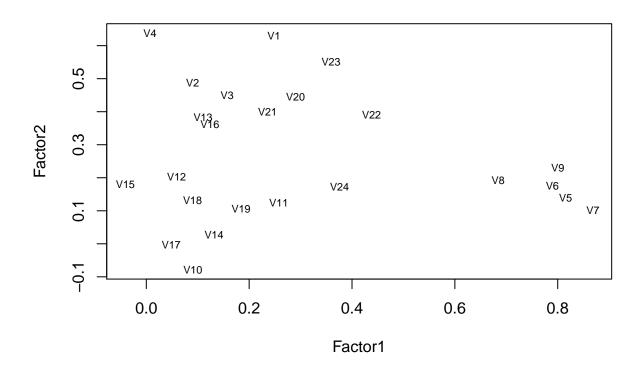
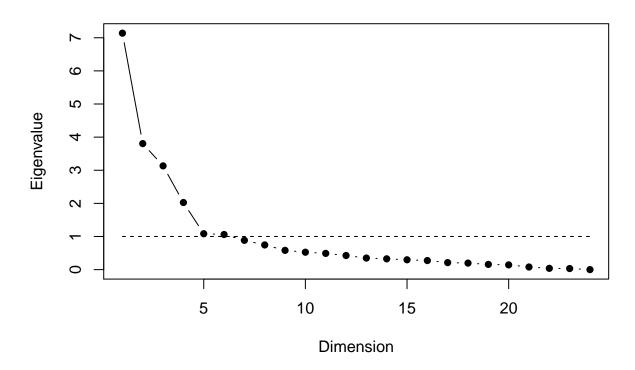
456F2

```
p = read.csv("PSY.csv",header = T)
p = p[,5:28]
head(p)
     V1 V2 V3 V4 V5 V6 V7 V8 V9 V10 V11 V12 V13 V14 V15 V16 V17 V18 V19 V20
## 1 20 31 12 3 40
                    7 23 22
                             9
                                 78
                                     74 115 229 170
                                                      86
                                                          96
                                                               6
                                                                   9
## 2 32 21 12 17 34
                     5 12 22
                              9
                                 87
                                                      85 100
                                                                  12
                                                                          -3
                                     84 125 285 184
                                                              12
                                                                      10
## 3 27 21 12 15 20
                     3 7 12 3
                                 75
                                     49 78 159 170
                                                      85
                                                          95
                                                               1
                                                                   5
                                                                       6
## 4 32 31 16 24 42
                     8 18 21 17
                                 69
                                     65 106 175 181
                                                      80
                                                          91
                                                               5
                                                                   3
                                                                      10
                                                                          -2
                    8 16 25 18 85
## 5 29 19 12 7 37
                                     63 126 213 187
                                                      99 104
                                                              15
                                                                  14
                                                                      14
                                                                          29
## 6 32 20 11 18 31 3 12 25 6 100 92 133 270 164
                                                      84 104
                                                                   6
                                                                      14
     V21 V22 V23 V24
## 1 14
         34
               5 24
     13
## 2
          21
               1 12
## 3
               7 20
      9
         18
## 4 10
         22
               6 19
## 5
     15 19
               4
                  20
## 6
       2 16 10
##########
##Problem1
##########
library(stats)
#a.
#plugging in factor =6, I get that 6 factors can adeautely explain
#base on results from the scree plot and factanal analysis output
p = as.data.frame(scale(p))
res1p = factanal(p,factors = 6, rotation = "varimax", na.action = na.omit)
res1p
##
## Call:
## factanal(x = p, factors = 6, na.action = na.omit, rotation = "varimax")
## Uniquenesses:
##
      V1
            V2
                  VЗ
                        ٧4
                              ۷5
                                    V6
                                          ۷7
                                                 87
                                                       ۷9
                                                            V10
                                                                  V11
                                                                        V12
## 0.488 0.739 0.763 0.547 0.299 0.311 0.214 0.442 0.278 0.037 0.469 0.592
                 V15
                       V16
                             V17
                                   V18
                                          V19
                                                V20
                                                      V21
                                                            V22
                                                                  V23
           V14
## 0.447 0.575 0.555 0.589 0.612 0.726 0.609 0.597 0.530 0.536 0.426 0.468
##
## Loadings:
       Factor1 Factor2 Factor3 Factor4 Factor5 Factor6
##
## V1
        0.248
                0.630
                                0.159
                                                 0.140
                                        0.107
## V2
                0.488
## V3
        0.157
                0.449
## V4
                0.638
                        0.101
                                0.182
## V5
        0.815
                0.140
                        0.119
                                0.143
## V6
        0.790
                0.176
## V7
        0.869
                0.102
                                                 0.106
## V8
        0.684
                0.192
                                0.105
                                         0.167
## V9
        0.800
               0.231
                                         0.125
```

```
## V10
                       0.954
                               0.164
                                               -0.105
## V11 0.258
               0.124
                       0.453
                               0.279
                                       0.128
                                               0.386
## V12
               0.204
                       0.539
                                       0.113
                                               0.235
## V13 0.110
               0.383
                                               0.456
                       0.414
## V14 0.132
                               0.617
                                       0.162
## V15
                               0.627
                                               -0.120
               0.181
## V16 0.124
              0.362
                               0.457
                                       0.220
## V17
                               0.552
                       0.259
                                               0.102
## V18
               0.132
                       0.153
                               0.443
                                       0.124
                                               0.117
## V19 0.184
                                       0.502
               0.106
                               0.275
                                               0.130
## V20
       0.290
               0.445
                               0.218
                                       0.243 -0.121
## V21 0.236
              0.399
                       0.359
                               0.142
                                       0.320
## V22 0.438
               0.392
                               0.101
                                       0.323
## V23 0.359
              0.551
                               0.154
                                       0.274
                       0.181
                                              -0.101
## V24 0.376
              0.173
                       0.345
                               0.192
                                       0.449
##
##
                 Factor1 Factor2 Factor3 Factor4 Factor5 Factor6
## SS loadings
                   4.016
                           2.643
                                   2.020
                                           1.917
                                                   0.996
                                                           0.559
## Proportion Var
                   0.167
                           0.110
                                   0.084
                                           0.080
                                                   0.042
                                                           0.023
## Cumulative Var
                   0.167
                           0.277
                                   0.362
                                           0.441
                                                   0.483
                                                           0.506
##
## Test of the hypothesis that 6 factors are sufficient.
## The chi square statistic is 155.66 on 147 degrees of freedom.
## The p-value is 0.297
#I look at the sums of squared (SS) loadings; these are the eigenvalues,
#or the variance in all variables which is accounted for by that factor
#(i.e., the eigenvalue/# of variables = proportion variance). If a factor has a
#"high" SS loading/eigenvalue, then it is helping to explain the variances in the
#variables. In the factanal() output, the factors are ordered by their eigenvalues,
#with higher eigenvalues first. As factor is important if its
#eigenvalue is greater than 1.
#Base on those information, factors 1-6 appear to be important.
#So six factor model can indeed explain the relationship
#among the variables
#Therefore, I might conclude that 6 factors are enough for this model
#Scree plot code
load1 = res1p$loadings
library(psy)
plot(load1,type="n")
text(load1,labels = names(p),cex=0.7)
```



Scree Plot



#choose 6 factors since their engivalues are larger than 1

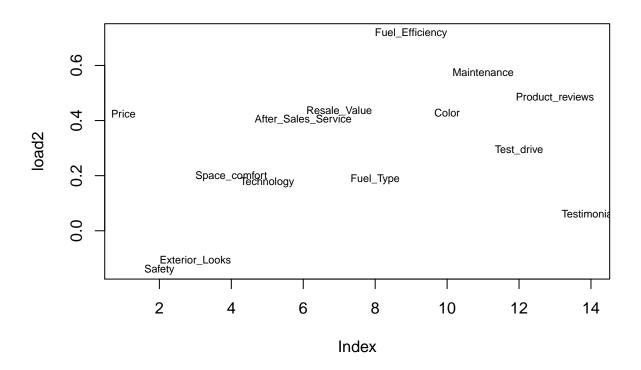
```
load1 = res1p$loadings[,1:2]
load1
```

```
##
            Factor1
                          Factor2
## V1
        0.248346042
                      0.630429035
## V2
        0.089987640
                      0.488103474
  VЗ
##
        0.157270612
                      0.449219675
##
  ۷4
        0.007057571
                      0.637816210
## V5
        0.815272541
                      0.140018254
##
  ۷6
        0.789648169
                      0.176312699
## V7
        0.868559515
                      0.102210686
##
  ٧8
        0.684044352
                      0.192287914
##
  ۷9
        0.800179986
                      0.230863259
        0.090486883 -0.078182626
## V10
## V11
        0.257605778
                      0.124361433
                      0.203651243
## V12
        0.058818886
## V13
        0.110282356
                      0.382597859
## V14
        0.131677255
                      0.028161035
## V15 -0.040601309
                      0.180993829
## V16
        0.123546691
                      0.362168707
## V17
        0.048479326
                     -0.003177894
## V18
        0.089805774
                      0.131595980
## V19
        0.184343199
                      0.106448930
## V20
        0.290130380
                      0.445141522
## V21
        0.235735989
                      0.399384337
```

```
## V22 0.438044519 0.391772164
## V23 0.359196416 0.550931685
## V24 0.375657269 0.173021006
#Interpretation:
##############
#Note: I will give communalities and variance(uniqueness)
#for all 24 variables
###############
#engivalues for the 1st factor ==
loadings_fac1 = res1p$loadings[,1]
eigenv_fac1 = sum(loadings_fac1^2)
eigenv_fac1
## [1] 4.015961
#res1p$uniquenesses
loadings_fac1 = res1p$loading[1,]
communality_fac1 = sum(loadings_fac1^2)
#communalities = 1-uniqueness
#Answer to question(c)
communality_fac1
## [1] 0.5120692
uniqueness_fac1 = 1-communality_fac1
uniqueness_fac1
## [1] 0.4879308
#This is the answer for the (d): specific variances
#variance are simply the uniqueness;
#Give the four plots that helps explain
pcaCharts <- function(x) {</pre>
   x.var <- x$sdev ^ 2
   x.pvar <- x.var/sum(x.var)</pre>
   print("proportions of variance:")
   print(x.pvar)
   par(mfrow=c(2,2))
   plot(x.pvar,xlab="Principal component", ylab="Proportion of variance explained", ylim=c(0,1), type=
   plot(cumsum(x.pvar),xlab="Principal component", ylab="Cumulative Proportion of variance explained",
   screeplot(x)
   screeplot(x,type="1")
   par(mfrow=c(1,1))
#pcaCharts(res1p)
#####################
######Part2
######################
e = read.csv("EFA.csv",header = T)
head(e)
```

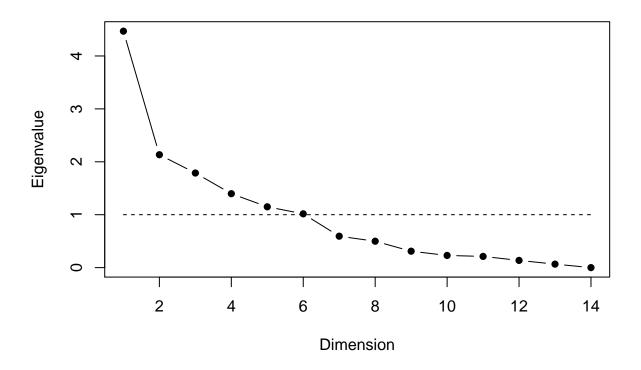
```
Price Safety Exterior_Looks Space_comfort Technology After_Sales_Service
## 1
         4
                 4
                                 5
                                                4
## 2
         3
                5
                                 3
                                               3
                                                           4
                                                                                 4
## 3
         4
                4
                                 3
                                               4
                                                           5
                                                                                 5
                                                3
                                                           3
## 4
         4
                 4
                                 4
                                                                                 4
## 5
         5
                5
                                 4
                                                4
                                                           5
                                                                                 4
                                 5
                                                3
     Resale_Value Fuel_Type Fuel_Efficiency Color Maintenance Test_drive
##
## 1
                5
                           4
                                            4
                                                   2
## 2
                3
                           4
                                            3
                                                   4
                                                                3
                                                                           2
## 3
                5
                           4
                                            5
                                                   4
                                                                5
                                                                           4
## 4
                5
                           5
                                            4
                                                   4
                                                                4
                                                                           2
## 5
                5
                           3
                                            4
                                                   5
                                                                5
                                                                           5
                                                   2
                                                                           2
## 6
                3
                           4
                                            3
                                                                3
     Product_reviews Testimonials
## 1
                    4
## 2
                    2
                                  2
## 3
                    4
                                  3
                                 3
## 4
                    5
                    5
                                  2
## 5
## 6
                    2
                                  3
##########
##Problem1
##########
library(stats)
#a.
#plugging in factor =6, I get that 6 factors can adeautely explain
#base on results from the scree plot and factanal analysis output
res2e = factanal(e,factors = 1, rotation = "varimax", na.action = na.omit)
res2e
##
## Call:
## factanal(x = e, factors = 1, na.action = na.omit, rotation = "varimax")
##
## Uniquenesses:
##
                  Price
                                      Safety
                                                   Exterior Looks
##
                  0.819
                                       0.980
                                                            0.988
##
         Space_comfort
                                 Technology After_Sales_Service
##
                  0.961
                                       0.969
                                                            0.836
##
          Resale Value
                                  Fuel_Type
                                                  Fuel_Efficiency
##
                  0.811
                                       0.965
                                                            0.486
##
                  Color
                                Maintenance
                                                       Test_drive
##
                  0.817
                                       0.669
                                                            0.913
##
                                Testimonials
       Product_reviews
##
                  0.766
                                       0.996
##
## Loadings:
##
                        Factor1
## Price
                         0.425
## Safety
                        -0.141
## Exterior_Looks
                        -0.108
## Space_comfort
                         0.198
## Technology
                         0.176
```

```
## After_Sales_Service 0.405
## Resale_Value
                        0.435
## Fuel_Type
                        0.187
## Fuel_Efficiency
                        0.717
## Color
                        0.428
## Maintenance
                        0.575
## Test drive
                        0.294
## Product_reviews
                        0.484
## Testimonials
##
##
                  Factor1
                    2.025
## SS loadings
## Proportion Var
                    0.145
##
## Test of the hypothesis that 1 factor is sufficient.
## The chi square statistic is 159.92 on 77 degrees of freedom.
## The p-value is 9.35e-08
#I look at the sums of squared (SS) loadings; these are the eigenvalues,
#or the variance in all variables which is accounted for by that factor
#(i.e., the eigenvalue/# of variables = proportion variance). If a factor has a
#"high" SS loading/eigenvalue, then it is helping to explain the variances in the
#variables. In the factanal() output, the factors are ordered by their eigenvalues,
#with higher eigenvalues first. As factor is important if its
#eigenvalue is greater than 1.
#Base on those information, factors 1-6 appear to be important.
#So six factor model can indeed explain the relationship
#among the variables
#Therefore, I might conclude that 6 factors are enough for this model
#Scree plot code
load2 = res2e$loadings
library(psy)
plot(load2,type="n")
text(load2,labels = names(e),cex=0.7)
```



#Determine # of factors to extract : 6 in this case
scree.plot(res2e\$correlation)

Scree Plot



#choose 6 factors since their engivalues are larger than 1