

# CAB320 – Constraint Satisfaction Problems

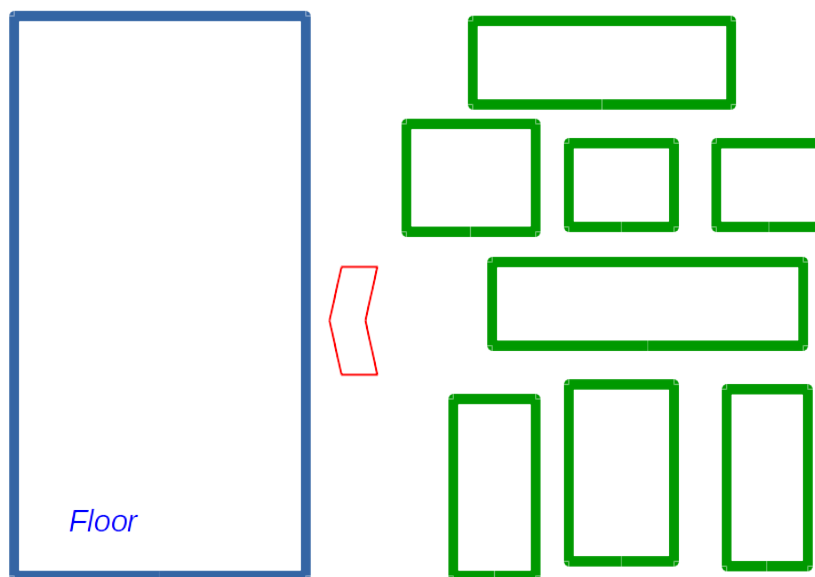
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The first exercise requires you to model a practical problem as a *Constraint Satisfaction Problem* (CSP). The challenge is to identify what are the relevant variables and what are the constants of an instance of the problem. In a CSP, each state is represented as a partial assignment of values to variables (some variables don't get assigned a value immediately). For example, in a map coloring problem, we associate a variable to each region. These variables get assigned a color in such a way that two adjacent regions receive distinct colors.

The second exercise is a programming exercise where you are asked to complete a subclass of our generic search *Problem* class for constraint satisfaction problems. The third exercise presents a *local repair* approach to CSP. We start in a state with conflicting variables and iteratively try to reduce the number of conflicts.

## Exercise 1 [non programming]

- Articulate a CSP formulation for the *Rectilinear floor planning problem*: find non-overlapping locations in a **large rectangle** for a set of **smaller rectangles**. Here we do not consider other constraints that would arise in practical applications. We are only interested in expressing with formulas the *non over-lapping* constraints the smaller rectangles have to satisfy. Assume that the smaller rectangles can be moved by translation only (no rotations) and that you are given the size of all rectangles.



*Illustration 1: Floor is in blue. Objective is to pack a set of non-overlapping green rectangles on the floor. We keep the rectangles axis parallel.*

## Exercise 2 (DFS for CSP)

- Open the file `cab320_csp.py`
- In the class `CSP`, how are state represented? What is the data structure used?
- What is an 'action' in the context of the `CSP` class? How is an action represented? (Hint: look at the method 'result')
- What are the 'neighbors' of a variable in 'csp\_vars' ?
- How do you translate the 'goal\_test' function in plain English?
- Complete the function 'actions' of the class `CSP`
- Test your `CSP` class implementation with a DFS on the `MapColoringCSP` problems.

## Exercise 3 (Stochastic hill climbing)

In a search by stochastic hill climbing, we first start in a state where each variable has been assigned a value. This state might contains conflicting variables. After this initialization, we keep trying to reduce the number of conflicted variables. That is, we loop until we find a state with no conflict or we run out of time. In other words, the body of the main loop consists in the following steps;

- compute the list of conflicted variables (hint: use 'csp.conflicted\_vars' method)
- if no variable are conflicted, we have reached a state that satisfy all the constraints
- Otherwise, we pick randomly one of the conflicted variables and assign to it a value that minimizes the number of conflicts (hint: use 'random.choice' and the function 'min\_conflicts\_value')

For the initialization step, we should also leverage the function 'min\_conflicts\_value' to start with a state that is better than a random assignment. We can create the initial state by iterating over the variables in 'csp.csp\_vars' and assigning the value returned by 'min\_conflicts\_value(csp, var, current)' where 'current' is the current state and 'var' is the variable for which we want to find a value.

Implement this algorithm as the 'min\_conflicts' function and test it on the `MapColoringCSP` problems.