

# Ionization of biological molecules by multicharged ions by using the stoichiometric model

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## Abstract

In this work we investigate the ionization of molecules of biological interest by impact of multicharged ions in the intermediate to high energy range. We performed full non-perturbative distorted-wave calculations (CDW) for thirty six collisional systems, six charged projectiles (antiprotons, H, He, B, C and O) and by six atomic targets H, C, N, O, F and S. These atoms are the constituents of most of the DNA and biological molecules. By considering the stoichiometric composition of the different molecules we approximate the ionization cross sections as linear combination of the atomic ones. We show that this simple stoichiometric model (SSM) gives reasonable good results for complex molecules. We focused on seventeen molecules including the DNA (adenine, cytosine, guanine, thymine, uracil), DNA backbone, the pyrimidines, tetrahydrofuran (THF), and the  $C_nH_n$  compounds. The full comparison of the total ionization cross sections for the different ions normalized to the square of the ion charge gives an interesting picture of the experimental state of art. The energy and angular distributions of the emitted electrons are also inspected due to its relation with the radiation damage. Our results show that these two parameters are highly dependent on the projectile charge state, which cannot be noted in a first order perturbative calculation. We also analyze the extensively used Toburen scaling of the total ionization cross sections of molecules with the number of weakly bound electrons. We tested this scaling for the seventeen different molecules and the six projectiles per each, which allows to have an insight on the limitation of this scaling. Instead, based on the present CDW results for the atoms, we propose a different number of electrons per atom. This CDW-based scaling highly improves the single curve behaviour for all the targets and ions studied here, in the intermediate to high energy region. The new scaling also describes well the available experimental data, including small molecules such as  $H_2$ , water, methane and ammonia. For completeness, we performed full molecular calculations for the five DNA molecules, and tested a corrected stoichiometric formula based on the actual number of electrons around each molecular center. The difference of these more realistic ionization cross sections and the SSM ones was less than 3%, being an indication of the reliability and robustness of the SSM to deal with this type of molecules. Based on the extensive ion-target systems included in the present study, and the results obtained, the possibilities of the SSM and the new scaling are of great impact.

## I. INTRODUCTION

The damage caused by the impact of multicharged heavy projectiles on biological targets has become a field of interest due to its recent implementation in ion-beam cancer therapy. The effectiveness of the radiation depends on the choice of the ions. In particular, theoretical and experimental studies with different projectiles have concluded that charged carbon ions could be the most suitable ions to be used. Nonetheless, the study of such systems represents a challenge from the theoretical point of view.

The ionization of biological molecules by multicharged ions constitutes the primary damage mechanism. The most widely used method to predict such processes is the first Born approximation. At high energies, this perturbative method warrants the  $Z^2$  laws, where  $Z$  is the projectile charge. However, the damage is concentrated in the vicinities of the Bragg peak—at energies of hundreds of keV/amu—, precisely where the Born approximation starts to fail. Another theoretical issue arises due to the targets themselves; we are dealing with complex molecules, and the description of such targets represents a hard task for *ab initio* calculations. The objective of this article is to deal with these two aspects; first, we perform more appropriate calculations on the primary damage mechanism, which can replace the Born results. Second, we inspect and test a stoichiometric model to describe the ionization of molecular targets.

To overcome the first perturbative approximation limitations, and since the projectiles are multicharged ions, we resort to the Continuum Distorted Wave-Eikonal Initial State (CDW), which includes higher perturbative corrections. We start from the premise that the ionization process is the mechanism that deposits the most significant amount of primary energy. Moreover, it is well known that the residual electrons from the ionization become a source of significant local biological damage. The secondary electrons are included in Monte Carlo simulations, and hence their behavior must be investigated. In Section II A and II B, we calculate the mean energy and angular distributions of the ejected electrons. Surprisingly, we found a substantial dependence of the charged projectile, which is unexpected in the first Born approximation. We deal with the molecular structure complexity of the target by implementing the simplest stoichiometric model (SSM): the molecules are assumed to be composed of isolated independent atoms, and the total cross-section by a linear combination of weighted atomic calculations.

By implementing the CDW and the SSM, we calculate ionization cross-section of several molecules of interest (see Table I) by the impact of antiprotons,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ . In Section 3, we show our results for different DNA and RNA molecules, such as adenine, cytosine, guanine, thymine, uracil, tetrahydrofuran (THF), pyrimidine, and also DNA backbone. In Section III B, we test the Toburen scaling rule [1, 2], which states that the ratio between the ionization cross-section and the number of weakly bound electrons can be arranged in a narrow universal band in terms of the projectile velocity. We applied this rule to several hydrocarbons and nucleobases and noted that the width of the resulting universal band could be significantly reduced if we redefine the effective number of active electrons in the collision. The new scaling is then tested by comparison with experimental data.

Although the multicharged projectiles are dealt with the CDW, the stoichiometric model used seems to be very simplistic. The approach considers each atom as neutral, which is not correct. In Section 3.5, we used the molecular electronic structure code GAMESS [3] to calculate the excess or defect of electron density on the atoms composing the molecules. Then, the SSM is modified to account for the departure from the neutrality of the atoms. We find that the modified SSM for the DNA molecules does not introduce substantial changes in the cross sections.

## II. THEORY: IONIZATION OF ATOMS

In the present study, we consider six atoms,  $\alpha = H, C, N, O, P,$  and  $S$ , and six projectiles, antiprotons  $\bar{p}$ ,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ . Most of the organic molecules are composed of these atoms. Some particular molecules also include halogen atoms such as fluor and bromine; ionization cross sections of these elements have been previously published [4].

The total ionization cross sections of these atoms were calculated using the CDW [4–6]. The initial bound and final continuum radial wave functions were obtained by using the RADIALF code, developed by Salvat and co-workers [7], and a Hartree-Fock potential obtained from the Depurated Inversion Method [8, 9]. We used a few thousand pivot points to solve the Schrödinger equation, depending on the number of oscillations of the continuum state. The radial integration was performed using the cubic spline technique. The number of angular momenta considered varied from 8, at very low ejected-electron energies, up to

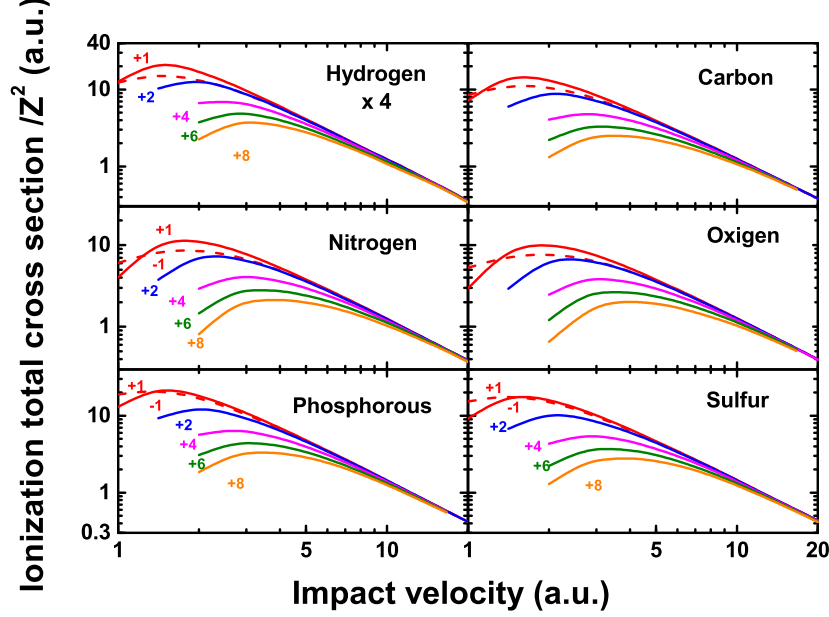


FIG. 1. Reduced CDW total ionization cross section of six atomic targets. The curves are labeled with the charge state corresponding to the six multicharged projectiles.

30, for the highest energies considered. The same number of azimuth angles were required to obtain the four-fold differential cross section. The calculation performed does not display prior-post discrepancies at all. Each atomic total cross section was calculated using 35 to 100 momentum transfer values, 28 fixed electron angles, and around 45 electron energies depending on the projectile impact energy. In our theoretical treatment, we expand our final continuum wave function as usual,

$$\psi_{\vec{k}}^{-}(\vec{r}) = \sum_{l=0}^{l_{\max}} \sum_{m=-l}^l R_{kl}^{-}(r) Y_l^m(\hat{r}) Y_l^{m*}(\hat{k}). \quad (1)$$

We are confident with our calculations up to  $l_{\max} \sim 30$ . Further details of the calculation are given in Ref. [10]. Simultaneously, we will be reporting state to state ionization cross sections for the 36 ion-target systems considered in the present work [11]. A great numerical effort was paid to obtain the present results, and we expect that they will be useful to estimate molecule fragmentation.

We report our total CDW ionization cross sections for the six essential elements by the impact of six projectiles in Fig. 1. To reduce the resulting 36 magnitudes into a single consistent figure, we considered the fact that in the first Born approximation the ionization cross section scales with the square of the projectile charge,  $Z^2$ . The values of the impact

energies considered range between 0.1 to 10 MeV/amu, where the CDW is supposed to hold. In fact, for the highest projectile charges the minimum impact energy where the CDW is expected to be valid could be higher than 100 keV. We also performed similar calculations with the first Born approximation, and we corroborated that it provides quite reliable results only for energies higher than a couple of MeV/amu. We use the same line color to indicate the projectile charge throughout all the figures of this work: dashed–red, solid–red, blue, magenta, olive and orange for antiprotons,  $H^+$ ,  $He^{+2}$ ,  $Be^{+4}$ ,  $C^{+6}$ , and  $O^{+8}$ , respectively. Notably, there is no complete tabulation of ionization of atoms by the impact of multicharged ions. We hope that the ones presented in this article will be of help for future works.

### A. Emitted electron energies

In a given biological medium, direct ionization by ion impact accounts for just a fraction of the overall damage. Secondary electrons, as well as recoil target ions, also contribute substantially to the total damage. We can consider the single differential cross section of the shell  $nl$  of the atom  $\alpha$ ,  $d\sigma_{\alpha nl}/dE$ , to be a function of the ejected electron energy  $E$  as a simple distribution function [12]. Then, we can define the mean value  $\overline{E}_\alpha$  as in Ref. [13],

$$\overline{E}_\alpha = \frac{\langle E_\alpha \rangle}{\langle 1 \rangle} = \frac{1}{\sigma_\alpha} \sum_{nl} \int dE E \frac{d\sigma_{\alpha, nl}}{dE}, \quad (2)$$

$$\langle 1 \rangle = \sigma_\alpha = \sum_{nl} \int dE \frac{d\sigma_{\alpha, nl}}{dE}, \quad (3)$$

where  $\Sigma_{nl}$  takes into account the sum of the different sub-shell contributions of the element  $\alpha$ .

The mean emitted electron energies  $\overline{E}_\alpha$  for H, C, N, O, P and S are shown in Fig. 2. The range of impact velocities was shortened to  $v = 10$  a.u. due to numerical limitations in the spherical harmonics expansion of Eq. (1). As the impact velocity  $v$  increases, so do  $\langle E_\alpha \rangle$  and  $l_{\max}$ , which results in the inclusion of very oscillatory functions in the integrand. Furthermore, the integrand of  $\langle E_\alpha \rangle$  includes the kinetic energy  $E$  (see Eq. (2)), which cancels the small energy region and reinforces the large values, making the result more sensible to large angular momenta. Regardless, for  $v > 10$  a.u., the first Born approximation holds.

In Fig. 2, we estimate  $\overline{E}_\alpha$  of the emitted electron in the 0.5–2.7 a.u. energy range, or equivalently from 15 to 70 eV, for all the targets. Our results agree with the experimental

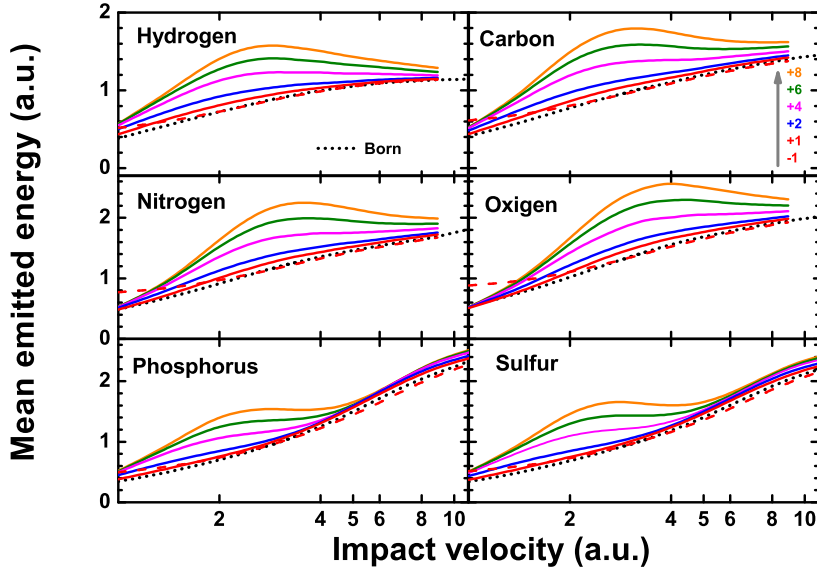


FIG. 2. Mean emitted energy distribution for ionization by impact of multicharged ions, given by Eq. (2). Dashed lines for  $\bar{p}$ , solid lines for ion charges +1, +2, +4, +6 and +8, as indicated.

findings [12]. As can be noted in the figure, the mean energy value is surprisingly sensible to the projectile charge  $Z$ , which can duplicate the proton results in the intermediate region, i.e. 100–400 keV/amu. The effect observed can be attributed to the depletion caused by the multicharged ions to the yields of low energy electrons. This behavior cannot be found in the first Born approximation, where the  $Z^2$  law cancels the  $Z$  dependence in Eq. (2). At high energies,  $\bar{E}_\alpha$  tends to a universal value for all ions, as can be seen in Fig. 2.

## B. Emitted electron angles

As mentioned before, secondary electrons contribute to the total damage. Then, not only is the ejection energy important but also the angle of emission. Once again, we can consider the single differential cross section in terms of the ejected electron solid angle  $\Omega$ ,  $d\sigma_{\alpha,nl}/d\Omega$ , to be expressed as a distribution function, and the mean angle  $\bar{\theta}_\alpha$  can be defined as

$$\bar{\theta}_\alpha = \frac{\langle \theta_\alpha \rangle}{\langle 1 \rangle} = \frac{1}{\sigma_\alpha} \sum_{nl} \int d\Omega \theta \frac{d\sigma_{\alpha,nl}}{d\Omega} \quad (4)$$

The mean emitted electron angles  $\bar{\theta}_\alpha$  for the six atoms of interest are shown in Fig. 3, and an important dependence of  $\bar{\theta}_\alpha$  with  $Z$  is observed. Once again, this effect is not observed in

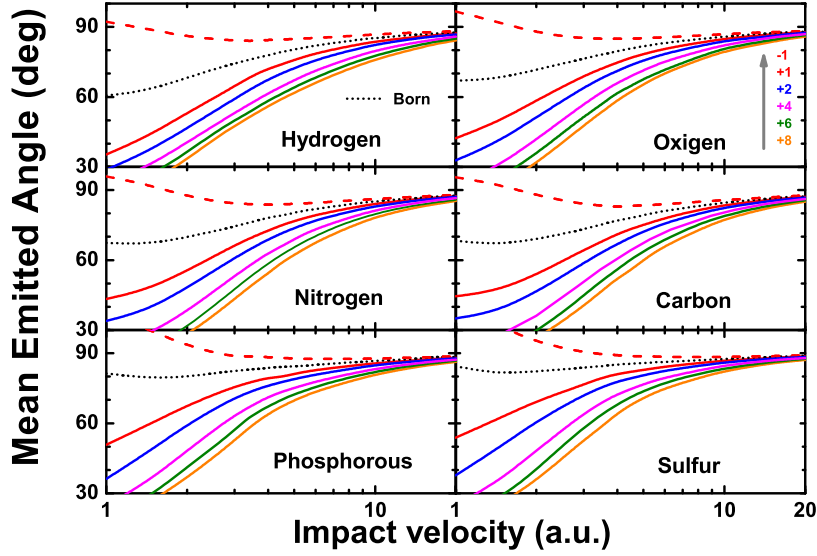


FIG. 3. Mean emitted angle distribution for ionization by impact of multicharged ions.

the first Born approximation. It is a general belief [14] that the angular dispersion of emitted electrons are nearly isotropic. This behavior is caused by the insignificant angular anisotropy of sub-50-eV yield. A typical value for the ejection angle considered in the literature is  $\bar{\theta}_\alpha \sim 70^\circ$  [12], and it is quite correct in the range of validity of the first Born approximation for any target. But, when a distorted wave approximation is used,  $\bar{\theta}_\alpha$  decreases substantially with  $Z$  in the intermediate energy region, as observed in Fig. 3. For example, for  $C^{+6}$  impact, the Bragg peak occurs at 0.3 MeV/amu, where  $\bar{\theta}_\alpha$ , computed with the CDW method, is about half of the value obtained with the first Born approximation. This correction closes the damage to the forward direction.

We can attribute this forward direction correction to the capture to the continuum effect; the larger the charge  $Z$ , the smaller  $\bar{\theta}$  will be. Of course, this effect only holds at intermediate energies and not at high impact energies, where the Born approximation rules. One illustrative observation is the behavior of antiprotons: the projectile in this case repels the electrons, being  $\bar{\theta}_\alpha \sim 90^\circ$ . Note the opposite effect of proton and antiprotons; they run one opposite to the other, as compared with the first Born approximation, constituting an angular Barkas effect.



### III. IONIZATION OF MOLECULES

#### A. The stoichiometric model

Lets us consider a molecule  $M$  composed by  $n_\alpha$  atoms of the element  $\alpha$ , the SSM approaches the total ionization cross section of the molecule  $\sigma_M$  as a sum of ionization cross sections of the isolated atoms  $\sigma_\alpha$  weighted by  $n_\alpha$ ,

$$\sigma_M = \sum_{\alpha} n_{\alpha} \sigma_{\alpha} . \quad (5)$$

We classified the molecular targets of our interest in three families: CH, CHN and DNA, as in Table I.

CH	CH <sub>4</sub> (methane), C <sub>2</sub> H <sub>2</sub> (acetylene), C <sub>2</sub> H <sub>4</sub> (ethene), C <sub>2</sub> H <sub>6</sub> (ethane), C <sub>6</sub> H <sub>6</sub> (benzene)
CHN	C <sub>5</sub> H <sub>5</sub> N (pyridine), C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> (pyrimidine), C <sub>2</sub> H <sub>7</sub> N (dimenthylamine), CH <sub>5</sub> N (monomethylamine)
DNA	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> (adenine), C <sub>4</sub> H <sub>5</sub> N <sub>3</sub> O (cytosine), C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> O (guanine), C <sub>5</sub> H <sub>6</sub> N <sub>2</sub> O <sub>2</sub> (thymine), C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> O <sub>2</sub> (uracil), C <sub>4</sub> H <sub>8</sub> O (THF), C <sub>5</sub> H <sub>10</sub> O <sub>5</sub> P (DNA backbone), C <sub>20</sub> H <sub>27</sub> N <sub>7</sub> O <sub>13</sub> P <sub>2</sub> (dry DNA)

TABLE I. Molecular targets studied in this work, classified in three families.

In Fig. 4, we report the total ionization cross sections by the impact of multicharged ions for adenine, cytosine, guanine and thymine. For adenine, the agreement with the experimental data available [15] is very good. To the best of our knowledge, there are not experimental data on ion–collision ionization for the rest of the molecules. We included electron impact measurements [16] with the corresponding equivelocity conversion for incident energies higher than 300 eV. In this region, the proton and electron cross section should converge. Although the electron impact measurements are above our findings for all the molecular targets, it is worth stating that our results agree very well with other electron impact theoretical predictions [17, 18].

Our results for uracil, DNA backbone, pyrimidine and THF are displayed in Fig. 5. For uracil, the agreement with the experimental proton impact measurements by Itoh *et al.* [19]

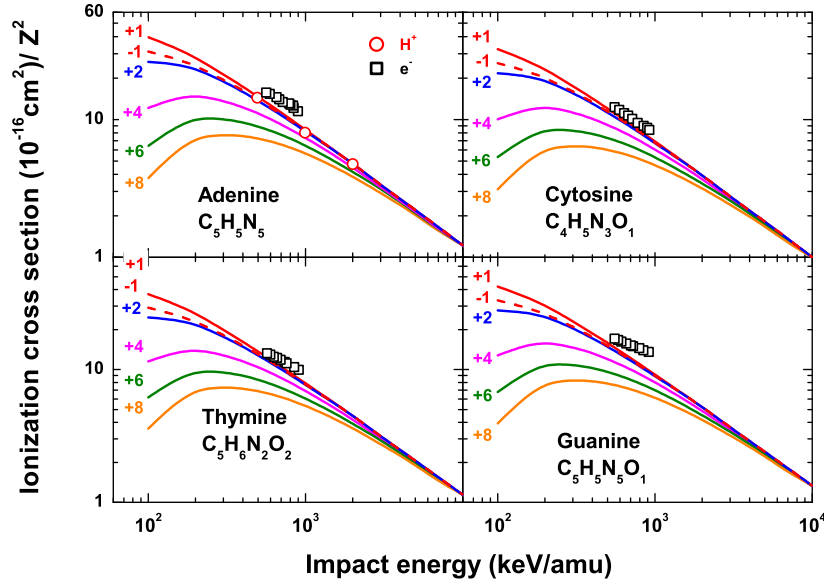


FIG. 4. Reduced CDW ionization cross section by impact of multicharged ions. Experiments:  $\circ$  [15] for proton impact and  $\square$  [16] for electron impact with equivelocity conversion.

is good. However, for the same target, our theory fails by a factor of two for the experimental ionization values by the impact of  $C^{+4}$ ,  $O^{+6}$  and  $O^{+8}$  ions [20, 21]. Nonetheless, it should be stated that our theoretical results coincide with calculations by Champion, Rivarola and collaborators [20, 22], which may indicate a possible misstep of the experiments. For pyrimidine, we show comparison of our results with experimental data for proton [23] and electron [24] ionization. The electron impact measurements agree with our calculations for energies higher than 500keV. Unexpectedly, the proton impact cross sections are significantly lower than our findings. The THF molecule results are compared with proton [25] and electron [24, 26, 27] impact measurements, showing overall good agreement with our theory.

## B. Scaling rule

### 1. Toburen rule

The first attempt to develop a comprehensive but straightforward phenomenological model for electron ejection from large molecules was proposed by Toburen and coworkers [1, 2]. The authors found it convenient to scale the experimental ionization cross section

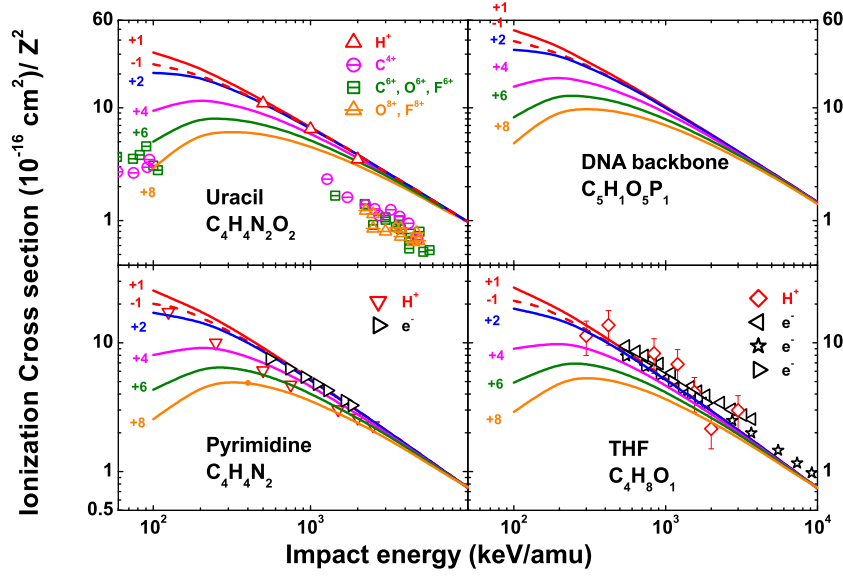


FIG. 5. Reduced CDW ionization cross section by impact of multicharged ions. Experiments: proton impact on  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23] and  $\diamond$  THF [25]. Impact of  $\ominus$   $C^{+4}$ ,  $\boxminus$   $C^{+6}$ ,  $O^{+6}$ ,  $F^{+6}$ , and  $\triangleleft$   $O^{+8}$ ,  $F^{+8}$  on uracil [20, 21]. Symbols  $\triangleright$  [24],  $\triangleleft$  [26], and  $\star$  [27] for electron impact with equivalency conversion.

in terms of the number of weakly-bound electrons,  $n_e$ . For instance, for C, N, O, P and S, this number is the total number of electrons minus the K-shell. Following Toburen, the scaled ionization cross section per weakly bound electron  $\sigma_e^T$  is

$$\sigma_e^T = \frac{\sigma_M}{n_e}, \quad (6)$$

where  $n_e = \sum_{\alpha} n_{\alpha} \nu_{\alpha}^T$ , and  $\nu_{\alpha}^T$  are the Toburen numbers given by

$$\nu_{\alpha}^T = \begin{cases} 1, & \text{for H,} \\ 4, & \text{for C,} \\ 5, & \text{for N and P,} \\ 6, & \text{for O and S.} \end{cases} \quad (7)$$

The Toburen rule can be stated by saying that  $\sigma_e$  is a *universal* parameter independent on the molecule, which depends solely on the impact velocity, and holds for high impact energies (i.e. 0.25–5 MeV/amu). These  $\nu_{\alpha}^T$  can be interpreted as the number of active electrons in the collision. Of course, at very high energies also de K-shell electrons will be ionized and

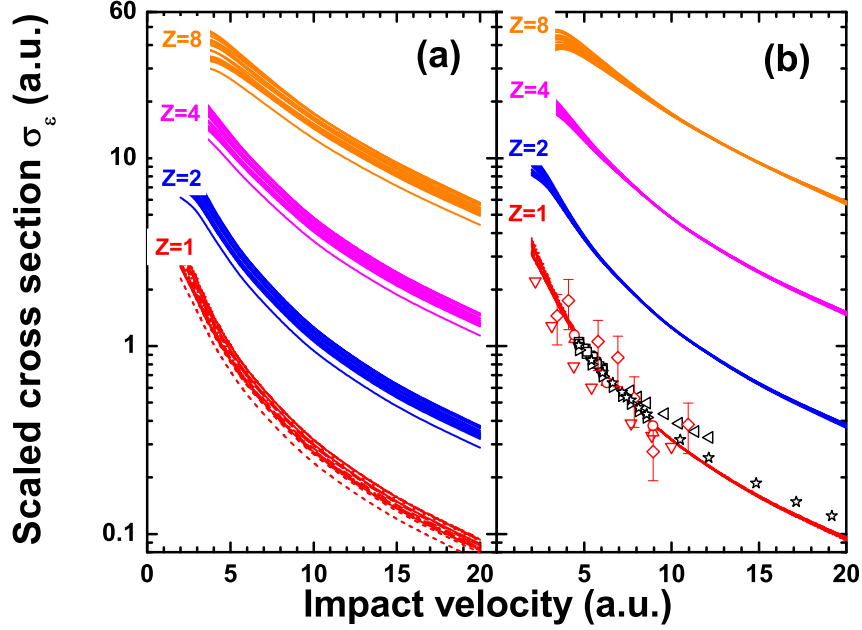


FIG. 6. Scaled ionization cross section per weakly bound electron using (a) the Toburen numbers  $\nu_\alpha^T$ , and (b) our proposed numbers  $\nu_\alpha^{\text{CDW}}$ . Experiments: proton impact on  $\circ$  adenine [15],  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23] and  $\diamond$  THF [25]; electron impact on  $\triangleright$  pyrimidine [24], and  $\triangleleft$ ,  $\star$  [26, 27] THF.

these numbers will be different. A similar dependence with the number of weakly bound electrons was found in Ref. [19] for proton impact on uracil and adenine.

By implementing the SSM, we computed the scaled CDW cross sections  $\sigma_e^T$  for the molecular targets of Table I. Our results are shown in Fig. 6a as a function of the impact energy for different projectile charges. Although the Toburen scaling holds for high energies, its performance is still not satisfactory: the universal band is quite broad, as can be noted in Fig. 6a.

## 2. New scaling

The departure of our theoretical results from the Toburen rule can be easily understood by inspecting Fig. 1. It can be noted that the rule  $\sigma_\alpha/\nu_\alpha^T \sim \sigma_e^T$ , approximately constant, is not well satisfied by the CDW. For example, Fig. 1 shows that the cross sections for O are

actually very similar to the cross sections for C, suggesting 4 active electrons in O instead of 6. In the same way, the number of active electrons for N, P and S are also different from the  $\nu_\alpha^T$  of Eq. (7).

Based on the CDW results, we propose a new scaling,

$$\sigma_e = \frac{\sigma_M}{n'_e}, \quad (8)$$

where  $n'_e = \sum_\alpha n_\alpha \nu_\alpha^{\text{CDW}}$ , and  $\nu_\alpha^{\text{CDW}}$  are the numbers of active electrons per atom obtained from the CDW ionization cross sections for different ions in H, C, N, O, P, and S targets, given as follows,

$$\nu_\alpha^{\text{CDW}} \sim \begin{cases} 1, & \text{for H,} \\ 4, & \text{for C, N, and O,} \\ 4.5, & \text{for P and S.} \end{cases} \quad (9)$$

The new scaled cross sections  $\sigma_e$  are plotted in Fig. 6b. A much better sharp band is observed, especially for impact energies  $E = (0.5 - 8)$  MeV/amu for  $Z = 1$  and  $Z = 2$ , and  $E = (2.5 - 8)$  MeV/amu for  $Z > 2$ . In fact, the experimental data for ionization of adenine [15], uracil [19], pyrimidine [23] and THF [25] by proton impact in Fig. 6b seems to corroborate the new scaling. We also included the electron impact ionization measurements with equivelocity conversion on pyrimidine [24], and THF [24, 26, 27]. It will be interesting to cross-check for experiments with higher projectile charge states.

Molecule	$n_e$	Molecule	$n_e$	Molecule	$n_e$
H <sub>2</sub>	2	C <sub>2</sub> H <sub>7</sub> N	19	C <sub>4</sub> H <sub>5</sub> N <sub>3</sub> O	37
H <sub>2</sub> O	6	C <sub>4</sub> H <sub>8</sub> O	28	C <sub>5</sub> H <sub>6</sub> N <sub>2</sub> O <sub>2</sub>	42
NH <sub>3</sub>	7	C <sub>4</sub> H <sub>4</sub> N <sub>2</sub>	28	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub>	45
CH <sub>4</sub>	8	C <sub>6</sub> H <sub>6</sub>	30	C <sub>5</sub> H <sub>5</sub> N <sub>5</sub> O	49
CH <sub>5</sub> N	13	C <sub>4</sub> H <sub>4</sub> N <sub>2</sub> O <sub>2</sub>	36	C <sub>5</sub> H <sub>10</sub> O <sub>5</sub> P	54.5

TABLE II. New scaling numbers for some molecular targets of biological interest.

By using Eq. (9), we define new active electron numbers  $n'_e$  for some molecular of interest in Table II. These values are very different from the ones proposed by Toburen and used by other authors [19]. Moreover, an alternative way of showing the scaling can be attained by plotting the ionization cross sections of molecules as a function of the number of active

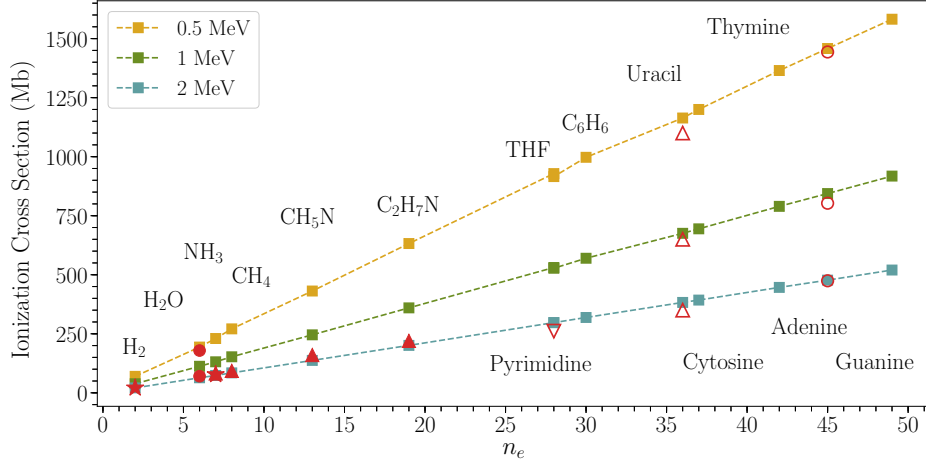


FIG. 7. Ionization cross sections by impact of protons at 0.5, 1 and 2 MeV in terms of the number of active electrons given by Table II. Experiments:  $\circ$  adenine [15],  $\triangle$  uracil [19],  $\nabla$  pyrimidine [23],  $\blacktriangle$  C<sub>2</sub>H<sub>7</sub>N, CH<sub>5</sub>N, methane and ammonia [28],  $\star$  ammonia and H<sub>2</sub> [29], and  $\bullet$  water [30].

electrons from Table II. Our findings are displayed in Fig. 7 for impact energies 0.5, 1 and 2 MeV. As can be noted, the computed CDW ionization cross sections for all the molecules show a linear dependence with the number of electrons from Table II. We obtain similar results even for  $E = 10$  MeV. The comparison with the experimental data available shows very nice agreement, from the smallest molecules, H<sub>2</sub>, H<sub>2</sub>O and CH<sub>4</sub>, up to the most complex ones, like adenine. For electron impact data, the experimental data was interpolated between close neighbors.

Finishing the present work we noted an accepted manuscript by Luedde *et al.* [31] who also noted a similar scaling at least for C, N, and O and reinforces the present finding.

### C. Molecular structure of targets

To test the range of validity of the SSM, we performed a full molecular structure calculation of five nucleobases. We employed the GAMESS code and used the 6-31G(d,p) basis set, which includes polarization functions for all the atoms. The calculations were carried out implementing the B3LYP functional [32, 33] to account for the correlation and exchange effects.

The molecular binding energies of the valence electrons for adenine, cytosine, guanine, thymine and uracil are shown in Fig. 8. We can compute the center of gravity of these

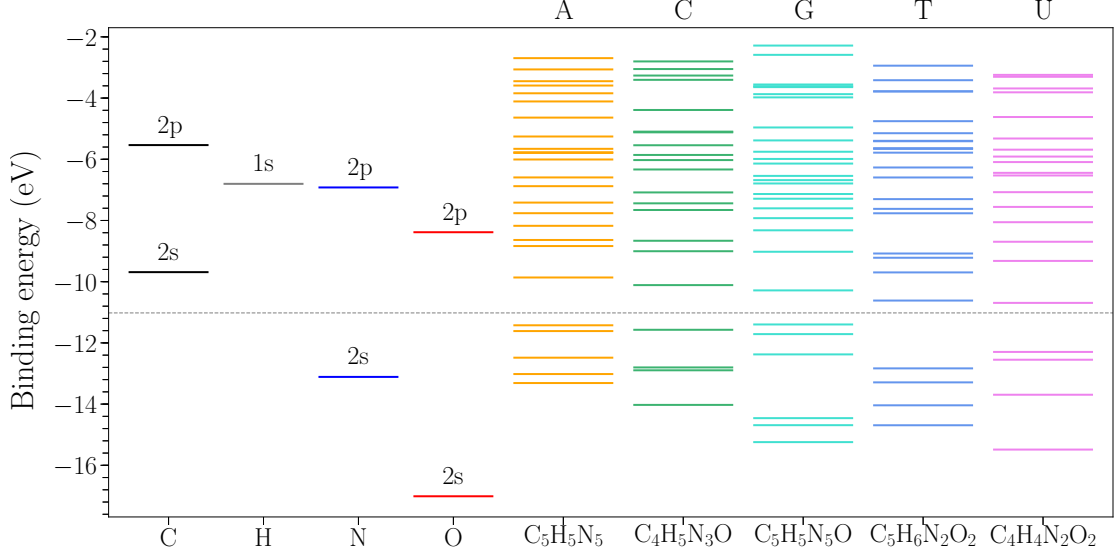


FIG. 8. Theoretical molecular binding energies for adenine, cytosine, guanine, thymine and uracil compared to those of atomic constituents.

molecular energy levels as an average weighted by the electronic occupation number. The results obtained from the full molecular calculation are given in the first row of Table III. Similarly, we can compute the baricenter of the energy levels defined by the Toburen rule and the new rule, given by Eq. (9), which are also given in Table III. The average energy values obtained from the Toburen rule are around 20% of the full molecular ones. Surprisingly, the new scaling rule gives a significant improvement in the average energy values, reducing the relative errors to about 7%. This improvement would seem to indicate that the new scaling is appropriate.

$E_{av}$ (eV)	A	C	G	T	U
	<chem>C5H5N5</chem>	<chem>C4H5N3O</chem>	<chem>C5H5N5O</chem>	<chem>C5H6N2O2</chem>	<chem>C4H4N2O2</chem>
Theoretical calc.	-7.1955	-6.9058	-7.4725	-7.5304	-7.6224
Toburen rule	-8.4236	-8.6743	-8.7275	-8.7947	-9.0022
Present work	-7.9027	-7.8639	-7.9420	-7.8066	-7.8839

TABLE III. Center of gravity of the molecular energy levels of five nucleobases.

Furthermore, on the left side of the Fig. 8, we show the atomic Hartree–Fock energies of the constituent elements, which gives an insight on the distribution of the weakly bound

electrons. A dashed line around  $-11$  eV is drawn to separate the band in two. We can consider the atomic energy levels above this line as the ones corresponding to the weakly bound electrons from Eq. (9). For example, the  $2s$  and  $2p$  electrons of carbon are placed above the separating line, which corresponds to the 4 electrons given by Eq. (9). In the case of O, only the 4 electrons of the  $2p$  orbitals are located above the separating line, which corresponds to the number of weakly bound electron given by our new scaling. The N case is not as straightforward; the  $\nu_\alpha^{\text{CDW}}$  value given for N would suggest that some  $2s$  electrons corresponding to the molecular scheme are also weakly bonded, leading to 4 electrons.

### 1. A modified stoichiometric model

The SSM considers the molecule to be assembled by isolated neutral atoms, which is definitively unrealistic. A first improvement can be suggested by assuming that the atoms are not neutral and that they have an uneven distribution of electrons within the molecule; this distribution can be given by an effective charge  $q_\alpha$ . A possible value for  $q_\alpha$  is given by the Mulliken charge. However, there are a wide variety of charge distributions, such as the net or natural atomic charge [34], the Löwdin charge, etc.

Consider that the total amount of electrons  $Q_\alpha$  on the element  $\alpha$  are equally distributed on all the  $\alpha$  atoms. Therefore, each element  $\alpha$  will have an additional charge:  $q_\alpha = Q_\alpha/n_\alpha$ , which can be positive or negative. This value will depend on the relative electronegativity value with respect to the other atoms [35]. Now, instead of an integer number of elements  $n_\alpha$  of the atom  $\alpha$ , we have a fractional number of atoms given by

$$n'_\alpha = n_\alpha - \frac{q_\alpha}{\nu_\alpha^{\text{CDW}}} \quad (10)$$

In the case of neutral atoms,  $q_\alpha = 0$  and we recover  $n'_\alpha = n_\alpha$ , as it should be. In Table IV, we display the average effective charge per atom  $q_\alpha$  of C, H, N and O, for five DNA molecules. The charges were obtained from the full molecular calculation described above.



Element	C	H	N	O	New stoichiometry
Adenine	+0.32	+0.23	-0.55		C <sub>4.92</sub> H <sub>4.77</sub> N <sub>5.14</sub>
Cytosine	+0.28	+0.21	-0.56	-0.53	C <sub>3.93</sub> H <sub>2.79</sub> N <sub>5.14</sub> O <sub>1.13</sub>
Guanine	+0.46	+0.20	-0.58	-0.36	C <sub>4.89</sub> H <sub>4.80</sub> N <sub>5.15</sub> O <sub>1.09</sub>
Thymine	+0.20	+0.19	-0.54	-0.52	C <sub>4.95</sub> H <sub>1.81</sub> N <sub>6.13</sub> O <sub>2.13</sub>
Uracil	+0.31	+0.22	-0.59	-0.47	C <sub>3.92</sub> H <sub>1.78</sub> N <sub>4.15</sub> O <sub>2.12</sub>

TABLE IV. Average effective Mulliken charge per atom  $q_\alpha$ , and new stoichiometric formula defined by Eq. (10) for five DNA molecules.

By implementing Eq. (10), it is possible to determine a new stoichiometric formula (last column of Table IV). Now, instead of having an integer number of atoms  $n_\alpha$ , we obtain a fractional number  $n'_\alpha$ . New molecular cross sections  $\sigma'_M = \sum_\alpha n'_\alpha \sigma_\alpha$  can be computed considering such values. Relative errors for the ionization cross sections were computed for the DNA bases from Table IV. The differences obtained were less than 3%, which indicates that the modified SSM is a quite robust model to handle these type of molecules within the range error expected for this model.

#### IV. CONCLUSIONS

In this work we have encouraged the calculation of ionization cross sections of seventeen biological molecules containing H, C, N, O, P and S by impact of antiprotons,  $H^+$ ,  $He^{2+}$ ,  $Be^{4+}$ ,  $C^{6+}$ , and  $O^{8+}$ . To that end we have employed the full CDW method including... and a simple stoichiometric model. The mean energy and angle of the emitted electrons, of importance in post-collisional radiation damage, has also been calculated, showing a clear dependence with the ion charge  $Z$ . For a given target as  $Z$  increases,  $\bar{E}_\alpha$  increases, but  $\bar{\theta}_\alpha$  decreases. At impact energies larger than 1 MeV/amu, these values converge to the Born approximation, which embodies the simple  $Z^2$  law.

Total ionization cross sections for adenine, cytosine, thymine, guanine, uracil, DNA backbone, pyrimidine and THF are presented and compared with the scarce available experiments. We explore the rule of Toburen which scales all the molecular ionization cross section normalizing with certain number of weakly bound or valence electrons. We found

that ionization cross sections scales much better when normalizing with the number of active electrons in the collision obtained from the CDW results for atoms. This new scaling was tested with very good results for the six projectiles and seventeen molecules studied here. The comparison with the experimental data reinforce this results. Moreover, we also test the scaling by including experimental data of ionization of H<sub>2</sub>, water, methane and ammonia by proton impact showing good agreement at intermediate to high energies. Finally, we performed full molecular calculations for the DNA basis. By inspecting the molecular binding energy from quantum mechanical structure calculations, we were able to understand the number of electrons proposed in our new CDW-based scaling. We attempt to improve the stoichiometric model by using the Mulliken charge to get fractional rather than integer proportions. It is interesting to remark that no substantial correction was found, which indicates that the SSM works quite well.

The main objective of this article was to provide the tools to estimate any inelastic parameter –such as emission angle, emitted mean energy and cross section– by the impact of any multicharged projectiles on any molecule containing H, C, N, O, P and S, with the help of the stoichiometrical model. Our goal was quite ambitious, considering the simplicity of our proposal. However, the present results show the validity of the simple stoichiometric model to estimate the ionization magnitude with an acceptable level of uncertainty.

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