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Compilation Principle 编译原理

第16讲：中间代码(1)

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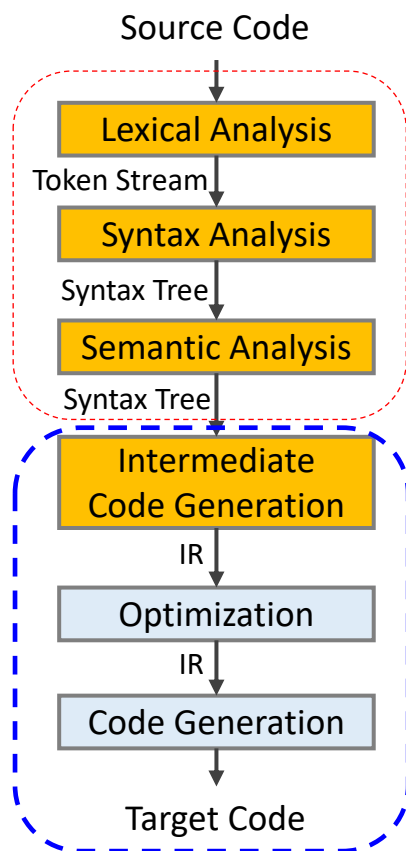
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Compilation Phases[编译阶段]



正确

Front End
(Analysis)

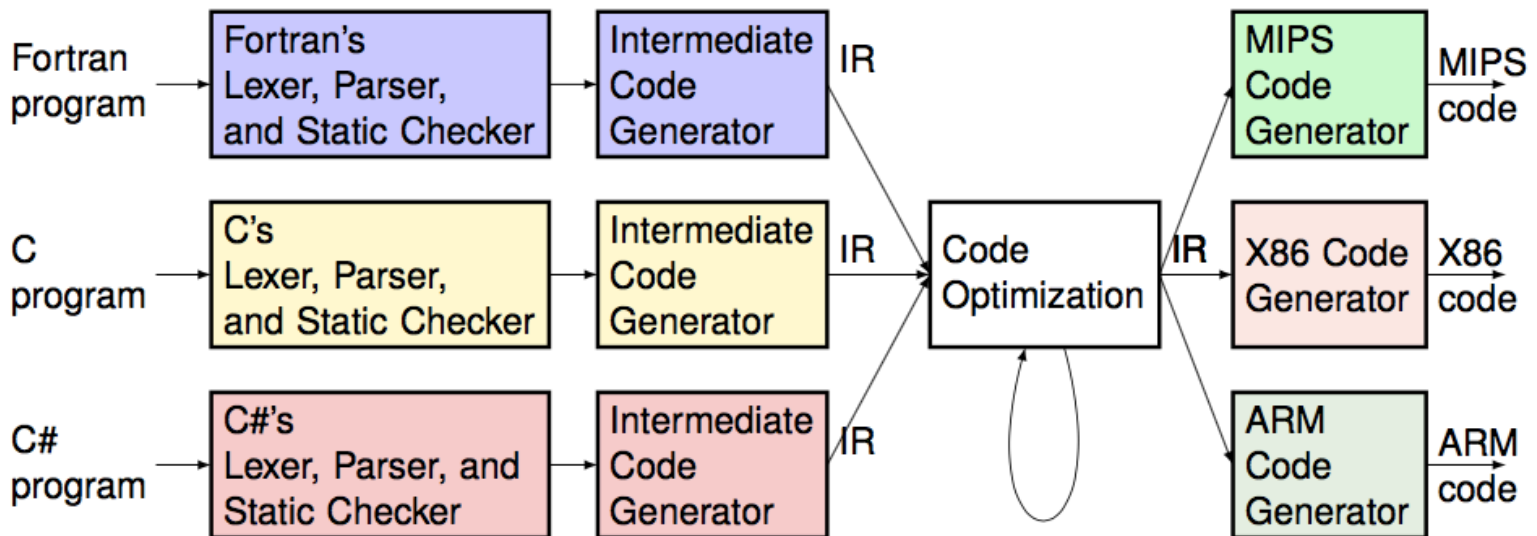
效率

Back End
(Synthesis)

- **Lexical:** source code \rightarrow tokens
 - RE, NFA, DFA, ...
 - Is the program **lexically** well-formed?
 - E.g., $x\#y = 1$
- **Syntax:** tokens \rightarrow AST or parse tree
 - CFG, LL(1), LALR(1), ...
 - Is the input program **syntactically** well-formed?
 - E.g., $x = 1 \ y = 2$
- **Semantic:** AST \rightarrow AST +symbol table
 - SDD, SDT, typing, scoping, ...
 - Does the input program has a well-defined **meaning**?
 - E.g., $\text{int } x; y = x(1)$

Modern Compilers

- Compilation flow [编译流程]
 - First, translate the source program to some form of intermediate representation (IR, 中间表示)
 - Then convert from there into machine code
- IR provides advantages [IR的优势]
 - Increased abstraction, cleaner separation, and retargeting, etc



Different IRs for Different Stages

- Modern compilers use different IRs at different stages
- **High-Level** IR: close to high-level language
 - Examples: Abstract Syntax Tree, Parse Tree
 - **Language dependent** (a high-level IR for each language)
 - Purpose: semantic analysis of program
- **Low-Level** IR: close to assembly
 - Examples: Three address code[三地址码], Static Single Assignment[静态单赋值]
 - Essentially an instruction set[指令集] for an abstract machine
 - **Language and machine independent** (one common IR)
 - Purpose: compiler optimizations to make code efficient
 - All optimizations written in this IR is automatically applicable to all languages and machines

Different IRs for Different Stages (cont.)

- **Machine-Level IR**

- Examples: x86 IR, ARM IR, MIPS IR
- Actual instructions for a concrete machine ISA
- **Machine dependent** (a machine-level IR for each ISA)
- Purpose: code generation / CPU register allocation
 - (Optional) Machine-level optimizations (e.g. strength reduction: $x / 2 \rightarrow x \gg 1$)

- Possible to have one IR (AST) — some compilers do

- Generate machine code from AST after semantic analysis
- Makes sense if compilation time is the primary concern (e.g. JIT)
 - Skip the IR generation step

- So why have multiple IRs?

Why Multiple IRs?

- Why multiple IRs?
 - Better to have an appropriate IR for the task at hand [针对性]
 - Semantic analysis much easier with AST
 - Compiler optimizations much easier with low-level IR
 - Register allocation only possible with machine-level IR
 - Easier to add a new front-end (language) or back-end (ISA) [易于扩展]
 - Front-end: a new AST → low-level IR converter
 - Back-end: a new low-level IR → machine IR converter
 - Low-level IR acts as a bridge between multiple front-ends and back-ends, such that they can be reused
- If one IR (AST), and adding a new front-end ...
 - Reimplement all compiler optimizations for new AST
 - A new AST → machine code converter for each ISA
 - Same goes for adding a new back-end

Three-Address Code[三地址码]

- High-level assembly where each operation has **at most three** operands. Generic form is $X = Y \text{ op } Z$ [最多3个操作数]
 - where X, Y, Z can be variables, constants, or compiler-generated temporaries holding intermediate values
- Characteristics [特性]
 - Assembly code for an 'abstract machine'
 - Long expressions are converted to multiple instructions
 - Control flow statements are converted to jumps [控制流->跳转]
 - Machine independent
 - Operations are generic (not tailored to specific machine)
 - Function calls represented as generic call nodes
 - Uses symbolic names rather than register names (actual locations of symbols are yet to be determined)
- Design goal: for easier machine-independent optimization

Three-Address Code Example

- For example, $x * y + x * y$ is translated to
 - $t1 = x * y$; $t1, t2, t3$ are temporary variables
 - $t2 = x * y$
 - $t3 = t1 + t2$
 - Can be generated through a depth-first traversal of AST
 - Internal nodes in AST are translated to temporary variables
- Notice: repetition of $x * y$ [重复]
 - Can be later eliminated through a compiler optimization called common subexpression elimination (CSE): [通用子表达式消除]
 - $t1 = x * y$
 - $t3 = t1 + t1$
 - Using 3-address code rather than AST makes it:
 - Easier to spot opportunities (just find matching RHSs)
 - Easier to manipulate IR (AST is much more cumbersome)

Three-Address Statements

- Assignment statement [二元赋值]

$x = y \text{ op } z$

where op is an arithmetic or logical operation (binary operation)

- Assignment statement [一元赋值]

$x = \text{op } y$

where op is an unary operation such as -, not, shift

- Copy statement [拷贝]

$x = y$

- Unconditional jump statement [无条件跳转]

$\text{goto } L$

where L is label

Three-Address Statements (cont.)

- Conditional jump statement [条件跳转]

`if (x relop y) goto L`

where relop is a relational operator such as `=, \neq , >, <`

- Procedural call statement [过程调用]

`param x_1 , ..., param x_n , call F_y , n`

As an example, `foo(x_1 , x_2 , x_3)` is translated to

`param x_1`

`param x_2`

`param x_3`

`call foo, 3`

- Procedural call return statement [过程调用返回]

`return y`

where y is the return value (if applicable)

Three-Address Statements (cont.)

- Indexed assignment statement [索引]

$x = y[i]$

or

$y[i] = x$

where x is a scalar variable and y is an array variable

- Address and pointer operation statement [地址和指针]

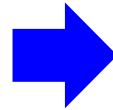
$x = \& y$; a pointer x is set to address of y

$y = * x$; y is set to the value of location
; pointed to by pointer x

$*y = x$; location pointed to by y is assigned x

Example

```
i = 1
do {
    a[i] = x * 5;
    i ++;
} while (i <= 10);
```



```
i = 1
L: t1 = x * 5
    t2 = &a
    t3 = sizeof(int)
    t4 = t3 * i
    t5 = t2 + t4
    *t5 = t1
    i = i + 1
    if i <= 10 goto L
```

a[i]

Source program

Three-address code

Implementation of TAC

- 3 possible ways (and more)
 - quadruples [四元式]
 - triples [三元式]
 - indirect triples [间接三元式]
- Trade-offs between, space, speed, ease of manipulation
- Using quadruples [四元式]

op arg1, arg2, result

- There are four(4) fields at maximum
- arg1 and arg2 are optional, depending on the *op*
- Examples:

□ $x = a + b$	=> + a, b, x
□ $x = -y$	=> - y, , x
□ goto L	=> goto , , L

Using Triples [三元式]

- Triple: quadruple without the result field
 - Result field is implicitly index of instruction
 - Result referred to by index of instructions computing it
 - Example: $a = b * (-c) + b * (-c)$

	Quadruples				Triples		
	op	arg1	arg2	result	op	arg1	arg2
(0)	-	c		t1	-	c	
(1)	*	b	t1	t2	*	b	(0)
(2)	-	c		t3	-	c	
(3)	*	b	t3	t4	*	b	(2)
(4)	+	t2	t4	t5	+	(1)	(3)
(5)	=	t5		a	=	a	(4)

More About Triples

- What if LHS of assignment is not a var but an expression?
 - Array location (e.g. $x[i] = y$)
 - Pointer location (e.g. $*(x+i) = y$)
 - Struct field location (e.g. $x.i = y$)
- Compute memory address of LHS location beforehand
- Example: triples for array assignment statement

$x[i] = y$

- is translated to

$(0): [] \ x \ i$ // Compute address of $x[i]$ location

$(1): = (0) \ y$ // Assign y to that location

- Complex LHS may require more triples to compute address

Using Indirect Triples [间接三元式]

- Problem with triples

- Compiler optimizations often involve moving instructions
- Hard to move instructions because numbering will change, even for instructions not involved in optimization
- See below CSE performed on the second $(-c) * b$:

Quadruples					Triples		
	op	arg1	arg2	result	op	arg1	arg2
(0)	-	c		t1	-	c	
(1)	*	b	t1	t2	*	b	(0)
(2)	-	c		t3	-	c	
(3)	*	b	t3	t4	*	b	(2)
(4) (2)	+	t2	t4 t2	t5	+	(1)	(3) (1)
(5) (3)	=	t5		a	=	a	(4) X

Using Indirect Triples [间接三元式]

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- See below CSE performed on second $(-c) * b$:

	Quadruples				Triples		
	op	arg1	arg2	result	op	arg1	arg2
(0)	-	c		t1	-	c	
(1)	*	b	t1	t2	*	b	(0)
(2)	+	t2	t2	t5	+	(1)	(1)
(3)	=	t5		a	=	a	(4)

Instruction (3) refers to (4) which is no longer there.

Using Indirect Triples (cont.)

- Triples are stored in a triple 'database'
- IR is a listing of pointers to triples in database
 - Can reorder listing without changing numbering in database
- Pointer indirection overhead but allows easy code motion

	Listing
	(ptr to triple database)
(0)	(0)
(1)	(1)
(2)	(2)
(3)	(3)
(4)	(4)
(5)	(5)

	Database		
	op	arg1	arg2
(0)	-	c	
(1)	*	b	(0)
(2)	-	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	=	a	(4)

After CSE Optimization

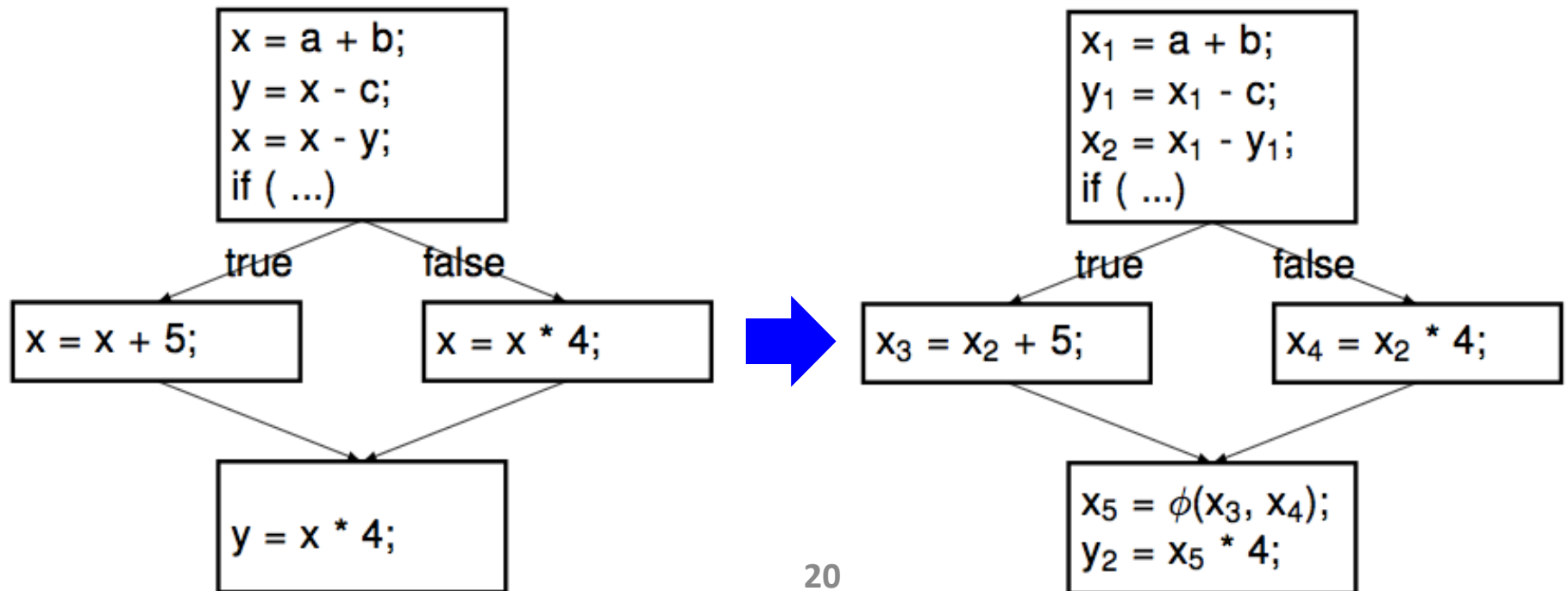
- After CSE, empty entries in database can be reused
 - Code in triple database becomes non-contiguous over time
 - That's fine since the listing is the code, not the database

	Listing
	(ptr to triple database)
(0)	(0)
(1)	(1)
(2)	(4)
(3)	(5)

	Database		
	op	arg1	arg2
(0)	-	c	
(1)	*	b	(0)
(2)	empty		
(3)	empty		
(4)	+	(1)	(1)
(5)	=	a	(4)

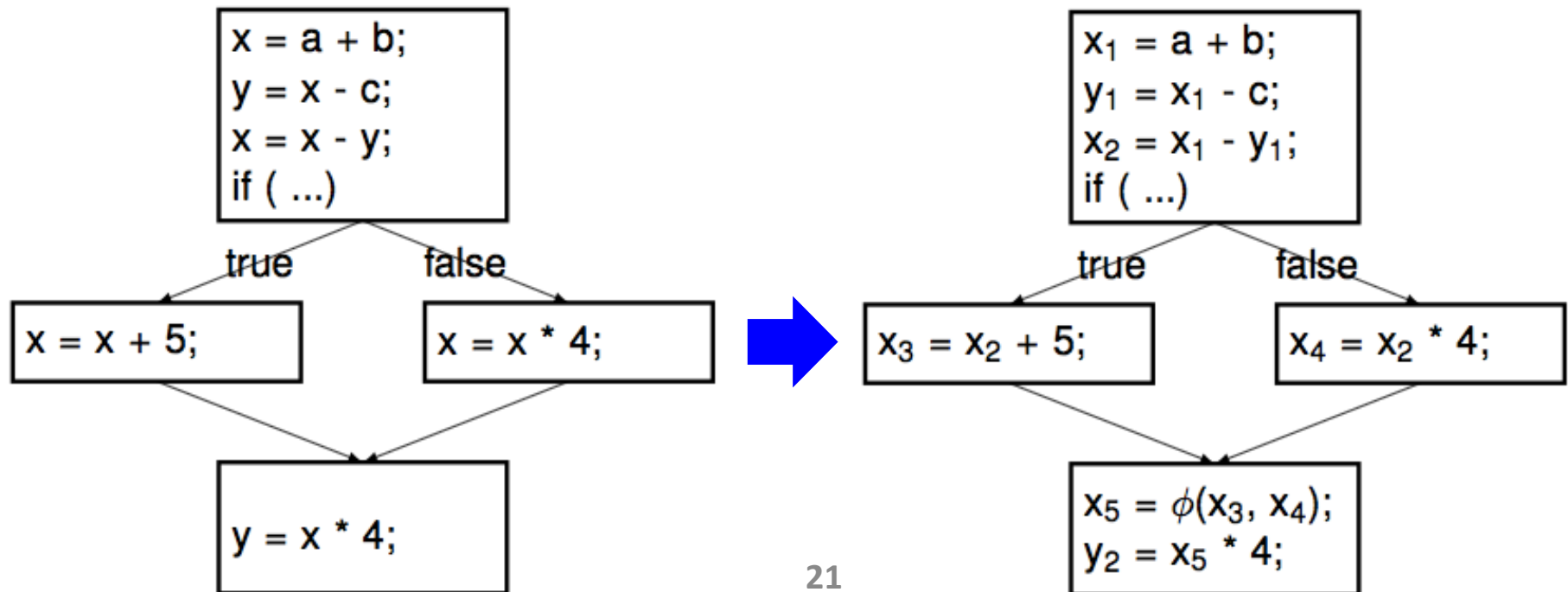
Single Static Assignment [静态单赋值]

- Every variable is assigned to exactly once statically
 - Give variable different version name on every assignment
 - e.g. $x \rightarrow x_1, x_2, \dots, x_5$ for each static assignment of x
 - Now value of each variable guaranteed not to change
 - On a control flow merge, ϕ -function combines two versions
 - e.g. $x_5 = \phi(x_3, x_4)$: means x_5 is either x_3 or x_4



Benefits of SSA

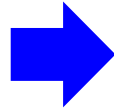
- SSA is an IR that facilitates certain code optimizations
 - SSA tells you when an optimization shouldn't happen
 - Suppose compiler performs CSE on previous example:
 - Without SSA, (incorrectly) tempted to eliminate second $x * 4$
 - With SSA, $x_2 * 4$ and $x_5 * 4$ are clearly different values



Benefits of SSA (cont.)

- SSA is an IR that facilitates certain code optimizations
 - SSA tells you when an optimization should happen
 - Suppose compiler performs dead code elimination (DCE): (DCE removes code that computes dead values)

```
x = a + b;  
x = c - d;  
y = x * b;
```



```
x1 = a + b;  
x2 = c - d;  
y1 = x2 * b;
```

- Without SSA, not clear whether there are dead values
 - With SSA, x_1 is never used and clearly a dead value
- Why does SSA work so well with compiler optimizations?
 - SSA makes flow of values explicit in the IR
 - Without SSA, need a separate dataflow graph
 - Will discuss more in **Compiler Optimization** section

SSA Orthogonal to IR Implementation

- SSA is expressed most commonly as 3-address code
- We learned 3 ways to implement 3-address code
 - quadruples
 - triples
 - indirect triples
- How you implement is orthogonal to SSA representation
 - After variable renaming, any 3-address code becomes SSA
- SSA is used widely in modern compilers:
 - GCC (GNU C Compiler)
 - LLVM (Low Level Virtual Machine) Compiler
 - Oracle Java JIT Compiler
 - Google Chrome JavaScript JIT Compiler
 - PyPy Python JIT Compiler

Generating Code

using Syntax Directed Translation

Syntax Directed Translation[语法制导翻译]

- Syntax directed translation used again for code generation
 - Since code generation is also dependent on syntax
 - Code generation is translating syntactic structures to code
- What language structures do we need to translate?
 - Definitions (variables, functions, ...)
 - Assignment statements
 - Control flow statements (if-then-else, for-loop, ...)
 - ...
- We are going to use the following strategy:
 - Specify SDD semantic rules (without ordering)
 - Convert SDD rules to SDT actions (with ordering)
 - In the process, we will discover SDD has non-*L-attributes*
 - We will also discuss what to do with those non-*L-attributes*

Code Generation Overview [代码生成]

- Program code is a collection of functions
 - By now, all functions are listed in symbol table
- Goal is to generate code for each function in that list
- Generating code for a function involves two steps:
 - Processing variable definitions [变量定义]
 - Involves laying out variables in memory
 - Processing statements [语句]
 - Involves generating instructions for statements
- We will start with processing variable definitions

Processing Variable Definitions

- To lay out a variable, both **location** and **width** are needed
 - Location: where variable is located in memory
 - Width: how much space variable takes up in memory
- Attributes for variable definition:
 - **T V** e.g. int x;
 - **T**: non-terminal for type name
 - **T.type**: type (int, float, ...)
 - **T.width**: width of type in bytes (e.g. 4 for int)
 - **V**: non-terminal for variable name
 - **V.type**: type (int, float, ...)
 - **V.width**: width of variable according to type
 - **V.offset**: offset of variable in memory
 - But offset from what...?

Calculate Variable Location from Offset

- Naive method: reserve a big memory section for all data
 - Size data section to be large enough to contain all variables
 - $\text{Location} = \text{var offset} + \text{base of data section}$
- Naive method wastes a lot of memory
 - Vars with limited scope need to live only briefly in memory
 - E.g. function variables need to last only for duration of call
- **Solution:** allocate memory briefly for each scope
 - Allocate when entering scope, free when exiting scope
 - Variables in same scope are allocated / freed together
 - $\text{Location} = \text{var offset} + \text{base of scope memory section}$
 - Will discuss more later in **Runtime Management**

Storage Layout of Variables in a Function

- When there are multiple variables defined in a function,
 - Compiler lays out variables in memory sequentially
 - Current offset used to place variable x in memory
 - $\text{address}(x) \leftarrow \text{offset}$
 - $\text{offset} += \text{sizeof}(x.\text{type})$

```
void foo() {  
    int a;  
    int b;  
    long long c;  
    int d;  
}
```

Address

0x0000

a

Offset = 0

$\text{Addr}(a) \leftarrow 0$

0x0004

b

Offset = 4

$\text{Addr}(b) \leftarrow 4$

0x0008

c

Offset = 8

$\text{Addr}(c) \leftarrow 8$

0x000c

c

0x0010

d

Offset = 16

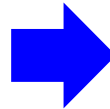
$\text{Addr}(d) \leftarrow 16$

Offset = 20

More about Storage Layout

- Allocation alignment [对齐]
 - Enforce $\text{addr}(x) \% \text{sizeof}(x.\text{type}) == 0$
 - Most machine architectures are designed such that computation is most efficient at $\text{sizeof}(x.\text{type})$ boundaries
 - E.g. Most machines are designed to load integer values at integer word boundaries
 - If not on word boundary, need to load two words and shift & concatenate → inefficient

```
void foo() {  
    char a;      // addr(a) = 0  
    int b;       // addr(b) = 1  
    int c;       // addr(c) = 5  
    long long d; // addr(d) = 9  
}
```



```
void foo() {  
    char a;      // addr(a) = 0  
    int b;       // addr(b) = 4  
    int c;       // addr(c) = 8  
    long long d; // addr(d) = 16  
}
```

More about Storage Layout (cont.)

- Endianness [字节序]

- Big endian: MSB (most significant byte) in lowest address
- Little endian: LSB (least significant byte) in lowest address

