

1.

(a) True

(b) True

(c) True

(d) False

(e) True

(f) False

(g) True

2.

(a) for $i = 1$ to $A.length - 1$

$min = i$

 for $j = i + 1$ to $A.length$

 if $A[j] < A[min]$

$min = j$

$A[i], A[min] = A[min], A[i]$

(b) Before the start of each iteration of the outer loop, the subarray from $A[i]$ to $A[i-1]$ contains the smallest elements of the original array and is sorted. The rest of the array contains the remaining elements in no particular order.

(c) The best-case and worst-case running times of selection sort are both $\Theta(n^2)$ since every element is compared with every other element.

3.

(a) def MOVE(n, start, end):

if n == 1:

PRINT(start, end)

else:

mid = (start + end) // 2

MOVE(n-1, start, mid)

PRINT(start, end)

MOVE(n-1, mid, end)

(b) $f(n) = 2f(n-1) + 1$

Since $f(1) = 1 = 2^1 - 1$

$$f(2) = 2f(1) + 1 = 2^2 - 2 + 1 = 2^2 - 1$$

$$f(3) = 2f(2) + 1 = 2^3 - 2 + 1 = 2^3 - 1$$

$$\dots$$
$$f(n) = 2^n - 1$$

4.

$$(a) T(n) = 2T(n-a) + T(n)$$

$$(b) a = \sqrt{n}$$

$$\left(\right) (2^{\sqrt{n}} - 1)$$

$$2^{\sqrt{n}} - 1$$

$$L=0$$

$$2(2^{\sqrt{n}} - 1)$$

$$L=1$$

$$2^{\sqrt{n}-1} \cdot (2^{\sqrt{n}} - 1)$$

$$L = \sqrt{n} - 1$$

$$\begin{aligned} T(n) &= (2^{\sqrt{n}} - 1) \cdot (2 + 4 + 8 + \dots + 2^{\sqrt{n}-1}) \\ &= (2^{\sqrt{n}} - 1) (2^{\sqrt{n}} - 2) \\ &\leq 2^{\sqrt{n}} \cdot 2^{\sqrt{n}} = 2^{2\sqrt{n}} \end{aligned}$$

Therefore, $c=2$ is sufficient for $T(n) \leq 2^{cn}$