
Statistical Multiplexing; Layered Network Architecture; End-to-end Arguments

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09/23/2021

Outline

- Admin. and recap
- A taxonomy of communication networks
- Layered network architecture

Admin.

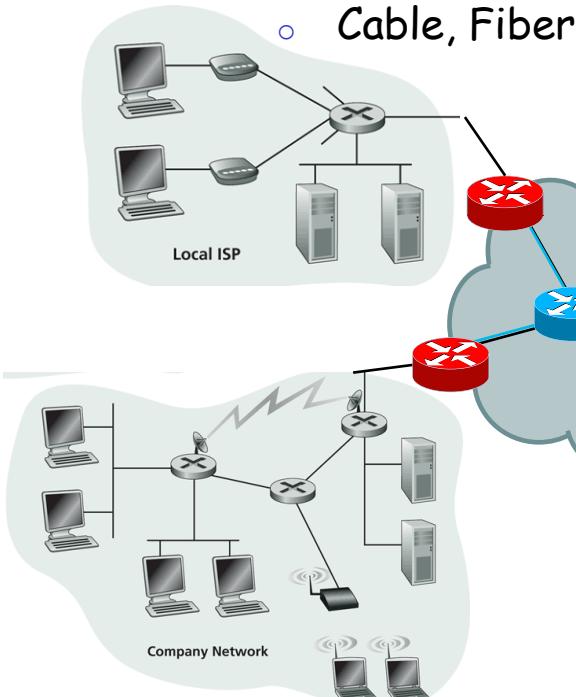
- Readings from the textbook and additional suggested readings
 - All are highly recommended
 - Some are marked as required

- Assignment one is linked on the schedule page
 - Oct. 14, in class or by email to the instructor

Recall: Internet Physical Infrastructure

Residential access, e.g.,

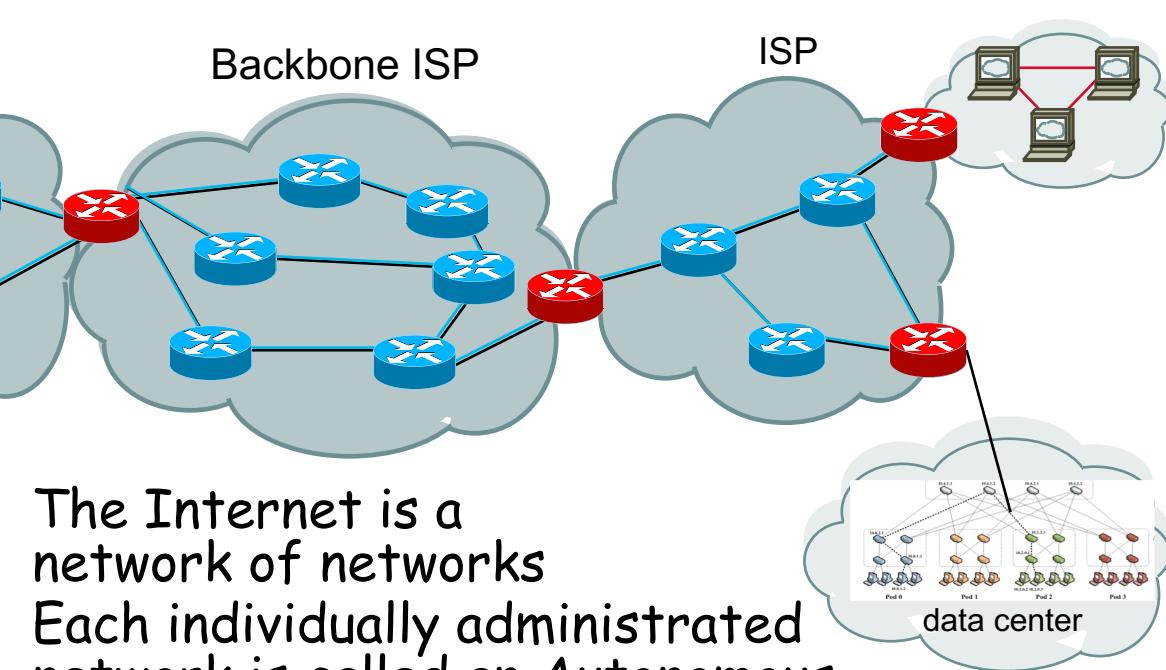
- Cable, Fiber, DSL, Wireless



Campus access, e.g.,

- Ethernet, Wireless

- ❑ The Internet is a network of networks
- ❑ Each individually administrated network is called an Autonomous System (AS)
 - ~ 58000 ASes; Avg 5.7 hops;
(<http://bgp.potaroo.net/as2.0/bgp-active.html>)



Recap: Challenges - Scale



“Developers who have worked at the small scale might be asking themselves why we need to bother when we could just use some kind of out-of-the-box solution. For small-scale applications, this can be a great idea. We save time and money up front and get a working and serviceable application. The problem comes at larger scales—there are no off-the-shelf kits that will allow you to build something like Amazon... There’s a good reason why the largest applications on the Internet are all bespoke creations: no other approach can create massively scalable applications within a reasonable budget.”

Recap: Challenges - General Complexity



- Complexity in highly organized systems arises primarily from design strategies intended to create robustness to uncertainty in their environments and component parts.
 - Scalability is robustness to changes to the size and complexity of a system as a whole.
 - Evolvability is robustness of lineages to large changes on various (usually long) time scales.
 - Reliability is robustness to component failures.
 - Efficiency is robustness to resource scarcity.
 - Modularity is robustness to component rearrangements.

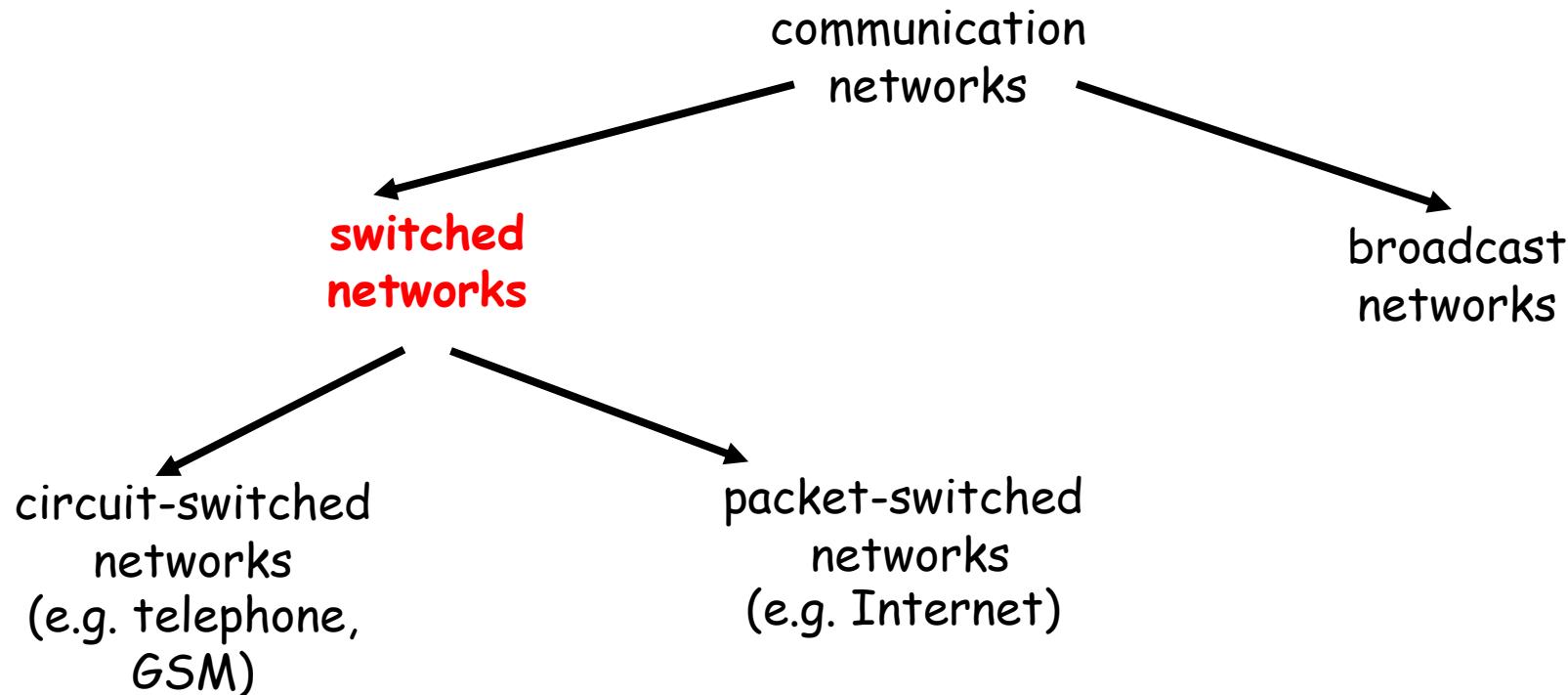
Recap: Challenges - Distributed vs Centralized



- Distributed computing is hard, e.g.,
 - FLP Impossibility Theorem
 - Arrow's Impossibility Theorem
- Achieved good design for only few specific tasks (e.g., state distribution, leader election). Hence, a trend in networking is Software Defined Networking, which is a way of moving away from generic distributed computing, by focusing on utilizing the few well-understood primitives, in particular logically centralized state.

Recap: A Taxonomy of Comm. Networks

- Basic question: how are data (the bits) transferred through communication networks?



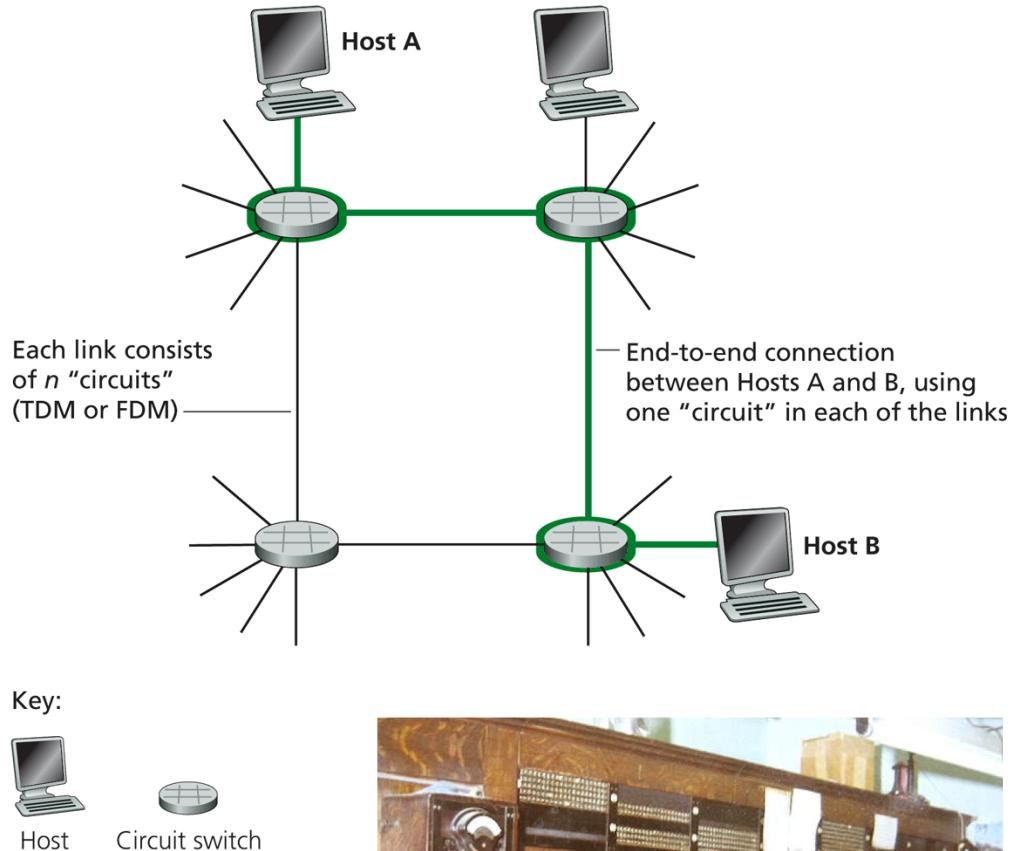
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 - circuit switched networks

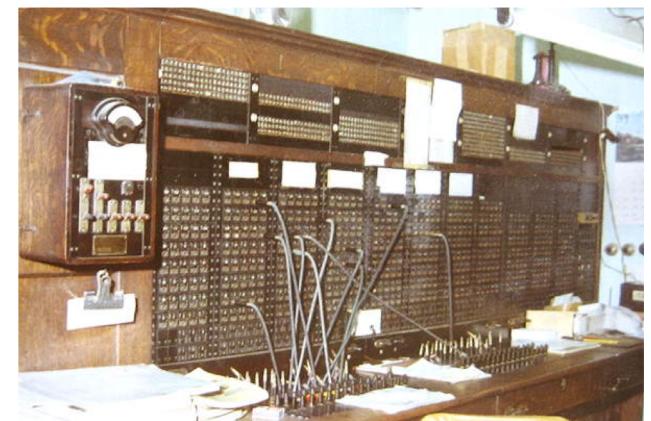
Circuit Switching

- Each link has a number of “circuits”
 - sometime we refer to a “circuit” as a channel or a line

- An end-to-end connection reserves one “circuit” at each link



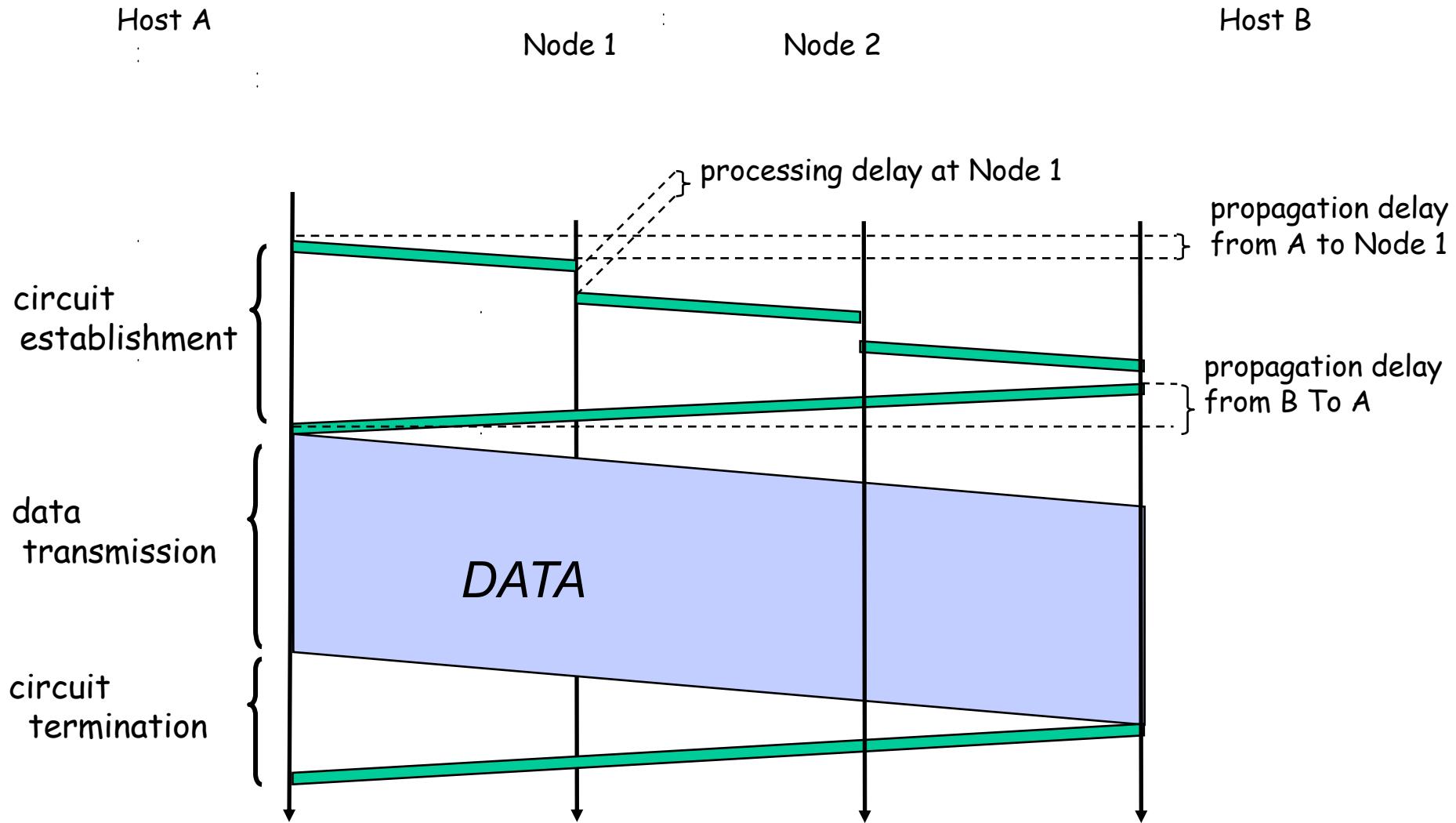
First commercial telephone switchboard was opened in 1878 to serve the 21 telephone customers in New Haven



Circuit Switching: The Process

- Three phases
 - circuit establishment
 - data transfer
 - circuit termination

Timing Diagram of Circuit Switching

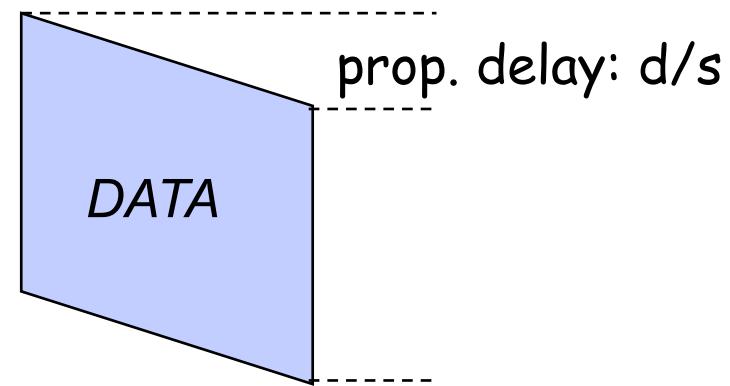


Delay Calculation in Circuit Switched Networks

- **Propagation delay:** delay for the first bit to go from a source to a destination

Propagation delay:

- d = length of physical link
- s = propagation speed in medium ($\sim 2 \times 10^5$ km/sec)

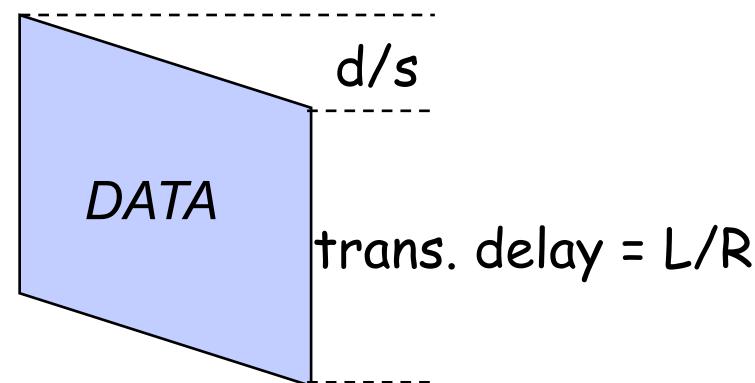


Delay Calculation in Circuit Switched Networks

- **Transmission delay:** time to pump data onto link at *line rate*

Transmission delay:

- R = reserved bandwidth (bps)
- L = message length (bits)



An Example

□ Propagation delay

- suppose the distance between A and B is 4000 km, then one-way propagation delay is:

$$\frac{4000 \text{ km}}{200,000 \text{ km/s}} = 20ms$$

□ Transmission delay

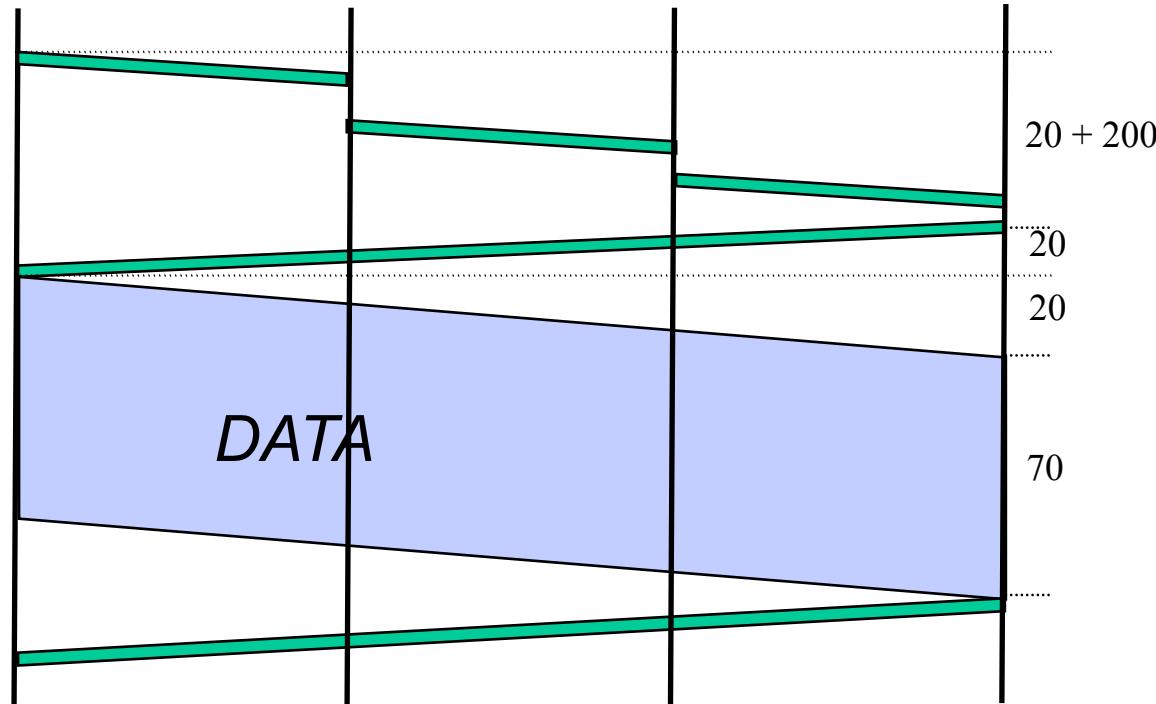
- suppose your iphone reserves a one-slot HSCSD channel
 - each HSCSD frame can transmit about 115 kbps
 - a frame is divided into 8 slots
- then the transmission delay of using one reserved slot for a message of 1 Kbits:

$$\frac{1kbit}{14kbps} \approx 70ms$$

An Example (cont.)

- Suppose the setup message is very small, and the total setup processing delay is 200 ms
 - Then the delay to transfer a message of 1 Kbits from A to B (from the beginning until host receives last bit) is:

$$20 + 200 + 20 + 20 + 70 = 330ms$$



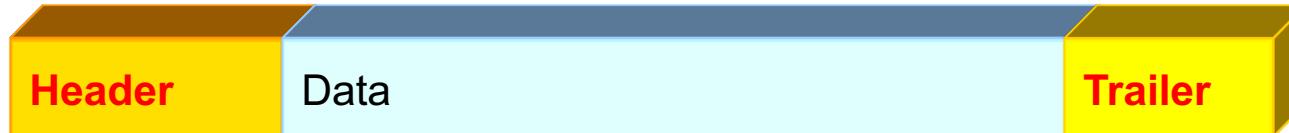
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- A brief introduction to the Internet: past and present
- Challenges of Internet networks and apps
- A taxonomy of communication networks
 - circuit switched networks
 - *packet switched networks*

Packet Switching

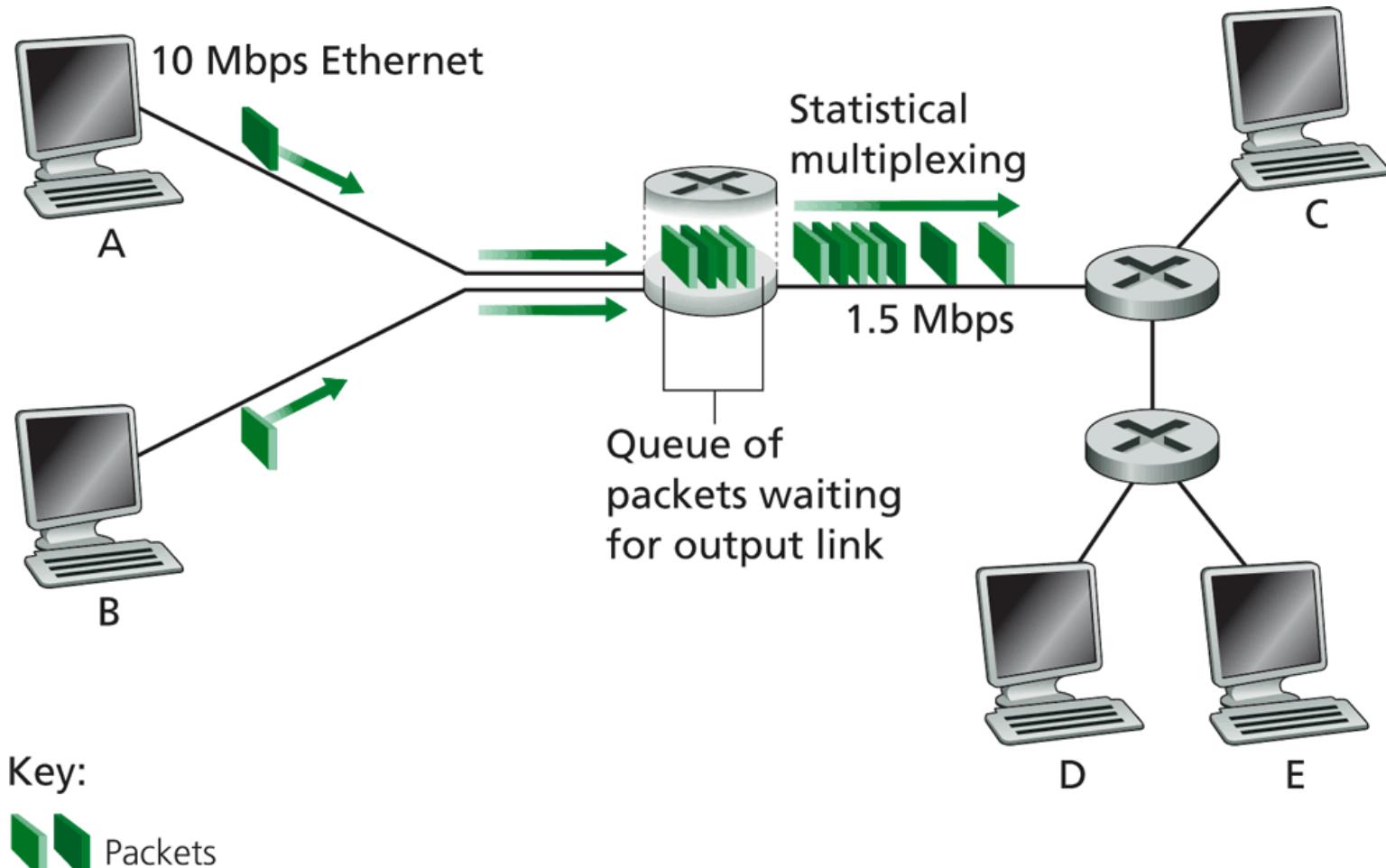
Each end-to-end data **flow** (i.e., a sender-receiver pair) divided into **packets**

- Packets have the following structure:



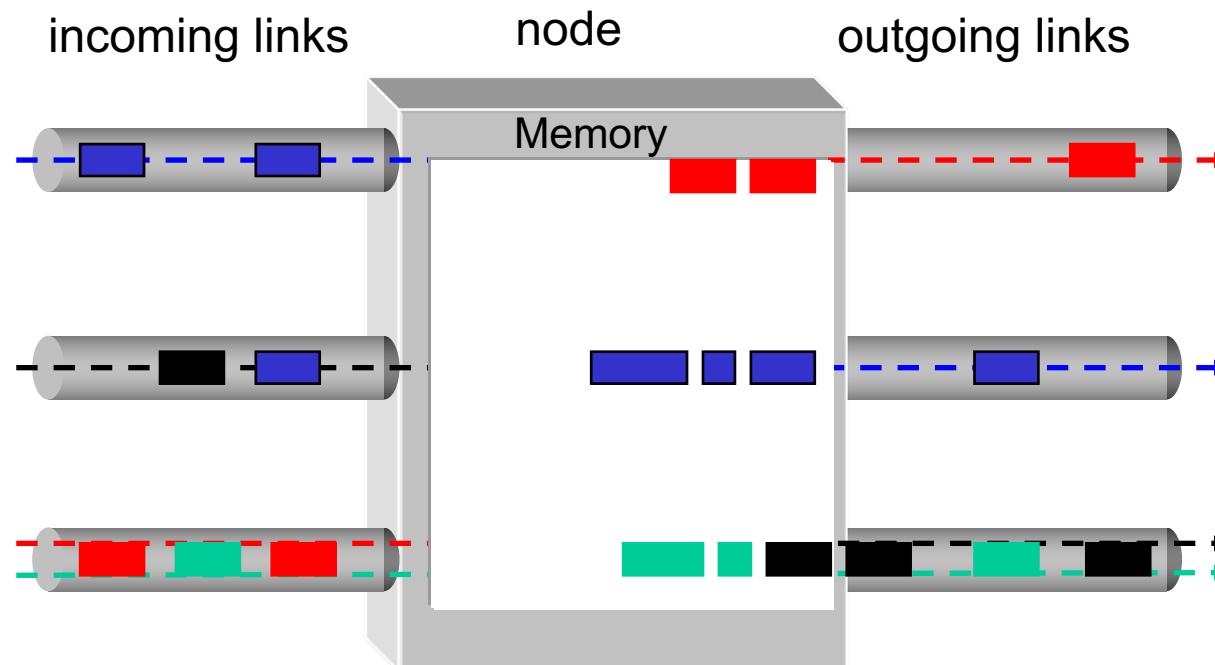
- header and trailer carry control information (e.g., destination address, check sum)
- where is the control information for circuit switching?
- At each node the entire packet is received, processed (e.g., routing), stored briefly, and then forwarded to the next node; thus packet-switched networks are also called **store-and-forward networks**. On its turn, a packet uses **full link bandwidth**

Packet Switching



Inside a Packet Switching Router

An output queueing switch



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Packet Switching vs. Circuit Switching

- The early history of the Internet was a heated debate between Packet Switching and Circuit Switching
 - the telephone network was the dominant network
- Need to compare packet switching with circuit switching

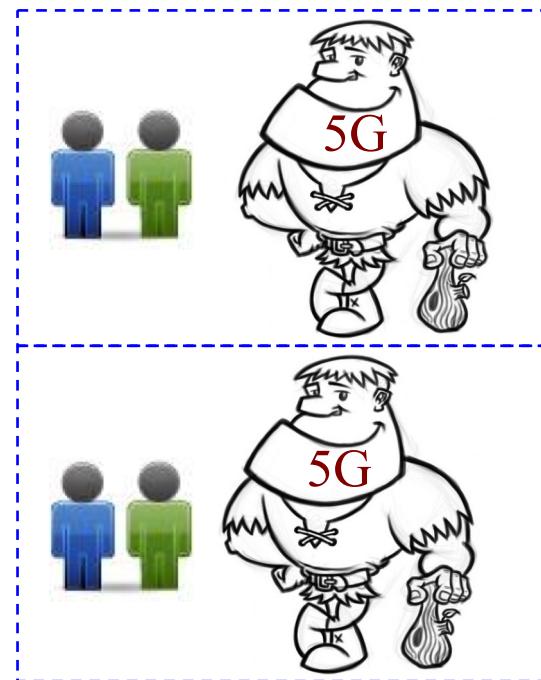
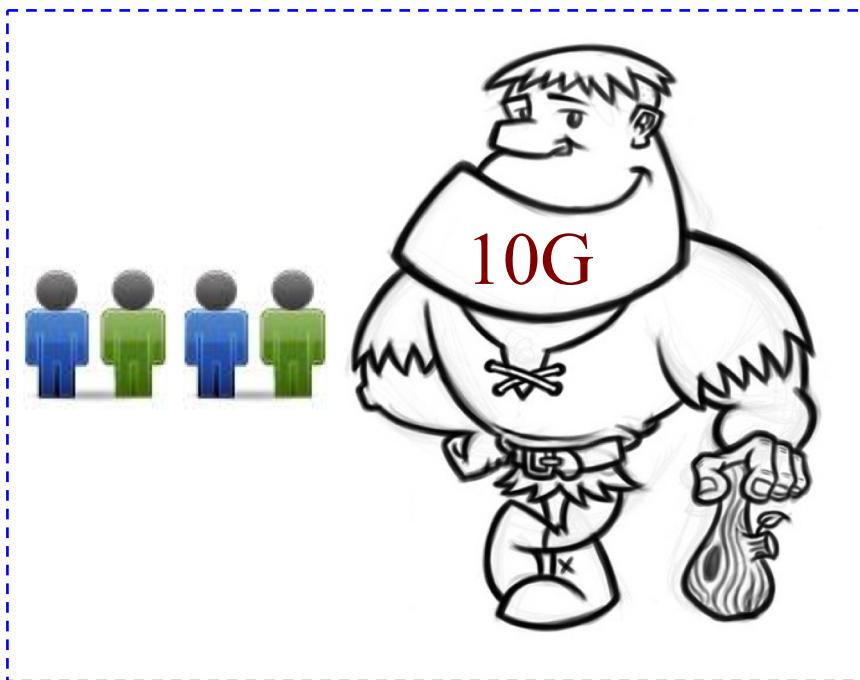


Circuit Switching vs. Packet Switching

	circuit switching	packet switching
resource usage		
reservation/setup		
resource contention		
charging		
header		
fast path processing		

Key Issue to be Settled

- A key issue: what is the efficiency of resource partition?



- Tool used to analyze the issue: queueing theory
 - Some basic results of queueing theory can be quite useful in many systems settings

Outline

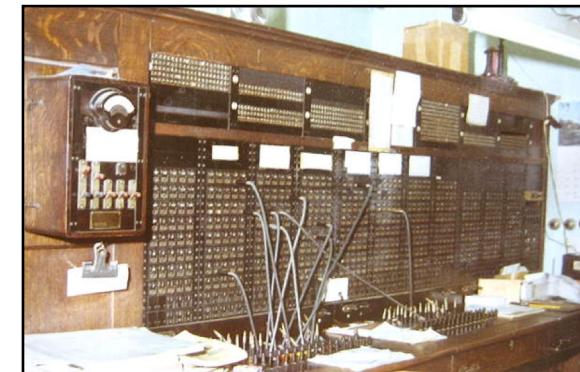
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- *M/M queues and statistical multiplexing*

Queueing Theory

- Strategy:
 - model **system state**
 - if we know the fraction of time that the system spends at each state, we can get answers to many basic questions: how long does a new request need to wait before being served?
- System state changes upon events:
 - introduce **state transition** diagram
 - focus on **equilibrium**: state trend neither growing nor shrinking (key issue: how to define equilibrium)
- Our approach: We are not interested in extremely precise modeling, but want quantitative intuition

Warm up: Analysis of Circuit-Switching Blocking (Busy) Time

- Assume a link has only a finite number of N circuits
- Objective: compute the percentage of time that a new session (call) is blocked
- Analogy in a more daily-life scenario?
- Key parameters?



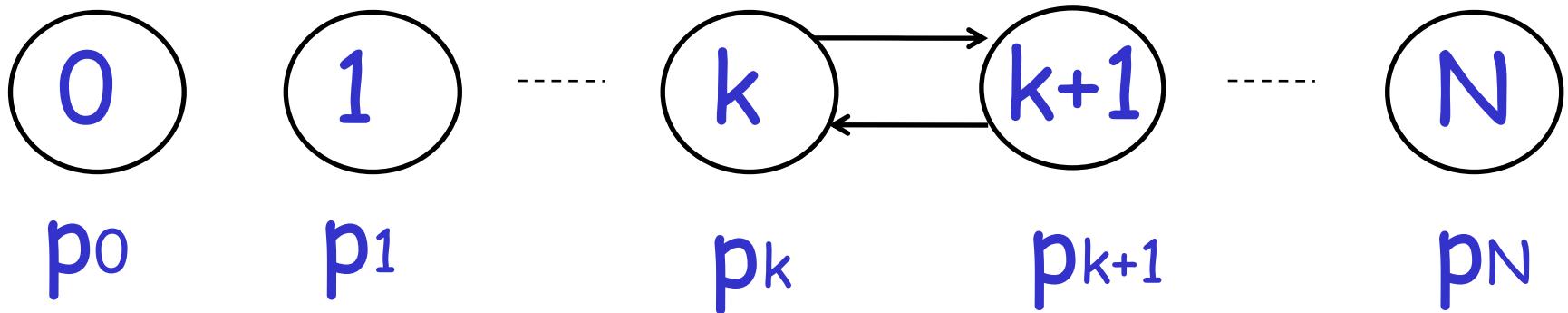
Analysis of Circuit-Switching Blocking (Busy) Time

- Consider a simple arrival pattern
 - client requests arrive at a rate of λ (lambda/second)
 - service rate: each call takes on average $1/\mu$ second
- Arrival and service patterns: memoryless (Markovian)
 - During a small interval Δt , the number of expected new arrivals is: $\lambda \Delta t$
 - During a small interval Δt , the chance (fraction) of a current call finishes is: $\mu \Delta t$
- This model is also called an M/M/N model

Analysis of Circuit-Switching

Blocking (Busy) Time: State

system state: # of busy lines



Q: How to characterize equilibrium?

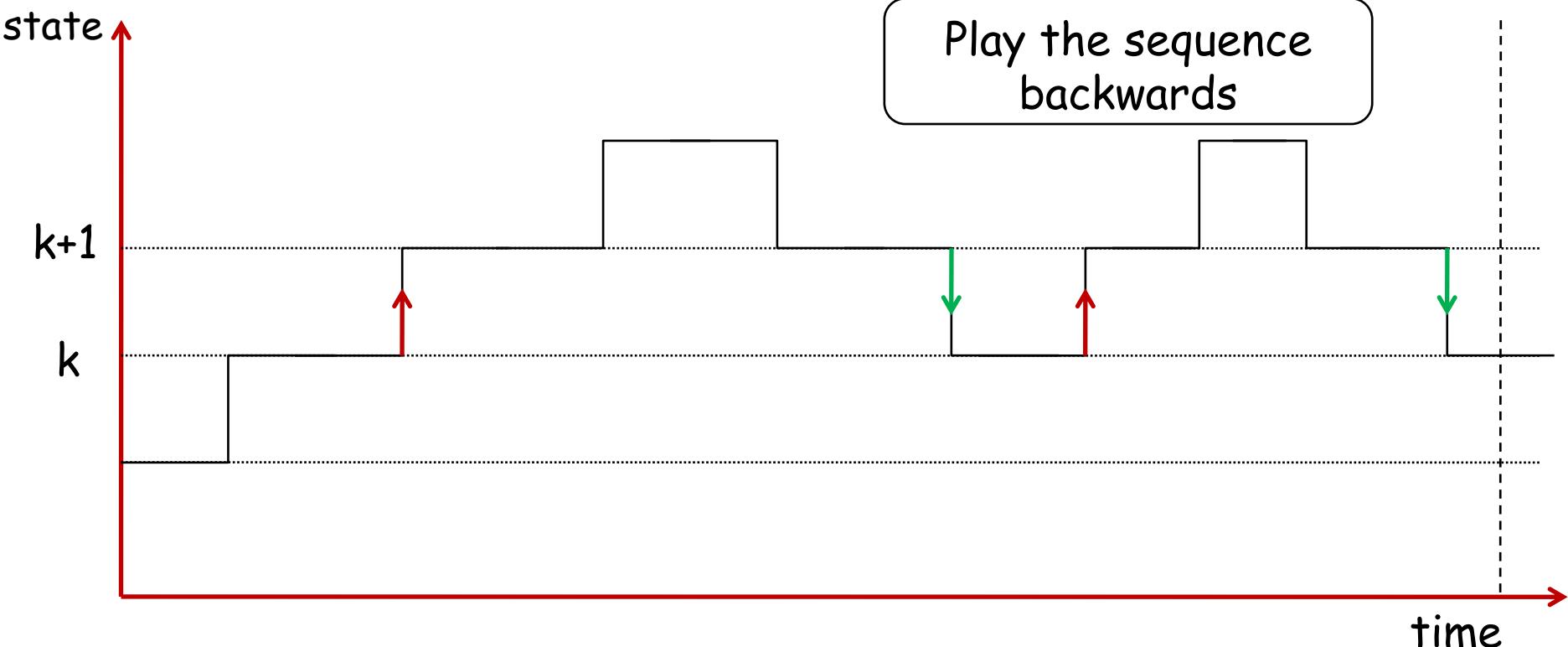
Equilibrium = Time Reversibility [Frank Kelly]

□ Statistically cannot distinguish

$$\# f_{k \rightarrow k+1} = \# f_{k+1 \rightarrow k}$$

$$\# b_{k \rightarrow k+1}, \# b_{k+1 \rightarrow k}$$

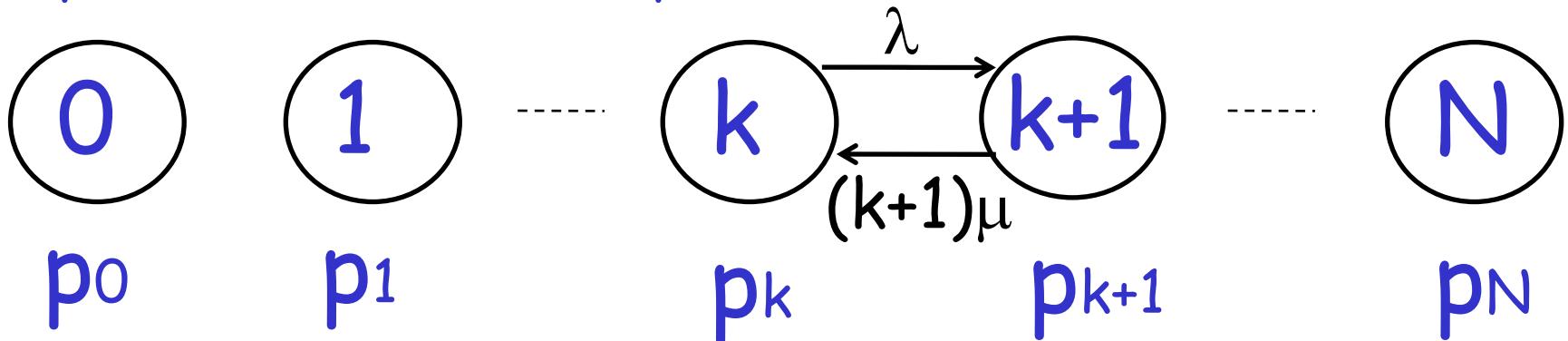
Play the sequence backwards



Analysis of Circuit-Switching

Blocking (Busy) Time: Sketch

system state: # of busy lines



at equilibrium (time reversibility) in one unit time:

$$\#(\text{transitions } k \rightarrow k+1) = \#(\text{transitions } k+1 \rightarrow k)$$

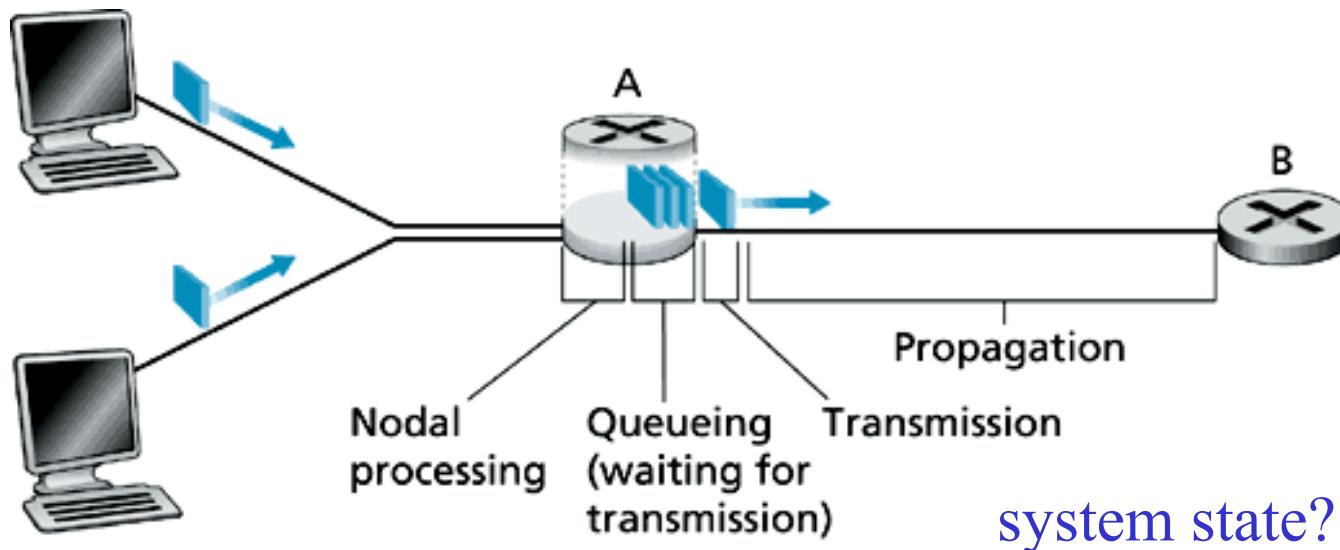
$$p_k \lambda = p_{k+1} (k+1) \mu$$

$$p_{k+1} = \frac{1}{k+1} \frac{\lambda}{\mu} p_k = \frac{1}{(k+1)!} \left(\frac{\lambda}{\mu}\right)^{k+1} p_0$$

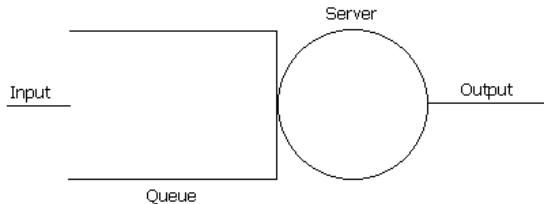
$$p_0 = \frac{1}{1 + \frac{1}{1!} \frac{\lambda}{\mu} + \frac{1}{2!} \left(\frac{\lambda}{\mu}\right)^2 + \dots + \frac{1}{N!} \left(\frac{\lambda}{\mu}\right)^N}$$

Queueing Analysis: Packet Switching Delay

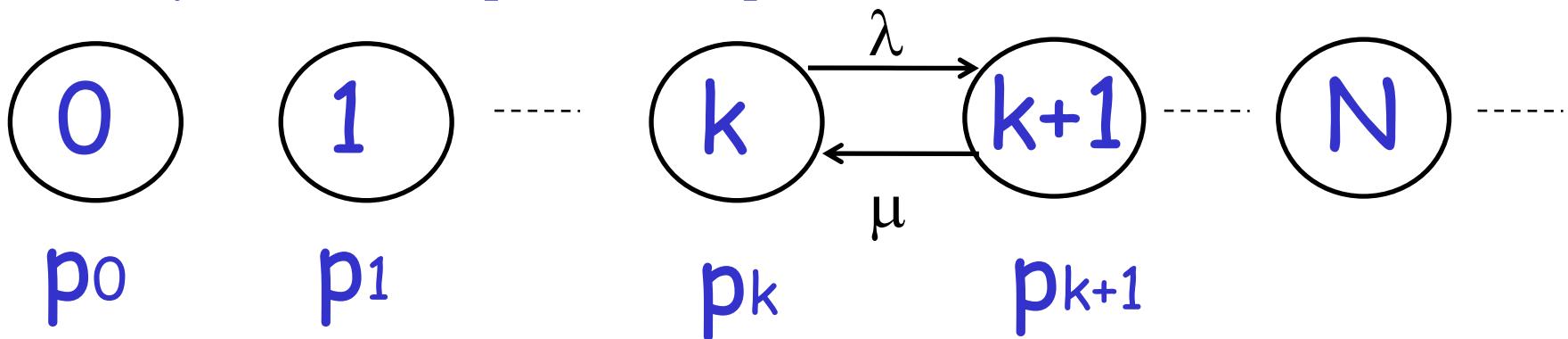
- Four types of delay at each hop
 - nodal processing delay: check errors & routing
 - queueing: time waiting for its turn at output link
 - transmission delay: time to pump packet onto a link at link speed
 - propagation delay: router to router propagation
- The focus is on **queueing and transmission delay**



Packet Switching Delay



system state: #packets in queue



at equilibrium (time reversibility) in one unit time:

$$\#(\text{transitions } k \rightarrow k+1) = \#(\text{transitions } k+1 \rightarrow k)$$

$$p_k \lambda = p_{k+1} \mu$$

$$\sum_{k=0}^{\infty} p_k = 1$$

$$p_{k+1} = \frac{\lambda}{\mu} p_k = \left(\frac{\lambda}{\mu}\right)^{k+1} p_0 = \rho^{k+1} p_0$$

$$p_0 = 1 - \rho$$

$$\rho = \frac{\lambda}{\mu}$$

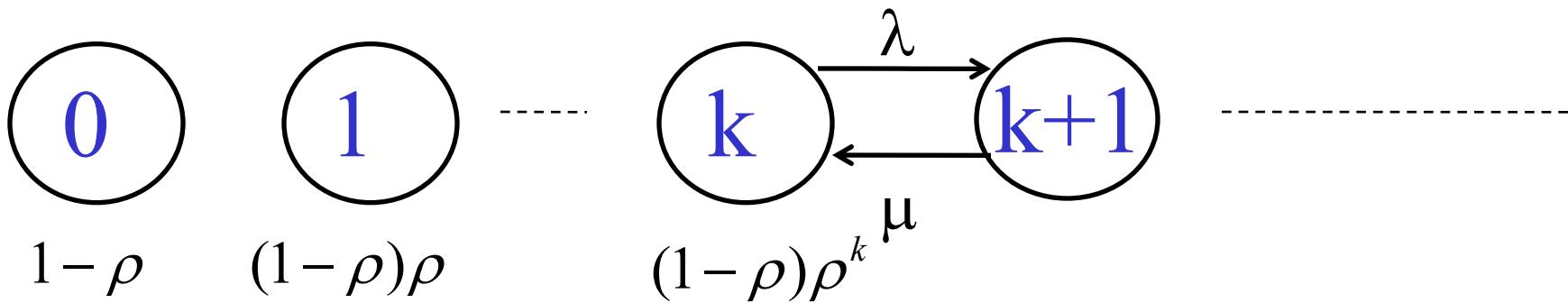
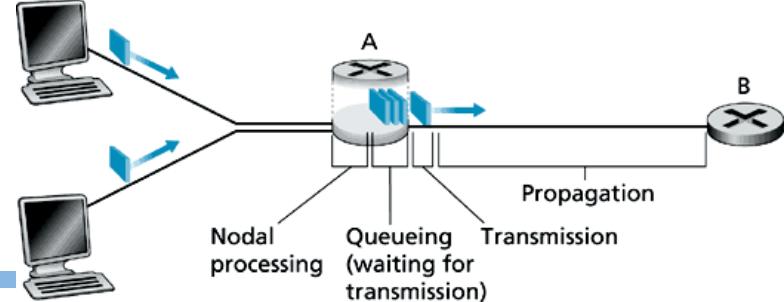
Summary: Queueing Theory

- Model system state
- Introduce state transition diagram
- Focus on equilibrium: state trend neither growing nor shrinking

Example

- Assume requests (packets) come in at a rate of one request per 50 ms $\lambda=1/50\text{ms} = 20/\text{s}$
- Each request (packet) takes on average 20 ms $1/\mu=20 \text{ ms}, \mu=50/\text{s}$
- What is the fraction of time that the system is empty? P_0
- What is the chance that a packet newly arrived needs to wait for 3 early packets? P_3

Analysis of Delay (cont')



□ Average queueing delay:

$$\sum_{k=0}^{\infty} p_k \cdot k \cdot \frac{1}{\mu} = \sum_{k=0}^{\infty} \rho^k (1 - \rho) k \frac{1}{\mu}$$

□ Transmission delay:

$$S = \frac{1}{\mu}$$

□ Queueing + transmission:

Delay

$$\rho = \frac{\lambda}{\mu}$$

$$S = \frac{1}{\mu}$$

average queueing delay: $w = S \frac{\rho}{1 - \rho}$

$$queueing + trans = S \frac{\rho}{1 - \rho} + S = S \frac{1}{1 - \rho}$$

For a demo of M/M/1, see:

http://www.dcs.ed.ac.uk/home/jeh/Simjava/queueing/mm1_q/mm1_q.html

Queueing Delay as a Function of Utilization

Assume:

R = link bandwidth (bps)

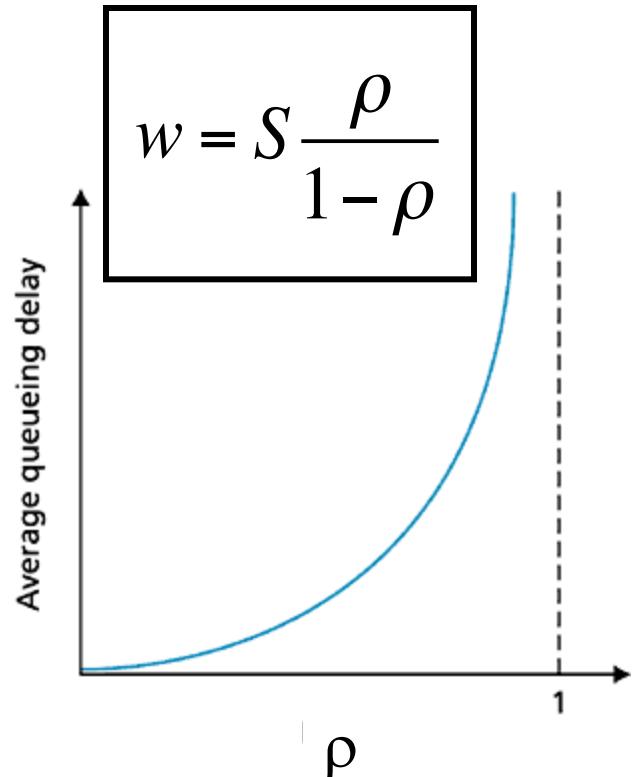
L = packet length (bits)

$S = L / R$

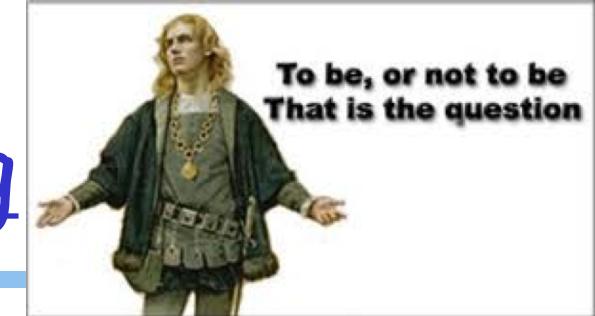
a = average packet arrival rate (pkt/sec)

$$\text{utilization: } \rho = \frac{a}{1/S} = aS$$

$$w = S \frac{\rho}{1 - \rho}$$



- $\rho \sim 0$: average queueing delay small
- $\rho \rightarrow 1$: delay becomes large
- $\rho > 1$: more “work” arriving than can be serviced, average delay infinite !



Statistical Multiplexing

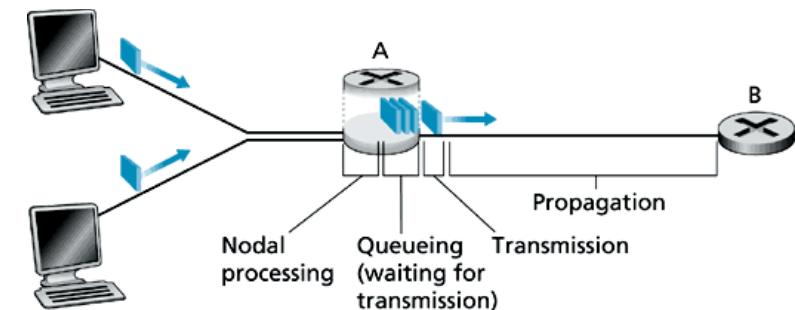
A simple model to compare bandwidth efficiency of

- reservation/dedication (aka circuit-switching) vs
- no reservation (aka packet switching)

setup

- a single bottleneck link with service rate μ
 - n flows; each flow has an arrival rate of λ/n
- no reservation: all arrivals into the single link, the queueing delay + transmission delay:

$$S \frac{1}{1 - \rho}$$



- reservation: each flow uses its own reserved (sub)link with rate μ/n , the queueing delay + transmission delay:

For each flow i:

$$\rho_i = \frac{\lambda/n}{\mu/n} = \rho \rightarrow n S \frac{1}{1 - \rho}$$

$$S_i = \frac{1}{\mu/n} = nS$$

Summary:

Packet Switching vs. Circuit Switching

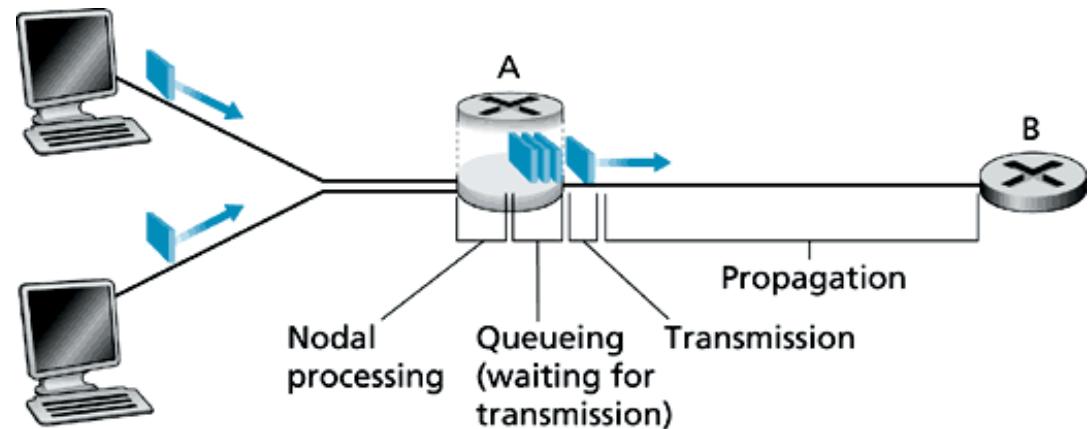
- Advantages of packet switching over circuit switching
 - most important advantage of packet-switching over circuit switching is **statistical multiplexing**, and therefore more efficient bandwidth usage
- Disadvantages of packet switching
 - **potential congestion:** packet delay and high loss
 - protocols needed for reliable data transfer, congestion control
 - it is possible to guarantee quality of service (QoS) in packet-switched networks and still gain statistical multiplexing, but it adds much complexity
 - **packet header overhead**
 - **per packet processing overhead**

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- *A taxonomy of communication networks*
 - circuit switched networks
 - packet switched networks
 - circuit switching vs. packet switching
 - *datagram and virtual circuit packet switched networks*

A Taxonomy of Packet-Switched Networks According to Routing

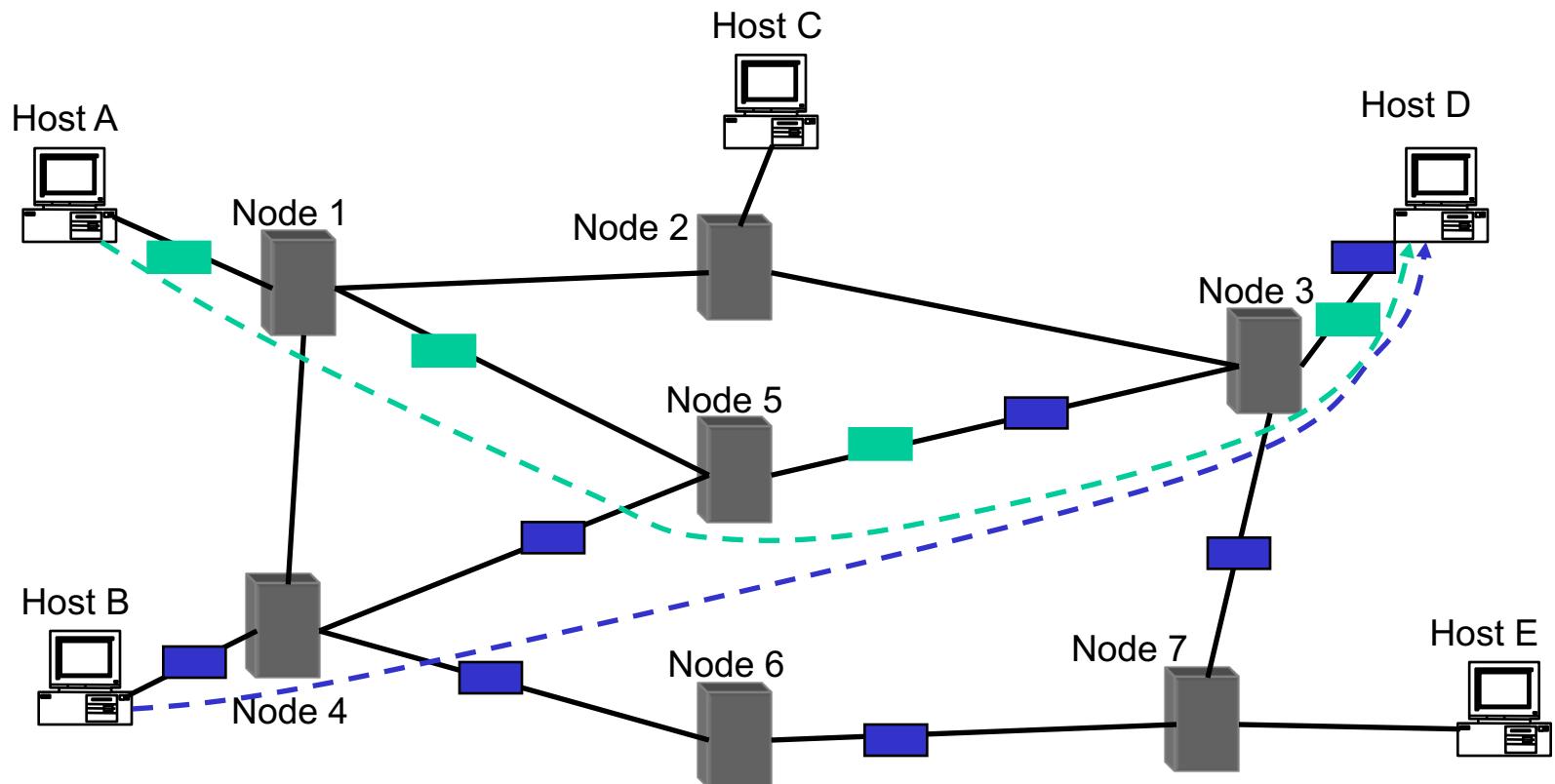
- Two types of packet switching
 - **datagram network**
 - each packet of a flow is switched **independently**
 - **virtual circuit network:**
 - all packets from one flow are sent along a **pre-established path** (= virtual circuit)



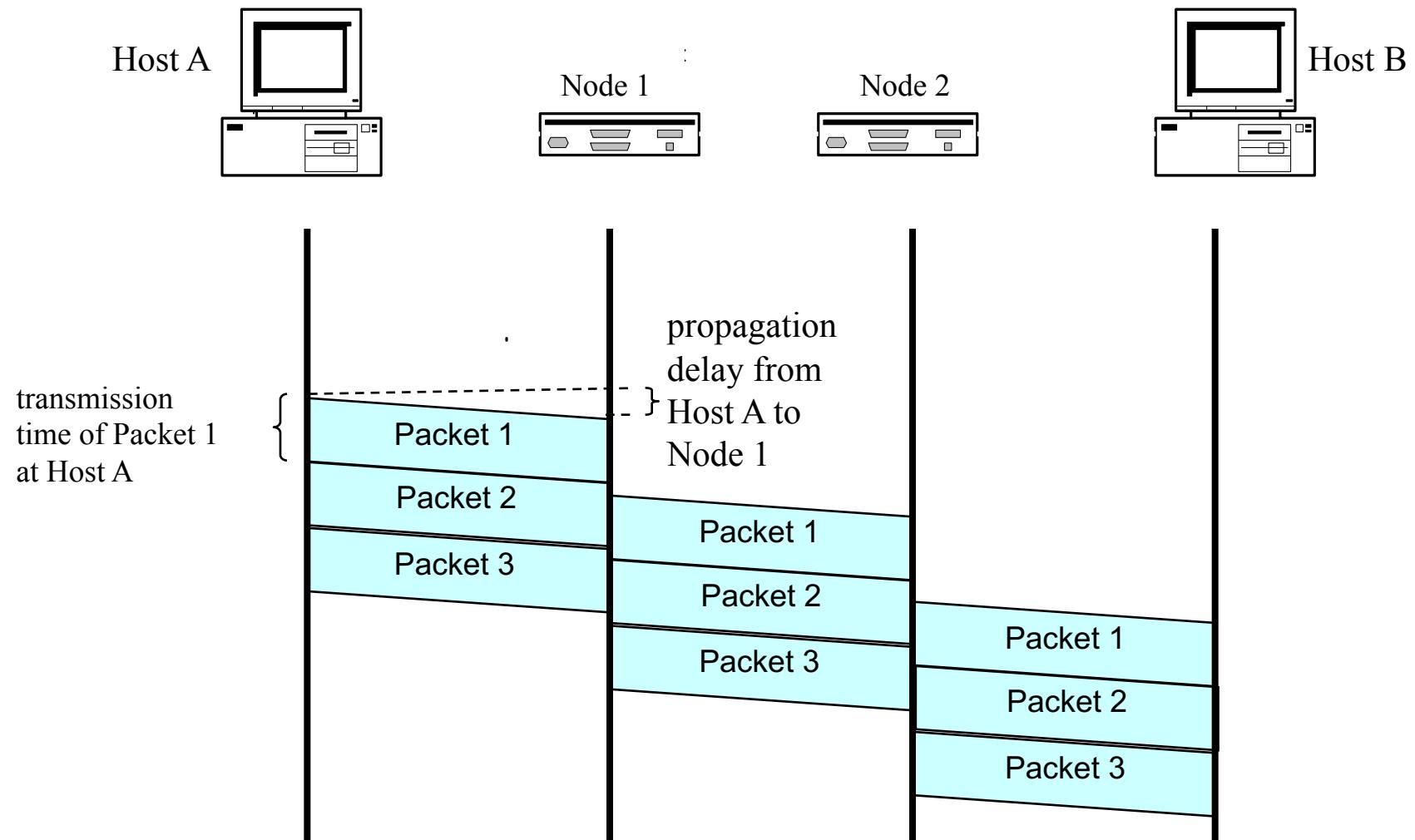
Datagram Packet Switching

- Commonly when we say packet switching we mean datagram switching
- Example: IP networks
- Each packet is independently switched
 - each packet header contains *complete destination address*
 - receiving a packet, a router looks at the packet's destination address and *searches* its current routing table to determine the possible next hops, and pick one
- Analogy: postal mail system

Datagram Packet Switching



Timing Diagram of Datagram Switching

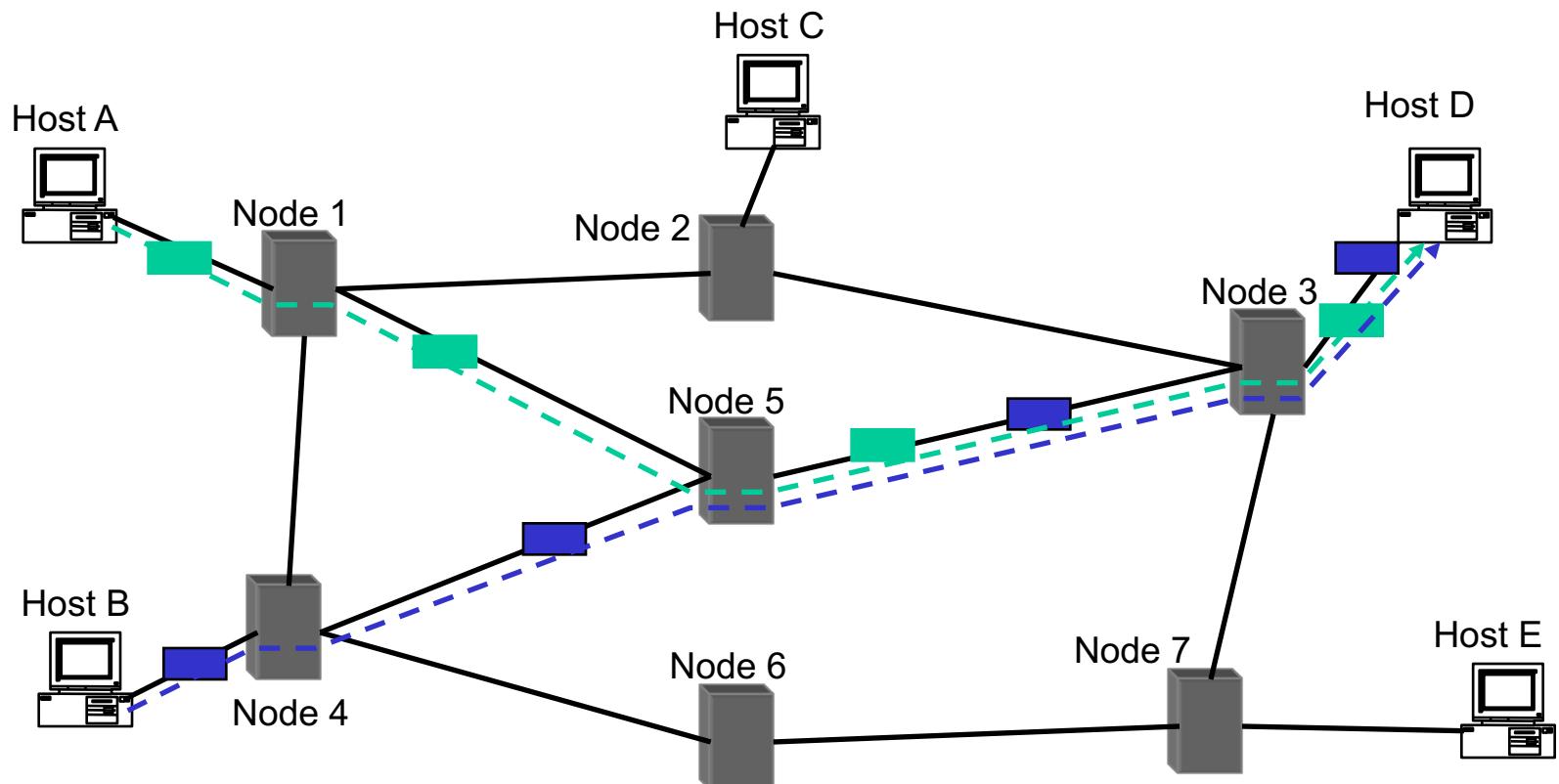


Virtual-Circuit Packet Switching

- Example: Multiple Label Packet Switching (MPLS) in IP networks
- Hybrid of circuit switching and datagram switching
 - fixed path determined at *virtual circuit setup time*, remains fixed thru flow
 - Implementation:
 1. each packet carries a short local, **tag** (virtual-circuit (VC) #); tag determines next hop

Incoming VC#	Outgoing Interface	QoS
12	2	
16	3	
20	3	
...		

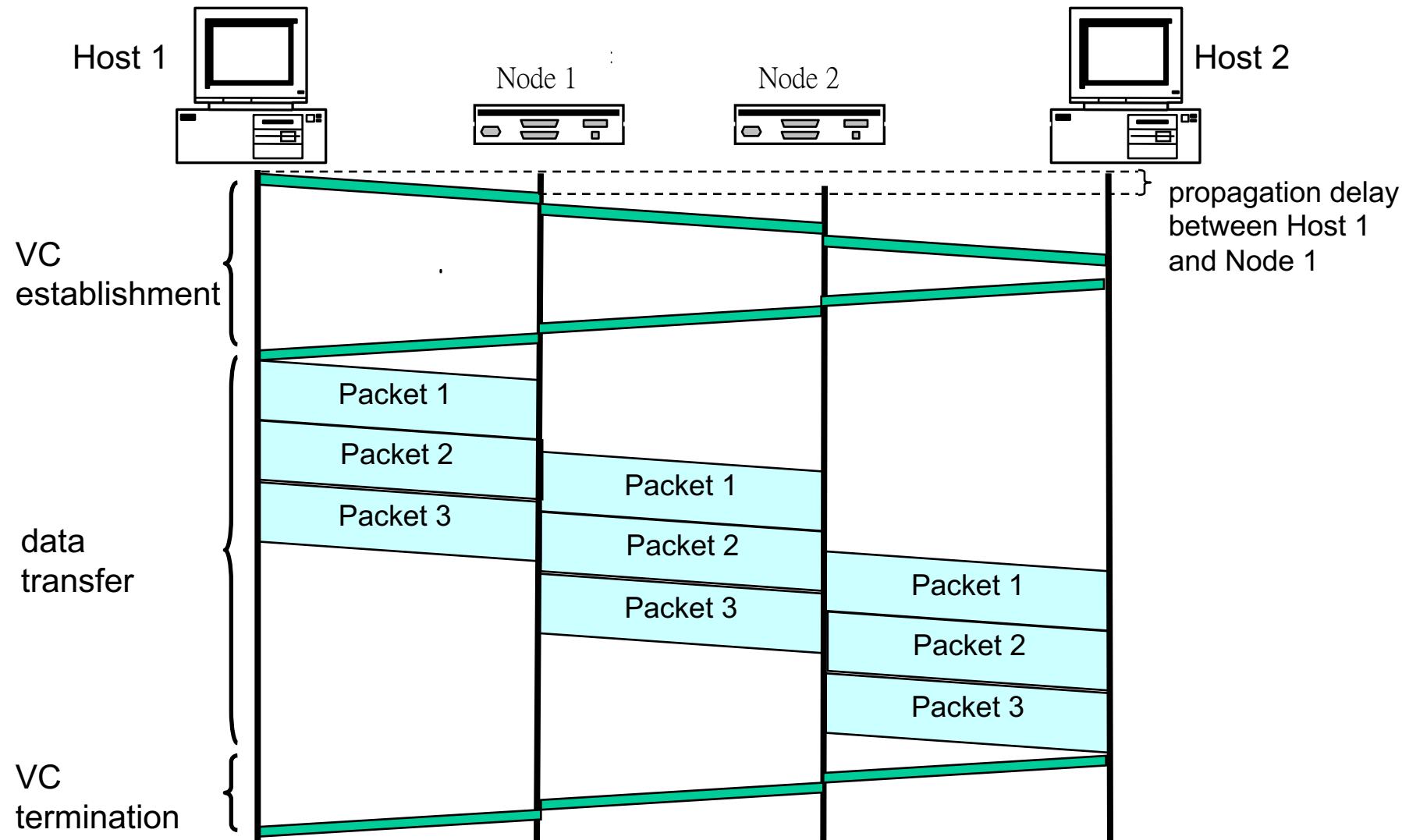
Virtual-Circuit Switching



Virtual-Circuit Packet Switching

- Three phases
 1. VC establishment
 2. Data transfer
 3. VC disconnect

Timing Diagram of Virtual-Circuit Switching

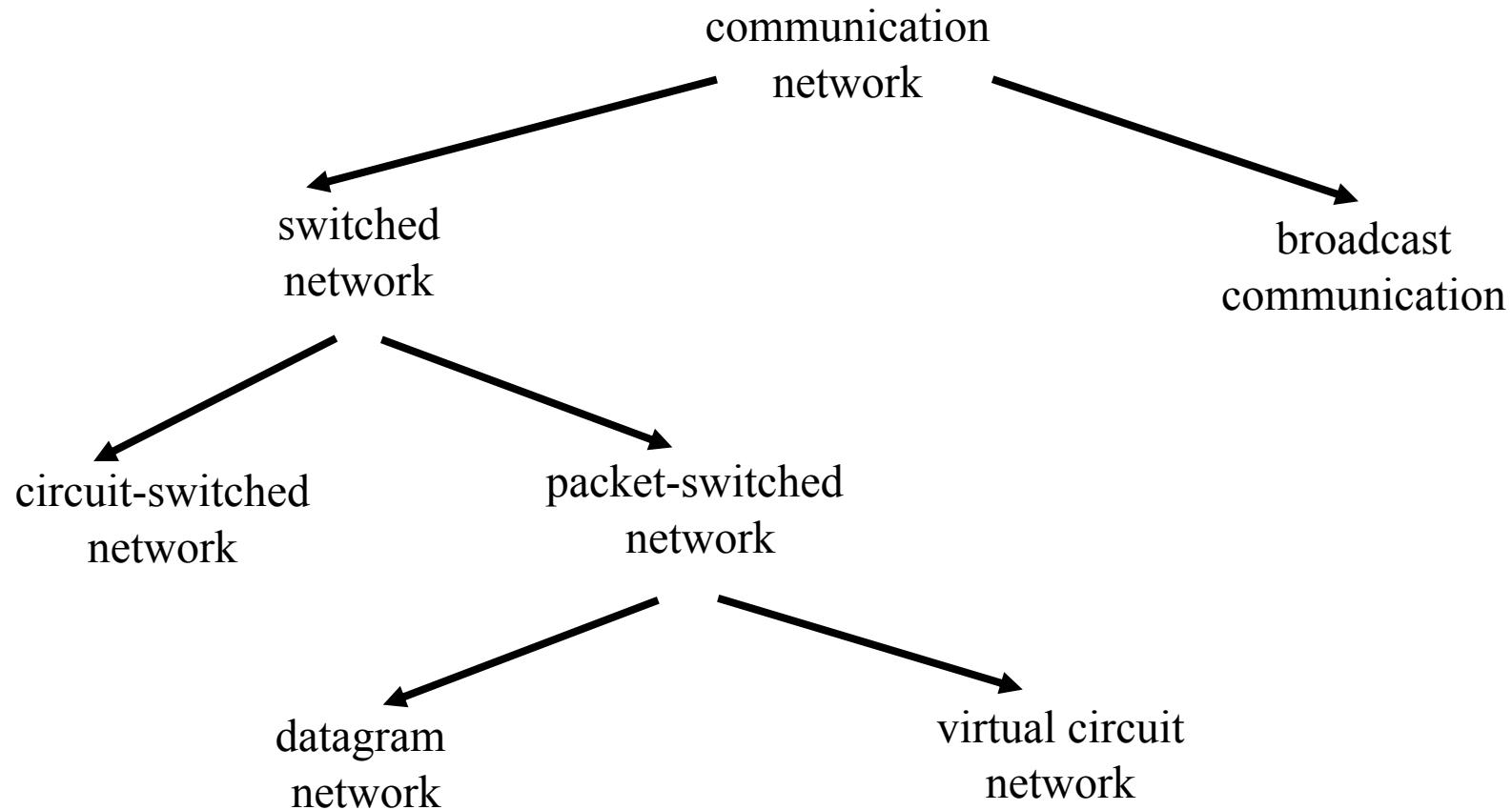


Discussion: Datagram Switching vs. Virtual Circuit Switching

- What are the benefits of datagram switching over virtual circuit switching?

- What are the benefits of virtual circuit switching over datagram switching?

Summary of the Taxonomy of Communication Networks



Summary of Progress

- We have seen the hardware infrastructure, the basic communication scheme, a next key question is how to develop the software system.