Pseudo Code for Repair Algorithm

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1 Introduction

In this section, we define some important definitions and algorithms....

Definition 1.1. (Mixed Integer Programming)

In this report we consider a generic mixed-integer programming problem (MIP) in the following form

(MIP) min
$$c^T x$$

 $s.t.$ $Ax \ge b$
 $x_j \in \mathbb{Z} \quad \forall j \in \mathcal{I}$
 $x_j \in \mathbb{R} \quad \forall j \in \mathcal{N} \setminus \mathcal{I}$

where the vector $b \in \mathbb{R}^m$ and the vector $c \in \mathbb{R}^n$ are input vectors. A is a input matrix of size $m \times n$, the variable input set $\mathcal{I} \subseteq \mathcal{N} = \{1, 2, ..., n\}$. We denote \mathcal{P} for this problem, which called a mixed-integer programming problem (MIP) with minimize objective function $c^T x$ subject to the constraints $Ax \geq b$. Besides, some variables are restricted to integer values while the else of are restricted to real value. S is a set of feasible solution if S satisfy all the constraints in the problem. A vector s^* with $s^* \in S$ is called optimal solution when $c^T x_{s^*} \leq c^T x_s$ for $\forall s \in S$. When all of the variables are restricted to integer, the problem is called pure integer linear program (IP) for $\mathcal{I} = \mathcal{N}$. If there is no integrality constraint, the program is called linear program

(MIP)
$$\min c^T x$$

 $s.t.$ $Ax \ge b$
 $x_j \in \mathbb{R} \quad \forall j \in \mathcal{N}$

Definition 1.2. (LP-relaxation)

Lp relaxation is obtained by removing all integrity constraints $\mathcal{I} \leftarrow \emptyset$. LP-relaxation is the foundation of LP-based branch-and-bound technology. As the searching space is increase by removing integrity restrictions, the optimal solution in MIP problem could not better than LP-relaxation, which is $s_{MIP}^* \geq s_{LP}^*$. This means the optimal solution found in LP problem could provide a lower or prime bound for MIP problem.

2 Input

- A MIP problem \mathcal{P}^0 with n variables x, constraint set C^0 with an optimal solution s^0 , where s^0 is a n-vector.
- A MIP problem \mathcal{P}^1 with n variables x, constraint set C^1 , such that $C^0 \subseteq C^1$.

3 Output

• An optimal solution s^1 to \mathcal{P}^1 , where s^1 is a n-vector too.

4 Pseudo Code

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Algorithm 1: Solving Problem with Reoptimization
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Input: \mathcal{P}^1 where C^0 \subsetneq C^1 and s^0, k
Output: optimal solution s^* to \mathcal{P}^1
  1 begin
           if s^0 is feasible to \mathcal{P}^1 then
  \mathbf{2}
                  return s^0
  3
            else
  4
                  \alpha \longleftarrow k \times c^T s^0
  \mathbf{5}
                  for j in \mathcal{I} do
  6
                       \mathcal{P}^2 \leftarrow create new variables and add it to \mathcal{P}^1 : y_j

\mathcal{P}^2 \leftarrow add new constraints to \mathcal{P}^2 : y_j \geq x_j - s_j^0
                                                                                                                             // add new variables
  7
                                                                                                                         // add new constraints
  8
                       \mathcal{P}^2 \leftarrow add new constraints to \mathcal{P}^2 : y_j \geq s_j^0 - x_j
\mathcal{P}^2 \leftarrow add penalty function to \mathcal{P}^2 : \alpha \times y_j
  9
                                                                                                                       // add penalty function
10
11
                  end
                  r \longleftarrow 1
12
                  for \alpha \geq 0 do
                        s^r \leftarrow solve \mathcal{P}_r^2 (r-th iteration) to optimal or stop criterion with reoptimization
16
17
                  end
                  s^* \longleftarrow s^r
18
                  return s^*
           end
20
21 end
```