Advanced Machine Learning : from Theory to
Practice
Lecture 7
Graphs and Machine Learning II - Semi-supervised
learning

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Fall 2017

Introduction to Semi-supervised learning Outline

- 1 Introduction to Semi-supervised learning
- Self-training approaches
- Margin-based approaches
- 4 Graph-based approaches
- 5 Semi-supervised Deep learning
- 6 Conclusion and references

Introduction to Semi-supervised learning Learning from labeled and unlabeled data

Why Semi-supervised learning?

- Labels are expensive
- Benefit from the availability of huge sets of unlabeled data
- Unlabeled data inform us about the probability distribution of the data p(x)
- Can we use it? does it improve the performance of the resulting regressors/classifiers?

Applications

- image search, (Fergus et al., 2009)
- genomics (Shi and Zhang,2011)
- natural language parsing (Liang, 2005)
- speech analysis (Liu and Kirchhoff, 2013)

Goal

- Labeled data : $S_{\ell} = \{(x_1, y_1), \dots, (x_{\ell}, y_{\ell})\}$, it Assumption : i.i.d. data drawn from the joint probability distribution P(X,Y)
- Unlabeled data : $\mathcal{X}_u = \{x_{\ell+1}, \dots, x_{\ell+u}\}, \underline{n = \ell + u}$: available during training! Assumption : i.i.d. data drawn from the marginal P(X)
- Usually $\ell << u$
- Test data : $\mathcal{X}_{test} = \{x_{n+1}, \dots, x_{n+\frac{m}{n}}\}$: not available during training, again with *Assumption* : i.i.d. data drawn from the marginal P(X)
- Learn a function $f: \mathcal{X} \to \mathcal{Y}$ (regression/classification) that it generalizes well on test data

Goal

- Labeled data : $S_{\ell} = \{(x_1, y_1), \dots, (x_{\ell}, y_{\ell})\}$, **Assumption :** i.i.d. data drawn from the joint probability distribution P(X,Y)
- Unlabeled data : $\mathcal{X}_u = \{x_{\ell+1}, \dots, x_{\ell+u}\}$, $n = \ell + u$: available during training! **Assumption :** i.i.d. data drawn from the marginal P(X)
- Usually $\ell << u$
- No Test data
- Learn $Y_U \in \{-1,1\}$ the prediction vector of size u for the sole unlabeled data available during training!

Example : link prediction in a protein-protein network (a binary classification task on pairs of nodes)

- For some species, you know that the set of all proteins is perfectly known.
- You already know the "test" data and you assume that you won't get anymore data to test on

Of course, a semi-supervised learning algorithm (inductive approach) can do the job.

Introduction to Semi-supervised learning Assumptions for Semi-supervised learning

Learn
$$f$$
 from \mathcal{X} to \mathcal{Y} using $\mathcal{S}_{\ell} = \{(x_1, y_1), \dots, (x_{\ell}, y_{\ell})\}$ and $\mathcal{X}_u = \{x_{\ell+1}, \dots, x_{\ell+u}\}$

Smoothness assumption of semi-supervised learning

SSL cannot work in all cases. Certain assumptions have been proposed.

Continuous assumption

• if two input points x_1 and x_2 in a high density region are close, then so should be the corresponding y_1 and y_2 .

Introduction to Semi-supervised learning Different Assumptions for Semi-supervised learning

Cluster assumption

- if two input points x₁ and x₂ are close, they belong to the same class
- in other words, it is a *Low density separation assumption*: the frontier between two classes lies on a low-density region

Manifold assumption

 the (input) data roughly lie in a low-dimensional manifold. We view the manifold as an approximation of high density regions, the smoothness assumption of SSL reduces to the smoothness assumption of supervised-learning applied on the manifold.

Finally, let us emphasize that SSL won't work for uniform P(X).

Introduction to Semi-supervised learning Methods

- Learn f from \mathcal{X} to \mathcal{Y} using $\mathcal{S}_{\ell} = \{(x_1, y_1), \dots, (x_{\ell}, y_{\ell})\}$ and $\mathcal{X}_u = \{x_{\ell+1}, \dots, x_{\ell+u}\}$
- Methods
 - Self-training
 - Margin for unlabeled data
 - Smoothness penalty (graph-based semi-supervised learning)
 - Deep learning (a short view)

Self-training approaches Self-training algorithm for supervised classification

Any classifier : f

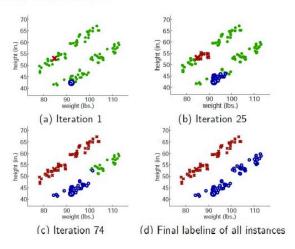
Principle

- $\bullet k=0; \mathcal{S}_0=\mathcal{S}; \mathcal{D}_0=\emptyset$
- **2** Learn f_0 by training on S_0
- **3** Delta = 1000
- WHILE (Delta $\geq \varepsilon$ and $k \leq \text{Max}$) DO
 - Use f_k to label $\mathcal{X}_u \mathcal{D}_k$ and get \mathcal{D}_{k+1} , subset of $\mathcal{X}_u \mathcal{D}_k$ with the most confident labels predicted by f_k
 - build $\mathcal{S}_{k+1} = \mathcal{S}_k \cup \mathcal{D}_{k+1}$
 - Learn f_{k+1} by training on S_{k+1}
 - $Delta = Distance(f_{k+1}, f_k)$; k := k+1
 - How to define the most confident labels? and how many?

Self-training approaches Self-training: example with k-NN (1)

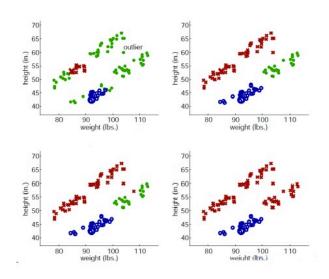
• Two nice clusters without outliers [example Piyush Ray]

Base learner: KNN classifier



Self-training approaches Self-training: example with k-NN (2)

Two clusters with outliers



Log-likelihood for a mixture model:

$$\mathcal{L}(\theta, X, Y) = \log P(\theta)) + \sum_{x_i \in \mathcal{X}_u} \log \sum_{j=1}^M P(c_j | \theta) P(x_i | c_j, \theta) + \dots$$

$$\sum_{x_i \in \mathcal{S}_\ell} \log(P(y_i = c_j | \theta) P(x_i | y_i = c_j | \theta)$$

NB: the constants are dropped.

- a basic model one cluster per class
- More expressive model is possible

Self-training approaches Self-training algorithm with generative models

Basic algorithm

Algorithm 3.1 Basic EM algorithm for semi-supervised learning of a text classifier

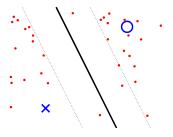
- Inputs: Collections X_l of labeled documents and X_u of unlabeled documents.
- Build an initial naive Bayes classifier, $\hat{\theta}$, from the labeled documents, X_l , only. Use maximum a posteriori parameter estimation to find $\hat{\theta} = \arg \max_{\theta} P(X_l | \theta) P(\theta)$ (see Eqs. 3.5 and 3.6).
- Loop while classifier parameters improve, as measured by the change in $l(\theta|X,Y)$ (the log probability of the labeled and unlabeled data, and the prior) (see Equation 3.8):
 - (E step) Use the current classifier, $\hat{\theta}$, to estimate component membership of each unlabeled document, i.e., the probability that each mixture component (and class) generated each document, $P(c_j|x_i;\hat{\theta})$ (see Eq. 3.7).
 - (M step) Re-estimate the classifier, $\hat{\theta}$, given the estimated component membership of each document. Use maximum a posteriori parameter estimation to find $\hat{\theta} = \arg \max_{\theta} P(X, Y | \theta) P(\theta)$ (see Eqs. 3.5 and 3.6).
- \bullet Output: A classifier, $\hat{\theta},$ that takes an unlabeled document and predicts a class label.

Ref: (Nigam et al. 2006)

Self-training approaches Self-training

- Pros
 - Can be used with any classifier
 - Simple
- Cons
 - Heuristic and ad hoc approach
 - Not well founded
 - Even in case of generative models: Avrum and Cohen (2006) showed a possible performance degradation.

Using Transductive SVM : here is the data



Idea : during the learning phase, learn both the parameters of the SVM and the unknown labels of \mathcal{X}_u

Margin-based approaches Transductive Support Vector Machine (Joachims, 1999)

Joachims proposed a Transductive SVM with a soft margin. Let us call $\mathbf{y}^* = [y_1^*, \dots, y_u^*]$ the prediction vector for the unknown labels of the unlabeled part of the training set.

TSVM

minimize
$$\frac{1}{\mathbf{w}} \| \mathbf{w} \|^2 + C \sum_{i=1}^{\ell} \xi_i + C^* \sum_{j=1}^{u} \xi_i^*$$
 under the constraints $y_i(\mathbf{w}^T \mathbf{x}_i + \mathbf{b}) \ge 1 - \xi_i, \ i = 1, \dots, n$ $y_j^*(\mathbf{w}^T \mathbf{x}_{\ell+j} + \mathbf{b}) \ge 1 - \xi_j^*, \ i = 1, \dots, n$ $y_j^* \in \{-1, +1\}, \ j = 1, \dots, u$ $\xi_i \ge 0$ $\xi_i^* \ge 0$

Ref: Joachims, 1999.

A few remarks about the nature of the method

- It is called transductive because the algorithm seems to focus
 on learning the unknown labels of the training set
 it solves a transductive problem
- However it is an inductive method in the sense that after learning you can use the resulting prediction function on new un labeled data: a single name for different variants of the method is now used Semi-Supervised SVM or S³VM

About the optimization problem :

- It is a combinatorial problem
- It is NP-hard to find the integer y_i^* 's!

Margin-based approaches Solution to the optimization problem in S^3VM

Keeping the exact/combinatorial problem

- Mixed integer programming method : S^3VM by Bennet and Demiriz 1999, 2001 :
- Branch and bound algorithm, Chapelle, Sindwani and Keerthi, 2006

Margin-based approaches Solution to the optimization problem in S^3VM

Relaxing the exact/combinatorial problem

- Relaxation by Semi-definite programming: De Bie and Cristianini, 2004,2006
- Heuristic Joachims, 2003

Margin-based approaches Semi-definite programming for S^3VM (1) **Idea**:

solve the problem in the dual space

$$\begin{aligned} & \min_{Y_u} \max_{\alpha} 2\alpha^T 1 - \alpha^T (K \odot YY^T) \alpha \\ & \text{under the constraints} \\ & Y = \begin{pmatrix} Y \\ Y_u \end{pmatrix} \\ & Y_u = \{-1,1\}^u \end{aligned}$$

Reformulate with matrix
$$\Gamma = YY^T$$

$$\min_{\Gamma} \max_{\alpha} 2\alpha^T 1 - \alpha^T (K \odot \Gamma) \alpha$$
 under the constraints

$$\Gamma = \begin{pmatrix} Y_{\ell} Y_{\ell}^T & Y_{\ell} Y_{u}^T \\ Y_{u} Y_{\ell}^T & Y_{u} Y_{u}^T \end{pmatrix}$$
$$Y_{U} = \{-1, 1\}^{u}$$

Re-parametrize the problem in terms of Γ a sdp matrix, with rank 1 constraint. ref: De Bie, Cristianini, 2006, http://www.tijldebie.net/publications/SSLusingSDP Let us go further, we do not need to explicitly find Y_u . Let us define a margin for the unlabeled data as : $\rho(x, h) = |h(x)|$. Then,

$$\underset{\mathbf{w},b,\xi}{\mathsf{minimize}} \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^{\ell} \xi_i + C^* \sum_{i=\ell+1}^{\ell+u} \xi_i$$

under the constraints

$$y_{i}(\mathbf{w}^{T}\mathbf{x}_{i} + \mathbf{b}) \geq 1 - \xi_{i}, i = 1, ..., \ell$$

 $|\mathbf{w}^{T}\mathbf{x}_{i} + \mathbf{b}| \geq 1 - \xi_{i}, i = \ell + 1, ..., \ell + u$
 $\xi_{i} \geq 0, i = 1, ..., n = \ell + u$

ref :Collobert et al., JMLR, 2006.

Use differentiable functions of the margin to solve the problem + concave - convex methods

- Margin : $\rho(x, y, h) = y.h(x)$
- Which margin for unlabeled data?
- Reinforce the confidence of the classifier
 - $\rho_2(x,h) = h(x)^2$
 - $\rho_1(x,h) = |h(x)|$
 - Implicit assumption : cluster assumption : data in the same cluster share the same label
- Worked for SVM, MarginBoost, ...

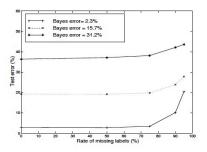
Margin-based approaches Semi-supervised MarginBoost

- $h_t \in \mathcal{H}$: base classifier
- Boosting model : $H_T(x) = \sum_t \alpha_t h_t(x)$
- Loss function : $J(H_t) = \sum_{i=1}^{\ell} exp(-\rho(x_i, y_i, H_t)) + \lambda \sum_{i=\ell+1}^{n} exp(-\rho_u(x_i, H_t))$

ref :Semi-Supervised MarginBoost, NIPS, 2001.

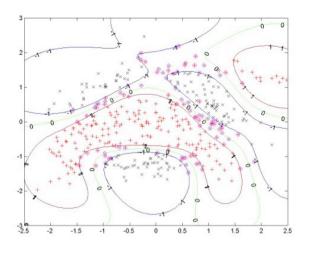
Margin-based approaches Semi-supervised MarginBoost

• Toys problems with different level of difficulty (we control Bayes error by mixing more or less the generative models)



[figure: NIPS 2001]

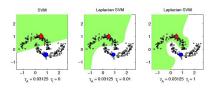
Margin-based approaches Data used in the previous sample



The key ideas:

- We assume that a better knowledge of the marginal distribution $P_x(x)$ will give us bette knowledge of P(Y|x).
- If two points x_1 and x_2 are close in the intrinsic geometry of P_x then the conditional distribution $P(y|x_1)$ and $P(y|x_2)$ will be close.

Graph-based approaches Manifold regularization



• If \mathcal{M} , the support of P_x is a submanifold $\subset \mathbb{R}^p$, then we can try to minimize the penalty :

$$||f||_I^2 = \int_{\mathcal{M}} ||\nabla_{\mathcal{M}} f||^2 dP_{\mathsf{x}}$$

tat reflects the intrinsic structure of the distribution P_x .

The gradient of f is taken with respect to the Riemanian manifold \mathcal{M} , meaning that we take into account the geometry underlying the support of P_{\times} .

Expression of $||f||_{L}^{2}$

If the manifold is infinite or if the support of P_x vanishes at the boundary of \mathcal{M} , then the following holds :

$$||f||_{I}^{2} = \int_{\mathcal{M}} ||\nabla_{\mathcal{M}} f||^{2} dP_{x} = \int_{\mathcal{M}} f \mathcal{L} f dP_{x} = \langle f, \mathcal{L} f \rangle_{L^{2}(P_{x})}$$
(1)

where \mathcal{L} is the Laplace-Beltrami operator on functions :

$$\mathcal{L}f = \operatorname{div} \nabla f$$

Graph-based approaches Analogue of Laplace-Beltrami operator in graph theory

Let \mathcal{G} be a graph with an adjacency matrix W. $L^2(\mathcal{G})$ is a space of functions $\mathcal{G} \to \mathbb{R}$. The graph Laplacian :

$$L = D - W$$

where D is the diagonal matrix of degrees (sum of weights of each node),

is a positive definite operator on $L^2(\mathcal{G})$. Eigenfunctions of the Laplacian for an orthonormal basis for $L^2(\mathcal{G})$.

Graph-based approaches Approximation of $||f||_I^2$

We have :

$$\sum_{ij} w_{ij} (f(x_i) - f(x_j))^2 = 2f^T L f$$

Manifold regularization: smoothness on the data graph

$$||f||_I^2 \approx \sum_{ij} w_{ij} (f(x_i) - f(x_j))^2,$$

Ref :Belkin, Nyogi and Sindwani (2006)

Let k be a positive definite kernel and \mathcal{H}_k the unique RKHS induced by k.

Smoothness constraint / Manifold regularization 1/2

- Training data : $S_{\ell} = \{(x_i, y_i, i =, \dots \ell)\}$ and $S_u = \{x_{\ell+1}, \dots, x_{\ell+u}\}$
- ullet For $f \in \mathcal{H}_k$ and W a similarity matrix between data
- Impose an additional penalty that ensures smoothness of function f: for two close inputs, f takes close values

•

Ref :Belkin, Nyogi and Sindwani (2006)

Let k be a positive definite kernel and \mathcal{H}_k the unique RKHS induced by k.

Smoothness constraint / Manifold regularization

Minimize J(f) in \mathcal{H}_k :

$$J(f) = \frac{1}{\ell} \sum_{i=1}^{\ell} V(x_i, y_i, f) + \lambda ||f||_k^2 + \lambda_u \sum_{ij} w_{ij} (f(x_i) - f(x_j))^2$$

Let k be a positive definite kernel and \mathcal{H}_k the unique RKHS induced by k.

Smoothness constraint / Manifold regularization

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$$= \frac{1}{\ell} \sum_{i=1}^{\ell} V(x_i, y_i, f) + \lambda ||f||_k^2 + \lambda_u f^T L f$$

Graph-based approaches Representer theorem

$$J(f) = \frac{1}{\ell} \sum_{i=1}^{\ell} V(x_i, y_i, f) + \lambda ||f||_k^2 + \lambda_u \sum_{ij=1}^{\ell+u} w_{ij} (f(x_i) - f(x_j))^2$$
$$= \frac{1}{\ell} \sum_{i=1}^{\ell} V(x_i, y_i, f) + \lambda ||f||_k^2 + \lambda_u f^T L f$$

Any minimizer of J(f) admits a representation $\hat{f}(\cdot) = \sum_{i=1}^{\ell+u} \alpha_i k(x_i, \cdot)$

• Closed-from solution : extension of ridge regression

$$V(x_i, y_i, f) = (y_i - f(x_i))^2$$

$$\lambda_L = \frac{\lambda_u}{u + \ell}$$

$$\hat{\alpha} = (JK + \lambda \ell Id + \frac{\lambda_u \ell}{(u + \ell)^2} LK)^{-1} Y$$

K : Gram matrix for all data $J: (\ell+u) \times (\ell+u)$ diagonal matrix with the first ℓ values equal to 1 and the remaining ones to 0.

Graph-based approaches Laplacian SVM

We choose the hinge loss functions:

$$\min_{f \in \mathcal{H}_k} \frac{1}{\ell} \sum_{i=1}^{\ell} (1 - y_i f(x_i))_+ + \lambda ||f||_k^2 + \frac{\lambda_u}{u + \ell} f^T L f$$

We benefit from the representer theorem.

Graph-based approaches Laplacian SVM

In practise, we solve:

$$\begin{split} \min_{\alpha \in \mathbb{R}^{l+u}, \xi \in \mathbb{R}^l} \frac{1}{l} \sum_{i=1}^{l} \xi_i + \gamma_A \alpha^T K \alpha + \frac{\gamma_l}{(u+l)^2} \alpha^T K L K \alpha \\ \text{subject to: } y_i (\sum_{j=1}^{l+u} \alpha_j K(x_i, x_j) + b) \geq 1 - \xi_i, \quad i = 1, \dots, l \\ \xi_i \geq 0 \quad i = 1, \dots, l. \end{split}$$

Graph-based approaches Laplacian SVM

In practise, we solve:

$$\begin{split} \min_{\alpha \in \mathbb{R}^{l+u}, \xi \in \mathbb{R}^l} \frac{1}{l} \sum_{i=1}^{l} \xi_i + \gamma_A \alpha^T K \alpha + \frac{\gamma_l}{(u+l)^2} \alpha^T K L K \alpha \\ \text{subject to: } y_i (\sum_{j=1}^{l+u} \alpha_j K(x_i, x_j) + b) \geq 1 - \xi_i, \quad i = 1, \dots, l \\ \xi_i \geq 0 \quad i = 1, \dots, l. \end{split}$$

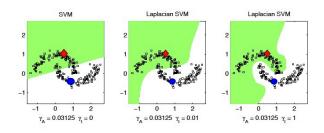
Graph-based approaches Laplacian SVM/RLS algorithm

Results : Belkin et al. 2006, in Book : Semi-supervised Learning .

	Laplacian SVM/RLS
Input:	l labeled examples $\{(x_i, y_i)\}_{i=1}^l$, u unlabeled examples $\{x_j\}_{j=l+1}^{l+u}$
Output:	Estimated function $f: \mathbb{R}^n \to \mathbb{R}$
Step 1	Construct data adjacency graph with $(l+u)$ nodes using, e.g, k nearest neighbors. Choose edge weights W_{ij} , e.g., binary weights or heat kernel weights $W_{ij} = e^{-\ x_i - x_j\ ^2/4t}$.
Step 2	Choose a kernel function $K(x, y)$. Compute the Gram matrix K_{ij}
	$K(x_i,x_j)$.
Step 3	Compute graph Laplacian matrix : $L = D - W$ where D is a diagonal matrix given by $D_{ii} = \sum_{j=1}^{l+u} W_{ij}$.
Step 4	Choose γ_A and γ_I .
Step 5	Compute α^* using Eqn (11.7) for squared loss (Laplacian RLS) or using Eqns (11.9,11.10) together with the SVM QP solver for soft margin loss (Laplacian SVM).
Step 6	Output function $f^*(x) = \sum_{i=1}^{l+u} \alpha_i^* K(x_i, x)$.
	Equivalently, after step 4 construct the kernel function $\tilde{K}(x,y)$ given by Eqn 11.15, and use it in standard SVM/RLS (or with other suitable kernel methods).

Graph-based approaches Laplacian SVM :results

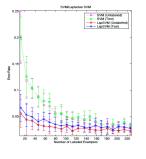
Results: Belkin et al. 2006.

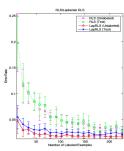


Graph-based approaches Laplacian SVM :results on image classification (2 classes)

Results: Belkin et al. 2006.

 ${\bf Figure~11.5~Image~Classification:~Laplacian~SVM/RLS~performance~with~respect~to~number~of~labeled~examples~on~unlabeled~and~test~data.}$





Again, working in RKHS \mathcal{H}_k , we would like to solve the following (relaxed) clustering problem :

$$\min_{f \in \mathcal{H}_k, \sum_i f(x_i) = 0, \sum_i f(x_i)^2 = 1} \gamma \|f\|_k^2 + \sum_{ij} w_{ij} (f(x_i) - f(x_j))^2$$
 (2)

This approach can be seen as a *regularized spectral clustering*. It also benefits from a representer theorem : f^* the minimizer of Eq. 2 satisfies :

$$f^*(\cdot) = \sum_{i=1}^n \alpha_i \ k(\cdot, x_i)$$

Therefore the problem boils down to solve :

$$\min_{\alpha \in \mathbb{R}^n, 1^T K \alpha = 0, \alpha^T K^2 \alpha = 1} \gamma \alpha^T K \alpha + \alpha^T K L K \alpha$$

$$\min_{\alpha \in \mathbb{R}^n, \mathbf{1}^T K \alpha = \mathbf{0}, \alpha^T K^2 \alpha = \mathbf{1}} \gamma \alpha^T K \alpha + \alpha^T K \mathbf{L} K \alpha$$

- show that $\alpha^* = Pv$, v being the eigenvector with the smallest eigenvalue of a generalized eigenvector problem.
- Remark : This clustering provides a natural out-of-sample extension (classification of new datapoints)

Semi-supervised Deep learning Semi-supervised embedding

3 ways proposed by Weston et al. 2008.

(a) Add a semi-supervised loss (regularizer) to the supervised loss on the entire network's output (6):

$$\sum_{i=1}^{M} \ell(f(x_i), y_i) + \lambda \sum_{i,j=1}^{M+U} L(f(x_i), f(x_j), W_{ij})$$
 (9)

This is most similar to the shallow techniques described before, e.g. equation (5).

(b) Regularize the kth hidden layer (7) directly:

$$\sum_{i=1}^{M} \ell(f(x_i), y_i) + \lambda \sum_{i,j=1}^{M+U} L(f^k(x_i), f^k(x_j), W_{ij})$$
(10)

where $f^k(x) = (h_1^k(x), \dots, h_{HU_k}^k(x))$ is the output of the network up to the k^{th} hidden layer (HU_k) is the number of hidden units on layer k).

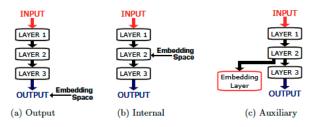
(c) Create an auxiliary network which shares the first k layers of the original network but has a new final set of weights:

$$g_i(x) = \sum_j w_j^{AUX,i} h_j^k(x) + b^{AUX,i}$$
 (11)

We train this network to embed unlabeled data simultaneously as we train the original network on labeled data.

Semi-supervised Deep learning Semi-supervised embedding

Architectures



Semi-supervised Deep learning Semi-supervised embedding

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Algorithm 1 EmbedNN
```

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Input: labeled data (x_i, y_i), i = 1, ..., M, unlabeled data x_i, i = M + 1, ..., U, set
of functions f(\cdot), and embedding functions g^k(\cdot), see Figure 1 and equations (9), (10)
and (11).
repeat
Pick a random labeled example (x_i, y_i)
```

Pick a random labeled example (x_i, y_i) Make a gradient step to optimize $\ell(f(x_i), y_i)$

for each embedding function $g^k(\cdot)$ do

Pick a random pair of neighbors x_i, x_j . Make a gradient step for $\lambda L(g^k(x_i), g^k(x_j), 1)$

Pick a random unlabeled example x_n .

Make a gradient step for $\lambda L(g^k(x_i), g^k(x_n), 0)$

end for

until stopping criteria is met.

Ref: Weston et al., ICML 2008.

Conclusion and references Outline

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Conclusion and references Semi-supervised methods

- Self-training method no more used
- Generative methods within deep learning are still used howver (group of Welling)
- Transductive SVM and S3VM avriants lack of scalability
- Manifold regularization are the most founded ones but again lack of scalability if not applying kernel approximation
- Theory is still lacking but semi-supervised learning can still bring improvement if the hyperparameter governing its weights is well chosen

Conclusion and references Exercises and references

- Code the Laplacian SVM or the Laplacian Kernel Ridge regressor
- Study the effect of graph construction
- Book : Semi-supervised learning, Chapelle, Scholpkoft, Zien,MIT