ST/02 Week 15

Settings: given an i.i.d. random sample $\{X_i, J_i^n\}$ from some population with mean u and variance o^2 .

and actually $\widehat{\mu} = \overline{X}$

Fact $MSE(\hat{\mu}) := E[(\hat{\mu} - \mu)^2] = \frac{\sigma^2}{n}$

Quite often ue can only approximate it.

By CLT we know, we nis large,

 $\overline{X} \stackrel{\text{approx}}{\sim} N(\mu, \frac{\alpha^2}{n})$

Then,

 $P(1.\overline{X} - \mu) = 1.96 \frac{O}{\sqrt{n}}) \approx 0.95$

P(1x-M1 = 1.96 \frac{S}{\int_n}) \approx 0.95

Def. The estimated standard error of \overline{X} is

 $E.S.E.(\widehat{X}) := \frac{S}{\sqrt{n}} = \left[\frac{1}{n(n-1)} \frac{h}{n(n-1)} (X_i - \widehat{X})^2 \right]^{\frac{1}{2}}$

Def. Let $L(0) = f(x_1,, x_n; 0)$ be the joint prob.
(density) function of r.v.'s \-X; yn. The maximum
likelihood estimator of 0 is
when the common of the common
G = max L(O)
RK. Log-likelihood: -los:= ln[L(0)]
Rk. (Invariance Principle)
If $\hat{\partial}$ is MLE of $\hat{\partial}$, the $\hat{\beta} = g(\hat{\partial})$ is MLE of $g(\hat{\partial})$.
2) 0 / / (22) 0 / W.Z. / O (3 / 12)
(Not as easy to understand as it looks)
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