

# Ionization of biological molecules by multicharged ions by using the stoichiometric model

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## Abstract

In the present work, we investigate the ionization of molecules of biological interest by the impact of multicharged ions in the intermediate to high energy range. We performed full non-perturbative distorted-wave calculations (CDW) for thirty-six collisional systems. Six atomic targets compose these systems: H, C, N, O, F and S –which are the constituents of most of the DNA and biological molecules– and six charged projectiles (antiprotons, H, He, B, C, and O). On account of the radiation damage caused by secondary electrons, we also inspect the energy and angular distributions of the emitted electrons from the atomic targets. We examine seventeen molecules: DNA and RNA bases, DNA backbone, pyrimidines, tetrahydrofuran (THF), and several  $C_nH_n$  compounds. We show that the simple stoichiometric model (SSM), which approximates the molecular ionization cross sections as a linear combination of the atomic ones, gives reasonably good results for complex molecules. We also inspect the extensively used Toburen scaling of the total ionization cross sections of molecules with the number of weakly bound electrons. Based on the present atomic CDW results, we propose new active electron numbers. The CDW-based scaling improves significantly the single curve behavior for all the targets and ions studied here, from the intermediate to the high energy region. Furthermore, the new scaling describes well the available experimental data for proton impact, including small molecules such as  $H_2$ , water, methane, and ammonia. For completeness, we perform full molecular calculations for five nucleobases and test a modified stoichiometric formula based on the Mulliken charge of the composite atoms. The difference introduced by the new stoichiometric formula is less than 3%, which indicates the reliability and robustness of the SSM to deal with this type of molecules. The results of the extensive ion-target examination included in the present study allow us to assert that the SSM and the CDW-based scaling will be useful tools in this area.

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## I. INTRODUCTION

The damage caused by the impact of multicharged heavy projectiles on biological targets has become a field of interest due to its recent implementation in ion-beam cancer therapy. The effectiveness of the radiation depends on the choice of the ions. In particular, theoretical and experimental studies with different projectiles have concluded that charged carbon ions could be the most suitable ions to be used. Nonetheless, the study of such systems represents a challenge from the theoretical point of view.

The ionization of biological molecules by multicharged ions constitutes the primary damage mechanism. The most widely used method to predict such processes is the first Born approximation. At high energies, this perturbative method warrants the  $Z^2$  laws, where  $Z$  is the projectile charge. However, the damage is concentrated in the vicinities of the Bragg peak—at energies of hundreds of keV/amu—, precisely where the Born approximation starts to fail. Another theoretical issue arises due to the targets themselves; we are dealing with complex molecules, and the description of such targets represents a hard task for *ab initio* calculations. The objective of this article is to deal with these two aspects; first, we perform more appropriate calculations on the primary damage mechanism, which can replace the Born results. Second, we inspect and test a stoichiometric model to describe the ionization of molecular targets.

To overcome the first perturbative approximation limitations, and since the projectiles are multicharged ions, we resort to the Continuum Distorted Wave–Eikonal Initial State (CDW) [1–3], which includes higher perturbative corrections. Details on the CDW calculation are given in Section II. We start from the premise that the ionization process is the mechanism that deposits the most significant amount of primary energy. Moreover, the residual electrons from the ionization are known to be a source of significant local biological damage. The secondary electrons are included in Monte Carlo simulations, and hence their behavior requires further investigation. In Section II A and II B, we calculate the mean energy and angular distributions of the ejected electrons. Surprisingly, we found a substantial dependence on the projectile charge, which is unexpected in the first Born approximation.

In Section III A, we deal with the molecular structure complexity of the targets by implementing the simplest stoichiometric model (SSM): the molecules are assumed to be composed of isolated independent atoms, and the total cross section by a linear combination

of stoichiometric weighted atomic calculations. By implementing the CDW and the SSM, we calculate ionization cross section of several molecules of biological interest, including DNA and RNA molecules, such as adenine, cytosine, guanine, thymine, uracil, tetrahydrofuran (THF), pyrimidine, and DNA backbone, by the impact of antiprotons,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ . In Section III B, we test the Toburen scaling rule [4, 5], which states that the ratio between the ionization cross section and the number of weakly bound electrons can be arranged in a narrow universal band in terms of the projectile velocity. We applied this rule to several hydrocarbons and nucleobases and noted that the width of the resulting universal band could be significantly reduced if we consider the number of active electrons in the collision based on the CDW results for the different atoms. The new scaling was then tested theoretically and by comparison with experimental data available.

The approach SSM considers the atoms in the molecule as neutral, which is not correct. In Section III C, we used the molecular electronic structure code GAMESS [6] to calculate the excess or defect of electron density on the atoms composing the molecules. Then, we modified the SSM to account for the departure from the neutrality of the atoms. We find that the modified SSM for the DNA molecules does not introduce substantial changes in the cross sections.

## II. THEORY: IONIZATION OF ATOMS

In the present study, we consider six atoms,  $\alpha = H, C, N, O, P,$  and  $S$ , and six projectiles, antiprotons  $\bar{p}$ ,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ . Most of the organic molecules are composed of these atoms. Some particular molecules also include halogen atoms such as fluor and bromine; ionization cross sections of these elements have been previously published [2].

The total ionization cross sections of these atoms were calculated using the CDW. The initial bound and final continuum radial wave functions were obtained by using the RADIALF code, developed by Salvat and co-workers [7], and a Hartree-Fock potential obtained from the Depurated Inversion Method [8, 9]. We used a few thousand pivot points to solve the Schrödinger equation, depending on the number of oscillations of the continuum state. The radial integration was performed using the cubic spline technique. We expand our final

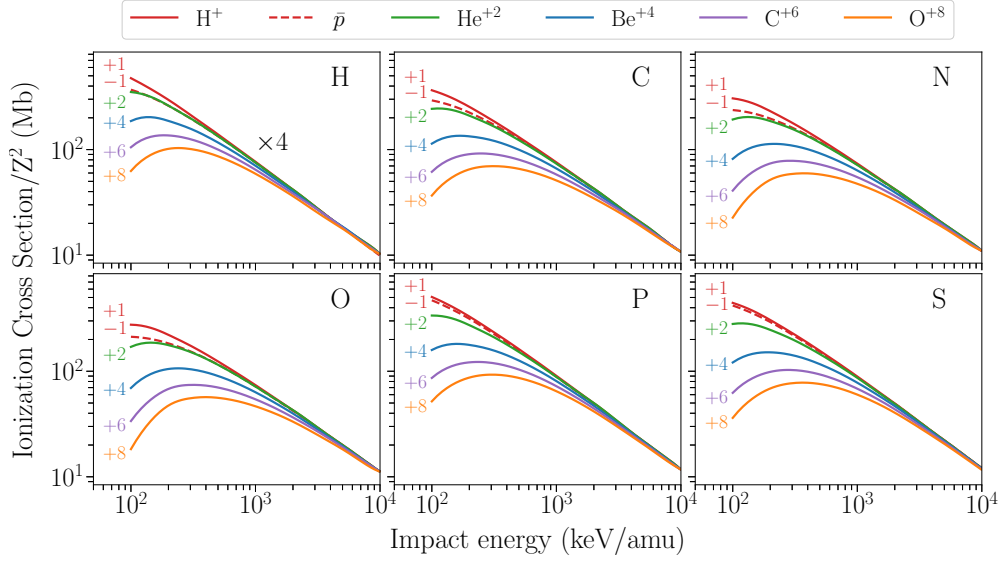


FIG. 1: Reduced CDW total ionization cross section of six atomic targets. The curves are labeled with the charge state corresponding to the six multicharged projectiles.

continuum wave function as usual,

$$\psi_{\vec{k}}^{-}(\vec{r}) = \sum_{l=0}^{l_{\max}} \sum_{m=-l}^l R_{kl}^{-}(r) Y_l^m(\hat{r}) Y_l^{m*}(\hat{k}). \quad (1)$$

The number of angular momenta considered varied from 8, at very low ejected-electron energies, up to  $l_{\max} \sim 30$ , for the highest energies considered. The same number of azimuth angles were required to obtain the four-fold differential cross section. The calculation performed does not display prior-post discrepancies at all. Each atomic total cross section was calculated using 35 to 100 momentum transfer values, 28 fixed electron angles, and around 45 electron energies depending on the projectile impact energy. Further details of the calculation are given in Ref. [10].

We display our total CDW ionization cross sections for the six essential elements by the impact of the six projectiles in Fig. 1. To reduce the resulting 36 magnitudes into a single consistent figure, we considered the fact that in the first Born approximation the ionization cross section scales with the square of the projectile charge,  $Z^2$ . The impact energies considered range between 0.1 to 10 MeV/amu, where the CDW is supposed to hold. In fact, for the highest projectile charges the minimum impact energy where the CDW is expected to be valid could be higher than 100 keV. We also performed similar calculations with the first Born approximation, and we corroborated that it provides quite

reliable results only for energies higher than a couple of MeV/amu. We use the same line color to indicate the projectile charge throughout all the figures of this work: dashed–red, solid–red, blue, magenta, olive and orange for antiprotons,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ , respectively. Notably, there is no complete tabulation of ionization of atoms by the impact of multicharged ions. We hope that the ones presented in this article will be of help for future works.

Simultaneously, we will be reporting state to state ionization cross sections for the 36 ion–target systems considered in the present work [11]. A great numerical effort was paid to obtain these results, and we expect that they will be useful to estimate molecule fragmentation.

### A. Emitted electron energies

In a given biological medium, direct ionization by ion impact accounts for just a fraction of the overall damage. Secondary electrons, as well as recoil target ions, also contribute substantially to the total damage. We can consider the single differential cross section of the shell  $nl$  of the atom  $\alpha$ ,  $d\sigma_{\alpha nl}/dE$ , to be a function of the ejected electron energy  $E$  as a simple distribution function [12]. Then, we can define the mean value  $\overline{E}_\alpha$  as in Ref. [13],

$$\overline{E}_\alpha = \frac{\langle E_\alpha \rangle}{\langle 1 \rangle} = \frac{1}{\sigma_\alpha} \sum_{nl} \int dE E \frac{d\sigma_{\alpha, nl}}{dE}, \quad (2)$$

$$\langle 1 \rangle = \sigma_\alpha = \sum_{nl} \int dE \frac{d\sigma_{\alpha, nl}}{dE}, \quad (3)$$

where  $\Sigma_{nl}$  takes into account the sum of the different sub–shell contributions of the element  $\alpha$ .

The mean emitted electron energies  $\overline{E}_\alpha$  for H, C, N, O, P and S are shown in Fig. 2. The range of impact velocities was shortened to  $v = 10$  a.u. due to numerical limitations in the spherical harmonics expansion of Eq. (1). As the impact velocity  $v$  increases, so do  $\langle E_\alpha \rangle$  and  $l_{\max}$ , which results in the inclusion of very oscillatory functions in the integrand. Furthermore, the integrand of  $\langle E_\alpha \rangle$  includes the kinetic energy  $E$  (see Eq. (2)), which cancels the small energy region and reinforces the large values, making the result more sensible to large angular momenta. Regardless, for  $v > 10$  a.u., the first Born approximation holds.

In Fig. 2, we estimate  $\overline{E}_\alpha$  of the emitted electron in the 0.5–2.7 a.u. energy range, or equivalently from 15 to 70 eV, for all the targets. Our results agree with the experimental

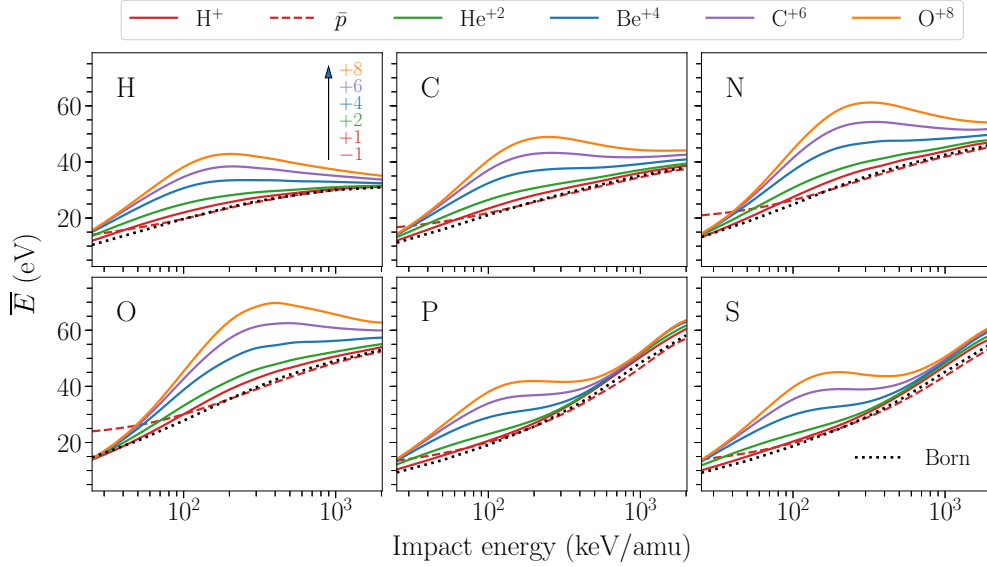


FIG. 2: Mean emitted energy distribution for ionization by the impact of multicharged ions, given by Eq. (2). Dashed lines for  $\bar{p}$ , solid lines for ion charges +1, +2, +4, +6 and +8, as indicated.

findings [12]. As can be noted in the figure, the mean energy value is surprisingly sensitive to the projectile charge  $Z$ , which can duplicate the proton results in the intermediate region, i.e., 100–400 keV/amu. The effect observed can be attributed to the depletion caused by the multicharged ions to the yields of low energy electrons. This behavior cannot be found in the first Born approximation, where the  $Z^2$  law cancels the  $Z$  dependence in Eq. (2). At high energies,  $\bar{E}_\alpha$  tends to a universal value for all ions, as can be seen in Fig. 2.

### B. Emitted electron angles

As mentioned before, secondary electrons contribute to the total damage. Then, not only the ejection energy is essential but also the angle of emission. Once again, we can consider the single differential cross section in terms of the ejected electron solid angle  $\Omega$ ,  $d\sigma_{\alpha,nl}/d\Omega$ , to be expressed as a distribution function, and the mean angle  $\bar{\theta}_\alpha$  can be defined as

$$\bar{\theta}_\alpha = \frac{\langle \theta_\alpha \rangle}{\langle 1 \rangle} = \frac{1}{\sigma_\alpha} \sum_{nl} \int d\Omega \theta \frac{d\sigma_{\alpha,nl}}{d\Omega} \quad (4)$$

The mean emitted electron angles  $\bar{\theta}_\alpha$  for the six atoms and six ions of interest are shown in Fig. 3. A significant dependence of  $\bar{\theta}_\alpha$  with  $Z$  is noticed for all the cases. Once again, this effect could not be observed in the first Born approximation (dotted line).

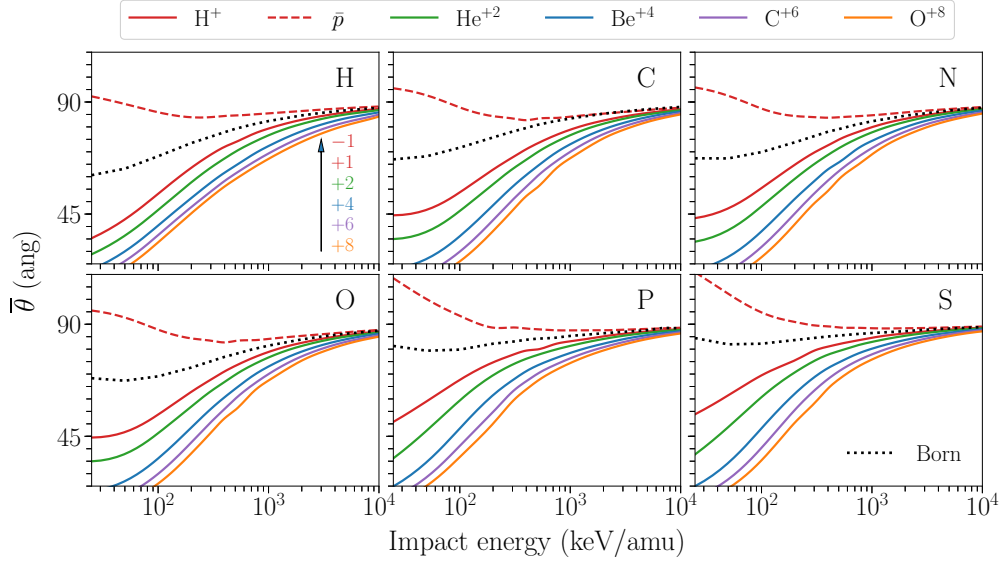


FIG. 3: Mean emitted angle distribution for ionization by impact of multicharged ions.

It is a general belief [14] that the angular dispersion of emitted electrons is nearly isotropic. This behavior is caused by the insignificant angular anisotropy of sub-50-eV yield. A typical value for the ejection angle considered in the literature is  $\bar{\theta}_\alpha \sim 70^\circ$  [12], and it is quite correct in the range of validity of the first Born approximation for any target. However, when a distorted wave approximation is used,  $\bar{\theta}_\alpha$  decreases substantially with  $Z$  in the intermediate energy region. This effect is evident in Fig. 3; for example, at 0.3 MeV/amu –where the Bragg peak for  $C^{+6}$  impact occurs– the CDW  $\bar{\theta}_\alpha$  is half of the first Born value. This correction closes the damage to the forward direction. We can attribute this forward direction correction to the capture to the continuum effect; the higher the charge  $Z$ , the smaller  $\bar{\theta}$  will be. Of course, this effect only holds at intermediate energies and not at high impact energies.

Furthermore, Fig. 3 provides an illustrative description of the behavior of antiprotons: the projectile repels the electrons, being  $\bar{\theta}_\alpha \sim 90^\circ$ . Note the opposite effect of proton and antiprotons respect to the first Born approximation; this phenomenon constitutes an angular Barkas effect.



### III. IONIZATION OF MOLECULES

#### A. The stoichiometric model

Lets us consider a molecule  $M$  composed by  $n_\alpha$  atoms of the element  $\alpha$ , the SSM approaches the total ionization cross section of the molecule  $\sigma_M$  as a sum of ionization cross sections of the isolated atoms  $\sigma_\alpha$  weighted by  $n_\alpha$ ,

$$\sigma_M = \sum_{\alpha} n_{\alpha} \sigma_{\alpha} . \quad (5)$$

We classified the molecular targets of our interest in three families: CH, CHN, and DNA, as in Table I.

CH	CH <sub>4</sub> (methane), C <sub>2</sub> H <sub>2</sub> (acetylene), C <sub>2</sub> H <sub>4</sub> (ethene), C <sub>2</sub> H <sub>6</sub> (ethane), C <sub>6</sub> H <sub>6</sub> (benzene)
CHN	C <sub>5</sub> H <sub>5</sub> N (pyridine), C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> (pyrimidine), C <sub>2</sub> H <sub>7</sub> N (dimenthylamine), CH <sub>5</sub> N (monomethylamine)
DNA	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> (adenine), C <sub>4</sub> H <sub>5</sub> N <sub>3</sub> O (cytosine), C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> O (guanine), C <sub>5</sub> H <sub>6</sub> N <sub>2</sub> O <sub>2</sub> (thymine), C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> O <sub>2</sub> (uracil), C <sub>4</sub> H <sub>8</sub> O (THF), C <sub>5</sub> H <sub>10</sub> O <sub>5</sub> P (DNA backbone), C <sub>20</sub> H <sub>27</sub> N <sub>7</sub> O <sub>13</sub> P <sub>2</sub> (dry DNA)

TABLE I: Molecular targets studied in this work, classified in three families.

In Fig. 4, we report the total ionization cross sections by the impact of multicharged ions for adenine, cytosine, guanine, and thymine, by combining the SSM and CDW results in Eq. 5. For adenine, the agreement with the experimental data available for proton impact [15] is excellent. To the best of our knowledge, there are no experimental data on ion-collision ionization for the rest of the molecules. We have also included in this figure electron impact measurements [16] with the corresponding equivelocity conversion for electron incident energies higher than 300 eV. In this region, the proton and electron cross section should converge. Although the electron impact measurements are above our findings for all the molecular targets, it is worth stating that our results agree very well with other electron impact theoretical predictions [17, 18].

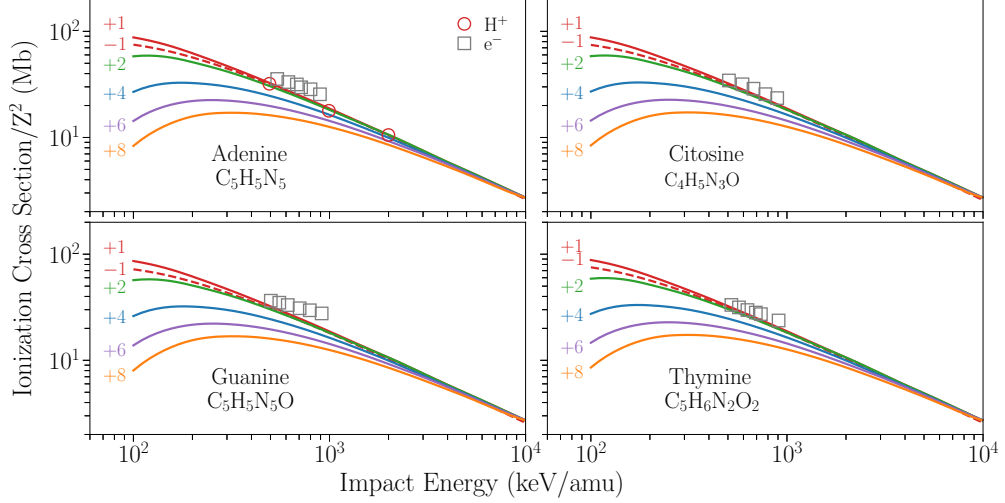


FIG. 4: Reduced CDW ionization cross section by the impact of multicharged ions. Experiments:  $\circ$  [15] for proton impact and  $\square$  [16] for electron impact with equivelocity conversion.

Our results for uracil, DNA backbone, pyrimidine, and THF are displayed in Fig. 5. For uracil, the agreement with the experimental proton impact measurements by Itoh *et al.* [19] is good. However, for the same target, our theory is a factor of two above the experimental ionization measurements by Tribedi and collaborators [20, 21] by the impact of multicharged ions. Nonetheless, it should be stated that our theoretical results coincide with calculations by Champion, Rivarola, and collaborators [20, 22], which may indicate a possible misstep of the experiments.

For pyrimidine, we show a comparison of our results with experimental data for proton impact by Wolff [23] and also for electron impact ionization [24] at high energies. The electron impact measurements agree with our calculations for energies higher than 500keV. Unexpectedly, the proton impact cross sections are significantly lower than our findings. Much more experiments are available for ionization of THF molecule by proton [25] and by electron [24, 26, 27] impact. Our SSM with CDW results show overall good agreement with these data.

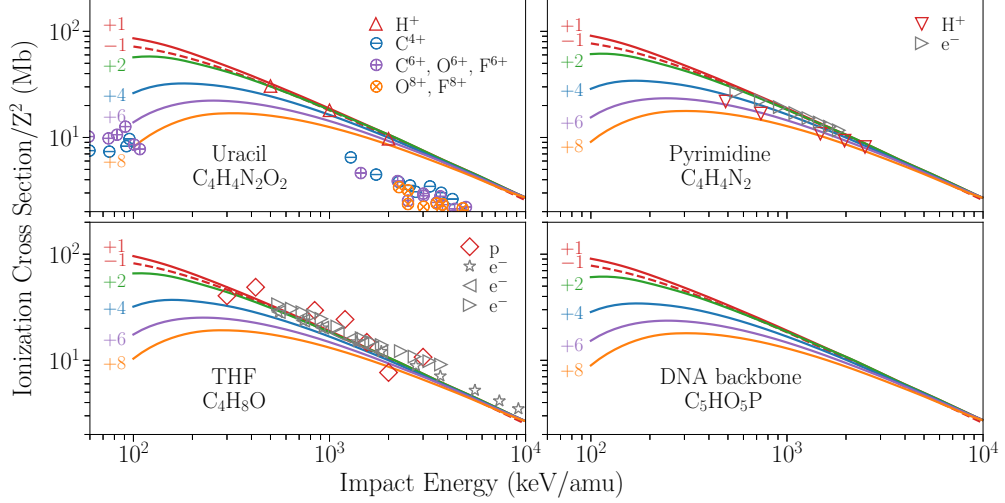


FIG. 5: Reduced CDW ionization cross section by the impact of multicharged ions. Experiments: proton impact on  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23] and  $\diamond$  THF [25]. Impact of  $\ominus$   $C^{+4}$ ,  $\boxplus$   $C^{+6}$ ,  $O^{+6}$ ,  $F^{+6}$ , and  $\triangleleft$   $O^{+8}$ ,  $F^{+8}$  on uracil [20, 21]. Symbols  $\triangleright$  [24],  $\triangleleft$  [26], and  $\star$  [27] for electron impact with equivelocity conversion.

## B. Scaling rules

### 1. Toburen rule

The first attempt to develop a comprehensive but straightforward phenomenological model for electron ejection from large molecules was proposed by Toburen and coworkers [4, 5]. The authors found it convenient to scale the experimental ionization cross section in terms of the number of weakly-bound electrons,  $n_e$ . For instance, for C, N, O, P, and S, this number is the total number of electrons minus the K-shell. Following Toburen, the scaled ionization cross section per weakly bound electron  $\sigma_e^T$  is

$$\sigma_e^T = \frac{\sigma_M}{n_e}, \quad (6)$$

where  $n_e = \sum_{\alpha} n_{\alpha} \nu_{\alpha}^T$ , and  $\nu_{\alpha}^T$  are the Toburen numbers given by

$$\nu_{\alpha}^T = \begin{cases} 1, & \text{for H,} \\ 4, & \text{for C,} \\ 5, & \text{for N and P,} \\ 6, & \text{for O and S.} \end{cases} \quad (7)$$

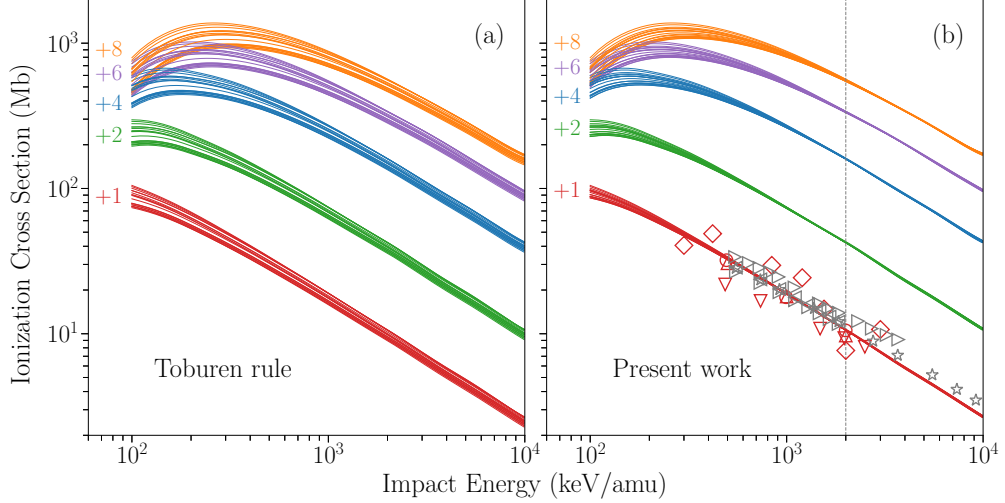


FIG. 6: Scaled ionization cross section per weakly bound electron using (a) the Toburen numbers  $\nu_\alpha^T$ , and (b) our proposed numbers  $\nu_\alpha^{\text{CDW}}$ . Experiments: proton impact on  $\circ$  adenine [15],  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23] and  $\diamond$  THF [25]; electron impact on  $\triangleright$  pyrimidine [24], and  $\triangleleft$ ,  $\star$  [26, 27] THF.

The Toburen rule can be stated by saying that  $\sigma_e$  is a *universal* parameter independent on the molecule, which depends solely on the impact velocity, and holds for high impact energies (i.e., 0.25–5 MeV/amu). These  $\nu_\alpha^T$  can be interpreted as the number of active electrons in the collision. At very high energies, the K-shell electrons will also be ionized, and these numbers will be different. A similar dependence with the number of weakly bound electrons was found in Ref. [19] for proton impact on uracil and adenine.

Following the Toburen scaling, we computed the scaled CDW cross sections  $\sigma_e^T$  for the molecular targets of Table I. Our results are shown in Fig. 6a as a function of the impact energy for different projectile charges. Although the Toburen scaling holds for high energies, its performance is still not satisfactory: the universal band is quite broad, as can be noted in this figure.

## 2. CDW-based scaling

The departure of our theoretical results from the Toburen rule can be easily understood by inspecting Fig. 1. It can be noted that the rule  $\sigma_\alpha/\nu_\alpha^T \sim \sigma_e^T$ , approximately constant, is not well satisfied by the CDW. For example, Fig. 1 shows that the cross sections for O are

very similar to the cross sections for C, suggesting 4 active electrons in O instead of 6. In the same way, the number of active electrons for N, P, and S obtained with the CDW are also different from the  $\nu_\alpha^T$  of Eq. (7).

Based on the CDW results, we propose a new scaling,

$$\sigma_e = \frac{\sigma_M}{n'_e}, \quad (8)$$

where  $n'_e = \sum_\alpha n_\alpha \nu_\alpha^{\text{CDW}}$ , and  $\nu_\alpha^{\text{CDW}}$  are the numbers of active electrons per atom obtained from the CDW ionization cross sections for different ions in H, C, N, O, P, and S targets, given as follows,

$$\nu_\alpha^{\text{CDW}} \sim \begin{cases} 1, & \text{for H,} \\ 4, & \text{for C, N, and O,} \\ 4.5, & \text{for P and S.} \end{cases} \quad (9)$$

The new scaled cross sections  $\sigma_e$  are plotted in Fig. 6b. A much better sharp band is observed, especially for impact energies  $E = (0.5-8)$  MeV/amu for  $Z = 1$  and  $Z = 2$ , and  $E = (2.5-8)$  MeV/amu for  $Z > 2$ . The experimental data for ionization of adenine [15], uracil [19], pyrimidine [23], and THF [25] by proton impact in Fig. 6b seems to corroborate the new scaling. We also included the electron impact ionization measurements with equivelocity conversion on pyrimidine [24] and THF [24, 26, 27]. It will be interesting to cross-check with future experiments, mainly for higher projectile charge states.

Molecule	$n_e$	Molecule	$n_e$	Molecule	$n_e$
H <sub>2</sub>	2	C <sub>2</sub> H <sub>7</sub> N	19	C <sub>4</sub> H <sub>5</sub> N <sub>3</sub> O	37
H <sub>2</sub> O	6	C <sub>4</sub> H <sub>8</sub> O	28	C <sub>5</sub> H <sub>6</sub> N <sub>2</sub> O <sub>2</sub>	42
NH <sub>3</sub>	7	C <sub>4</sub> H <sub>4</sub> N <sub>2</sub>	28	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub>	45
CH <sub>4</sub>	8	C <sub>6</sub> H <sub>6</sub>	30	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> O	49
CH <sub>5</sub> N	13	C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> O <sub>2</sub>	36	C <sub>5</sub> H <sub>10</sub> O <sub>5</sub> P	54.5

TABLE II: New scaling numbers for some molecular targets of biological interest.

By using Eq. (9), we define new active electron numbers  $n'_e$  for some molecules of interest in Table II. These values are very different from the ones proposed by Toburen and used by other authors [19]. Moreover, an alternative way of showing the scaling can be attained by plotting the ionization cross sections of molecules as a function of the number of active

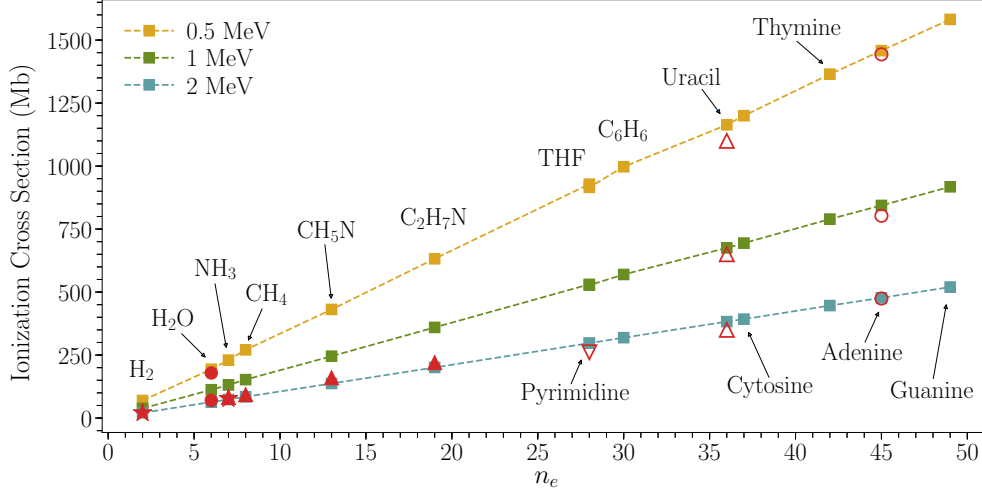


FIG. 7: Ionization cross sections by the impact of protons at 0.5, 1, and 2 MeV in terms of the number of active electrons given by Table II. Experiments:  $\circ$  adenine [15],  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23],  $\blacktriangle$  C<sub>2</sub>H<sub>7</sub>N, CH<sub>5</sub>N, methane and ammonia [28],  $\star$  ammonia and H<sub>2</sub> [29], and  $\bullet$  water [30].

electrons from Table II. Our findings are displayed in Fig. 7 for impact energies 0.5, 1, and 2 MeV. As can be noted, the computed CDW ionization cross sections for all the molecules show a linear dependence with the number of electrons from Table II. We obtain similar results even for  $E = 10$  MeV. The comparison with the experimental data available shows overall good agreement, for the smallest molecules, H<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>, up to the most complex ones, like adenine. For electron impact data, the experimental data was interpolated between close neighbors.

While finishing the present work, we noted an accepted manuscript by Luedde *et al.* [31] on total ionization of biological molecules by proton impact, using an independent-atom-model pixel counting method. The authors also raised a scaling with  $\nu_\alpha = 4$  for C, N, and O, but  $\nu_\alpha = 6$  for P. The agreement with this independent method for proton impact reinforces our multicharged-ion findings.

### C. Molecular structure of targets

To test the range of validity of the SSM, we performed a full molecular structure calculation of five nucleobases. We employed the GAMESS code and used the 6-31G(d,p) basis

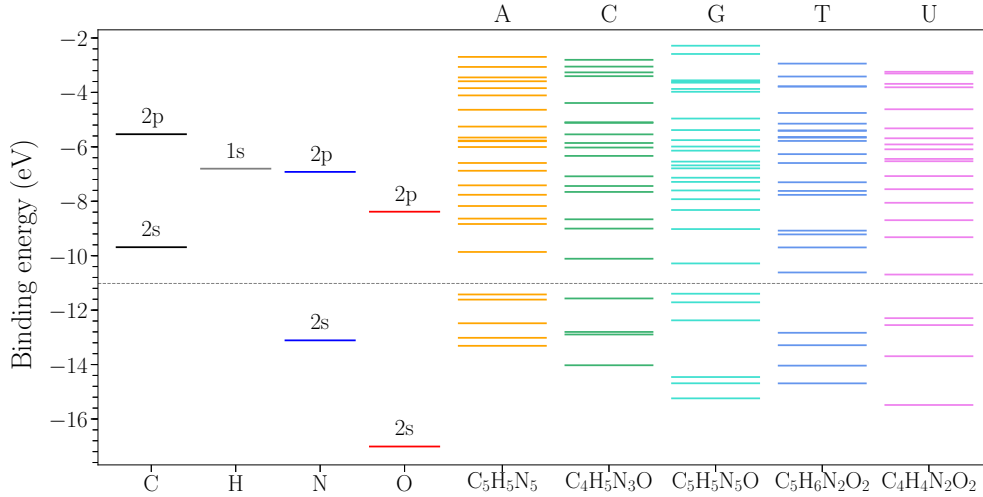


FIG. 8: Theoretical molecular binding energies for adenine, cytosine, guanine, thymine, and uracil compared to those of atomic constituents.

set, which includes polarization functions for all the atoms. The calculations were carried out implementing the B3LYP functional [32, 33] to account for the correlation and exchange effects.

The molecular binding energies of the valence electrons for adenine, cytosine, guanine, thymine, and uracil are shown in Fig. 8. We can compute the center of gravity of these molecular energy levels as an average weighted by the electronic occupation number. The results obtained from the full molecular calculation are given in the first row of Table III. Similarly, we can compute the barycenter of the energy levels defined by the Toburen and the CDW-based rules, which are also given in Table III. The average energy values obtained from the Toburen rule are around 20% of the full molecular ones. Surprisingly, the new scaling rule gives a significant improvement in the average energy values, reducing the relative errors to about 7%. This improvement would indicate that the new scaling is appropriate.

$E_{av}$ (eV)	A C <sub>5</sub> H <sub>5</sub> N <sub>5</sub>	C C <sub>4</sub> H <sub>5</sub> N <sub>3</sub> O	G C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> O	T C <sub>5</sub> H <sub>6</sub> N <sub>2</sub> O <sub>2</sub>	U C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> O <sub>2</sub>
Theoretical calc.	-7.1955	-6.9058	-7.4725	-7.5304	-7.6224
Toburen rule	-8.4236	-8.6743	-8.7275	-8.7947	-9.0022
Present work	-7.9027	-7.8639	-7.9420	-7.8066	-7.8839

TABLE III: Center of gravity of the molecular energy levels of five nucleobases.

Furthermore, on the left side of Fig. 8, we show the atomic Hartree–Fock energies of the constituent elements, which gives an insight into the distribution of the weakly bound electrons. A dashed line around  $-11$  eV is drawn to separate the band in two. We can consider the atomic energy levels above this line as the ones corresponding to the weakly bound electrons from Eq. (9). For example, the  $2s$  and  $2p$  electrons of carbon are placed above the separating line, which corresponds to the 4 electrons given by Eq. (9). In the case of O, only the 4 electrons of the  $2p$  orbitals are located above the separating line, which corresponds to the number of weakly bound electron given by our new scaling. The N case is not as straightforward; the  $\nu_{N=4}^{CDW}$  would suggest the  $2s$  electrons partially contribute to the molecular scheme.

### 1. A modified stoichiometric model

The SSM considers the molecule to be assembled by isolated neutral atoms, which is definitively unrealistic. A first improvement can be suggested by assuming that the atoms are not neutral and that they have an uneven distribution of electrons within the molecule, which can be expressed as an effective charge  $q_\alpha$  per atom. The Mulliken charge gives a possible value for  $q_\alpha$ ; however, there are a wide variety of charge distributions [34].

To take this effect into account, we can consider that the total amount of electrons  $Q_\alpha$  on the element  $\alpha$  is equally distributed on all the  $\alpha$  atoms. Therefore, each element  $\alpha$  will have an additional charge,  $q_\alpha = Q_\alpha/n_\alpha$ , which can be positive or negative. This amount will depend on the relative electronegativity respect to the other atoms [35]. Following this idea,



we can define a new number of atoms per molecule  $n'_\alpha$ , given by

$$n'_\alpha = n_\alpha - \frac{q_\alpha}{\nu_\alpha^{\text{CDW}}} \quad (10)$$

In the case of neutral atoms,  $q_\alpha = 0$  and  $n'_\alpha = n_\alpha$ , as it should be. In Table IV, we display the average effective charge per atom  $q_\alpha$  of C, H, N, and O, for five DNA molecules, obtained from the full molecular calculation described above.

Element	C	H	N	O	New stoichiometry
Adenine	+0.32	+0.23	-0.55		$\text{C}_{4.92}\text{H}_{4.77}\text{N}_{5.14}$
Cytosine	+0.28	+0.21	-0.56	-0.53	$\text{C}_{3.93}\text{H}_{2.79}\text{N}_{5.14}\text{O}_{1.13}$
Guanine	+0.46	+0.20	-0.58	-0.36	$\text{C}_{4.89}\text{H}_{4.80}\text{N}_{5.15}\text{O}_{1.09}$
Thymine	+0.20	+0.19	-0.54	-0.52	$\text{C}_{4.95}\text{H}_{1.81}\text{N}_{6.13}\text{O}_{2.13}$
Uracil	+0.31	+0.22	-0.59	-0.47	$\text{C}_{3.92}\text{H}_{1.78}\text{N}_{4.15}\text{O}_{2.12}$

TABLE IV: Average effective Mulliken charge per atom  $q_\alpha$ , and new stoichiometric formula defined by Eq. (10) for five DNA molecules.

By implementing Eq. (10), it is possible to determine a new stoichiometric formula (last column of Table IV). Now, instead of having an integer number of atoms  $n_\alpha$ , we obtain a fractional number  $n'_\alpha$ . New molecular cross sections  $\sigma'_M = \sum_\alpha n'_\alpha \sigma_\alpha$  can be computed considering such values. Relative errors for the ionization cross sections were computed for the DNA bases from Table IV. The differences obtained were less than 3%, which indicates that the modified SSM is a quite robust model to handle these type of molecules within the range error expected for this model.

#### IV. CONCLUSIONS

In this work, we have encouraged the calculation of ionization cross sections of seventeen biological molecules containing H, C, N, O, P, and S by the impact of antiprotons,  $\text{H}^+$ ,  $\text{He}^{2+}$ ,  $\text{Be}^{4+}$ ,  $\text{C}^{6+}$ , and  $\text{O}^{8+}$ . To that end, we have employed the full CDW method and the simple stoichiometric model. The mean energy and angle of the emitted electrons, of importance in post-collisional radiation damage, has also been calculated, showing a clear dependence with the ion charge  $Z$ . For a given target as  $Z$  increases,  $\overline{E}_\alpha$  increases, but  $\overline{\theta}_\alpha$  decreases, showing

a clear tendency to the forward direction. At impact energies greater than 2 MeV/amu, these values converge to the Born approximation, which embodies the simple  $Z^2$  law.

Total ionization cross sections for adenine, cytosine, thymine, guanine, uracil, DNA backbone, pyrimidine, and THF are presented and compared with the scarcely available experiments. We explore the rule of Toburen, which scales all the molecular ionization cross section normalizing with a certain number of weakly bound or valence electrons. We found that the ionization cross sections scales much better when normalizing with the number of active electrons in the collision obtained from the CDW results for atoms. This new scaling was tested with good results for the six projectiles and seventeen molecules studied here. The comparison with the experimental data reinforce these results. Furthermore, we also tested the scaling by including experimental data of ionization of  $H_2$ , water, methane, and ammonia by proton impact showing good agreement at intermediate to high energies.

Finally, we performed full molecular calculations for the DNA basis. By inspecting the molecular binding energy from quantum mechanical structure calculations, we were able to understand the number of electrons proposed in our new CDW-based scaling. We attempt to improve the stoichiometric model by using the Mulliken charge to get fractional rather than integer proportions. We found no substantial correction, which indicates that the SSM works quite well.

In conclusion, the present results reinforce the reliability of the SSM to deal with complex molecules in the intermediate to high energy range. Moreover, the simple stoichiometric model and the CDW cross sections in Ref. [11] opens the possibility to describe a wide range of molecules containing H, C, N, O, P, and S, by the impact of multicharged ions.

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