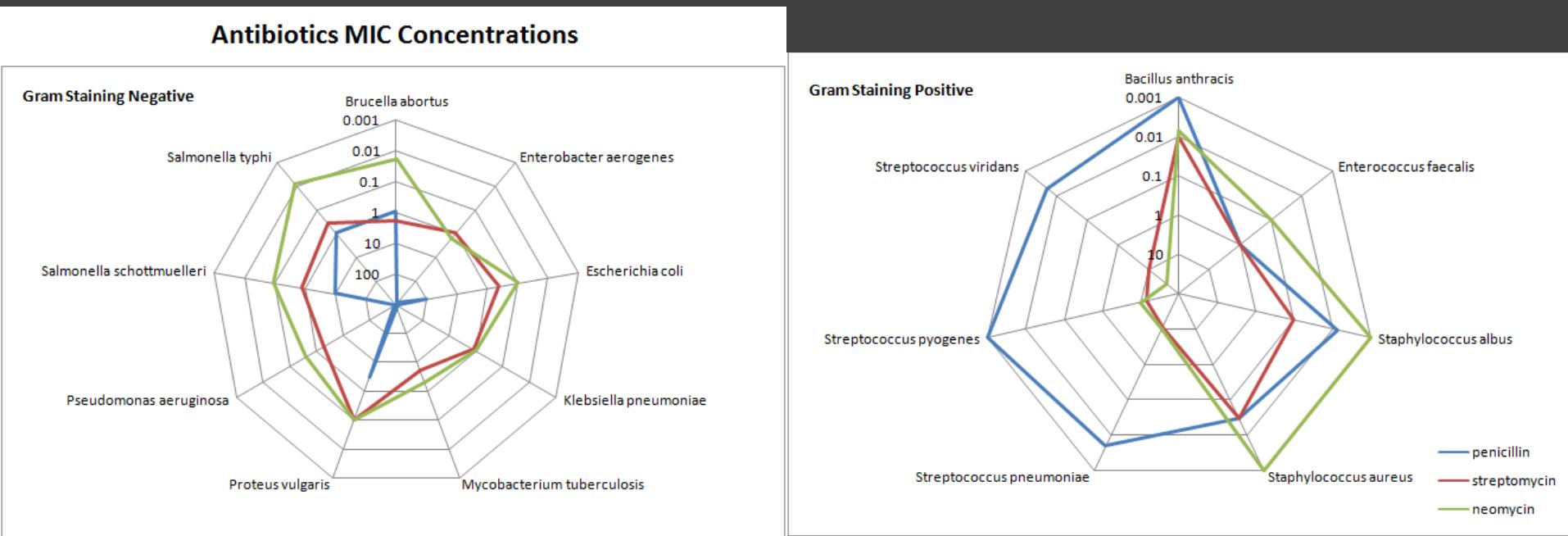


Notice that X6 behaves differently.

Allow 2 defects, including X6 -> best batches



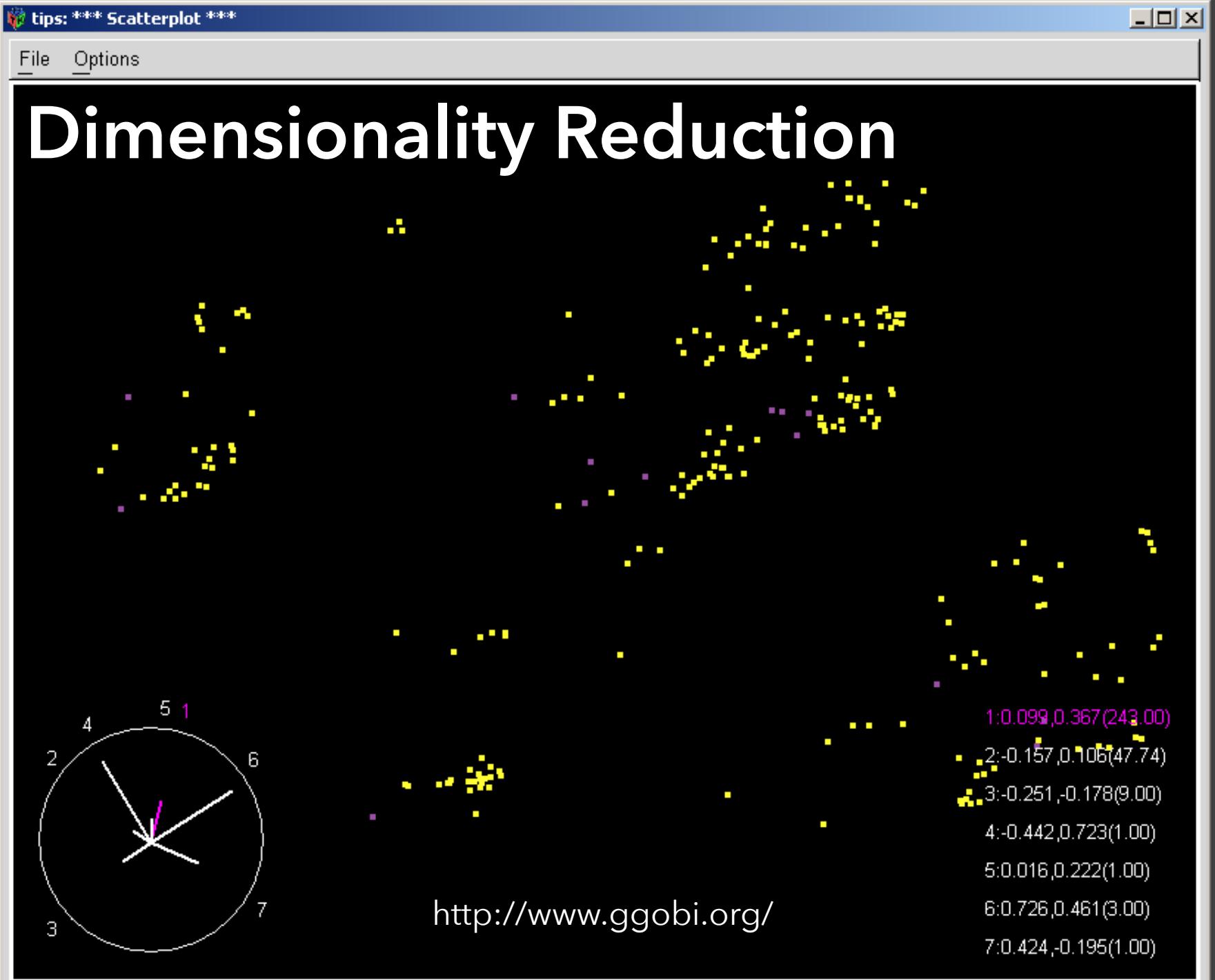
# Radar Plot / Star Graph



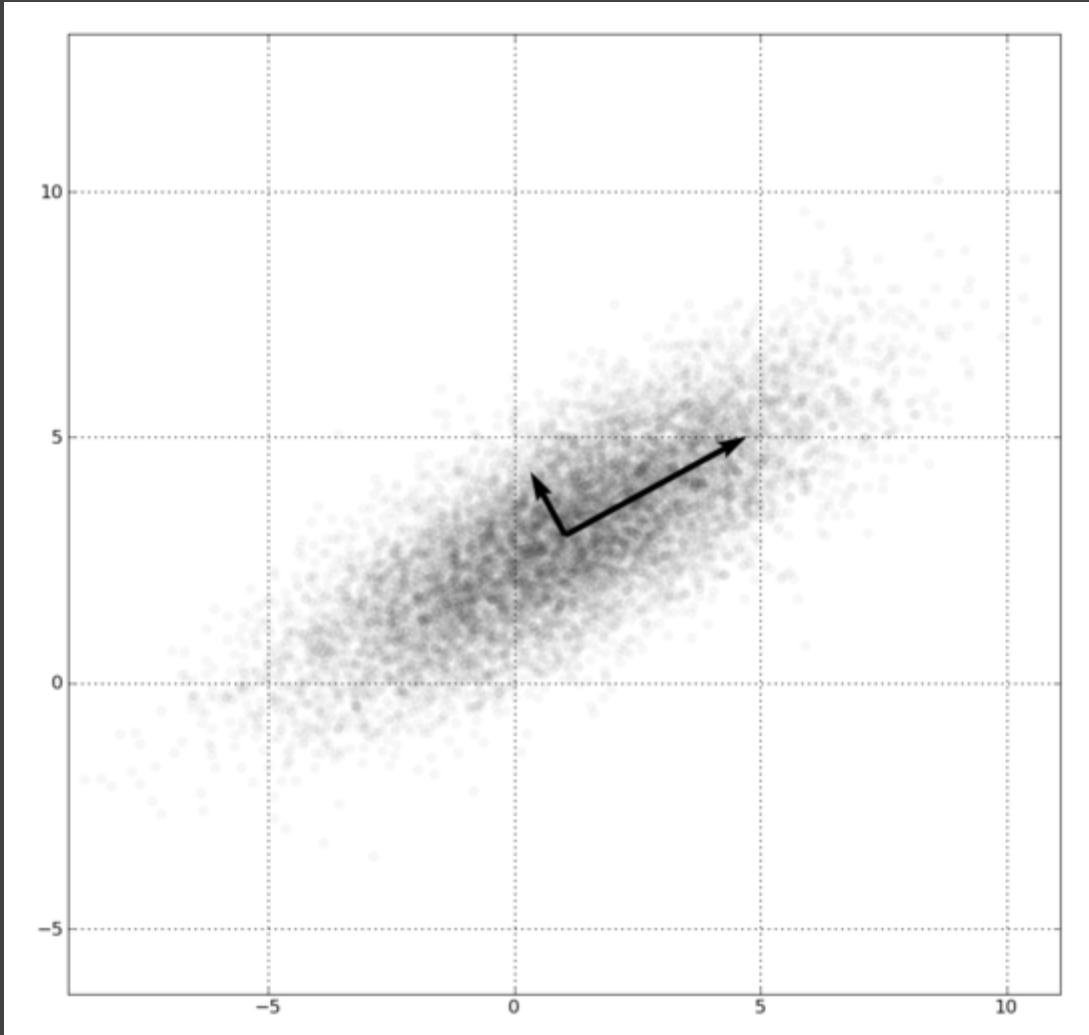
“Parallel” dimensions in polar coordinate space

Best if same units apply to each axis

# Dimensionality Reduction

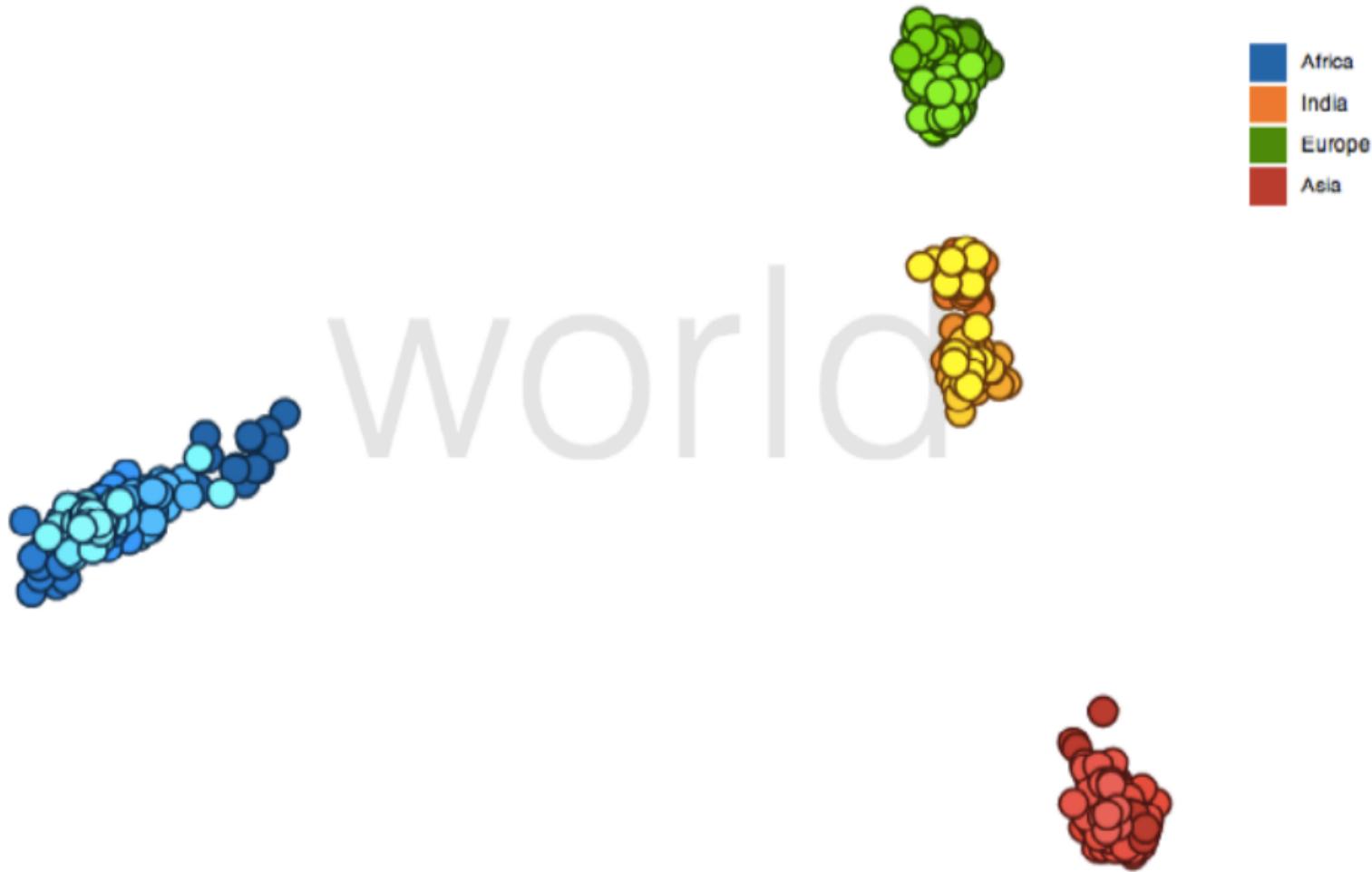


# Principal Components Analysis



1. Mean-center the data.
2. Find  $\perp$  basis vectors that maximize the data variance.
3. Plot the data using the top vectors.

# PCA of Genomes [Demiralp et al. '13]



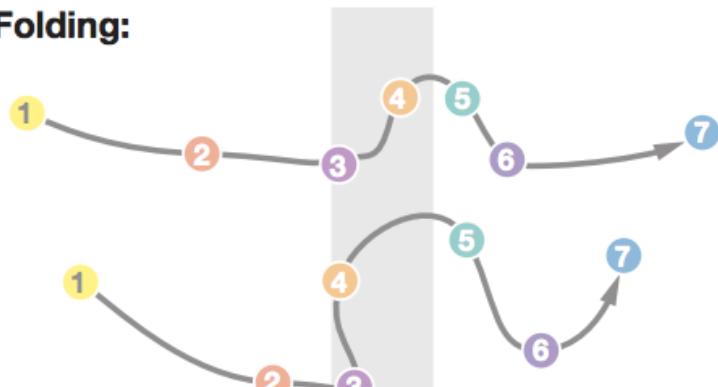
# Time Curves [Bach et al. '16]

## Timeline:



Circles are data cases with a time stamp.  
Similar colors indicate similar data cases.

## Folding:

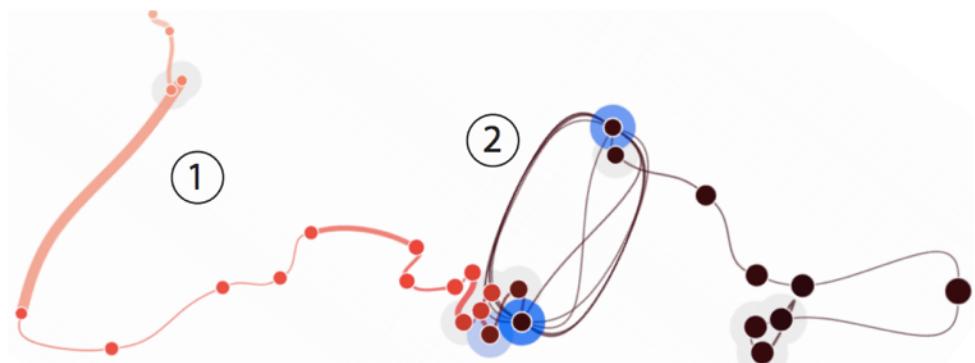


## Time curve:

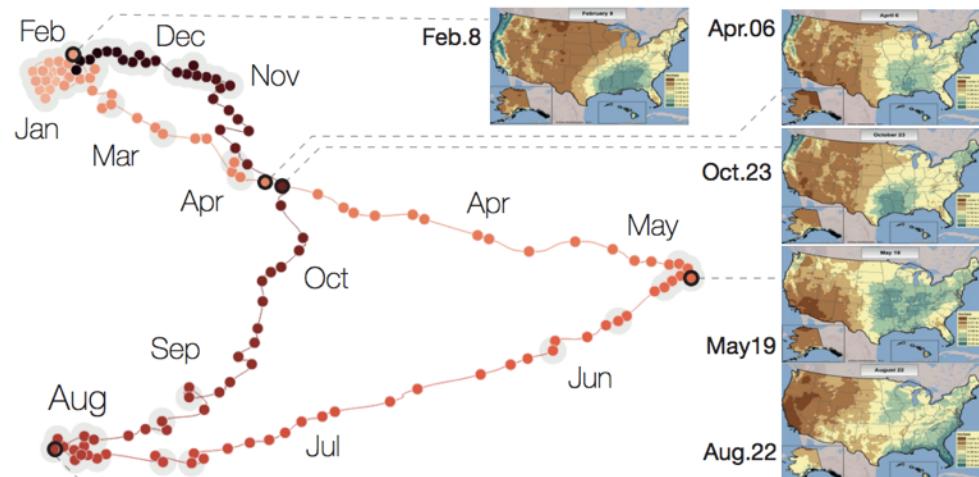


The temporal ordering of data cases is preserved.  
Spatial proximity now indicates similarity.

(a) Folding time



Wikipedia "Chocolate" Article



U.S. Precipitation over 1 Year

# Many Reduction Techniques!

Principal Components Analysis (PCA)

Multidimensional Scaling (MDS)

Locally Linear Embedding (LLE)

t-Dist. Stochastic Neighbor Embedding (t-SNE)

Isomap

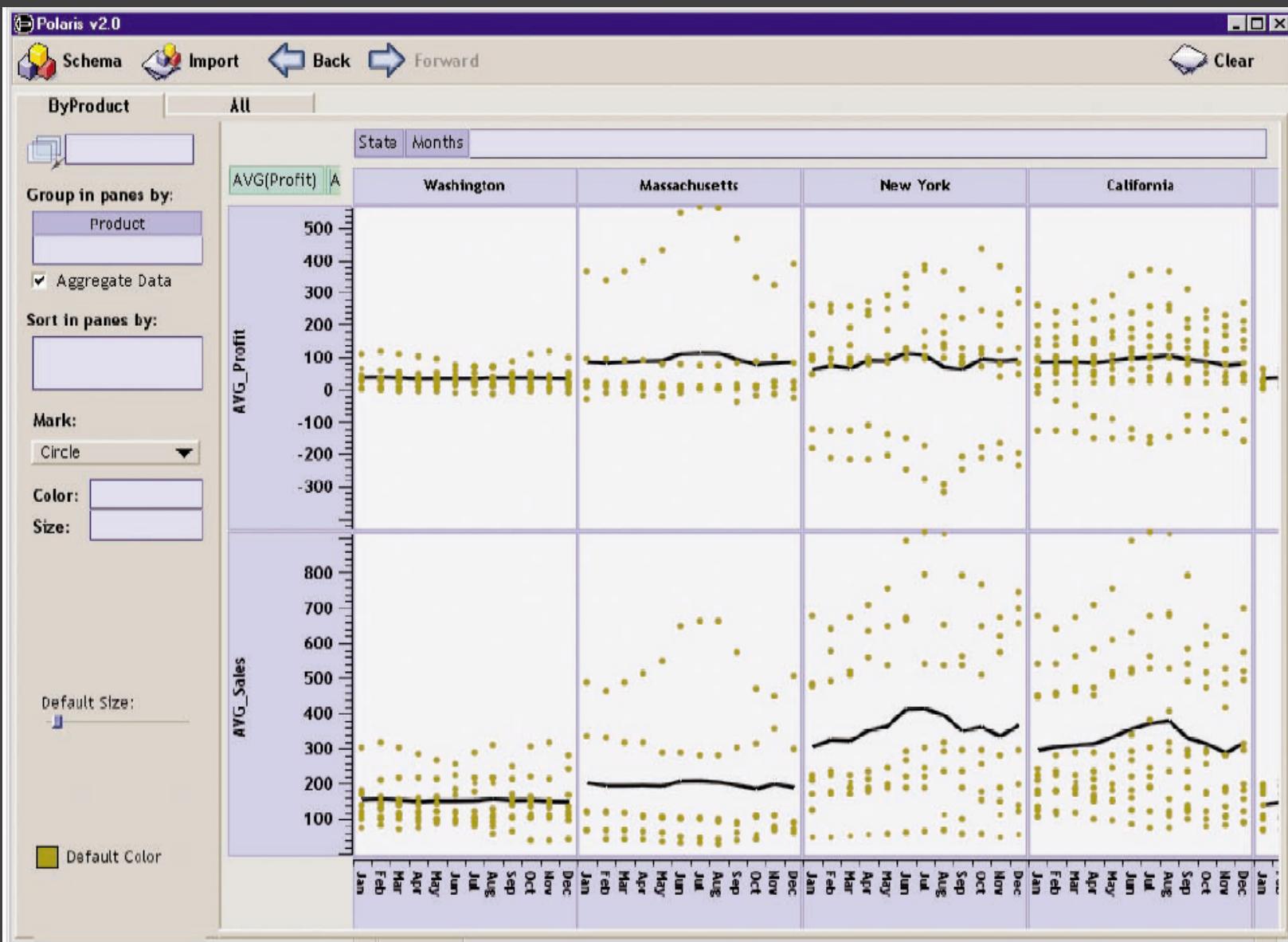
Auto-Encoder Neural Networks

Topological methods

...

# Tableau / Polaris

# Polaris [Stolte et al.]



# Tableau

**Encodings**

**Data Display**

**Data Model**

The screenshot shows the Tableau interface with a bar chart on the right and various encoding controls on the left.

**Schema:** congress.csv Connection (highlighted with a red circle)

**Dimensions:**

- # Party
- Abc Candidate
- Abc Candidate ID
- Abc General Elec Status
- Abc Incumbent/Challenger/Open-Seat
- Abc Party Desig
- Abc Primary Elec Status
- Abc Runoff Elec Status
- Abc Spec Elec Status
- Abc State Code
- # Year
- Abc Measure Names

**Measures:**

- # District
- # General Elec Pct
- # Total Receipts
- # Measure Values

**Groups:**

**Columns:** Party, Year

**Rows:** SUM(Total Receipts)

**Level of Detail:** (empty)

**Mark:** Automatic

**Text:** (empty)

**Color:** Party

**Size:** (empty)

**Legend:**

- 1 (Blue)
- 2 (Orange)
- 3 (Green)

**Size:** (empty slider)

**Sheet 1 /**

Year	Party	SUM(Total Receipts)
1996	1	~350M
1998	1	~360M
2000	1	~530M
2002	1	~480M
1996	2	~430M
1998	2	~410M
2000	2	~520M
2002	2	~490M
1996	3	~10M
1998	3	~10M
2000	3	~15M
2002	3	~10M

# Tableau Demo

The dataset:

Federal Elections Commission Receipts

Every Congressional Candidate from 1996 to 2002

4 Election Cycles

9216 Candidacies

# Dataset Schema

Year (Qi)

Candidate Code (N)

Candidate Name (N)

Incumbent / Challenger / Open-Seat (N)

Party Code (N) [1=Dem,2=Rep,3=Other]

Party Name (N)

Total Receipts (Qr)

State (N)

District (N)

This is a subset of the larger data set available from the FEC.

# Hypotheses?

What might we learn from this data?

# Hypotheses?

What might we learn from this data?

Correlation between receipts and winners?

Do receipts increase over time?

Which states spend the most?

Which party spends the most?

Margin of victory vs. amount spent?

Amount spent between competitors?

# Tableau Demo

# Tableau/Polaris Approach

Insight: can simultaneously specify both database queries and visualization

Choose data, then visualization, not vice versa

Use smart defaults for visual encodings

More recently: automate visualization design

# Specifying Table Configurations

**Operands are the database fields**

Each operand interpreted as a set {...}

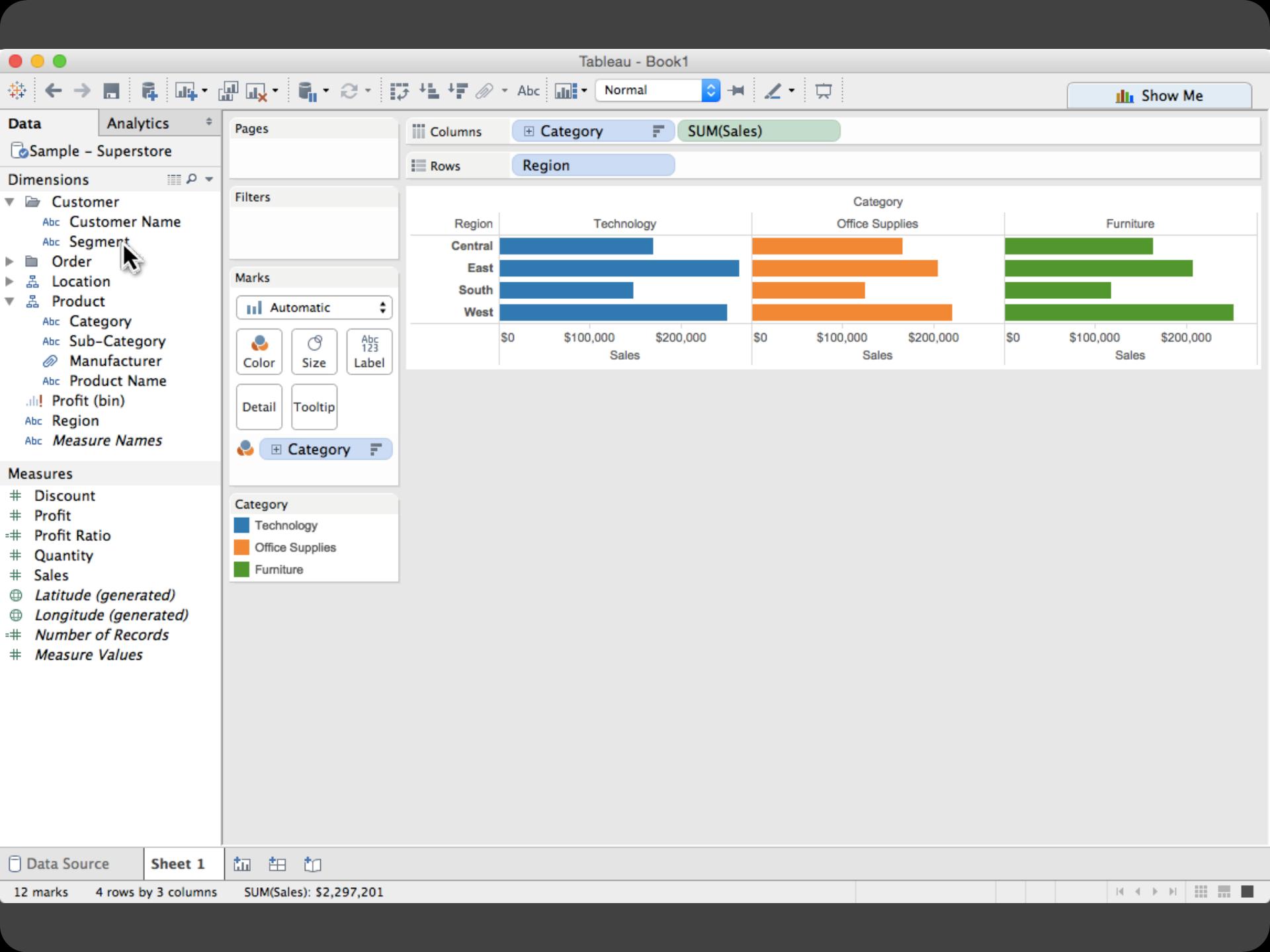
Quantitative and Ordinal fields treated differently

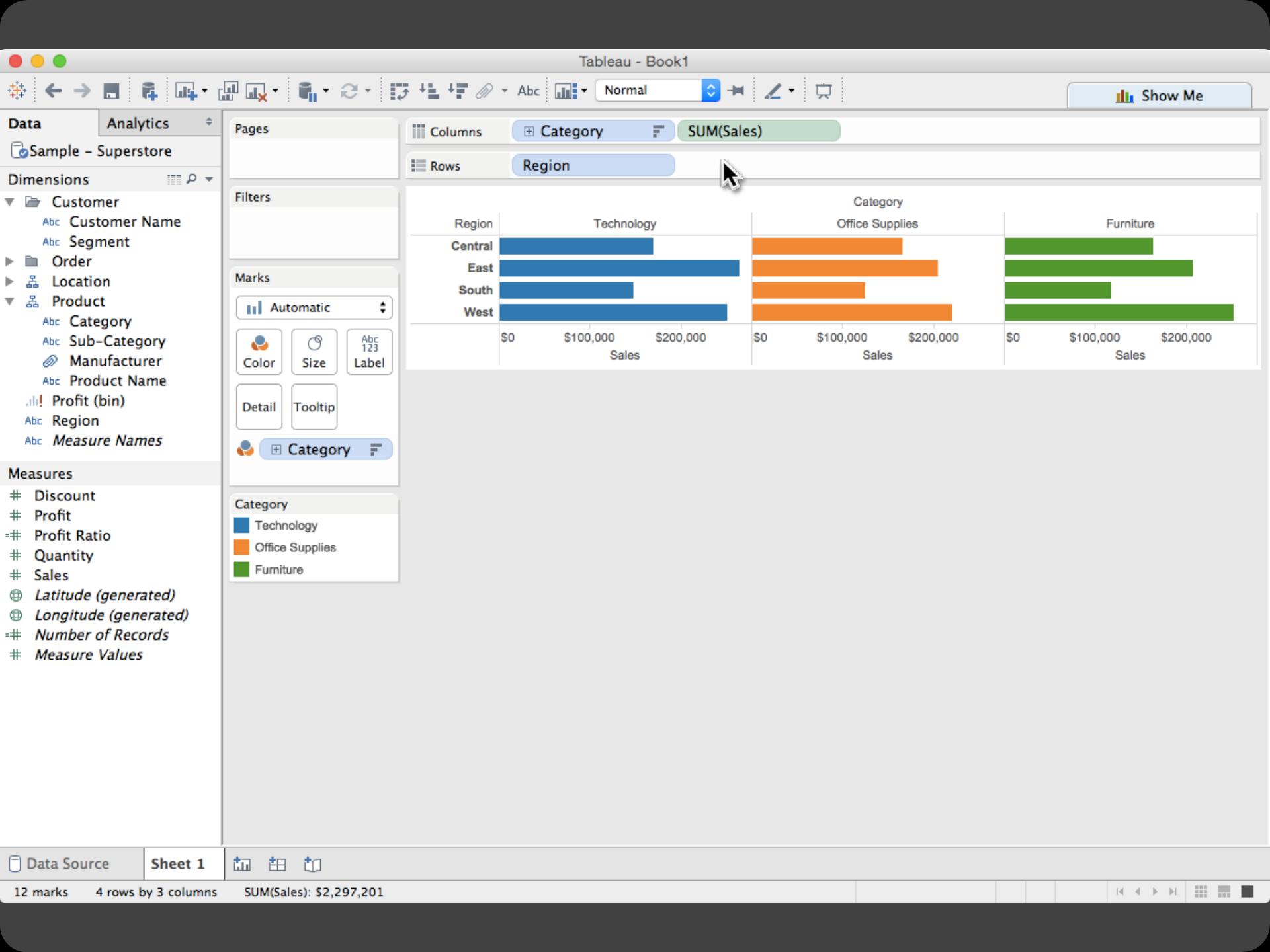
**Three operators:**

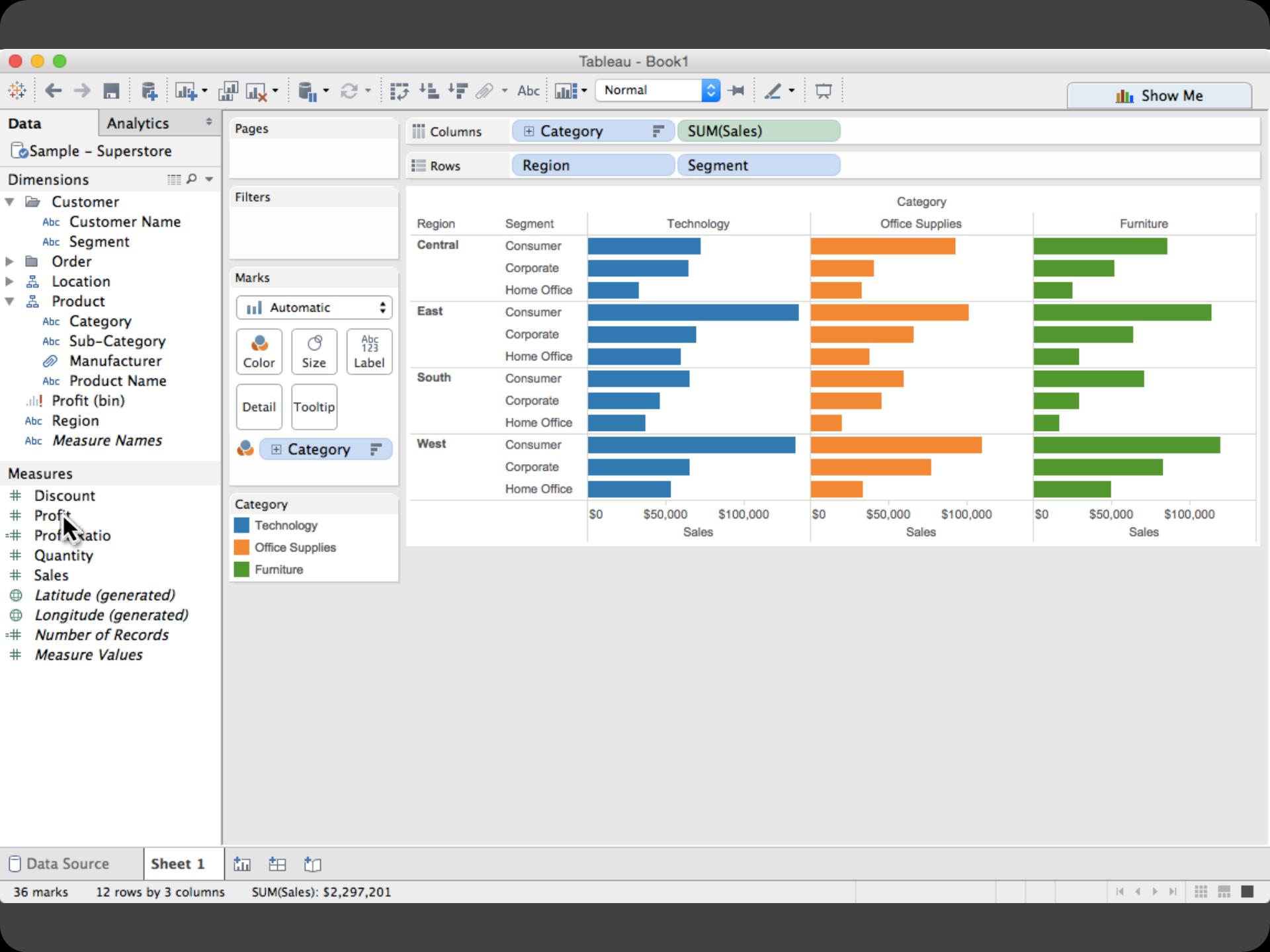
concatenation (+)

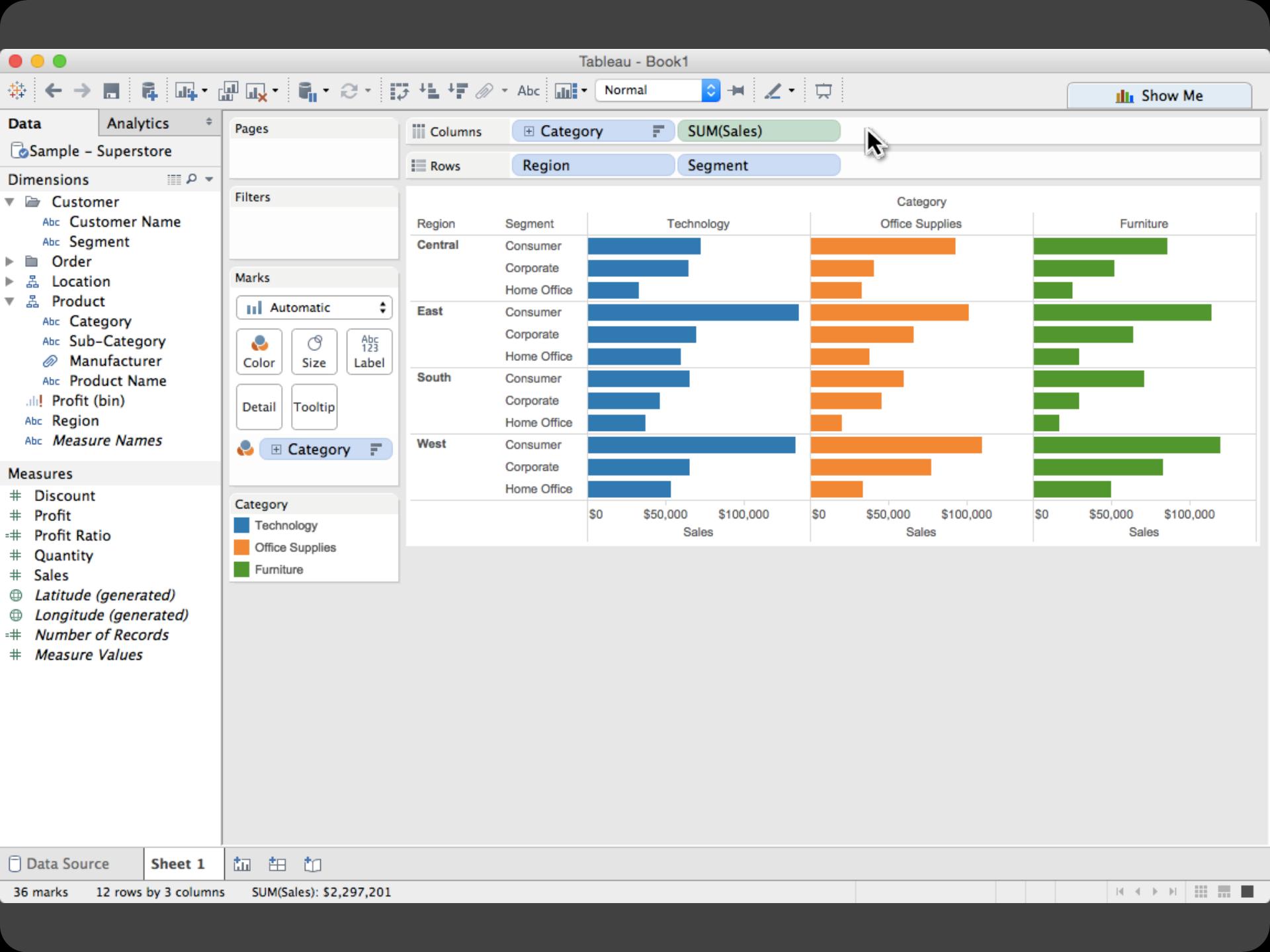
cross product (x)

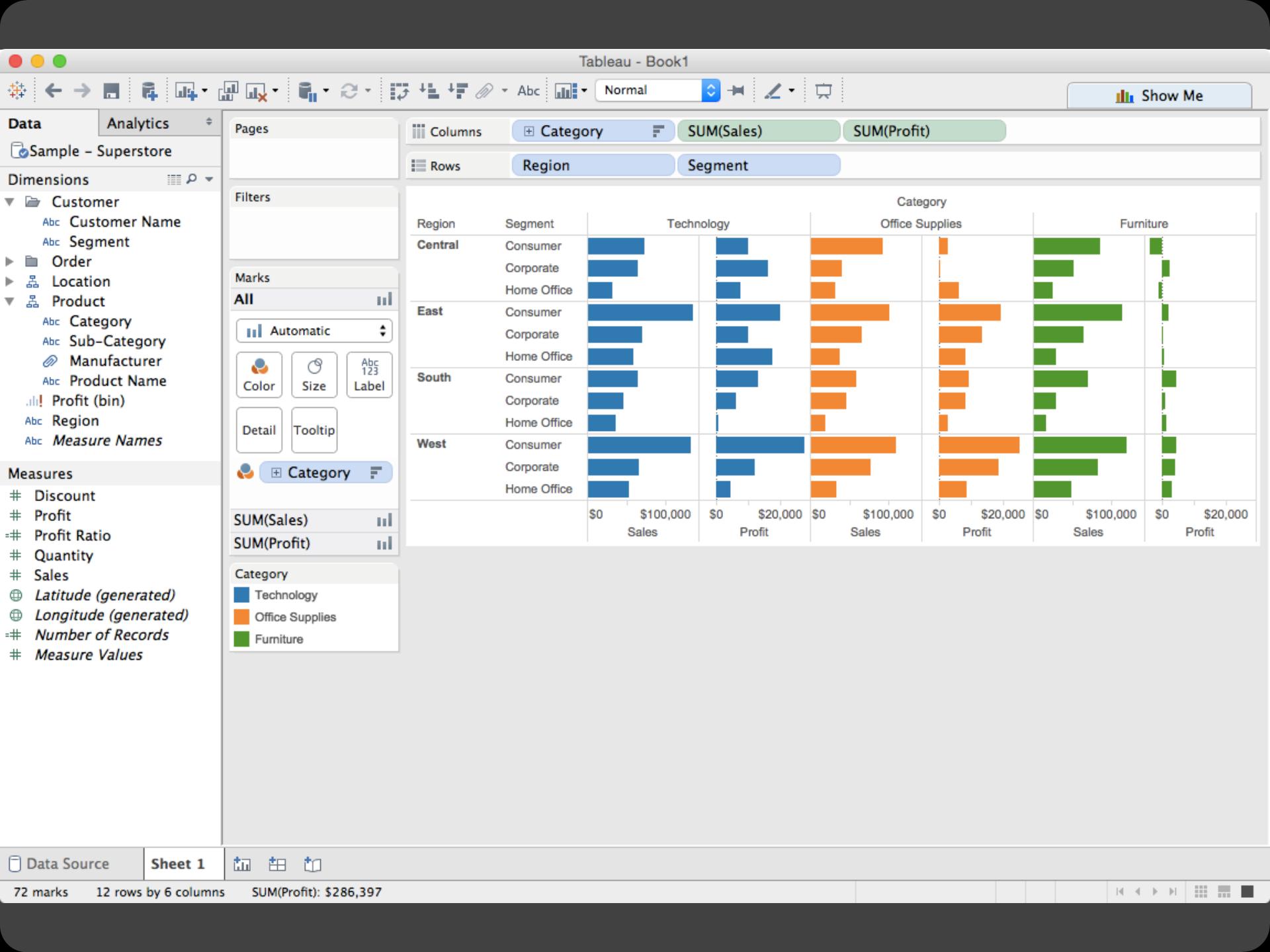
nest (/)

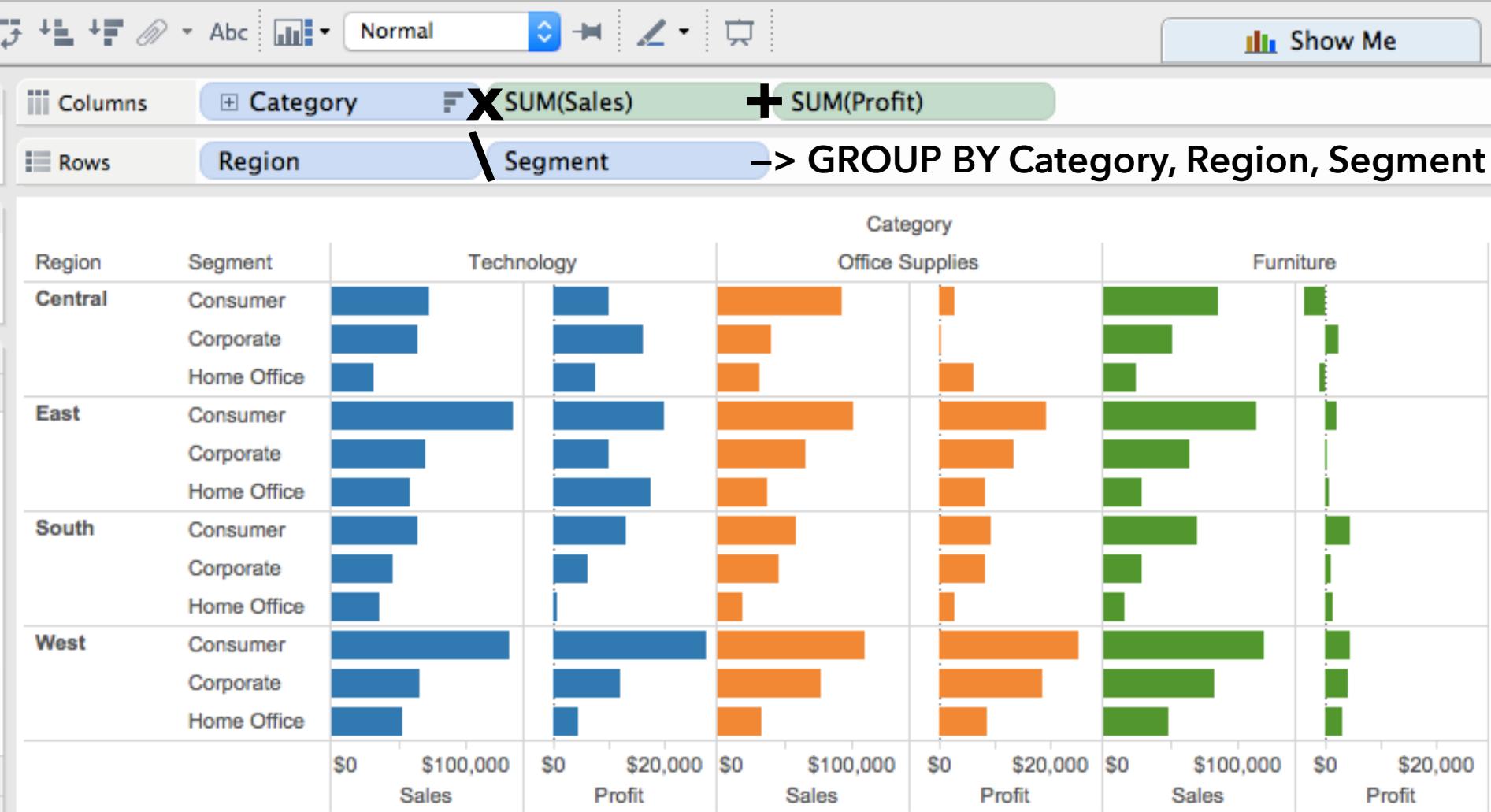












# Table Algebra: Operands

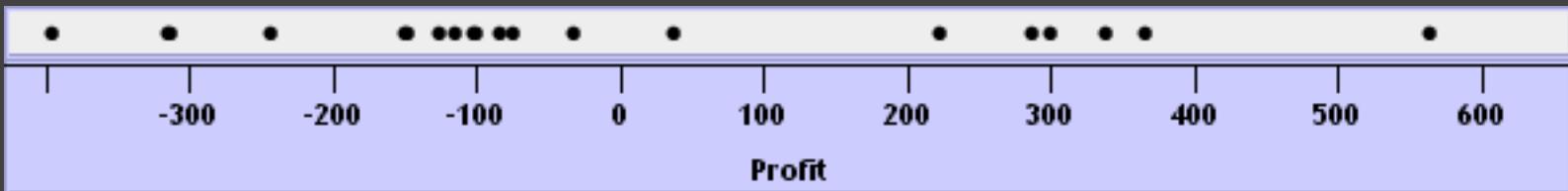
**Ordinal fields:** interpret domain as a set that partitions table into rows and columns.

Quarter = {(Qtr1),(Qtr2),(Qtr3),(Qtr4)} ->

Qtr1	Qtr2	Qtr3	Qtr4
95892	101760	105282	98225

**Quantitative fields:** treat domain as single element set and encode spatially as axes.

Profit = {(Profit[-410,650])} ->



# Concatenation (+) Operator

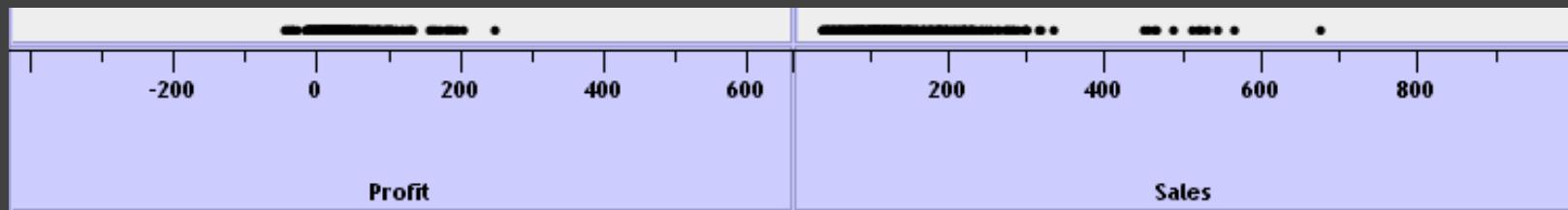
Ordered union of set interpretations

Quarter + Product Type

$$\begin{aligned} &= \{(Qtr1), (Qtr2), (Qtr3), (Qtr4)\} + \{(Coffee), (Espresso)\} \\ &= \{(Qtr1), (Qtr2), (Qtr3), (Qtr4), (Coffee), (Espresso)\} \end{aligned}$$

Qtr1	Qtr2	Qtr3	Qtr4	Coffee	Espresso
48	59	57	53	151	21

Profit + Sales =  $\{(Profit[-310, 620]), (Sales[0, 1000])\}$



# Cross (x) Operator

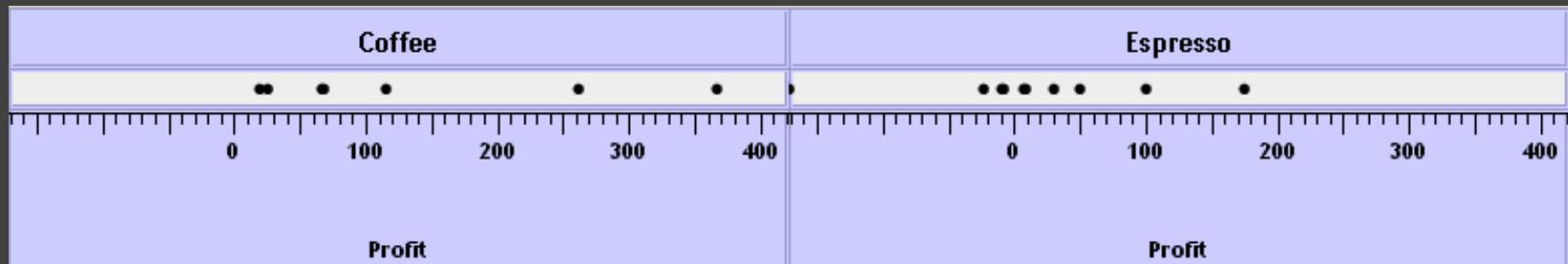
## Cross-product of set interpretations

Quarter x Product Type =

$\{(Qtr1, \text{Coffee}), (Qtr1, \text{Tea}), (Qtr2, \text{Coffee}), (Qtr2, \text{Tea}), (Qtr3, \text{Coffee}), (Qtr3, \text{Tea}), (Qtr4, \text{Coffee}), (Qtr4, \text{Tea})\}$

Qtr1		Qtr2		Qtr3		Qtr4	
Coffee	Espresso	Coffee	Espresso	Coffee	Espresso	Coffee	Espresso
131	19	160	20	178	12	134	33

Product Type x Profit =



# Nest (/) Operator

**Cross-product filtered by existing records**

Quarter x Month ->

creates twelve entries for each quarter. i.e.,  
(Qtr1, December)

Quarter / Month ->

creates three entries per quarter based on  
tuples in database (not semantics)

# Table Algebra

The operators (+, x, /) and operands (O, Q) provide an *algebra* for tabular visualization.

Algebraic statements are then mapped to:

**Visualizations** - trellis plot partitions, visual encodings

**Queries** - selection, projection, group-by aggregation

In Tableau, users make statements via drag-and-drop

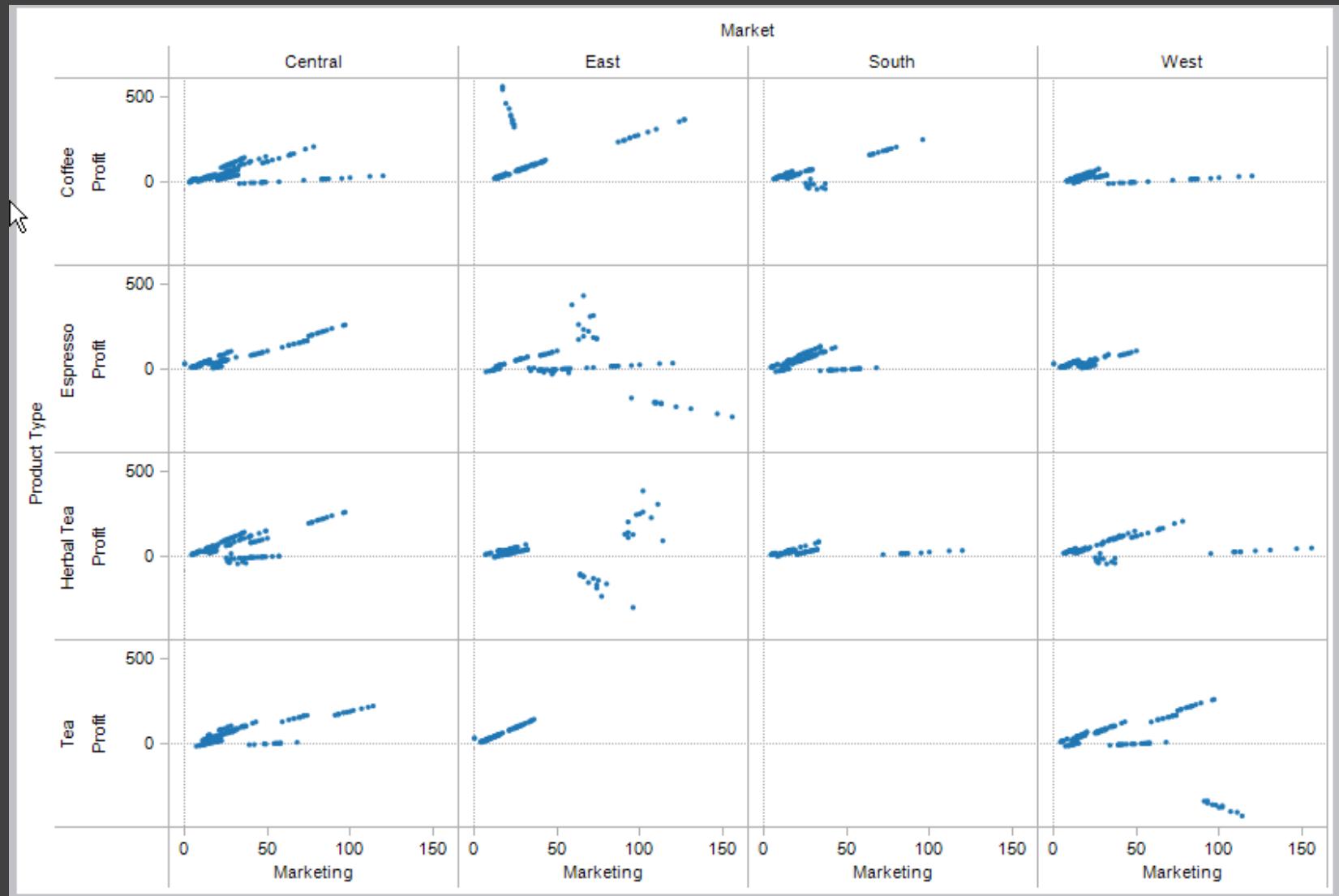
Note that this specifies operands *NOT* operators!

Operators are inferred by data type (O, Q)

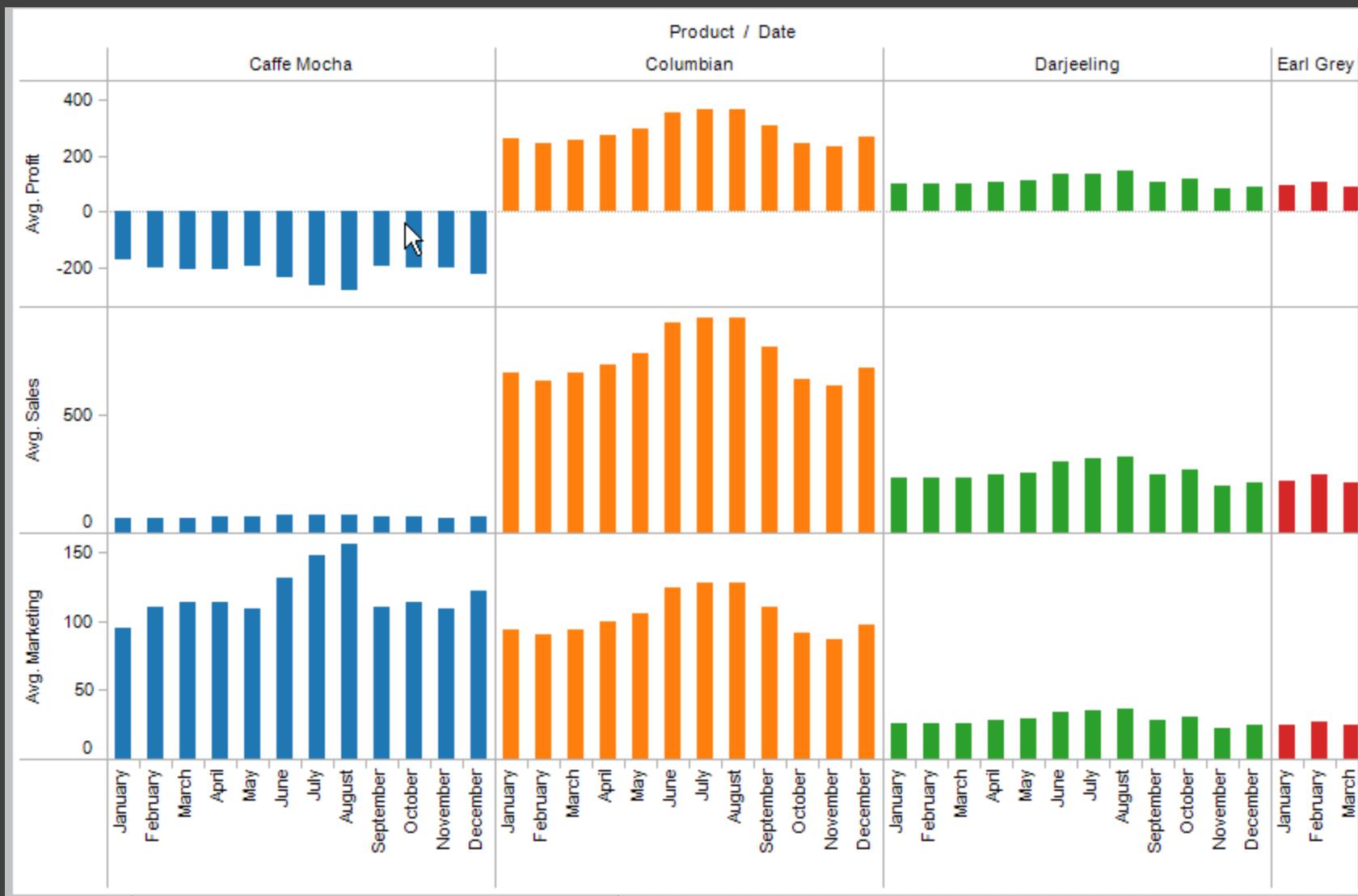
# Ordinal-Ordinal

State	Product Type			
	Coffee	Espresso	Herbal Tea	Tea
Colorado	●	●	●	●
Connecticut	●	●	●	●
Florida	●	●	●	●
Illinois	●	●	●	●
Iowa	●	●	●	●
Louisiana	●	●	●	
Massachusetts	●	●	●	●
Missouri	●	●	●	●
Nevada	●	●	●	●
New Hampshire	●	●	●	●
New Mexico	●	●	●	●
New York	●	●	●	●
Ohio	●	●	●	●
Oklahoma	●	●	●	
Oregon	●	●	●	●
Texas	●	●	●	
Utah	●	●	●	●
Washington	●	●	●	●
Wisconsin	●	●	●	●

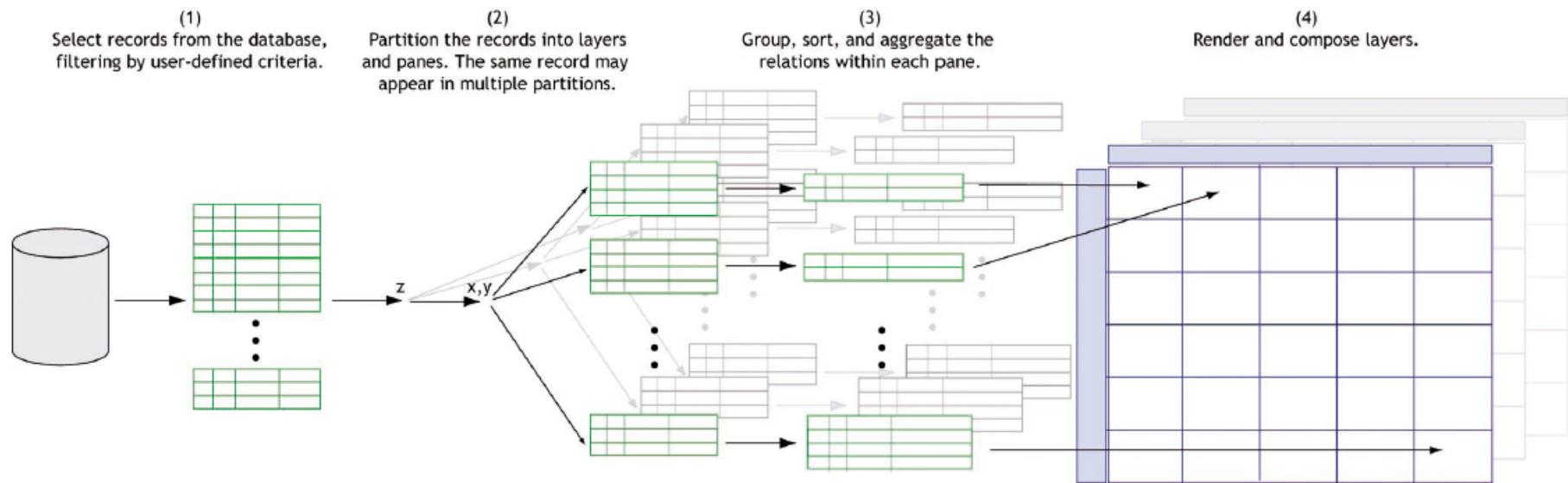
# Quantitative-Quantitative



# Ordinal-Quantitative



# Querying the Database



# Visualizing Multiple Dimensions

## Strategies:

Avoid “over-encoding”

Use space and small multiples intelligently

Reduce the problem space

Use interaction to generate *relevant* views

Rarely does a single visualization answer all questions. Instead, the ability to generate appropriate visualizations quickly is key.