Pseudo Code for Repair Algorithm

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April 5, 2019

1 Introduction

In this section, we define some important definitions and algorithms....

Definition 1.1. (Mixed Integer Programming)
In this report we consider a generic mixed-integer programming problem (MIP) in the following form

$$\begin{aligned} \text{(MIP)} \quad & \min \ c^T x \\ s.t. \quad & Ax \geq b \\ & x_j \in \mathbb{Z} \quad \forall j \in \mathcal{I} \\ & x_j \in \mathbb{R} \quad \forall j \in \mathcal{N} \setminus \mathcal{I} \end{aligned}$$

where the vector $b \in \mathbb{R}^m$ and the vector $c \in \mathbb{R}^n$ are input vectors. A is a input matrix of size $m \times n$, the variable input set $\mathcal{I} \subseteq \mathcal{N} = \{1, 2, \ldots, n\}$. We denote $\mathcal{P}$ for this problem, which called a mixed-integer programming problem (MIP) with minimize objective function $c^T x$ subject to the constraints $Ax \geq b$. Besides, some variables are restricted to integer values while the else of are restricted to real value. S is a set of feasible solution if S satisfy all the constraints in the problem. A vector s^* with $s^* \in S$ is called *optimal solution* when $c^T x_{s^*} \leq c^T x_s$ for $\forall s \in S$. When all of the variables are restricted to integer, the problem is called *pureintegerlinearprogram*(IP) for $\mathcal{I} = \mathcal{N}$. If there is no integrality constraint, the program is called *linearprogram*

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Definition 1.2. (LP-relaxation)
Lp *relaxation* is obtained by removing all integrity constraints $\mathcal{I} \leftarrow \emptyset$. LP-*relaxation* is the foundation of LP-based branch-and-bound technology. As the searching space is increase by removing integrity restrictions, the optimal solution in MIP problem could not better than LP-*relaxation*, which is $s^*_{MIP} \geq s^*_{LP}$. This means the optimal solution found in LP problem could provide a lower or prime bound for MIP problem.

2 Input

- A MIP problem $\mathcal{P}^0$ with n variables x,constraint set C^0 with an optimal solution s^0, where s^0 is a n-vector.
- A MIP problem $\mathcal{P}^1$ with n variables x, constraint set C^1, such that $C^0 \subsetneq C^1$.

3 Output

- An optimal solution s^1 to $\mathcal{P}^1$, where s^1 is a n-vector too.

4 Pseudo Code

Algorithm 1: Solving Problem with Reoptimization

Input: $\mathcal{P}^1$ where $C^0 \subsetneq C^1$ and s^0 , k
Output: optimal solution s^* to $\mathcal{P}^1$

begin
    if s^0 *is feasible to* $\mathcal{P}^1$ **then**
        return s^0
    else
        $\alpha \longleftarrow c^T s^0 \times k$
        for i *in* $\mathcal{I}$ **do**
            $\mathcal{P}^2 \longleftarrow$ create new variables y_i with objective value α and add it to $\mathcal{P}^1$: `// add new variables`
            $\mathcal{P}^2 \longleftarrow$ add new constraints to $\mathcal{P}^2$: $y_i \geq x_i - s_i^0$ `// add new constraints`
            $\mathcal{P}^2 \longleftarrow$ add new constraints to $\mathcal{P}^2$: $y_i \geq s_i^0 - x_i$
        end
        enable Reoptimization Feature
        stop gap $\longleftarrow 0.5$
        $j \longleftarrow$ number of variables in y
        coefs [ ] $\longleftarrow$ array of coefficients for all varialbes in $\mathcal{P}^2$
        if *the sense of* $\mathcal{P}^2$ *is minimize* **then**
            the sense of $\mathcal{P}^2 \longleftarrow$ *minimize*
        end
        $r \longleftarrow 1$
        while $k > 0$ **do**
            solving the sub-MIP problem in r-th iteration to stop criterion
            frees branch and bound tree and all solution process data
            $k \longleftarrow k - 1$
            $\alpha \longleftarrow \alpha \times k$
            change the last j coefficients in coefs[ ] $\longleftarrow \alpha$
            $r \longleftarrow r + 1$
        end
        stop gap $\longleftarrow 0.0$
        $s^* \longleftarrow$ solve the sub-MIP problem in the last interation
        if s^* *is feasiable to* $\mathcal{P}^1$ **then**
            return s^*
        end
    end
end