

# Information Asymmetry and Monetary Non-Neutrality: A Sequential Search Approach \*

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## Abstract

This paper develops a model of monetary non-neutrality driven by information asymmetry between consumers and firms about nominal marginal costs in a sequential search framework. With only consumer-side frictions, this approach is distinguished from the standard one that relies on firm-side pricing frictions. Consumers' value of search is determined by their information about the price index, and firm's elasticity of demand depends on the perceived relative price. The passthrough of aggregate shocks to prices is therefore incomplete. The key mechanism is that, following a monetary shock, consumers attribute some of the resulting price changes to firm-specific adverse shocks, inducing them to search for alternatives. To dissuade search, firms compress the markup and limit the passthrough of the shock. I further show that the output gap is proportional to the nowcast error of price index in the Phillips curve. Despite its parsimonious nature, the calibrated dynamic general equilibrium model can generate substantial monetary non-neutrality. Consistent with the mechanism, higher inflation is associated empirically with more active consumer search.

**Keywords:** Monetary non-neutrality, Phillips curve, Search, Information frictions, Information asymmetry, Passthrough, Higher-order beliefs

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*“This paper presents a theory that justifies price stickiness, namely, that firms, fearing to upset their customers, attribute a cost to price changes.”*

— Rotemberg (1982)

Monetary policy is known to have large real effects on the economy in the short run. Both output and inflation decline following an unexpected increase in interest rate. This pattern has been repeatedly uncovered in the empirical literature.<sup>1</sup> Most of existing theories explain this phenomenon by focusing on frictions on the firm side. Models of price stickiness posit that price adjustments are infrequent due to either exogenous factors (Taylor, 1980; Calvo, 1983) or fixed costs (Mankiw, 1985; Golosov and Lucas, 2007). Another theory which dates at least back to Phelps (1969) and Lucas (1972) suggests that firms set prices based on incomplete information about aggregate shocks. Reis (2006) and Alvarez et al. (2016) further argue that costs of acquiring and processing information contribute to price rigidity.

Growing evidence suggests that consumers face more severe frictions than firms. For instance, consumers have misperception about inflation (Binetti et al., 2024; Candia et al., 2023) and pay particular attention to salient prices (Kumar et al., 2015; D’Acunto et al., 2021). Moreover, Kaplan and Menzio (2015) and Kaplan et al. (2019) document a large price dispersion for an identical product even within the same market and week. This firms’ market power reveals consumer-side frictions that prevent them from finding the cheapest product. These evidence motivates two central questions: Can we micro-found monetary non-neutrality using only the consumer-side frictions? How do these consumer-side frictions affect the transmission of monetary policy?

To address these questions, I develop a new monetary model that places consumer-side frictions at the center. Consumers face two frictions: (i) information friction about firms’ nominal marginal costs and (ii) search frictions on the goods market. On the other hand, firms have full information about the model economy and set the prices flexibly. The monetary authority sets the nominal wage. A monetary shock is modeled as a shock to the nominal wage. The main mechanism operates as follows. Following a positive monetary shock, the nominal wage increases. Firms tend to increase prices. However, shoppers with incomplete information about the nominal wage attribute much of

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<sup>1</sup>Christiano et al. (1999) identify this effect using timing restrictions in VAR. Recently, high-frequency identification approach helps resolve the endogeneity bias in the VAR approach and confirms this finding (Gertler and Karadi, 2015; Bauer and Swanson, 2023). Hazell et al. (2022) estimate the slope of Phillips curve to be very flat using cross-state variation in price indices. Ramey (2016) provides a great summary of this literature.

this price increase to firm-specific adverse shocks. Shoppers who are initially indifferent between purchasing and searching are now incentivized to seek outside options. To dissuade search, firms compress markups, thereby limiting the passthrough of the monetary shock.

I start with a static model to show the core mechanism. The model features shoppers, firms, and a monetary authority. The shopper's problem follows the sequential search literature (Wolinsky, 1986; Anderson and Renault, 1999). Specifically, shoppers search sequentially and randomly without commitment. Shoppers must incur a search cost to visit a firm and learn the price. I extend the framework from the literature in two ways. First, firms are heterogeneous in productivity. Second, shoppers have incomplete information about the nominal wage. These two features lead to shoppers' rational confusion between the aggregate (nominal wage) and idiosyncratic (firm productivity) components of the cost. In particular, when observing a price, shoppers who believe the nominal wage is low will interpret the price as indicative of encountering a firm with low productivity and vice versa.

Each shopper receives a signal about the nominal wage before shopping. They construct their own perceived price distributions using posterior belief of the nominal wage and the knowledge imposed by the rational expectations equilibrium. The value of an additional search depends crucially on the perceived price distribution. I show that the optimal search strategy is characterized by a threshold rule: if the value of a good exceeds the threshold, the shopper proceeds with the purchase. Otherwise, the shopper continues shopping. Firm's demand is derived from the aggregation of individual shopper's optimal search decisions. Firms then select the optimal pricing strategy that maps the idiosyncratic productivity and the nominal wage to its price.

I start with the characterization of the full-information rational expectations equilibrium where the only friction is consumers' search costs. First, I prove the existence of a unique equilibrium in which shoppers search actively. Then, I show the first main result of this paper: under full information about the nominal wage, the monetary policy is neutral. The key takeaway of this result is that the search friction alone is not sufficient to generate monetary non-neutrality. We need the interplay of these two frictions.

To characterize the incomplete-information rational expectations equilibrium, I rely on first-order approximations. I show that the threshold decreases with shopper's expectation of the price index. The intuition is simple: shoppers are more inclined to make purchases when they expect a higher price index and therefore, worse outside options. Next, I show that the elasticity of demand

increases with the perceived relative price, defined as the ratio between the actual firm's price and the average expectation of price index. Due to the information friction, the average expectation of the change in price index is typically dampened compared to the actual one. As a result, firms behave as if they are competing against other firms setting lower prices. In response, firms lower their prices, which compresses the markup and limits the passthrough of the shock. The key takeaway is that firms respond to shopper's expectation of the price index rather than the actual one.

Next, I characterize the aggregate total passthrough, i.e., the passthrough from the shock to the price index. The total passthrough is composed of two fundamental passthroughs as seen in the literature (Amiti et al., 2019): own-cost passthrough and cross-price passthrough. I then present the main theorem of this paper: (i) the aggregate total passthrough is generically incomplete and (ii) high-productivity firms contribute more to the incompleteness, and (iii) the aggregate total passthrough decreases with both frictions, with one friction amplifies the effect of the other.

The aggregate total passthrough brings the intuition we developed before for the individual firms to the aggregate. Consider an extreme case where shoppers have no information about the nominal wage. In this scenario, a nominal wage shock resembles an idiosyncratic shock to firms, and the aggregate total passthrough reduces to the aggregate own-cost passthrough. When shoppers possess some information, firms start to respond to other firms' prices perceived by shoppers. The aggregate response of firms can be understood as occurring in iterative rounds. In each round, firms incorporate part of the additional change in the price index from the previous round into their prices, with the passthrough attenuated by shoppers' information frictions. Iterating ad infinitum, the aggregate total passthrough ultimately represents the infinite sum of these rounds of cross-price passthroughs, with each successive round increasingly attenuated, leading to the incomplete passthrough.

In the last section of the static model, I characterize the Phillips curve. It has following properties. First, it does not depend on the future inflation expectation. In particular, the output gap is proportional to the nowcast error of price index. Second, unlike the modern Phillips curve literature that emphasizes the role of firm's expectation in the determination of the slope, this model provides a mechanism through which household expectations can influence firms' pricing decision. Moreover, the slope of Phillips curve can be decomposed into two parts, each corresponding to a specific consumer-side friction. The slope decreases in both frictions.

Then, I incorporate the main mechanism from the static model into a dynamic general equilibrium model. In the model, monetary policy sets the nominal interest rate. Shocks are persistent. Shoppers search period by period, and in each period, they receive a signal about the inflation and learn about the shock over time. I present a three-equation system that describes the joint dynamics of aggregate consumption, inflation and interest rate.

I then calibrate the model parameters to match the moments from the literature and my own empirical finding. In particular, the aggregate own-cost passthrough is a sufficient statistic that summarizes the “deep” parameters related to the search friction. I take its value from Amiti et al. (2019) and Gopinath et al. (2011). Next, I estimate the impulse responses of inflation and inflation expectation following a main inflation shock (Angeletos et al. (2020a)). I calibrate the information friction such that the time needed for the nowcast error shrinking to zero in the model is similar to its empirical counterpart.

Despite the model’s parsimonious nature, the calibrated model can generate substantial monetary non-neutrality comparable to a standard New-Keynesian (NK) model with Calvo parameter equal to 0.7. That is, 70% firms cannot adjust prices in each period. The new insight in the dynamic model is that since the output response depends on the gap between the actual inflation and inflation nowcast, rapid learning can close this gap before the shock fully dissipates, leading to endogenously reduction in the persistence of the output response.

Finally, I present empirical evidence that supports my mechanism. I use the 2006–2019 NielsenIQ Consumer Panel data, which includes approximately 55,000 households annually, with each household participating in the panel for an average of 30 quarters. The search behavior observed in the data demonstrates path-dependence and a “one-stop” shopping pattern. To capture actual search efforts, I first calculate the spending in a given product category that does not occur in the store the consumer visits most frequently. I then derive the non-routine share of total spending by summing this spending across all product categories. The average non-routine share of spending is about 35%. I find that one standard deviation (51 bp) increase in unanticipated inflation for food and drinks leads to a 26.5 bp increase in the non-routine share of spending. The response is highly statistically significant. The magnitude of response is modest (about a half) and I discuss several reasons that could potentially bias the estimate downward.

I conclude the empirical section by documenting the secular decline in both the non-routine share of spending and the average shopping time. I argue that this trend aligns with the increasing

market concentration and price uniformity in the retail industry. Furthermore, I connect this empirical pattern to the observed decline in the secular slope of the Phillips curve, highlighting the potential macroeconomic implications of these structural changes in consumer behavior and market dynamics.

**Related Literature** – This paper contributes to three strands of literature. The first studies the price stickiness and monetary non-neutrality by focusing on the consumer-side mechanisms. The prominent paper in this literature is Matějka (2015). He shows that firms set discrete prices as consumers “hate” price fluctuations, which increases their costs of attention. My paper has the similar flavor in the sense that the price stickiness originates from the strategic interaction between consumers and firms. However, my paper has different mechanisms and investigates these mechanisms in general equilibrium. Gabaix and Graeber (2024) and Rebelo et al. (2024) propose behavioral theories of price stickiness. My paper is within the realm of rational expectations.

Second, it adds to the research on the role of search frictions in explaining price stickiness. Based on Burdett and Judd (1983), Head et al. (2012) show that price stickiness can result from the mixed pricing strategy. As nominal price increases, profit can still be maximized despite a fall in real price. However, in their model, the money is neutral. Similarly, Burdett and Menzio (2018) incorporate same mechanism into a menu-cost model, where a broader range of optimal prices leads to larger price adjustments. Benabou (1988) shows that when monopolistic competition arises from costly consumer search, the inaction region in a menu-cost model expands with increasing search costs. Gaballo and Paciello (2021) show a model where consumers are motivated to leave the monopolistic firm and find lower prices in a separate market where firms have perfect competition, when the inflation rises. The price is sticky because some demand shifts to the low-price market. However, my paper does not rely on the separation of markets, and firms are heterogeneous in productivity and compete monopolistically in a unified market. This paper advances this second stream by integrating search models à la Wolinsky (1986) and Anderson and Renault (1999) with a heterogeneous firm block, a monetary general equilibrium framework, and incomplete information on the consumer side.

Third, this paper contributes to the literature on the role of consumer-side information frictions in explaining monetary non-neutrality. Bénabou and Gertner (1993), L’Huillier (2020) and L’Huillier and Zame (2022) focus on the role of individual prices consumers observe during the search as revealing the information about aggregate shocks. Especially, L’Huillier (2020) consider

a signaling game between a monopolistic firm and consumers. The price of one firm is rigid if we select the pooling equilibrium. That price becomes more volatile in the separating equilibrium than the full-information case. I shut down the signaling effect and my mechanism does not rely on the equilibrium selection. This paper also broadly contributes to the literature on information frictions and the transmission of monetary policy. For example, Angeletos and La'O (2013) model aggregate demand fluctuations driven by sentiment in beliefs. Venkateswaran (2014) examines an incomplete-information version of the Diamond–Mortensen–Pissarides model. Angeletos and Lian (2018) show that incomplete information games among consumers can mitigate the forward guidance puzzle.

**Outline** – The rest of the paper is organized as follows. Section 1 presents a static model and establishes the main results on the passthrough. Section 2 presents the dynamic model and the calibration results. Section 3 shows empirical evidences. The last section concludes. Appendix A contains some of the proofs omitted from the text. Appendix B contains the proof of the dynamic model and additional calibration details. Appendix C contains details of empirical setup and additional empirical evidence.

## 1 Static Model

I develop a macroeconomic model with (i) information asymmetry between shoppers and firms about marginal costs and (ii) search frictions on the goods market. I proceed in two steps. First, I present a static model to explain the core mechanism. Second, I present a full-fledged dynamic general equilibrium framework in the next section.

I first consider static partial equilibrium model in which there are firms, shoppers and a monetary authority and then close the model in the general equilibrium.

**Notation** – I use lower case to denote  $\log Y$  for any variable  $Y$ , i.e.,  $y = \log Y$  and lower case with hat to denote log-deviation from the steady-state value, i.e.,  $\hat{y} = \log Y - \log \bar{Y}$ .

### 1.1 States, Strategies and Distributions

At the beginning of each period, the Nature draws the aggregate state  $w$  from a given distribution  $\Phi_w$ , idiosyncratic states for each firm  $a_k$  from  $\Phi_a$ , idiosyncratic noisy signals for each shopper  $x_i$  from  $\Phi_x$  about the aggregate state  $w$ .  $\Phi_w, \Phi_x, \Phi_a, G$  are the common knowledge for all agents. Each firm produces a good and selects the optimal pricing strategy that maps its state  $\{a_k, w\}$  to the price of its good, i.e.,  $p_k = p^*(a_k, w)$ , where  $p : \mathcal{R}^2 \rightarrow \mathcal{R}$ . The optimal pricing strategy

$p^*$  monotonically decreases in  $a_k$  and increases in  $w$ . Variation in  $a_k$  across firms induces a price distribution  $F(p|w)$ , which has a density distribution  $f(p|w)$ . Let  $p^{*-1}(p, w)$  denote the inverse mapping from  $p_k$  to  $a_k$  given  $w$ . It is straightforward to show that  $p^{*-1}$  monotonically decreases in  $a_k$  and increases in  $w$ . The price distribution conditional on  $w$  is given by,

$$F(p|w) = 1 - \Phi_a(p^{*-1}(p, w)) \quad (1)$$

In the rational expectations equilibrium, shoppers know the equilibrium pricing strategy  $p^*$ . Conditional on knowing  $p^*$  and  $w$ , the shoppers are able to derive the price distribution. However, they have incomplete information about  $w$ . Their posterior belief about  $w$  is denoted by  $H(w|x)$ . The shopper's perceived price distribution conditional on  $x$ ,  $f(p|x)$ , is given by,

$$f(p|x) = \int f(p|w)h(w|x)dw \quad (2)$$

The above equation has two implications. First, when  $x = w$ , the perceived and objective price distributions coincide. Second, if  $h(w|x_i)$  first-order stochastically dominates (FOSD)  $h(w|x_j)$ , then  $f(p|x_i)$  FOSD  $f(p|x_j)$ . Intuitively, when the shopper places more probability weights on low  $w$ , since prices increase in  $w$ , the perceived price distribution is stochastically smaller.

Moreover, the shopper forms the expected idiosyncratic state of firm  $k$  after observing the price  $p_k$ ,

$$E(a_k|x) = \int p^{*-1}(p_k, w)h(w|x)dw \quad (3)$$

Similarly, it is obvious to show that  $E(a_k|x_i) < E(a_k|x_j)$  when  $h(w|x_i)$  FOSD  $h(w|x_j)$ . The shopper who believes the nominal wage is low will perceive the firm's  $a_k$  as lower than its actual value.

Finally, shoppers search sequentially and have free recall. Each shopper's search strategy depends on the perceived price distributions  $F(p|x)$ . The optimal search strategy can therefore be represented as a function that maps  $x$  to an optimal utility level,  $v_i = v^*(x)$ , where  $v^* : \mathcal{R} \rightarrow \mathcal{R}$ . This strategy then determines the demand allocation across firms on the aggregate. In the rational expectations equilibrium, firms know the equilibrium search strategy  $v^*$  and select optimal pricing strategy  $p^*$  that maximizes the profit.

## 1.2 Setup

Now, I state the model. Time is discrete and infinite  $t \in \mathbf{N}$ . The timeline is as follows. Within a period, the monetary authority first sets the nominal wage. Shoppers are endowed with cash and



form a conditional distribution about prices. Firms post prices and shoppers search sequentially. A fraction of shoppers make the purchase in a given round and the remaining keep searching. The period ends until all shoppers make the purchase. I denote the round of search  $r = 1, 2, 3, \dots$  within a period. All rounds of search happen within one period.

**Firm** – The economy is populated with a unit mass of firms indexed  $k \in [0, 1]$ , each of which produces a differentiated product using the following production technology,

$$Y_k = A_k L_k \quad (4)$$

where  $L_k$  is the amount of labor employed.  $A_k$  is the firm's productivity, which is i.i.d. across firms. Specifically, I assume that  $\log A_k$  draw from the normal distribution  $\mathcal{N}(0, \sigma_a^2)$ . The marginal cost is  $\frac{W}{A_k}$ , where  $W$  is the nominal wage. The nominal wage represents the average nominal marginal cost. Labor is supplied outside this economy for now.

**Monetary Authority** – The monetary authority directly controls the nominal wage  $W$ . It draws  $w$  from the normal distribution  $\mathcal{N}(\bar{w}, \sigma_w^2)$ . Monetary shock is defined as  $\hat{w} = w - \bar{w}$ .

**Shopper** – The economy is populated with a continuum of shoppers indexed by  $i \in [0, 1]$ . At the beginning of the period, each shopper is endowed with cash  $X_i$ . It follows,

$$X_i = W \exp\left(\sigma_x \varepsilon_{xi} - \frac{\sigma_x^2}{2}\right) \quad (5)$$

where  $\varepsilon_{xi}$  is i.i.d. across shoppers and it follows  $\varepsilon_{xi} \sim \mathcal{N}(0, 1)$ . It is also independent of productivity shocks and monetary shocks. The shopper treats  $X_i$  as signal about  $w$ . The expected (log) nominal wage is then given by,

$$E(w|x_i) = \theta x_i + (1 - \theta)\bar{w} \quad (6)$$

where  $\theta = \frac{\sigma_x^{-2}}{\sigma_w^{-2} + \sigma_x^{-2}}$ . Let  $H(w|x_i)$  denote the posterior belief about the nominal wage with density  $h(w|x_i)$ . Based on Bayes' rule, it follows  $\mathcal{N}(E(w|x_i), (\sigma_w^{-2} + \sigma_x^{-2})^{-1})$ . Shoppers construct their perceived price distribution according to (2).

The shopper consume one good.<sup>2</sup> The utility that shopper  $i$  gains from consuming good  $k$  is given by,

$$\log \frac{Z_i}{P_k} + \frac{1}{\lambda} \epsilon_{ik} \quad (7)$$

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<sup>2</sup>In Section 1.5, I extend the model by allowing shoppers to get access to a bunch of goods by incurring one search cost.

where  $\epsilon_{ik} \sim G$  is match utility between shopper  $i$  and good  $k$ .  $G$  is twice continuously differentiable and its density function is  $g$ . It captures idiosyncratic consumer preferences for certain goods over others.  $\epsilon_{ik}$  are i.i.d across firms and shoppers.<sup>3</sup> Also, following the literature, I assume that  $G$  is log-concave. Note that some commonly used distribution functions are log-concave, e.g., normal distribution, uniform distribution, Gumbel distribution.<sup>4</sup> The parameter  $\lambda$  controls the relative importance between the two types of utility. A larger  $\lambda$  implies that the shopper places greater value on utility from consumption relative to match utility. Relative prices are less important in the purchase decision. Since  $X_i$  only affects the level of utility and does not change the relative utilities across goods, I define the normalized utility as follows,

$$y_{ik} = -p_k + \frac{1}{\lambda} \epsilon_{ik} \quad (8)$$

Shoppers search sequentially and randomly following Wolinsky (1986) and Anderson and Renault (1999). By incurring a search cost  $\kappa > 0$ , the shopper can visit a firm to learn both its price and the associated match utility. Shoppers have free recall, meaning there are no additional costs for purchasing goods from firms they have previously visited. According to (8), the distribution of value of drawing a random firm  $y$  is a convolution of the perceived price distribution and the distribution of match utility,

$$\psi(y|x) = \int f(u - y|x) \lambda g(\lambda u) du \quad (9)$$

Importantly, I assume that  $h(w|x)$  remains fixed throughout all rounds of search. I impose the following restriction on shoppers' information sets.

**Assumption 1.** *Shoppers do not infer the nominal wage from individual prices they observe during the search.*

This assumption is plausible if the idiosyncratic variations, contributed by productivity shocks, in prices are way larger than the aggregate variations induced by the nominal wage. Even when a shopper consistently encounters firms charging high prices, she attributes this to bad luck rather

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<sup>3</sup>The price distribution is not degenerated if the random utility term is match-specific. If it is only shopper-specific, it does not matter for the search strategy. Firms compete only on price. The price distribution is degenerated to a single optimal price. If it is only good-specific, the price distribution will be exogenous.

<sup>4</sup>See Bagnoli and Bergstrom (2005) for a broad discussion of log-concavity that do and do not satisfy this condition. The assumption of log-concavity ensures that the hazard rate  $\frac{g(x)}{1-G(x)}$  is monotonically increasing.

than an increased nominal wage. I make this assumption for tractability. If shoppers' information sets depend on the whole search history, it leads to exploding states and the model becomes intractable. As I will show, The main mechanism remains valid as long as information friction exists. It is independent of how shoppers acquire information. In Section 2, I assume that shoppers receive a signal about the current inflation before searching as an alternative way to incorporate learning from shopping.

I now state the shopper's problem. The shopper undertakes sequential search with perfect recall and without being restricted by any plan made before setting out to search. I refer to the latter as search without commitment.<sup>5</sup> Let  $v_{ir}$  denote the maximum value of previously visited firms in  $r$ th round. In particular, after sampling the first firm,  $v_{i1} = y_{i1}$ . I define  $v_{ir}$  for  $r > 1$  as follows,

$$v_{ir} = \max\{v_{ir-1}, y_{ir}\} \quad (10)$$

In the  $r$ th round of the sequential search, the state of the shopper is  $v_{ir}$ . The shopper has the option to stop searching and accept  $v_{ir}$  or continue searching. The value function for the shopper,  $U : \mathcal{R} \rightarrow \mathcal{R}$ , in each state  $v \in \mathcal{R}$ , satisfies,

$$U(v|x) = \max \left\{ v, -\kappa + U(v|x) \int_{-\infty}^v \psi(y|x) dy + \int_v^{\infty} U(y|x) \psi(y|x) dy \right\} \quad (11)$$

The maximum represents that the shopper can either receive the maximum value  $v$  until this round and stop searching more, or continue searching by incurring a search cost  $\kappa$  and drawing a random good. If the value of that good is lower than  $v$ , which occurs with probability  $\int_{-\infty}^{v_{ir}} \psi(y|x_i) dy$ , the shopper will retain the value  $U(v)$ , since she has free recall. Otherwise, she will obtain a higher value from the newly drawn good and update  $v$  according to (11). The value function  $U$  is stationary only when Assumption 1 holds. Otherwise, with the information sets expanding over the rounds of search, the value function  $U$  should be indexed by the search round.

The shopper's problem is solved in two steps. First, she finds the  $U$  function that solves the functional equation (11). Second, she keeps sampling firms until  $v$  first exceeds the expression to the right of the comma in (11).

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<sup>5</sup>If the shopper formulated her search plan prior to search and she committed to that plan, then she would take into account the expected total search costs of sampling., and she would stop with a lower quality match if she were unlucky and happened to sample a sequence of firms for which she ill-suited. In the case of a shopper doing sequential search without commitment, she ignores past fixed costs of search as sunk. Burdett and Judd (1983) considers a search problem with commitment and homogeneous firms.

**Partial Equilibrium** – The equilibrium concept is Perfect Bayesian Nash equilibrium (PBNE). Since productivity is assumed to have unbounded support, any positive price is an on-equilibrium price. The regulations on the off-equilibrium belief is not strictly needed in this model.<sup>6</sup> Formally, I define the equilibrium as follows:

**Definition 1** (Equilibrium). *A Perfect Bayesian Nash equilibrium is a triplet of allocation, prices, and beliefs such that*

1. *Firms choose the optimal pricing strategy  $p^*$  to maximize profits given the optimal search strategy.*
2. *Shoppers search without commitment. They do not update beliefs after observing prices during the search. Conditional on the information sets, they combine the optimal pricing strategy  $p^*$  and other exogenous distributions to compute  $U(v|x)$  for each state  $v$ . Shoppers' optimal search strategy is then determined by the stopping rule as shown in (11).*
3. *Nominal wage is chosen exogenously.*
4. *Goods market clears.*

In addition, I define the full-information equilibrium in which shoppers know the nominal wage. It serves a natural benchmark to analyze the incomplete-information equilibrium.

**Definition 2** (Full-Information Equilibrium). *A full-information equilibrium is the equilibrium defined above, except that shoppers know  $w$ .*

### 1.3 Equilibrium Characterization

I now characterize the equilibrium. I proceed in three steps. First, I characterize the search strategy and the pricing strategy. Second, I show the existence and properties of full-information equilibrium. Third, I show the monetary neutrality under full information.

**Characterization of the Search Strategy** – I first characterize the search strategy. The shopper needs to first find the  $U$  function and then decide when to stop searching. The solution to the shopper's problem is presented in the following proposition,

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<sup>6</sup>In the standard search literature, prices are bounded and consumers know the range of prices. Therefore, they are able to detect the off-equilibrium prices. The regulation of off-equilibrium belief in the case where consumers observe prices not in this range is needed.

**Proposition 1.** *Under Assumption 1, the optimal search strategy follows a threshold rule. The threshold is denoted  $v^*(x)$ . If  $v < v^*(x)$ , the shopper keeps searching; otherwise, she stops and makes the purchase. The threshold is unique for each  $x$ . It is determined by,*

$$v^*(x) = -\frac{\kappa}{1 - \Psi(v^*(x)|x)} + \frac{\int_{v^*(x)}^{\infty} y\psi(y|x)dy}{1 - \Psi(v^*(x)|x)} \quad (12)$$

where  $\Psi(p|x)$  is the perceived distribution of the value of a random draw. In addition,  $v^*(x)$  decreases in  $x$ .

*Proof.* See Appendix A. ■

The optimal search strategy is simple. The shopper keeps sampling firms until the target value  $v^*(x)$  is reached. Indeed, in Appendix A, I show that the value function  $U(v|x)$  is given by,

$$U(v|x) = \max\{v, v^*(x)\} \quad (13)$$

This implies that, regardless of the current state  $v$ , the value of conducting an additional search is constant, equal to the threshold  $v^*(x)$ . When  $v < v^*(x)$ , the value function is always  $v^*(x)$ , indicating that the shopper opts to continue searching. Conversely, when  $v \geq v^*(x)$ , the value function equals the state  $v$ , implying that the shopper accepts  $v$ .

The result extends the standard threshold rule in the literature (Weitzman, 1979; Wolinsky, 1986) by incorporating both endogenous price distribution and incomplete information. In the literature, firms are homogeneous and shoppers have correct belief about the optimal price. Here, firms are heterogeneous and shoppers have incomplete information about the price distribution. Proposition 1 shows that under Assumption 1, the optimal search strategy still follows the threshold rule.<sup>7</sup> The threshold decreases in the shopper's information set  $x$ . In particular, a higher signal about the nominal wage leads to a lower threshold. Intuitively, a shopper who perceives a lower nominal wage believes the price distribution is shifted leftward. The increased perceived likelihood of encountering a low-price firm raises the threshold.

To make clear how two distributions affect the threshold, the following Corollary shows an alternative way to solve the threshold.

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<sup>7</sup>One can show that the threshold rule holds when shoppers can learn from individual prices, only if variance of productivity shocks is sufficiently larger than the variance of monetary shocks. Rothschild (1974) shows that the consumers still follow a threshold rule if the difference between these two prices is smaller than their informational content. The threshold in this case depends on the whole history of price observations.

**Corollary 1.** *The threshold  $v^*(x)$  is given by,*

$$\int \int_{\lambda(v^*(x)+p)}^{\infty} \left(\frac{1}{\lambda}\epsilon - p - v^*(x)\right) g(\epsilon) d\epsilon f(p|x) dp = \kappa \quad (14)$$

where  $f(p|x)$  is the perceived price distribution.

The left-hand side represents the expected additional benefit of additional search at the threshold, i.e., when shopper's state is  $v^*(x_i)$ . From Proposition 1, she is indifferent between sampling another firm and stopping searching. Suppose she samples another firm  $k$ , she will prefer the new good if  $\frac{1}{\lambda}\epsilon_{ik} - p_k > v^*(x_i)$ . Since the shopper can return without cost, the additional utility obtained in this case is  $\max\{\frac{1}{\lambda}\epsilon_{ik} - p_k - v^*(x_i), 0\}$ . The threshold is achieved when the expected additional utility is equal to the search cost.

**Aggregation** – I now show the aggregation of optimal search decisions. In particular, I show the expenditure allocation across firms and the resulting profits. According to the optimal search strategy, the shopper only purchases the good  $k$  if  $\frac{1}{\lambda}\epsilon_{ik} - p_k > v^*(x)$ . The shopper's probability of purchasing from firm  $k$  in each round is  $1 - G(\lambda(v^*(x) + p_k))$ . Since learning from shopping is prohibited, this probability is the same for all rounds of search. The probability of any shopper purchasing from any firm in each search given  $w$  is given by,

$$\rho = \int \int (1 - G(\lambda(v^*(x) + p))) d\Phi_x(x) f(p|w) dp \quad (15)$$

Suppose the mass of shoppers who visit any firm in the first round is one. A fraction  $\rho$  of these shoppers settle with the firms they visit in the first round. The remaining  $1 - \rho$  shoppers search in the second round, a further  $(1 - \rho)^2$  search in the third round, and so on. It is straightforward to show that the expected number of searches of each shopper is  $\rho^{-1}$ . Firms are atomistic and take  $\rho$  as given when setting prices. Furthermore, the total expenditure spent in firm  $k$  after all rounds of search is given by,

$$\omega_k = \frac{1}{\rho} \int X(1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x) \quad (16)$$

The dispersion in the cash in hand affects the expenditure through the dispersion of thresholds. The inequality also matters through the covariance between the cash in hand and the threshold. The more cash in hand induces higher expectation of the nominal wage. The profit for firm  $k$  is given by,

$$\pi_k = \frac{1}{\rho} \int X(1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x) \frac{1}{P_k} (P_k - \frac{W}{A_k}) \quad (17)$$

The demand is derived by dividing the total expenditure spent in firm  $k$  by  $P_k$ . The profit is thus the total demand times the profit per sale.

**Characterization of the Pricing Strategy** – Monopolistic firms compete on prices. They maximize the profit in (17) with respect to its price. The following proposition presents the optimal pricing strategy,

**Proposition 2.** *Let  $\mu_k$  denote the markup and  $e_k$  denote the elasticity of demand Firm charges a markup over the marginal cost,*

$$P_k = \mu_k \frac{W}{A_k}; \quad \mu_k = \frac{e_k}{e_k - 1} \quad (18)$$

*The elasticity of demand  $e_k$  is determined by,*

$$e_k = \lambda \frac{\int X g(\lambda(v^*(x) + p_k)) d\Phi_x(x)}{\int X (1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x)} + 1 \quad (19)$$

*Proof.* See Appendix A. ■

The optimal price is a markup times the marginal cost. Firm's market power is determined by two factors. One is the relative importance of the utility of a match with the utility of consumption,  $\lambda$ . Larger  $\lambda$  implies higher elasticity.<sup>8</sup> Another is that search friction naturally gives rise to monopoly power (Diamond, 1971). In particular, the effect of search friction on the elasticity is represented by a hazard function, where the density  $g$  represents the marginal shoppers who are indifferent between making purchase and continuing searching. The survival function  $1 - G$  indicates that the adjustment of the price will affect the profit obtained from all infra-marginal shoppers. The ratio between these two captures the trade-off that setting a higher price motivates shoppers to search, while extracting more profit from the infra-marginal shoppers.

**Characterization of the Full-Information Equilibrium** – In the full-information equilibrium, shoppers know the nominal wage. Let  $v^*(w)$  denote the value of threshold in this equilibrium. Similar to Corollary 1, it is given by,

$$\int \int_{\lambda(v^*(w)+p)}^{\infty} \left( \frac{1}{\lambda} \epsilon - p - v^*(w) \right) g(\epsilon) d\epsilon f(p|w) dp = \kappa \quad (20)$$

where  $f(p|w)$  is the actual price distribution. It is easy to show that firm's profit is given by,

$$\pi_k = \frac{1}{\rho} \left( 1 - G(\lambda(v^*(w) + p_k)) \right) \frac{W}{P_k} \left( P_k - \frac{W}{A_k} \right) \quad (21)$$

---

<sup>8</sup>Anderson et al. (1987) shows that without search frictions, if  $G$  is Gumbel distribution, the demand system is exactly CES and the elasticity of substitution is  $\lambda + 1$ .

where  $\rho = \int (1 - G(\lambda(v^*(w) + p)))f(p|w)dp$ . The difference between (21) and (17) is two-fold. First, the distribution of thresholds is reduced to a single value  $v^*(w)$ . Second, the inequality in cash in hand is no longer correlated with the threshold. I can similarly define the expenditure allocation in the full-information case,

$$\omega_k = \frac{1}{\rho} \left( 1 - G(\lambda(v^*(w) + p_k)) \right) \quad (22)$$

The first-order condition of firm's problem results in,

$$P_k = \frac{e_k}{e_k - 1} \frac{W}{A_k} \quad (23)$$

$$e_k = \lambda \frac{g(\lambda(v^*(w) + p_k))}{1 - G(\lambda(v^*(w) + p_k))} + 1 \quad (24)$$

Since  $G$  is log-concave, the elasticity of demand is increasing in firm's own price. It has two implications. First, high-productivity firms will set lower price and have higher markup. Second, when firms face pickier shoppers implied by the larger threshold, the markup declines.

Now, I present an important property of  $v^*(w)$ . It is a crucial step in proving the existence of the equilibrium. This property is also useful to understand the effect of search frictions on other equilibrium objects I will discuss in Section 1.5.

**Lemma 1.** *The full-information threshold  $v^*(w)$  decreases with the search cost,  $\kappa$ .*

*Proof.* See Appendix A. ■

The Lemma establishes a one-to-one relationship between the full-information threshold and the search cost. A lower threshold directly raises the expected value of additional search at the threshold as in (20). However, it simultaneously reduces this value indirectly by increasing prices through (24). The direct effect outweighs the indirect effect. I now establish the existence of the full-information steady-state equilibrium.

**Theorem 1** (Existence of the Full-Information Steady-State Equilibrium). *There exists a unique full-information steady-state equilibrium in which consumers search actively.*

*Proof.* See Appendix A. ■

This theorem is proved in two steps. First, the elasticity of demand increases in price. It implies that higher price induces higher elasticity and lower markup. Therefore, the individual prices are uniquely determined by (23) and (24). Second, from Lemma 1, the threshold  $v^*(w)$  is uniquely



determined by (20) for the given price distribution that is derived from optimal pricing strategy. The equilibrium is then the fixed point of the reservation value and the price distribution. Note that there always exist equilibria in which firms charge sufficiently high prices and shoppers do not search. However, there is only one equilibrium in which shoppers search actively. From now on, I refer to the full-information equilibrium where  $w = \bar{w}$  as the full-information steady state.

Next, I present the first main result about monetary non-neutrality.

**Theorem 2.** *In the full information equilibrium, monetary policy is neutral.*

*Proof.* See Appendix A. ■

This theorem is an exact result. It establishes that when shoppers know the monetary shock, the passthrough from the monetary shock to prices is complete. This is true because in equilibrium, each firm understands that, if itself and all its competitors raise their prices one-to-one with a monetary shock, consumers will know that there is no gain from searching more, which in turn sustains the equilibrium in which the aggregate passthrough of a monetary shock is indeed 100%. In other words, search friction alone is not sufficient to generate monetary non-neutrality.

## 1.4 Approximate Optimal Strategies

Both the threshold shown in Proposition 1 and the pricing strategy shown in Proposition (2) are highly non-linear. Following the literature, I consider the case in which the monetary authority draws monetary shocks from a distribution with small standard deviation, i.e.,  $\sigma_w \rightarrow 0$ . At the same time, I keep variance ratio  $\frac{\sigma_x^2}{\sigma_w^2}$  fixed, which correspond to fixed values of  $\theta$ . The fixed ratio preserve a constant level of information friction about the nominal wage. The existence of the full-information equilibrium allows us to approximate the non-linear strategies to the first order around the full-information steady state.

To proceed, I define the passthrough from the monetary shock  $\hat{w}$  to prices in equilibrium. The first-order approximation to the optimal pricing strategy  $p^*$  is given by,

$$p^*(a_k, w) = p^*(a_k, \bar{w}) + p_w^*(a_k, \bar{w})\hat{w} \quad (25)$$

I refer to  $\varphi_k = p_w^*(a_k, \bar{w})$  as the total passthrough, as it reflects the sum of two passthroughs which I will show in Section 1.5. Shoppers know the distribution of total passthrough as they know  $p^*, \bar{w}$  and  $\Phi_a$  in equilibrium.

Unlike the standard demand system where an aggregate demand function is available and then the price index is naturally defined, in the model with search frictions, there is no obvious way to

define a price index. However, the standard theory (Hulten, 1973, Hulten, 1978) offers a simple non-parametric formula for the change in price index. Under the assumptions of homotheticity and preference stability<sup>9</sup>, the log change in the price index is the expenditure share-weighted log changes in all the prices. The expenditure share is measured in the base period. Apparently, both conditions are satisfied here<sup>10</sup>, I define the expenditure share-weighted log change in the price index.

$$\hat{p} = \Phi \hat{w} \quad (26)$$

where  $\Phi = \int \varphi_k \bar{\omega}_k dk$  and  $\bar{\omega}_k = \frac{1}{\bar{p}}(1 - G(\lambda(v^*(\bar{w}) + p_k)))$  is the expenditure share in the full-information steady state. The aggregate effect of a monetary shock on price index is measured by the aggregate total passthrough  $\Phi$ . In particular, shoppers know  $\Phi$  since they know the distribution of  $\varphi_k$  and  $\bar{\omega}_k$ . Therefore, the average expectation of the change in price index is  $\bar{E}\hat{p} = \Phi \bar{E}\hat{w} = \theta \hat{p}$ . For larger information friction,  $\theta$  is closer to zero, indicating more dampening response of  $\bar{E}\hat{p}$ .

The following proposition presents a first-order approximation to the optimal search strategy in (14) and the optimal pricing strategy in (19).

**Proposition 3.** Fix the variance ratio  $\frac{\sigma_w^2}{\sigma_w^2}, \frac{\sigma_s^2}{\sigma_w^2}$ . To the first order as  $\sigma_w \rightarrow 0$ ,

[Part 1] the threshold  $v^*(x)$  is given by,

$$v^*(x) = v^*(\bar{w}) - \Phi E(\hat{w}|x) \quad (27)$$

where  $\Phi$  is the aggregate total passthrough.

[Part 2] The elasticity of demand is given by,

$$e_k = \lambda \frac{g(\lambda(v^*(w) + \bar{p}_k + \hat{p}_k - \bar{E}\hat{p}))}{1 - G(\lambda(v^*(w) + \bar{p}_k + \hat{p}_k - \bar{E}\hat{p}))} + 1 \quad (28)$$

where  $\bar{E}\hat{p} = \theta \hat{p}$ . In addition,  $e_k$  increases in  $\hat{p}_k - \bar{E}\hat{p}$ .

*Proof.* See Appendix A. ■

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<sup>9</sup>Homotheticity requires that the income elasticity of demand must equal one for each good. Stability requires that consumers adjust their spending only in response to changes in income and relative prices. Baqaee and Burstein (2023) show how to generalize the standard theory to more general preferences.

<sup>10</sup>According to 17, the demand for firm  $k$  is proportional to the aggregate income  $W = \int X_i di$ , which implies homotheticity. In addition, there is no other factors, such as taste shocks, state of nature, other than relative prices and income, that can affect the demand.

This proposition shows that the threshold under incomplete information is equal to the threshold under full-information steady state, adjusted downward the expected change in the price index,  $E(\hat{p}|x) = \Phi E(\hat{w}|x)$ . As discussed in Proposition 1, the threshold is negatively related to  $x$ .

The aggregate total passthrough,  $\Phi$ , governs the passthrough from the expected monetary shock to the threshold for any information set. The aggregate total passthrough encapsulates all the changes in the price distribution as denoted in (25) following the shock. To see the intuition, suppose the total passthrough is uniform for all firms, i.e.,  $\varphi_k = \varphi_0$ , then  $\Phi = \varphi_0$ . In this scenario, an increase in the perceived nominal wage shifts the entire price distribution uniformly to the right, as occurs in the full-information equilibrium where  $\varphi_k = 1, \forall k$ . If, however, the passthrough distribution is non-uniform, the price distribution's shape changes after the shock. If high-productivity firms have larger expenditure share, and they also pass through less of the increase in nominal wage to prices, it increases the value of additional search, thereby lowering the aggregate total passthrough.

Finally, the average change of the thresholds is equal to  $\bar{E}\hat{p}$ . It implies that after a positive monetary shock, the decline in threshold is smaller, leading to increased search activities compared to the full-information benchmark. To dissuade the search, firms react by adjusting their pricing strategy.

The second part of the proposition characterizes the elasticity of demand. On the first order, the distribution of the thresholds and covariance between cash in hand and thresholds vanish to zero and only  $\bar{E}\hat{p}$  is retained, which is inherited from the average change in the thresholds. It shows that the elasticity depends on the perceived relative price,  $\hat{p}_k - \bar{E}\hat{p}$ . Due to the information friction, it is larger than the actual relative price. As a result, firms act as though they are competing with rivals setting prices lower than their actual levels, prompting them to reduce their own prices. This pricing strategy increases the elasticity of demand and in turn decreases markup, leading to incomplete passthroughs from the monetary shock to prices. We will explore the passthroughs in detail in Section 1.5.

## 1.5 Characterization of Passthroughs in Equilibrium

I now characterize passthroughs in the equilibrium. I present the main finding: the aggregate passthrough of a money supply shock to the price index is generically incomplete. The total passthrough is composed of the own-cost passthrough and the cross-price passthrough. Decompos-

ing the total passthrough into these two elements is crucial to understand the intuition behind the main finding. Following Amiti et al. (2019), I define both passthroughs using markup elasticities.

**Lemma 2.** *The price responds to both firm's own cost shocks and competitors' prices,*

$$\hat{p}_k = \gamma_k(\hat{w} - \hat{a}_k) + \xi_k \hat{p} \quad (29)$$

where  $\gamma_k$  is the own-cost passthrough and  $\xi_k$  is the cross-price passthrough.

$$\gamma_k = \left(1 - \frac{d \log \mu_k}{dp_k} \Big|_{\hat{w}=0}\right)^{-1}; \xi_k = \frac{d \log \mu_k}{dp} \Big|_{\hat{w}=0} \gamma_k \quad (30)$$

where  $\mu_k$  is the markup. The total passthrough of each firm is given by,

$$\varphi_k = \gamma_k + \Phi \xi_k \quad (31)$$

The aggregate total passthrough  $\Phi$  is given by,

$$\Phi = \frac{\Gamma}{1 - \Xi} \quad (32)$$

where  $\Gamma = \int \gamma_k \bar{\omega}_k dk$ ,  $\Xi = \int \xi_k \bar{\omega}_k dk$ .

*Proof.* See Appendix A. ■

The lemma links passthroughs with the elasticity of demand through the markup elasticities. Plugging the definition of the total passthrough, the lemma then derives the total passthrough for each firm in equilibrium. Integrating on both sides, the aggregate total passthrough is obtained. Importantly, the own-cost passthrough,  $\gamma$ , does not depend on the information friction  $\theta$  when evaluated at the steady state. Firms pass part of their idiosyncratic cost shocks to prices regardless of the aggregate shocks and the associated information friction. In contrast, the cross-price passthrough,  $\xi$ , depends on how shoppers perceive the price index.

I now state our main results on passthroughs under incomplete information. To push the results on monotone comparative statics as far as possible, I assume that the distribution of the match utility,  $G$ , follows the Gumbel distribution.

**Theorem 3** (Aggregate Total Passthrough under Incomplete Information). *Under incomplete information about the nominal wage, the aggregate total passthrough has following properties,*

1. **[Incompleteness]**  $\Phi < 1$
2. **[Composition]**  $\varphi_k$  decreases in productivity;  $\bar{\omega}_k$  increases in productivity.

3. *[MCS on  $\kappa$ ]  $\Phi$  decreases in search friction  $\kappa$  given  $\theta$ . Limits:  $\lim_{\kappa \rightarrow \infty} \Phi = 0$ ;  $\lim_{\kappa \rightarrow 0} \Phi = 1$*   
*[MCS on  $\theta$ ]  $\Phi$  increases in information friction  $\theta$  given  $\kappa$ . Limits:  $\lim_{\theta \rightarrow 1} \Phi = 1$ ;  $\lim_{\theta \rightarrow 0} \Phi = \Gamma$*

*Proof.* See Appendix A. ■

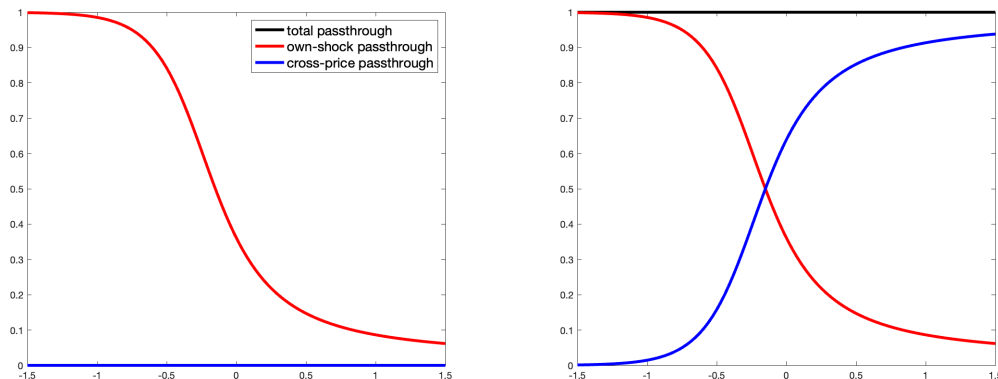
This is the main theorem of this paper. It establishes that the total passthrough is generically incomplete if there exists any information friction. The full-information case is a knife-edge case. I first explain the result on incompleteness. The key equation to understand the intuition is:

$$1 - (\gamma_k + \xi_k) = (1 - \gamma_k)(1 - \theta) > 0 \quad (33)$$

It shows that the difference between the sum of the passthroughs,  $\gamma_k + \xi_k$ , and one can be decomposed into two terms. The first term captures the role of the search friction. The own-cost passthrough is not related to the information friction. The second term captures the role of information asymmetry about the nominal wage between consumers and firms. They are both positive. Figure 1 illustrates the three passthroughs. The right panel shows that under full information, the decrease in the own-shock passthrough over productivity is exactly offset by the increase in cross-price passthrough. The resulting total passthrough is always one for firms of any productivity. This result corresponds to Theorem 2 in which I prove the exact result. The decomposition on two passthroughs shows the contribution of each passthrough for different types of firms. Notably, Amiti et al. (2019) shows that the total passthrough is one for broad preferences including nested CES and first-order Kimball demand family as well as for the broad homothetic families of demand considered in Matsuyama and Ushchev (2017). The theorem complements their results and emphasizes that the complete information about the price index is also essential. In fact, in all these commonly used demand system, the complete knowledge of all prices is often assumed.

The left panel shows the case where shoppers have *no* information about the shock. The cross-price passthrough is uniformly *zero* for any firm. As a result, the total passthrough equals the own-cost passthrough. The intuition is that when shoppers do not perceive any change in the price index, the change in the nominal wage is as if an idiosyncratic cost shock to firms. Thus, firms find it optimal not to pass any of the actual change in the price index onto their own prices. In the intermediate case when information is incomplete, the increase in cross-price passthrough is still not sufficient to offset the decrease in own-shock passthrough, leading to incomplete total passthroughs.

Figure 1: Distribution of three types of passthroughs under incomplete and complete information



*Notes:* The figure plots distributions of passthroughs based on one calibration of the model. The red line represents own-cost passthrough. The blue line represents cross-price passthrough. The black line represents total passthrough. The left and right panels show passthroughs in the incomplete and complete information cases, respectively.

Moreover, the individual total passthrough is defined as  $\varphi_k = \gamma_k + \Phi\xi_k$ . The effect of strategic complementarity is further dampened by the aggregate total passthrough as  $\Phi < 1$ . This induces a even smaller individual total passthrough. Intuitively, the fact that shoppers understand that aggregate total passthrough is incomplete reduces the expected price index even more. Firms then reduce prices in response, resulting in even lower passthrough. Therefore, the incompleteness of the total passthroughs is amplified by the firms' incentive of setting prices close to the price index, which is a form of real rigidity (Klenow and Willis, 2016).

I leave the discussion of composition and comparative statics results to the later section. Here, I focus on clarify the main insight behind the incompleteness result.

**Main Insight: Strategic Complementarity Attenuation** – In Proposition 3, we have discussed that elasticity of demand for individual firms increases because shoppers perceive a dampened response of price index. In this section, I “dig deeper” to show how such mechanism for the *individual* firms relates to the attenuation on the strategic complementarity in pricing on the *aggregate*. For this purpose, I will borrow heavily from game theory as in Morris and Shin (2002), Woodford (2003), and Angeletos and Lian (2023). The following proposition presents a way to translate the above economy into a beauty contest game.

**Proposition 4.** *The model economy can be expressed as a beauty contest game as follows,*

$$\hat{p} = \Gamma \hat{w} + (1 - \Gamma) \bar{E} \hat{p} \quad (34)$$

where  $\bar{E} \hat{p}$  represents shoppers' average expectation of  $\hat{p}$ . In the rational expectations equilibrium, the change in price index can be expressed as the infinite sum of higher-order beliefs of  $\hat{w}$ ,

$$\hat{p} = \Gamma \sum_{h=0}^{\infty} (1 - \Gamma)^h \bar{E}^h \hat{w} \quad (35)$$

where shoppers'  $h$ -order average expectation  $\bar{E}^h \hat{w} = \bar{E}(\bar{E}^{h-1} \hat{w})$ , and  $\bar{E}^0 \hat{w} = \hat{w}$ . Using the fact that  $\bar{E}^h \hat{w} = \theta^h \hat{w}$ , the aggregate total passthrough is given by,

$$\Phi = \Gamma \sum_{h=0}^{\infty} (1 - \Gamma)^h \theta^h \quad (36)$$

*Proof.* See Appendix A. ■

The proposition frames the model economy as a beauty contest game, where firms exhibit strategic complementarity in response to *shoppers'* beliefs about the price index. This is distinguished from the standard beauty contest game between firms (Woodford, 2003), where strategic complementarity is in terms of *firms'* beliefs about the price index. Therefore, to write the game into the infinite sum of higher-order beliefs as in (35), the requirement on rationality is different. In particular, we need (i) firms are rational and (ii) shoppers know that firms are rational and (iii) the common knowledge of rationality among shoppers.<sup>11</sup> In Appendix A, I show which rationality is required in each step of derivation. The rational expectations equilibrium is a “super” concept that includes all these rationality.

To understand the intuition, we can interpret this infinite sum as the aggregate response of firms unfolding in the notional time within one period. In the first round, consider no firm has yet responded to the monetary shock. The shock therefore acts as an idiosyncratic shock to each firm. The resulting price increase is thus  $\Gamma \hat{w}$ . In the second round, it is the common knowledge among firms that the price index has increased by this amount. Then, due to the strategic complementarity to other firms' price increases, they pass additional portion of the shoppers' believed increase in the price index from the first round to prices, i.e.,  $(1 - \Gamma) \bar{E} \Gamma \hat{w}$ . Iterate forward, in the  $h + 1$ th round, the additional passthrough is  $(1 - \Gamma)^h \bar{E}^h \hat{w}$ .<sup>12</sup> The intuition is also related to the literature

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<sup>11</sup>The first iteration requires that shoppers know that firms and other shoppers are rational, the second iteration requires that shoppers know that others know they are rational and firms are rational, and so on.

<sup>12</sup>This intuition leverages another layer of rationality: firms know the common knowledge of rationality among shoppers.

on level- $k$  thinking (García-Schmidt and Woodford, 2019 and Farhi and Werning, 2019) where the rounds of thinking  $k \rightarrow \infty$ .

Moreover, the information friction attenuates the strategic complementarity in pricing. It attenuates more the high-order strategic complementarity, since the higher-order beliefs of shoppers are more anchored to the prior. For  $\theta$  close to zero (meaning a sufficiently large departure from common knowledge of the shock), the aggregate total passthrough is arbitrarily close to the aggregate own-cost passthrough. But as  $\theta$  increases (meaning a higher degree of common knowledge of the shock), the higher-order strategic complementarity rises rapidly and thus increases overall passthrough. Therefore, by varying  $\theta$  between 0 and 1, we can thus span all the values between the aggregate own-cost passthrough and the full-information outcome.

**Symmetry** – I explain the intuition behind the symmetry of incomplete passthrough for both positive and negative monetary shocks. Consider a positive monetary shock, e.g., the nominal wage increases by 1%. Assume  $\Phi = 0.4$  and  $\theta = 0.5$ , yielding  $\bar{E}\hat{p} = 0.2\%$ . Now suppose a firm raises its price by 1%. According to Proposition 3, its markup decreases by  $(\gamma_k^{-1} - 1) \times 0.8\%$ . Consequently, a 1% price increase cannot be optimal. This is because the firm is more concerned about losing marginal shoppers to competitors than forfeiting profits from infra-marginal shoppers. This interpretation echos the message in Rotemberg (1982), which is that firms, fearing to upset marginal consumers, limit the passthrough.

On the other hand, suppose the nominal wage decreases by 1%. If a firm reduces its price by 1%, the firm will attract more shoppers, who perceive themselves as fortunate to have encountered a high-productivity firm. Therefore, its markup increases. To maximize profits, the firm opts not to fully lower its price, balancing increased profits from infra-marginal shoppers with the benefit of attracting additional shoppers. Therefore, the appropriate interpretation in the case of negative monetary shock is that firms limit the passthrough to gain more profits from infra-marginal consumers.

**Firm Heterogeneity in Passthroughs** – To discuss the second part of Theorem 3, I first complete the picture by showing the cross-sectional properties of three types of individual total passthroughs and their limit results. I define passthroughs on the primitive:  $\varphi_k = \varphi(a_k)$ ,  $\gamma_k = \gamma(a_k)$  and  $\xi_k = \xi(a_k)$ .



**Proposition 5.** *In a given equilibrium, markup  $\mu(a)$  and cross-price passthrough  $\xi(a)$  increases in productivity; own-cost passthrough  $\gamma(a)$  and total passthrough  $\varphi(a)$  decreases in productivity. Also, the following limit results hold:*

1.  $\lim_{a \rightarrow \infty} \mu(a) = \infty$ ;  $\lim_{a \rightarrow \infty} \varphi(a) = \Phi\theta$ ;  $\lim_{a \rightarrow \infty} \gamma(a) = 0$ ;  $\lim_{a \rightarrow \infty} \xi(a) = \theta$
2.  $\lim_{a \rightarrow -\infty} \mu(a) = \frac{\lambda+1}{\lambda}$ ;  $\lim_{a \rightarrow -\infty} \varphi(a) = 1$ ;  $\lim_{a \rightarrow -\infty} \gamma(a) = 1$ ;  $\lim_{a \rightarrow -\infty} \xi(a) = 0$

*Proof.* See Appendix A. ■

High-productivity firms exhibit lower own-cost passthrough because their lower prices attract marginal consumers with lower match utility. Given  $G$  follows Gumbel distribution, these consumers are more sensitive to relative prices, leading to a lower passthrough of own-cost shocks. For similar reasons, high-productivity firms have strong incentives to keep up with competitors' prices, resulting in stronger strategic complementarity.

Furthermore, because information frictions dampen only the cross-price passthrough, high-productivity firms experience a more pronounced decline in cross-price passthrough and, therefore, total passthrough. Coupled with their high expenditure share, these firms disproportionately contribute to the incompleteness of aggregate total passthrough. According to the limit results, the total passthrough is bounded below by the response of  $\bar{E}\hat{p}$  to  $\hat{w}$ , i.e.,  $\Phi\theta$ . This implies that  $\hat{p}_k - \bar{E}\hat{p}$  is always positive, resulting in uniformly higher perceived relative prices. Consequently, following a positive monetary shock, shoppers are more likely to search and markups decrease for all firms.

In addition, high-productivity firms set lower prices, attract more shoppers, and choose higher markups. Similar to oligopolistic CES models, the lower bound of markups is determined by the degree of substitutability between goods, while the upper bound approaches infinity.

Proposition 5 also aligns with empirical evidence highlighted in the literature: (i) more productive firms charge higher markups (Amiti et al., 2014); (ii) more productive firms pass through less exchange rate shocks (Amiti et al., 2019).

**Supply Side Effect of Monetary Shock** — The positive monetary shock induces more search under incomplete information, with larger information frictions leading to even greater search intensity. Increased search raises the utility cost due to higher total search effort. However, shoppers are more likely to be drawn to high-productivity, low-price firms, leading to an expansion in demand for these firms and a contraction for low-productivity firms. This reallocation improves allocative efficiency and boosts aggregate productivity (Baqae et al., 2024). In general equilibrium with

finite labor elasticity, this amplifies the output response while dampening the inflation response as shown in Proposition 11.

**Monotone Comparative Statics** – To understand the results of comparative statics of the aggregate total passthroughs in Theorem 3, I establish that, all else equal, (i) the total passthrough is larger when the search cost is smaller for all firms and (ii) the total passthrough is larger when information friction is smaller for all firms.

**Proposition 6.** *Let equilibrium passthrough distributions  $\gamma(a; \kappa), \xi(a; \kappa), \varphi(a; \kappa)$  for given  $\kappa$ . Given  $\sigma_z > 0$ , for  $\kappa_2 > \kappa_1$ ,*

1. *Own-cost passthrough:*  $\forall a, \gamma(a; \kappa_2) < \gamma(a; \kappa_1); \lim_{\kappa \rightarrow \infty} \gamma(a) = 0; \lim_{\kappa \rightarrow 0} \gamma(a) = 1$
2. *Cross-price passthrough:*  $\forall a, \xi(a; \kappa_2) > \xi(a; \kappa_1); \lim_{\kappa \rightarrow \infty} \xi(a) = \theta; \lim_{\kappa \rightarrow 0} \xi(a) = 0$
3. *Total passthrough:*  $\forall a, \varphi(a; \kappa_2) < \varphi(a; \kappa_1); \lim_{\kappa \rightarrow \infty} \varphi(a) = 0; \lim_{\kappa \rightarrow 0} \varphi(a) = 1$

*Proof.* See Appendix A. ■

This proposition establishes that, all else equal, total passthrough is lower in an economy with higher search costs for any given productivity. Therefore, the search friction can amplify the effect of the information asymmetry on total passthroughs. As we know from Lemma 1, higher search cost lowers the thresholds, which results in lower elasticity of demand. Higher markups are more sensitive to the change in prices, leading to lower own-cost passthrough. Based on (33), lower own-cost passthrough implies larger gap between the sum of two fundamental passthroughs and one, resulting in lower total passthrough. In addition, the limit results implies that the total passthrough can vary from zero to one, implying the possibility of large degree of monetary non-neutrality.

**Proposition 7.** *Let equilibrium passthrough distributions  $\gamma(a; \theta), \xi(a; \theta), \varphi(a; \theta)$  for given  $\theta$ . For  $\theta_2 > \theta_1$ ,*

1. *Own-cost passthrough:*  $\forall a, \gamma(a; \theta_2) = \gamma(a; \theta_1)$
2. *Cross-price passthrough:*  $\forall a, \xi(a; \theta_2) > \xi(a; \theta_1); \lim_{\theta \rightarrow 1} \xi(a) = 1 - \gamma(a); \lim_{\theta \rightarrow 0} \xi(a) = 0$
3. *Total passthrough:*  $\forall a, \varphi(a; \theta_2) > \varphi(a; \theta_1); \lim_{\theta \rightarrow 1} \varphi(a) = 1; \lim_{\theta \rightarrow 0} \varphi(a) = \gamma(a)$

*Proof.* See Appendix A. ■

This proposition highlights that, all else equal, the total passthrough increases at any given productivity as information becomes more precise. Intuitively, if shoppers are more aware of changes in price index, firms will be more responsive to changes in competitors' prices. Higher cross-price passthrough pushes up the total passthrough. In contrast, the own-cost passthrough is irrelevant to the information frictions. In the dynamic model, shoppers will learn the shock over time. This proposition shows that if learning leads to the common knowledge of the shock, the monetary policy will be neutral in the long run.

Taken together, Theorem 3 shows that the passthrough from changes in the nominal wage to price index is generically incomplete. The incompleteness is mostly contributed by high-productivity firms. The aggregate passthrough is lower when there is more search frictions and information frictions. Proposition 4 shows that the main insight lies on the attenuation effect of the information friction on strategic complementarity. Propositions 5-7 yield more disaggregated predictions of three types of passthroughs for individual firms and additional limit results.

## 1.6 General Equilibrium

In this section, I extend the partial equilibrium model—where the nominal wage and cash in hand are exogenous—in a general equilibrium framework by introducing a new agent: the worker. In particular, there is a representative household which consists of a single worker and a continuum of shoppers. The worker makes the labor supply and aggregate consumption spending decisions, leaving only the decisions about where to buy particular goods to the shoppers. I assume the worker has full information about the model economy, but there is no communication between the worker and the shoppers. Under this setup, a monetary shock can affect both nominal marginal costs and nominal aggregate demand, yet remain unknown to the shoppers. In addition, there is no security markets where shoppers can trade claims that are contingent on the search process and final choices.<sup>13</sup>

The timeline is as follows. The period is divided into morning and afternoon. In the morning, the monetary authority sets the nominal GDP, and the worker makes decision on labor supply and aggregate consumption spending they send to shoppers. In the afternoon, firms post prices, and

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<sup>13</sup>For example, a security might provide positive returns if a shopper experiences a long sequence of unfavorable draws or if the final choice only slightly exceeds the threshold. Mongey and Waugh (2024) show that the demand allocations in a standard discrete-choice model without search frictions can be different when the market is complete.

each shopper searches sequentially and decides where to make the purchase. They are constrained by the amount of cash allocated to them.

I state the worker's problem in the morning. The worker maximizes the expected value that she will obtain from shoppers in the afternoon, net of the disutility associated with labor supply.

$$\begin{aligned} \max_{X,L} \int \left( \log \frac{X_i}{P_k} + \frac{1}{\lambda} \epsilon_{ik} \right) di - L_i \\ \text{s.t. } X = WL + \Pi \\ X_i = X \exp \left( \sigma_x \varepsilon_{xi} - \frac{\sigma_x^2}{2} \right) \end{aligned}$$

where  $X$  is the aggregate consumption spending. The division of  $X$  among shoppers is random, where  $\varepsilon_{xi} \sim \mathcal{N}(0,1)$  and  $\int X_i di = X$ .  $L$  is the labor effort,  $W$  is the nominal wage, and  $\Pi$  is firms' total nominal profit.  $P_k$  and  $\epsilon_{ik}$  are the price and the match utility of the firm that shopper  $i$  accepts in the search process. The uncertainty of final choice of firms is washed out on the household level. In other words, for the worker, the ex-ante sum of shoppers' value is equal to the ex-post one.

Due to the log utility, the consumption spending  $X_i$  only shifts the level of the value and does not affect the search decisions. Therefore, the worker and shopper problems can be separated. The first-order conditions imply  $X = W$ . It implies

$$\hat{p} + \hat{c} = \hat{w} \tag{37}$$

I assume that shoppers only learn about the aggregate nominal wage  $W$  from  $X_i$  and they search sequentially. The shopper problem is the same as before.

**Aggregate Supply Shocks** – The framework can also incorporate the aggregate supply shocks. Here, we consider aggregate supply shocks as aggregate productivity shocks. In particular, the firm's productivity has two components,

$$\log A_k = \log A + \sigma_a \varepsilon_{ak} \tag{38}$$

where  $A$  is the aggregate productivity shock. Let  $a = \log A$ . It draws from  $\mathcal{N}(0, \sigma_A^2)$ . I only consider one aggregate shock a time. Specifically, when analyzing aggregate supply shocks, the nominal wage is common knowledge to all agents. The shopper also receives noisy signal about  $a$ .

$$s_{ai} = a + \sigma_{as} \varepsilon_{ai} \tag{39}$$

where  $\varepsilon_{ai}$  is i.i.d across shoppers and it follows  $\varepsilon_{ai} \sim \mathcal{N}(0,1)$ .

Since both the nominal wage and the aggregate productivity affect prices only through the marginal costs, the optimal pricing strategy is homogeneous of degree zero in  $\{W, A\}$ , which implies,

$$p^*(a_k, w, a) = p^*(a_k, w - a) \quad (40)$$

Any positive change in aggregate productivity acts equivalently to a proportional decrease in the nominal wage. Therefore, I can similarly define  $\hat{p}_k = -\varphi_k \hat{a}$  and aggregate total passthrough  $\Phi$ . The value of  $\Phi$  depends on the information friction in this case.

**Phillips Curve** – The following proposition characterizes the Phillips curve.

**Proposition 8.** *The Phillips curve is given by,*

$$\hat{p} - \bar{E}\hat{p} = \frac{\Gamma}{1 - \Gamma}(\hat{c} - \hat{a}) \quad (41)$$

where  $\hat{a}$  is the aggregate productivity shock and  $\Gamma$  is the aggregate own-cost passthrough.

*Proof.* See Appendix A. ■

This proposition shows that the output gap is proportional to shoppers' nowcast error of inflation. It is well-documented that average expectation of inflation under-react to aggregate shocks, even among professional forecasters (Coibion and Gorodnichenko, 2015a; Bordalo et al., 2020; Angeletos et al., 2020b). When the information friction is larger, the inflation expectation deviate farther from actual inflation, leading to a larger output gap. Conversely, smaller information frictions lead to a smaller output gap. This intuition can be translate into a statement about the slope of Phillips curve. Rewriting (41), we have:

$$\hat{p} = \frac{\Gamma}{1 - \Gamma} \frac{1}{1 - \theta}(\hat{c} - \hat{a}) \quad (42)$$

where  $\theta$  is the average information friction about the particular shock of interest. This formulation reveals that the slope of the Phillips curve is determined by two components. First, the slope decreases with higher search costs, as own-cost passthrough declines with these costs. Second, the slope flattens when shoppers have less information about the shock. Under zero information, the slope approaches  $\frac{\Gamma}{1 - \Gamma}$ , indicating that the lower bound of the slope is governed by aggregate own-cost passthrough. This corresponds to the limit results established in Theorem 3. At the other extreme, the slope becomes vertical, implying monetary neutrality.

This Phillips curve, in its essence, is very similar to the one derived in Lucas (1972), except that here, shoppers, not producers, confuse the increase in firm's nominal prices with the increase

in firm’s relative prices. This highlights the main takeaway: in modern Phillips curve models, firms’ expectations play a central role in driving inflation. In contrast, the Phillips curve here presents an alternative view that household expectations can influence firms’ pricing decisions as well. This approach shows advantages in terms of explaining the data. In fact, the literature has been using household inflation expectation to explain some key puzzles in the data. Coibion and Gorodnichenko (2015b) show that household expectations are critical for understanding the “Missing Disinflation” during the Great Recession. Coibion et al. (2018) show that household expectations perform better for Phillips Curve estimation over the whole US time series. Recent paper by Beaudry et al. (2024) shows that household inflation expectation is important to explain the post-pandemic inflation.

## 2 Dynamic Model

I now present the full-fledged dynamic general equilibrium model. The dynamic model will translate the monetary shock as a shock to the nominal GDP to a shock to the interest rate. It also features persistent shocks and slow learning about the underlying shock for shoppers.

The timeline is as follows. In each period, in the morning, the monetary authority sets the interest rate, and the worker makes decisions on the labor supply, the bond position, and the aggregate consumption spending. In the afternoon, firms post prices, and shoppers search sequentially and decide where to buy. The worker has full information and shoppers have incomplete information about aggregate shocks.

**Firm** – Let  $A_{kt}$  denote the firm’s productivity

$$\log A_{kt} = \log A_t + \eta_{kt} \quad (43)$$

where  $\eta_{kt}$  is the idiosyncratic productivity. It follows,

$$\eta_{kt} = \rho_a \eta_{kt-1} + \sigma_a \varepsilon_{akt} \quad (44)$$

where the idiosyncratic productivity shock follows  $\varepsilon_{akt} \sim \mathcal{N}(0, 1)$ . Also,  $A_t$  is the aggregate productivity. Denote  $a_t = \log A_t$ . It follows an AR(1) process,

$$a_t = \rho_A a_{t-1} + \sigma_A \varepsilon_{At} \quad (45)$$

where  $\varepsilon_{At}$  is the shock to aggregate productivity. It follows  $\varepsilon_{At} \sim \mathcal{N}(0, 1)$ .

**Monetary Authority** – The monetary authority sets the nominal interest rate. It follows the Taylor rule,

$$\dot{i}_t = \phi \hat{\pi}_t + v_{mt} \quad (46)$$

where  $v_{mt}$  follows,

$$v_{mt} = \rho_m v_{mt-1} + \sigma_m \varepsilon_{mt} \quad (47)$$

where  $\varepsilon_{mt}$  is the monetary shock and it follows  $\varepsilon_{mt} \sim \mathcal{N}(0, 1)$ .

**Worker** – The worker maximizes the expected discounted utility with discount factor  $\beta \in (0, 1)$  and period utility defined over the sum of values which shoppers will obtain in the afternoon. Worker can save in risk-free bonds  $B_t$  (in zero net supply) that pay an interest rate of  $R_t$ .

$$\begin{aligned} \max_{B_t, X_t, L_t} \quad & E_0 \sum_{t=0}^{\infty} \beta^t \left( \int \left( \log \frac{X_{it}}{P_{kt}} + \frac{1}{\lambda} \epsilon_{ikt} \right) di - L_t \right) \\ \text{s.t.} \quad & X_t + B_t = W_t L_t + R_{t-1} B_{t-1} + \Pi_t \\ & X_{it} = X_t \exp \left( \sigma_x \varepsilon_{xit} - \frac{\sigma_x^2}{2} \right) \end{aligned}$$

where  $X_t$  is the total consumption expenditure transferred to all the shoppers. The division of the consumption expenditure among shoppers is random and i.i.d. across shoppers and time, where  $\varepsilon_{xit} \sim \mathcal{N}(0, 1)$  and  $\int X_{it} di = X_t$ .  $L_t$  is the labor effort,  $W_t$  is nominal wage, and  $\Pi_t$  is total nominal profits of firms. Again, the worker's problem can be simplified due to the log utility.

**Shopper** – The shopper solves the static problem in (11) period by period given the history of signals. I make the simplifying assumption that shoppers observe the past price level but do not extract information from it. Following Mondria et al. (2021) and Angeletos and Huo (2021), this assumption can be interpreted as a form of bounded rationality or inattention. This assumption is made for two reasons. First, measures of household price level expectation is not available. The assumption transforms the Phillips curve in (41) into a relationship that directly links the output gap to the nowcast error of inflation, rather than the log deviation of price index. This allows us to use the inflation expectation in Michigan Survey of Consumers to calibrate the model. Second, as I will show, it also allows for a direct comparison of the impulse responses generated by our dynamic general equilibrium model with those produced by the standard NK model.

Given the above assumption, the signal  $\tilde{x}_{it}$  is equivalent to the following signal,

$$\tilde{x}_{it} = \hat{\pi}_t + \hat{c}_t + \sigma_x \varepsilon_{xit}$$

Besides the signal  $X_{it}$ , each shopper receives a noisy signal about  $\hat{\pi}_t$  at the beginning of each period to accommodate learning from observed prices. Since these signals are about the endogenous variables, they can be applied to both monetary and supply shocks.

**Dynamic Equilibrium** – I present the proposition that describes the dynamics of consumption, inflation and interest rate in equilibrium.

**Proposition 9.** *The equilibrium dynamics of  $\{\hat{\pi}_t, \hat{c}_t, i_t\}$  is described by the following system of three equations:*

$$\begin{aligned}\hat{c}_t &= E_t \hat{c}_{t+1} - (i_t - E_t \hat{\pi}_{t+1}) \\ \hat{\pi}_t - \bar{E}^s \hat{\pi}_t &= \frac{\Gamma}{1 - \Gamma} (\hat{c}_t - \hat{a}_t) \\ i_t &= \phi \hat{\pi}_t + v_{mt}\end{aligned}$$

where  $\Gamma$  is the aggregate own-cost passthrough and  $\bar{E}^s$  is the shoppers' average expectation.

*Proof.* See Appendix B. ■

This system is only different from the standard NK model in terms of the Phillips curve. First, since the worker has full information and decides the aggregate consumption spending and bond decisions, we achieve standard Euler equation. Second, the monetary non-neutrality is determined by how accurately and fast shoppers learn about the inflation. In Appendix B, I discuss the dynamics of the system if we retain the Phillips curve in (41) combined with a price-level targeting monetary rule. I also consider another setup in which shoppers both work and search. I obtain incomplete-information Euler equation as in Angeletos and Lian (2018).

## 2.1 Calibration

In this section, I present a calibration of the model. I proceed in two steps. First, I calibrate the aggregate own-cost passthrough and deep parameters that are related to the search friction. Second, I calibrate the information friction based on the empirical evidence.

**Aggregate own-cost passthrough** – The search cost in the model is described as a utility cost, which is hard to measure in the data. Fortunately, the aggregate own-cost passthrough is a



sufficient statistic for “deep” parameters related to the search friction, i.e., search cost  $\kappa$ , relative importance of match utility  $\lambda$ , and standard deviation and persistence of idiosyncratic productivity  $\sigma_a$  and  $\rho$ . Another property of aggregate own-cost passthrough is that it does not depend on the information friction. Therefore, we can separate the calibration of these two frictions.

Amiti et al. (2019) show that the aggregate own-cost passthrough is around 0.5 in the universe of Belgian manufacturing firms. Gopinath et al. (2011) use a retail chain database which contains information on wholesale costs and demonstrate substantial variation in own-cost passthrough estimates, with a median of around 0.5 for U.S. stores and 0.25 for Canadian stores. Own-cost passthrough estimates are often biased upward because, without controlling for all competitors’ prices, the estimates may capture strategic complementarity effects. Specifically, other firms respond simultaneously to both the correlated cost shocks and change in that firm’s price. Therefore, I pick  $\Gamma = 0.3$  which is closed to the lower end of the their estimates.

Interestingly, Amiti et al. (2019) also show that the sum of own-cost and cross-price passthroughs cannot be rejected from being one. This seems to indicate that the passthrough from the shock to prices is close to one in the model. However, search and information frictions are more prevalent in non-tradable industries that directly engage with household, such as retail and broad service sectors. In contrast, the buyer-seller relationships in tradable industries usually involves firms on both sides and firms are generally better informed about prices compared to households. Their relationships are often governed by contracts (Gopinath et al., 2011).

Although the deep parameters related to the search friction are not relevant for impulse responses, it will still be valuable to check the sanity of the implied values of these parameters. To proceed, I use the estimate of elasticity of substitution from DellaVigna and Gentzkow (2019). They use NielsenIQ Retailer Scanner database and find that the average elasticity of substitution across stores and products is 0.25, implying a markup of 1.67. In the data, one retailer sell a wide range of products. In one of the extension, I generalize the model to the setup where one firm sell multiple products and there is no search friction within the store. I show that retailers charge the same markup for all products they sell. In addition, the idiosyncratic productivity dispersion  $\sigma_a$  and persistence are set to be consistent with Decker et al. (2020), i.e.,  $\sigma_a = 0.3$ ,  $\rho_a = 0.6$ . The following table shows the baseline calibration for deep parameters that do not relate to the information friction.

Table 1: Baseline calibration of the model

Parameter	Description	Value
$\kappa$	Search cost	0.22
$\lambda$	Relative importance of match utility	5.51

*Notes:* The table reports the calibrated values for parameters that are related to the aggregate own-cost passthrough.

Table 2: Model fit

	Moment	Model	Data	Source
<b>M1</b>	Average markup	1.67	1.67	DellaVigna and Gentzkow (2019)
<b>M2</b>	Average own-cost passthrough	0.3	0.3	Amiti et al. (2019); Gopinath et al. (2011)

*Notes:* The table summarizes the moments, model and data values of these moments, and the sources of the empirical values of these moments.

Table 1 summarizes the calibrated parameters, and Table 2 presents the fit of the model to data. Despite its parsimonious structure, the model is successful in matching key moments in the data. They have two implications. First, although the targeted elasticity of demand is 2.5, the implied  $\lambda+1$ , which represents the elasticity of demand when  $\kappa \rightarrow 0$  as shown in Proposition 6, is about 6.5. This suggests that the search friction accounts for a substantial bulk of the market power. Second, Based on the calibrated values of deep parameters, we can infer the average contact per shopper  $\rho^{-1}$  equal to 1.26. This suggests a relatively large search cost and about 80% shoppers make the purchase on the first search. Therefore, Assumption 1 is plausible, as shoppers only visit a limited number of firms.

**Information friction** – In our Phillips curve, the output gap is proportional to shoppers’ nowcast error of inflation. Understanding how households learn about inflation is therefore critical. However, households may draw on different sources of information about inflation depending on the nature of the shocks. For instance, Kumar et al. (2015) shows that households focus on salient prices, such as oil prices. Similarly, D’Acunto et al. (2021) find that households form expectations based on price changes in the retail sector. Moreover, Candia et al. (2023) document that households may confuse demand shocks with supply shocks, and Liu and Zhang (2024) highlight that a specific signal structure is necessary to generate such confusion.

To ensure the robustness of inflation learning in different scenarios, I consider four types of shocks. The first two are the main inflation shock and the main business cycle shock from Angeletos et al. (2020a). The main inflation shock is identified by maximizing its contribution to the business-cycle variation in inflation. A key feature of this shock is its minimal impact on real quantities and zero impact on TFP, making it akin to cost-push shocks in DSGE models. Since this shock affects only inflation without influencing real variables, household learning relies solely on observing inflation itself, capturing a “generic” way of learning about inflation, e.g., a noisy about inflation. The main business cycle shock is identified by maximizing its contribution to the business-cycle variation in unemployment. It accounts for the large bulk of the business-cycle comovements in unemployment, hours worked, output, consumption, and investment. It reveals how households learn about inflation when real quantities are also affected. Additionally, I include two other shocks: oil news shocks (Känzig, 2021) and monetary shocks (Bauer and Swanson, 2023). They are more cleanly identified but as I will show, they are also special in terms of inflation learning.

The main empirical strategy is to estimate impulse responses of inflation and household inflation expectation using the local projection method à la Jordà (2005). The specification is,

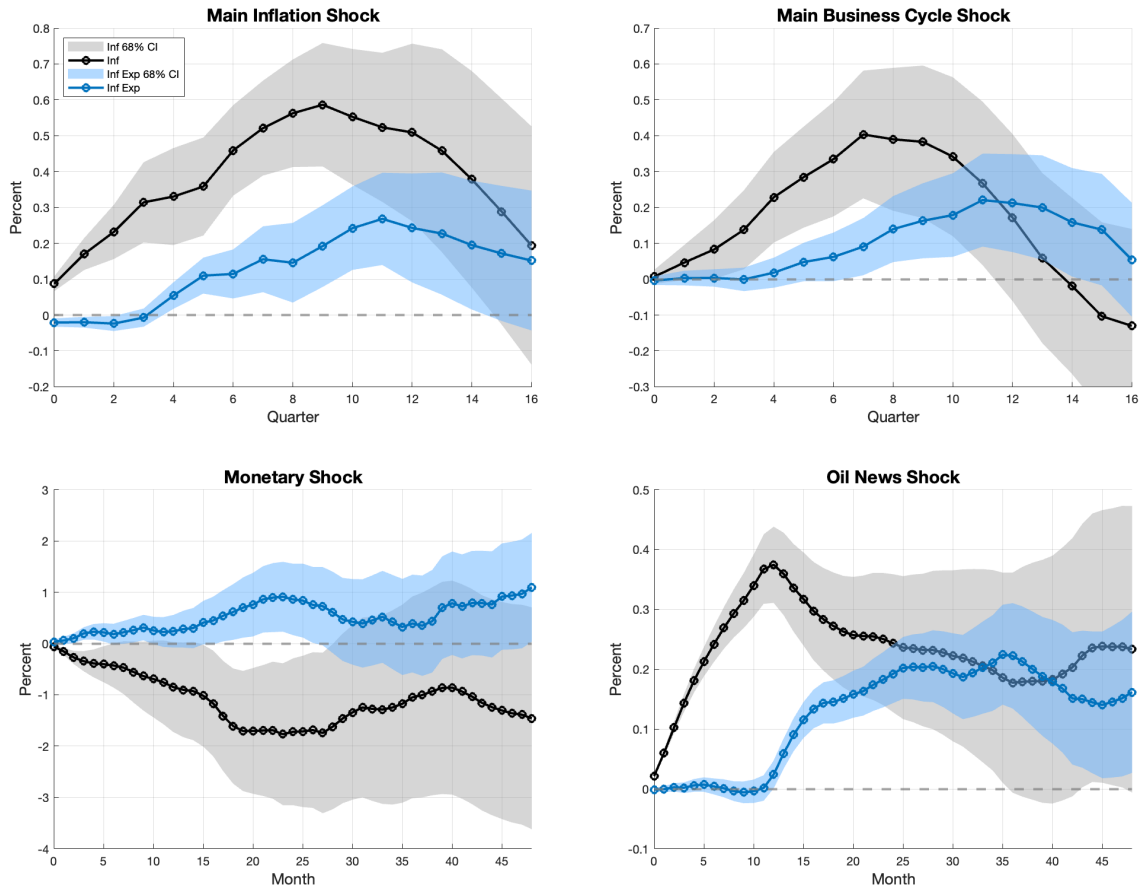
$$y_{t+h} = \alpha_h + \beta_h \varepsilon_t + \mathbf{\Gamma}' \mathbf{X}_t + u_{t+h} \quad (48)$$

where  $\{\beta_h\}_{h=0}^H$  trace out the dynamic responses of the outcome.  $y_t$  is the cumulative inflation  $\pi_t$  and the cumulative household average inflation expectation a year ago  $\bar{E}_{t-4}\pi_t$  based on Michigan Survey of Consumers.  $X_t$  is a vector of controls. It includes 4 lags of shock itself, inflation, inflation expectation a year ago, 1-year government bond rate, growth rate of industrial production. The sample period is Q3 1979–Q4 2017. I construct standard errors for the coefficients that are heteroskedasticity and autocorrelation robust (HAC). All reported error bands are 68% confidence intervals. In Appendix B, I show the robustness of the impulse responses across different empirical specifications.

Figure 2 shows the impulse responses of inflation and inflation expectation with 68% confidence interval. Since the shock is unanticipated, inflation expectations remain unchanged during the first year, adjusting only as households begin to observe and learn about inflation. Focusing first on the case of the main inflation shock, the key takeaway is that learning from inflation is slow. The inflation responses are always above the inflation expectation responses. The two error bands of the impulse responses begin to overlap at the end of the third year, and the median impulse

responses intersect after four years. In the case of main business cycle shock, the response of inflation expectation is remarkably similar, with both increasing gradually and peaking around three years after the shock. The difference lies in the behavior of actual inflation, which is less persistent and returns to zero within approximately three years. Consequently, the two impulse responses intersect earlier. These patterns suggest that households may employ a consistent approach to inflation learning—specifically, in terms of signal structure and signal precision—across most scenarios over business cycles.

Figure 2: Impulse Responses of Inflation and Household Inflation Expectation



*Notes:* Dynamic responses: outcomes and forecasts following four types of shocks. The sample period is Q3 1979–Q4 2017. The main inflation shock and main business cycle shock are in quarterly frequency. The monetary shock and oil news shock are in monthly frequency. The black line represents the impulse responses of inflation and the blue line represents the impulse responses of inflation expectation. The shaded areas are 68% confidence intervals based on heteroskedasticity and autocorrelation robust standard errors and 12 lags. The x-axis denotes months from the shock, starting at 0. The y-axis denotes percent.

In the bottom-right panel, I present the impulse responses following an oil news shock. The response of inflation expectations converge to the response of actual inflation much faster than in the case of main inflation shocks. This is consistent with Kumar et al. (2015) who shows that households in general pay more attention to the oil prices. As a result, inflation driven by oil news shocks is more readily and quickly observed by households. To the right, I display the responses following a monetary shock. Here, inflation decreases while inflation expectations rise after a contractionary shock, suggesting that households may confuse monetary shocks with supply shocks. Liu and Zhang (2024) propose a model in which agents must infer whether the underlying shock is demand or supply based on endogenous signals. Agents may perceive positive inflation if they believe the shock is a negative supply shock. As a result, to match such empirical impulse responses, we need additional bells and whistles in the model. I leave it to the future research.

Overall, we are confident that households learn inflation in a pretty consistent way over the business cycle. Therefore, I calibrate the signal-to-noise ratio of the signal about the inflation so that two impulse responses of the inflation and the inflation nowcast coincide approximately three years after the shock, which is a conservative calibration. At the same time, I assume that  $\tilde{x}_{it}$  completely uninformative.<sup>14</sup>

## 2.2 Impulse Responses of the Calibrated Model

In this section, I discuss the impulse responses of the calibrated model. The calibrated model is computed using the frequency-domain methods based on Rondina and Walker (2021), Huo and Takayama (2023), and Han et al. (2022). The Taylor rule parameter is calibrated as  $\phi = 1.5$ . Figure 3 presents the results. The first row shows the impulse responses of output, interest rate, inflation and inflation nowcast following a 100 basis-point interest rate cut based on the calibrated model. The second row presents the impulse responses following a 100 basis-point reduction in the aggregate productivity. In the third column, the blue line represents the inflation and the red line represents the inflation nowcast. Our theory predicts that the gap between these two lines is proportional to the output response. In addition, I compare our model with the standard NK model with the Phillips curve as follows,

$$\hat{\pi}_t = \kappa(\hat{y} - \hat{a}) + \beta E_t \pi_{t+1} \quad (49)$$

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<sup>14</sup>One can easily find other combinations of the calibration of these two shocks to match the empirical findings. The calibration results are similar.

where  $\kappa = (1 - \beta\psi)(1 - \psi)/\psi$  and  $\psi$  is the probability of a firm not being able to adjust its price, which we call Calvo parameter. Applying  $E_t\pi_{t+1} = \rho\pi_t$ ,

$$\hat{\pi}_t = \frac{1}{1 - \beta\rho}\kappa(\hat{y} - \hat{a}) \quad (50)$$

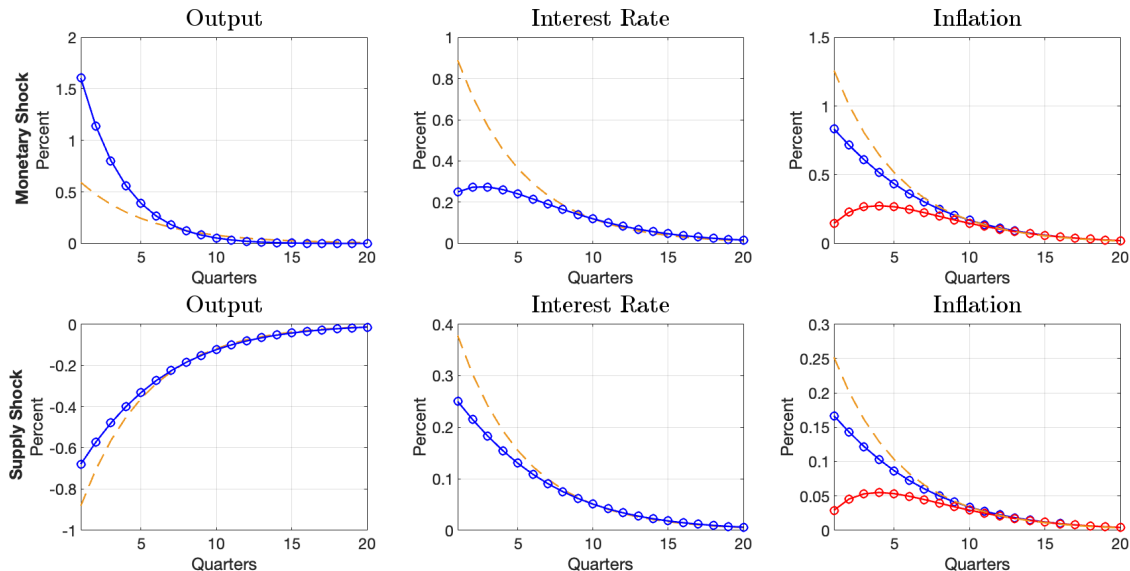
To show how big the impact of the information friction and learning channel, I impose the slope of Phillips curve as  $\kappa = \frac{\Gamma}{1-\Gamma}$ . Since  $\Gamma = 0.3$ , the implied value for Calvo parameter is 52.5%. The dashed orange line plots the impulse responses of the standard NK model with Calvo parameter 52.5% following two kinds of shocks.

There are three key implications about the monetary non-neutrality from the calibration analysis. First, with exogenously calibrated parameters  $\Gamma$  and  $\{\theta_t\}$ , the model exhibits substantial monetary non-neutrality. A 100 basis-point cut in the interest rate results in an initial output increase of approximately 160 basis points. This response is comparable to that in a standard NK model where the probability of not adjusting price being around 70%. This probability aligns with the value that is usually calibrated from a DSGE model (Christiano et al., 2005 and Smets and Wouters, 2007). This suggests that the degree of monetary non-neutrality generated by our mechanism is sufficient to explain and match the macro-level impulse-response evidence.

Second, the monetary non-neutrality generated by the standard NK model is three times smaller than that in our model when  $\kappa = \frac{\Gamma}{1-\Gamma}$ . The reason is that in the survey, household inflation expectation lags far behind the actual inflation. When we calibrate this evidence into the model instead of leveraging the knowledge imposed by the rational expectations, we achieve much larger monetary non-neutrality. To understand the magnitude of such difference, notice that the coefficient  $1/(1 - \beta\rho)$  in (50) is the counterpart of  $1/(1 - \theta)$  in our model. In practice, the discount factor  $\beta$  is close to one and the persistence of the shock is  $\rho = 0.8$ . Then,  $1/(1 - \beta\rho) = 5$ . In contrast, the implied information friction in the initial period from our calibration is  $1/(1 - \theta) = 1.2$ , making the slope of the Phillips curve about four times smaller in our model.

Third, since the output response depends on the gap between actual inflation and the inflation nowcast, rapid learning can close this gap before the shock fully dissipates. Consequently, the persistence of the output response is endogenously smaller than the persistence of the monetary shock. This is consistent with the empirical evidence. As shown in Figure 3 of Bauer and Swanson (2023), following a monetary shock, industrial production reaches its trough in a year, while the CPI continues to decline and approximately reaches its trough after 40 months. In addition, Figure

Figure 3: Impulse Responses of Inflation, Output and Interest Rate in the Calibrated Economy



*Notes:* The figure plots the impulse responses of output, interest rate, inflation and inflation nowcast following a 100 basis-point interest rate cut and a 100 basis-point decrease in the aggregate productivity based on the calibrated model. In the third column, the blue line represents the inflation and the red line represents the inflation nowcast. The dashed orange line represents the impulse responses generated from a standard NK model with the Calvo parameter 52.5%, i.e., 52.5% firms cannot adjust prices in each period. The x-axis is quarters. The y-axis is percent.

8 in Appendix B shows the impulse responses of unemployment rate and inflation following a main business cycle shock. The unemployment responses peaks earlier than inflation responses. The theory based on household expectation and slow learning provides an endogenous explanation for less persistent output responses.

Now, I turn to supply shock. Following a 100 basis-point reduction in the aggregate productivity is rather not surprising, the output declines and the inflation increases by less than 100 basis points. This occurs because prices remain below the full-information benchmark, which sustains aggregate demand above the natural output level and the higher labor supply in equilibrium. The persistence of the output response inherits the shock's persistence, when the gap between inflation and inflation nowcast narrows to zero. This differs from the case of a monetary shock, as the aggregate productivity shock directly impacts output.

Overall, our mechanism can generate substantial monetary non-neutrality, comparable in magnitude to the calibrated Calvo parameter commonly used in DSGE literature. The model sheds

light on how the survey data can be directly linked to the output gap. The persistence of the output response is endogenously determined, with faster learning leading to lower persistence.

**Applications** – I consider two applications of the model: (i) anticipated VAT reforms, and (ii) post-pandemic steepened slope of Phillips curve.

First, Buettner and Madzharova (2021) find a rapid passthrough of anticipated VAT-induced cost changes to prices within four months—two months before and two months after the reform as shown in their Figure 4. This finding contradicts the predictions of the standard NK model, which suggests that firms would begin raising prices at least one year prior to the reform. In contrast, my model predicts no price changes before the reform and full passthrough upon implementation, as these tax reforms are common knowledge to consumers, resulting in minimal price stickiness. In practice, additional factors influence price dynamics: intertemporal substitution of durable goods tends to elevate prices before the reform, while delays in cost passthrough within the supply chain can defer price increases until after implementation.

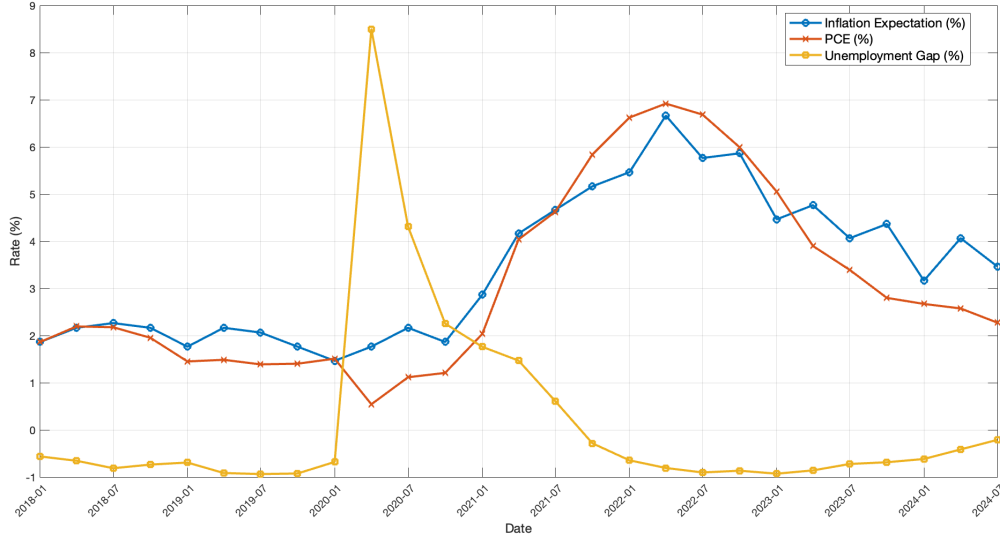
Second, two puzzles have emerged in the dynamics of inflation and unemployment rate in the post-pandemic era. First, the supply-induced inflation surged immediately after the pandemic and remained persistent, contrary to the prediction of a flat Phillips curve estimated using pre-COVID data (Hazell et al., 2022). Second, despite the Fed’s aggressive interest rate hikes beginning in August 2022, demand-driven inflation, caused by fiscal stimulus and labor market tightness (Blanchard and Bernanke, 2023), declined rapidly without a substantial rise in unemployment.

Theories have been proposed to address these puzzles. Benigno and Eggertsson (2023) introduces a non-linear New Keynesian Phillips curve in which labor becomes significantly more costly when the vacancy-to-unemployed ratio surpasses a critical threshold. However, as supply shortages have eased, this framework struggles to explain the second puzzle. Instead, I propose a unified explanation for both puzzles through the information channel in our model. The historically high media coverage and public discussion of supply chain disruptions, elevated inflation, and labor shortages likely reduced information asymmetry, enabling households to learn more quickly about the rising costs faced by firms.

Figure 4 illustrates the dynamics of the unemployment gap, PCE inflation, and inflation expectations based on the Michigan Survey of Consumers. To eliminate the level effect, I shift inflation expectations to coincide with actual inflation in January 2018 (D’Acunto et al., 2022). It is evident that inflation expectations closely track actual inflation during this period. In contrast,



Figure 4: Post-Pandemic Unemployment Rate, Inflation and Fed Funds Rate



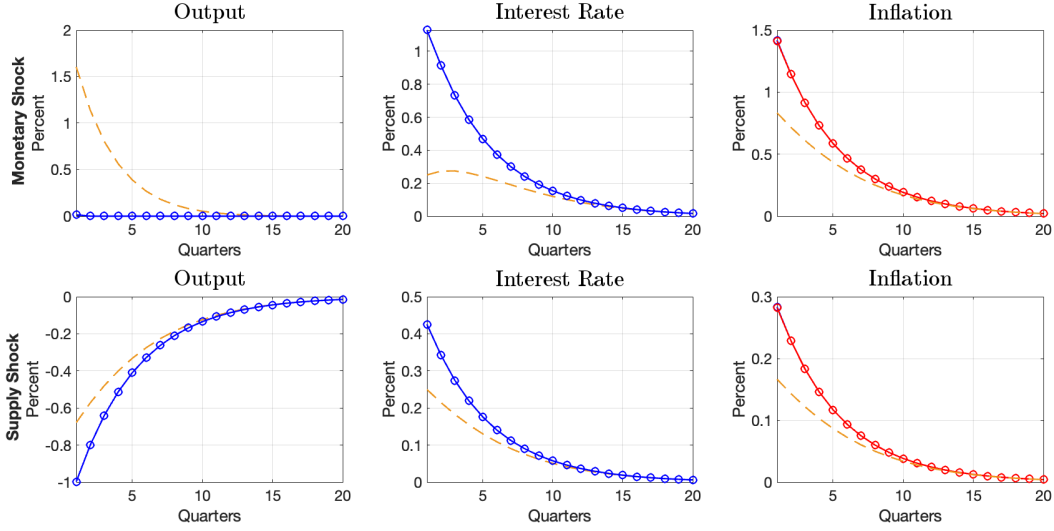
*Notes:* The figure shows the time series of unemployment gap measured by unemployment rate minus the noncyclical rate of unemployment (NROU), PCE inflation and mean inflation expectation based on Michigan survey from Jan 2018 to July 2024. The x-axis is date. The y-axis is rate.

the unemployment gap remains small and stable, consistent with our theory that a small difference between inflation and inflation expectations results in a small output gap.

This aligns with the findings of Beaudry et al. (2024), who argue that household inflation expectations are crucial for explaining recent inflation dynamics. Moreover, it is specifically household inflation expectations that matter. Hazell (2024) demonstrate that other measures of inflation expectations, such as those from the Survey of Professional Forecasters, one-year-ahead inflation expectations from swaps, and adaptive expectations (e.g., the fourth lag of inflation), do not exhibit the same degree of increase as household inflation expectations. Here, I provide a micro-foundation to justify the use of household inflation expectations in the Phillips curve.

Figure 5 illustrates the responses of inflation and output when information in the model is highly precise. The orange dashed line represents the impulse responses based on our benchmark calibrated model. In both types of shocks, inflation and inflation expectations closely overlap, as observed in Figure 4. First, the second row presents the impulse responses following a supply shock. The increase in inflation is approximately double that of the benchmark case, which aligns with the drastic inflation surge at the onset of the supply chain disruptions. However, the output and unemployment rate did not decline significantly in reality compared to the model's predictions,

Figure 5: Impulse Responses of Inflation and Household Inflation Expectation



*Notes:* The figure shows the impulse responses of output, interest rate, inflation and inflation nowcast following a 100 basis-point decrease in the aggregate productivity in a calibrated model with a large signal-to-noise ratio. The orange dashed line represents our benchmark calibrated model. In the third column, the blue line represents the inflation and the red line represents the inflation nowcast. The x-axis is quarters. The y-axis is percent.

likely due to the concurrent fiscal stimulus. Second, the first row of Figure 5 shows the impulse responses to a demand shock under precise information. The output response is negligible, while inflation declines as the interest rate rises, which explains the second puzzle.

**Policy Implication** – The main policy lesson from this application is that the slope of the Phillips curve is endogenous to the level of information available on the consumer side. Conventional Phillips curves, derived from reduced-form assumptions such as infrequent price adjustments and menu costs, are vulnerable to the Lucas Critique. Certain shocks, in particular, may trigger a sequence of public events, media reports, discussion in the public domain, and policy announcements, which significantly increase households’ awareness of the inflation, resulting in a steeper slope of Phillips curve. This has important implications for the conduct of monetary policy. The monetary authority should adopt a more aggressive stance when household inflation expectation is more accurate, as prices are more responsive to the shock in such environments.

### 2.3 Extensions

I discuss two extensions. In the first extension, I allow multiple goods to be produced by one firm. The firm produces goods with different productivity for each good.

$$\log A_{kj} = \log A + a_k + a_{kj}$$

where  $a_{kj}$  is the productivity of producing good  $j$  by firm  $k$ . It is i.i.d following  $a_{kj} \sim \mathcal{N}(0, \tilde{\sigma}_{ap}^2)$ . I assume that there is no search frictions when shopping within a firm. Shoppers decide which firm to purchase from and then buy the CES aggregation of all the goods in the firm. Let  $P_k$  denote the CES price index of multiple goods in firm  $k$ . We have the following result.

**Proposition 10.** *Each firm charges same markup over all the products it sells.*

$$P_{kj} = \frac{e_k}{e_k - 1} \frac{W}{A_{kj}} \quad (51)$$

where  $e_k$  is the elasticity of demand uniform for all  $j$ . It is determined by

$$P_k = \frac{e_k}{e_k - 1} \frac{W}{A_k}; e_k = \lambda \frac{\int X(g(\lambda(v^*(x) + p_k))) d\Phi_x(x)}{\int X(1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x)} + 1 \quad (52)$$

where  $P_k$  is the CES price index of  $P_{kj}$ . The passthrough of product-level productivity shocks  $a_{kj}$  increases toward one when the number of products increases.

This extension speaks to the empirical literature on passthrough of exchange rate shock to retail prices. Goldberg and Hellerstein (2013) and Nakamura and Zerom (2010) find complete passthrough of wholesale prices to retail prices for beer and coffee sales in retail stores.<sup>15</sup> The proposition shows that when there are many goods in one store, the passthrough of product-specific idiosyncratic shocks is closed to one. However, this does not mean that the passthrough of aggregate shocks and firm-specific shocks is complete.

In the second extension, I generalize the setup to accommodate finite labor supply elasticity. The details of setup and equilibrium are delegated to Appendix B. I present the following result.

**Proposition 11.** *The Phillips curve, when the elasticity of labor supply is  $\eta$ , is given by,*

$$\hat{p} = (1 + \eta) \frac{\Phi}{1 + \eta v - \Phi} \left( \hat{c} - \frac{1 + \eta - \eta v}{1 + \eta} \hat{a} \right) \quad (53)$$

where  $v$  is defined in the Appendix B.

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<sup>15</sup>See Gopinath et al. (2011) for a summary of this literature.

From Proposition 5, shoppers are more likely to search for all firms. They are more likely to be drawn to high-productivity, low-price firms, leading to an expansion in demand for these firms and a contraction for low-productivity firms. The parameter  $v$  captures the first-order effect of demand reallocation on the aggregate productivity. To understand the intuition, suppose the effect of demand reallocation is absent, i.e.,  $v = 0$ . Then  $\hat{p} = (1 + \eta)_{1-\Phi}(\hat{c} - \hat{a})$  and the price index response is larger if  $\eta > 0$ , because with finite labor elasticity, the real marginal cost increases. Now consider a monetary shock (similarly for a supply shock) with  $v > 0$ . Compared to the  $v = 0$  case, the price index response is smaller because demand reallocation toward high-productivity firms effectively raises aggregate productivity, mitigating the rise in the price index and enhancing the output response.

### 3 Empirics

In this section, I provide empirical support for the key mechanism of the model: unanticipated inflation increases search activities. To support this logic, we must establish two ingredients in the data: (i) the presence of information frictions and (ii) the reaction of search behavior under incomplete information about unanticipated inflation. The former is addressed in Section 2.1. Here, we focus on the second component.

In particular, I utilize a detailed consumer panel dataset that includes information on households' shopping trips, spending, store choices, and demographic characteristics to examine whether higher inflation is associated with increased measures of search behavior. My contribution to the literature lies in developing a novel measure of search activities that more accurately captures search efforts and aligns more closely with the predictions of standard sequential search models. Finally, I present evidence on the secular decline of search activities and explore how this trend may be connected to the decline in the slope of the Phillips curve.

#### 3.1 Search Activities and Unanticipated Inflation

I first briefly describe the data, then propose our measure of search activity, and lastly I present the results.

**Data** – The data source is the NielsenIQ Consumer Panel Data set.<sup>16</sup> The sample period is 2006 Q1 - 2019 Q4. NielsenIQ tracks the shopping behavior of average 55,000 households every year. Each household uses in-home scanners to record purchases. Households also record any deals used that may affect the price. These households represent a demographically balanced sample of households in 49 states and about 3,000 counties in the United States. Each household stays in the panel for 30 quarters on average. The dataset has over 1,000 NielsenIQ-defined product modules that are organized into over 100 product groups and covers around 30% of all expenditure on goods in the CPI.<sup>17</sup> The dataset contains information about each shopping trip the household takes, such as the retailer, the spending on each product defined as a barcode, the product module and group that the product belongs to, and the date of transaction. Moreover, the data includes households’ demographic information such as age, education, employment, marital status, which are updated annually. I aggregate the dataset to the household-quarter level. I only consider households live in the Metropolitan Statistical Area.<sup>18</sup>

**Measurement** – The search protocol described and characterized in the model simplifies the actual shopping process. In practice, shoppers tend to make the majority of their purchases at a primary retail store, while visiting other stores for specific needs. For instance, during the sample period, shoppers allocate an average of 65% of their total spending on a given product group to the store they visit the most frequently. Additionally, shoppers often purchase multiple items in a single trip, and most stores offer a wide range of product groups. As a result, search activities may manifest as a reallocation of spending across stores for the same product group. For example, a shopper may initially buy milk from store A and cheese from store B but, after a shock, begin purchasing both milk and cheese from store A while reducing cheese purchases from store B. This

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<sup>16</sup>Researcher’s own analyses calculated (or derived) based in part on data from Nielsen Consumer LLC and marketing databases provided through the NielsenIQ Datasets at the Kilts Center for Marketing Data Center at The University of Chicago Booth School of Business. The conclusions drawn from the NielsenIQ data are those of the researcher(s) and do not reflect the views of NielsenIQ. NielsenIQ is not responsible for, had no role in, and was not involved in analyzing and preparing the results reported herein.

<sup>17</sup>For further discussion of the NielsenIQ data, see Broda and Weinstein (2010).

<sup>18</sup>People living in the countryside may exhibit different search behaviors compared to those in urban areas. They are more likely to engage in "one-stop" shopping due to limited store availability. Their lower search activity may not indicate a lack of willingness to search but rather reflect physical constraints imposed by the environment.

suggests that simply counting the number of trips and the number of distinct stores shopper visits may not fully capture the search effort, even though it is the definition of a search in the model.

To account for the empirical patterns of shopping, I construct the measure of search effort as follows. First, for each consumer and each product group, I find the store she visits most frequently in the entire sample period. I call that store the *routine store*. Second, if she does not buy from the routine store or she buys from multiple stores for this product group, I record the total spending that she spends on the stores other than the routine store. Repeat this process for all the product groups. Finally, I define the non-routine share of spending as the ratio of all the non-routine spending over all groups and the total spending in the given quarter. The non-routine share captures the *extra* search effort to look for the products that shoppers usually buy from the routine store.

I also construct other two measures of search activities. The first is the number of trips each household takes in a quarter. Second, I measure the number of distinct retail stores visited by consumers in a quarter. Both measures captures some aspects of our primary measure. Table 1 presents the summary statistics for these search measures. On average, consumers' non-routine share of spending is 35.6%. They make about 3.5 shopping trips per week, visit approximately 12 different retailers per quarter. The variance of these measures is substantial. This is consistent with our model in which search is primarily driven by idiosyncratic match utility shocks and productivity shocks, which may have substantial variance.

Table 3: Descriptive Statistics of Household Search Behavior

	Mean	S.D.	10th Percentile	90th Percentile	Observations
Non-routine Share(%)	35.6	25.2	3.23	71.1	2,846,354
Number of Trips	40.5	29.3	11	80	2,846,354
Number of Distinct Retailers	11.7	7.27	4	22	2,846,354

*Notes:* The table reports summary statistics for key household search behavior variables in the sample. *Non-routine Share* is the share of non-routine spending in a quarter. *Number of Trips* is the total number of shopping trips per quarter per household. *Number of Retailers* is the distinct retailers visited by a household per quarter.

**Unanticipated Inflation** — Following the literature, I assume that consumers use historical data to forecast the current inflation. In particular, consumers estimate a simple OLS regression of inflation on four lags of the inflation for food and drinks and unemployment rate. The residual from

this regression is the unanticipated inflation, which has a mean of -7.8 bp and a standard deviation of 51 bp in the sample period. I focus on inflation for food and drinks because the majority of NielsenIQ products fall into this category.<sup>19</sup> Additionally, I consider the measure based on the inflation for overall goods and services. The anticipated inflation in this case has a mean of -7.5 bp and a standard deviation of 76 bp. I normalize the two series of unanticipated inflation, so their units are standard deviation in our sample. Appendix C provides further details of regression and discusses several robustness checks.

**Impact of Unanticipated Inflation on Consumers' Search Behavior** – To assess the changes in search behavior after an unanticipated inflation shock, our baseline specification is:

$$y_{it+1} = \lambda_i + \beta \tilde{\pi}_t + X_{it} + e_{it} \quad (54)$$

where  $t$  is time;  $i$  represents consumer.  $\lambda_i$  is the consumer fixed effect.  $\tilde{\pi}_t$  is the unanticipated inflation.  $\beta$  is the coefficient of interest. It measures the magnitude of the correlation between the unanticipated inflation and the consumers' search behavior.  $y_{it+1}$  is the non-routine share of spending in the next quarter. I use next-period value for two reasons. First, it avoids reverse causality because inflation and consumer search behavior are jointly determined in theory. Second, it may take time for consumers to change their shopping habits.  $X_{it}$  is the time-varying consumer controls. These controls include consumer age, employment, education, marital status, having children or not, and consumer  $i$ 's total spending in time  $t$ . As pointed out by Aguiar and Hurst (2007), these variables have large affect on the pattern of shopping behavior.

The results are presented in Table 4. The first column indicates that one standard deviation (51 bp) increase in unanticipated food and drink inflation leads to a 26.5 bp increase in the non-routine share of spending. This suggests that consumers respond to higher prices by engaging in more active search, shifting purchases to stores outside their routine stores. The magnitude of the response is modest, which is about a half (26.5 bp/51 bp). Given the information friction estimated in (48), small magnitude may indicates large search frictions.

The second column uses the unanticipated overall inflation. It shows a much smaller increase in the non-routine share and not statistically significant. The effect is smaller because the NielsenIQ data primarily covers food and beverages, and search behavior is more sensitive to inflation in

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<sup>19</sup>I do not use the main inflation shock since it is not correlated with the inflation in food and drinks. If any, there is insignificant negative relationship between these two time series. See Appendix C for details.

Table 4: Non-routine Share of Spending and Unanticipated Inflation

<i>Dep. var.:</i> Non-routine Share	(1)	(2)	(3)	(4)
Unanticipated inflation (F&D)	0.265*** (0.023)		0.253*** (0.023)	0.234*** (0.023)
Unanticipated inflation (overall)		0.022 (0.018)		
Number of trips			0.033*** (0.002)	-0.028*** (0.003)
Number of distinct stores				0.327*** (0.011)
Observations	2,660,735	2,660,735	2,660,735	2,660,735
Consumer fixed effect	✓	✓	✓	✓
Consumer varying effect	✓	✓	✓	✓

*Notes:* The table reports the estimates in specification (54). Each observation is at the consumer  $\times$  quarter level covering from 2006 Q1 to 2019 Q4. The coefficient represents the corresponding change in different measures of search behavior after a standard deviation increase in unanticipated inflation. Consumer fixed and time-varying effects are controlled. Standard errors are clustered at the consumer level. \*Significant at the 10% level; \*\*Significant at the 5% level; \*\*\*Significant at the 1% level.

these sectors. The third and fourth columns introduce controls for the number of shopping trips and the number of distinct stores visited. The coefficients decrease only slightly, suggesting these variables capture a very limited portion of search effort. This suggests that consumers allocate most of their search efforts to substituting products within the same categories across the stores they have already visited, rather than increasing trips or visiting new stores.

The estimated coefficient may be biased downward for several reasons. First, consumers only record purchases from stores included in the NielsenIQ dataset, which predominantly covers large retail stores. As a result, our measure may not fully capture the non-routine share of spending if consumers switch to stores not included in the dataset or to online purchases. Second, substantial substitution within a product group could contribute to the bias. For example, consumers may trade down to lower-quality goods within the same store (Jaimovich et al., 2019) after an increase in inflation. However, we do not observe the time spent in each shopping trip. Finally, the inflation



shock may not be entirely passed on to retail prices, as suppliers may absorb part of the shock in their wholesale costs. This incomplete pass-through could further dampen the observed relationship between inflation and non-routine spending.

Overall, this evidence supports a key aspect of the main mechanism: as prices rise after an aggregate shock, consumers are incentivized to search for alternatives. The evidence indicates the response of search activities to unanticipated inflation is statistically significant. There are potentially two reasons for the magnitude of the response being modest. One is that the search friction is large, and another is that the estimate is biased downwards.

### 3.2 Secular Decline in Non-routine Share and Shopping Time

In this final section, I show the secular decline in both non-routine share of spending and shopping time. I discuss the potential explanations and how they are related to the secular decline in the slope of Phillips curve (Del Negro et al., 2020).

To complement the analysis based on NielsenIQ Consumer Panel, I also use data from the 2003–2019 waves of the American Time Use Survey (ATUS) conducted by BLS. The ATUS sample is drawn from individuals exiting the Current Population Survey (CPS). Each wave is based on 24-hour time diaries, where respondents report their activities from the previous day in detailed time intervals. The ATUS includes over 400 detailed time-use categories, providing rich insights into daily activity patterns. Specifically, I use the time each respondent reports in the category “obtaining goods” as a proxy for shopping time.<sup>20</sup>

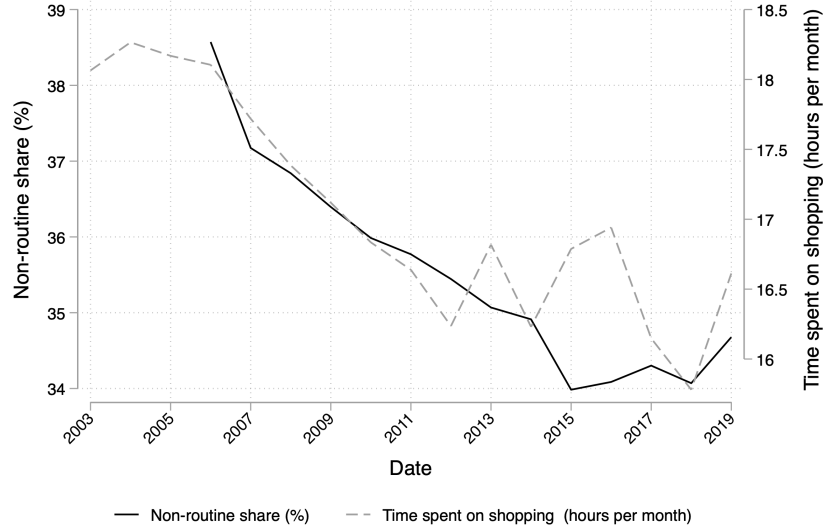
To map the empirical objects to the model concepts, we interpret both the non-routine share of spending and the total shopping time as the total search cost for an average shopper. In theory, the total search cost is defined as the average number of searches multiplied by the search cost per search, i.e.,  $\rho^{-1}\kappa$ . Figure C.1 illustrates that, in our calibrated model, the total search cost increases as the search cost per search rises, while there is a reduction in the number of searches. In the context of empirics, higher search frictions decrease both the non-routine share of spending and the total shopping time.

Figure 6 illustrates that the non-routine share of spending has declined by 5 percentage points over the sample period, while the average time spent on shopping has decreased by 2 hours per

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<sup>20</sup>I do not use the ATUS in the previous section because the data lacks a panel structure. Household characteristics are very important in explaining shopping patterns (Aguiar and Hurst, 2007).

Figure 6: Time Trend of Non-Routine Share of Spending and Shopping Time



*Notes:* The figure plots the average non-routine share of spending and shopping time over time. I use the American Time Use Survey (2003-2019) to compute the average shopping time.

month. According to our model, this empirical pattern contradicts the hypothesis that search frictions have decreased due to advancements in information and communication technology (ICT) (Ellison and Ellison, 2018). One possible explanation is that search frictions have actually increased over time. However, a more plausible interpretation is the rise of market power driven by a few dominant retail chains, which has crowded out local retail stores (Hausman and Leibtag, 2007; Federal Trade Commission, 2023). In addition, DellaVigna and Gentzkow (2019) shows that the stores within a chain tend to set uniform prices for identical products. Both factors contribute to a decline in the dispersion of the price distribution, reducing the average value of additional searches and the threshold in the model. It results in the decline of the number of searches, and consequently, decline in the total search cost. The lower threshold in the model indicates lower aggregate total passthrough as shown in Proposition 6. It implies that the secular decline in the slope of the Phillips curve (Del Negro et al. (2020)) may be related to the decline of outside options caused by both rising market concentration and price uniformity reduces the price dispersion. Quantification of the contribution of the search channel to the decline of the slope of Phillips curve is left to the future research.

## 4 Conclusion

This paper develops a new framework for understanding monetary non-neutrality, driven entirely by consumer-side frictions. At the heart of the model is the information asymmetry about nominal marginal costs between consumers and firms. Specifically, the framework integrates a heterogeneous firm block and incomplete consumer information into a standard sequential search model. When consumers observe a price increase, they attribute it to adverse productivity shocks rather than increases in nominal wages, prompting them to search for outside options. Firms, in turn, internalize this consumer search behavior, limiting the passthrough of cost changes to prices. The framework also accommodates aggregate supply shocks, providing a toolbox for analyzing a wide range of shocks as in the standard NK model. Future research can investigate the effect of fiscal policy in this model.

This paper further presents a Phillips curve that relates the output gap to household nowcast error of inflation. It emphasizes the role of household expectations in determining the slope of Phillips curve. After calibrating the model to moments drawn from the literature and empirical evidence, the dynamic model generates substantial monetary non-neutrality, highlighting the importance of consumer-side mechanisms in macroeconomic dynamics. In addition, empirical findings support for the model’s key mechanism. I also document a secular decline in search activity and connect this trend to the observed secular decline in the slope of the Phillips curve.

Several further topics of inquiry are left for future research. First, although this paper focuses on final goods markets, the framework can be extended to any market with many sellers and buyers, such as upstream and downstream firms in supply chains. An interesting extension would be embedding this model into production network models. Second, applying the model to the labor market could yield valuable insights. Given the parallels in the literature between search behavior in goods and labor markets, this extension might be straightforward. Workers’ incomplete information regarding the average posted wage could influence their job-search decisions, prompting firms to adjust wage-setting and potentially generating wage stickiness. Finally, to better calibrate the model and assess the quantitative importance of the mechanism, a micro-foundation for search costs is necessary. A spatial and industrial organization model would be a promising candidate.

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## Appendix

### A Proofs and Derivations in Static Model

#### Proof of Proposition 1:

*Proof.* We consider the case where the first draw does not need the search cost. Shoppers are randomly assigned a firm for free in the first round of search. This guarantees that they always participate the market.

I prove that for given  $x$ , if  $\int U(v|x)\psi(y|x)dy = -\infty$ , then  $v^*(x) = -\infty$ ; if  $\int U(v|x)\psi(y|x)dy > -\infty$ , there exists a unique threshold defined as follows.

$$v^*(x) = -\frac{\kappa}{1 - \Psi(v^*(x)|x)} + \frac{\int_{v^*(x)}^{\infty} y\psi(y)dy}{1 - \Psi(v^*(x)|x)} \quad (55)$$

First, given  $x$ , I consider two limits. When  $v \rightarrow -\infty$ ,

$$-\kappa + U(v|x) \int_{-\infty}^v \psi(y|x)dy + \int_v^{\infty} U(y|x)\psi(y|x)dy = -\kappa + \int U(y|x)\psi(y|x)dy$$

Then, if  $\int U(v|x)\psi(y|x)dy > -\infty$ ,  $U(v|x) > v$ . Intuitively, when the search cost is lower than the value of search when the agent has the worst value whatsoever, the agent should choose to continue searching. In the other limit where  $v \rightarrow \infty$ ,

$$-\kappa + U(v|x) \int_{-\infty}^v \psi(y|x)dy + \int_v^{\infty} U(y|x)\psi(y|x)dy = -\kappa + U(v|x)$$

Then,  $U(v|x) = v$ . Intuitively, when the agent has the best value whatsoever, the agent should stop search because she cannot get any other good that offers better value.

Second, I claim that if  $U(v|x) > v$ , then  $U'(v|x) = 0$ . To prove the claim, suppose there exist values of  $v$  on its support (at least at  $-\infty$ ) such that  $U(v) > v$ . Then,  $U(v)$  satisfies,

$$U(v|x) = -\kappa + U(v|x) \int_{-\infty}^v \psi(y|x)dy + \int_v^{\infty} U(y|x)\psi(y|x)dy \quad (56)$$

Equivalently,

$$U(v|x) = -\frac{\kappa}{1 - \Psi(v|x)} + \frac{\int_v^{\infty} U(y|x)\psi(y|x)dy}{1 - \Psi(v|x)} \quad (57)$$

It is easy to show that

$$U'(v|x) = \frac{\psi(v|x)}{(1 - \Psi(v|x))^2} \left\{ \int_v^{\infty} U(y|x)\psi(y|x)dy - U(v|x)(1 - \Psi(v|x)) - \kappa \right\} = 0 \quad (58)$$

The second equation holds due to (57). Then, it is easy to see that  $U(v|x)$  is a constant in  $(-\infty, v^*]$ , which is equal to  $v^*(x)$ , and then  $U(v) = v$  in  $(v^*, \infty)$ .  $v^*$  is unique. In addition, for  $v < v^*$ ,

$$-\kappa + U(v|x) \int_{-\infty}^v \psi(y|x) dy + \int_v^\infty U(y|x) \psi(y|x) dy = -\kappa + v^*(x) \Psi(v^*(x)) + \int_{v^*(x)}^\infty y \psi(y|x) dy = v^*(x) \quad (59)$$

The search problem in (11) is therefore simplified to

$$U(v|x) = \max\{v, v^*(x)\} \quad (60)$$

This implies that the value of an additional search does not depend on the state  $v$ . No matter what state the shopper has, she always compare the state with  $v^*(x)$ .

Now, we consider the case in which  $\int U(v|x) \psi(y|x) dy = -\infty$  for any  $x$ . This happens when firms charge arbitrarily high prices, which implies  $\psi(y|x)$  is a Dirac function at  $y = -\infty$ . Then, it is optimal to accept any firm in the first round and the resulting  $v^*(x) = -\infty, \forall x$ .

Now, we prove the second part:  $v^*(x)$  decreases in  $x$ . First, notice that the threshold is determined alternatively by the following,

$$\int \int_{\lambda(v^*(x)+p)}^\infty \left( \frac{1}{\lambda} \epsilon - p - v^*(x) \right) g(\epsilon) d\epsilon f(p|x) dp = \kappa \quad (61)$$

For  $x_1 < x_2$ ,  $f(p|x_1)$  is FOSD over  $f(p|x_2)$ . Since the inner integral in LHS decreases in  $p$ , that implies

$$v^*(x_1) > v^*(x_2)$$

■

## Proof of Proposition 2:

*Proof.* We take first-order condition of firm's profit in (17) with respect to  $P_k$ . It is easy to show that we can always express the pricing strategy as in (18) and define the elasticity of demand as:

$$e_k = -\frac{\partial \log D(P_k)}{\partial \log P_k} = -\frac{\partial \left( \int X(1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x) \right)}{\partial p_k} + 1 \quad (62)$$

■

**Proof of Lemma 1:**

*Proof.* We are interested in the case in which consumers search actively. We first define the markup elasticity,

$$\Lambda_k = -\frac{d \log \mu_k}{dp_k} = \frac{1}{e_k(e_k - 1)} \frac{\partial e_k}{\partial p_k}$$

Since  $G$  is log-concave,  $\frac{\partial e_k}{\partial p_k} > 0$ . Therefore, the markup elasticity is positive. We can further write out the definition,

$$\Lambda_k = \frac{\frac{g'}{g} \frac{1-G}{g} + 1}{\frac{1}{\lambda} \frac{1-G}{g} + 1}$$

Here, I omit the argument of functions for simplicity. The argument is  $\lambda(v^*(w) + p_k)$ . Note that equilibrium price is a function of  $v^*(w)$  and  $a_{kt}$ . I now rewrite the LHS of (20) in terms of the integral over productivity distribution, which is exogenous,

$$\int \int_{\lambda(v^*(w)+p^*(v^*(w),a))}^{\infty} \left( \frac{1}{\lambda} \epsilon - p^*(v^*(w), a) - v^*(w) \right) g(\epsilon) d\epsilon \phi_a(a) da = \kappa \quad (63)$$

where  $\phi_a(a)$  is the pdf of productivity distribution. Fix  $p^*(v^*(w), a)$ , the LHS is decreasing in  $v^*(w)$ . However, higher  $v^*(w)$  also decreases optimal prices. To know the net effect of these two forces, we need to derive  $\frac{\partial p(v^*(w), a_k)}{\partial v^*(w)}$ . From now on, we use  $x_k(v^*(w))$  to denote  $x(v^*(w), a_k)$  for any variable  $x$ .

$$\frac{\partial p_k(v^*(w))}{\partial v^*(w)} = \frac{\partial \mu_k(v^*(w))}{\partial v^*(w)} = -\frac{1}{e_k(v^*(w))(e_k(v^*(w)) - 1)} \frac{\partial e_k(v^*(w))}{\partial v^*(w)} \quad (64)$$

It is easy to show that

$$\frac{\partial e_k(v^*(w))}{\partial v^*(w)} = \lambda^2 \frac{g'(1-G) + g^2}{(1-G)^2} \left( 1 + \frac{\partial p_k(v^*(w))}{\partial v^*(w)} \right) \quad (65)$$

Combine the above equation with (64), we have:

$$\frac{\partial p_k(v^*(w))}{\partial v^*(w)} = -\frac{\Lambda_k}{1 + \Lambda_k} \quad (66)$$

Since  $\Lambda_k > 0$ ,  $\frac{\partial p_k(v^*(w))}{\partial v^*(w)} \in (-1, 0)$ . This implies that  $\frac{\partial(v^*(w) + p_k(v^*(w)))}{\partial v^*(w)} \in (0, 1)$ . Therefore, the LHS of (20) decreases in  $v^*(w)$ . ■

**Proof of Theorem 1:**

*Proof.* First, notice that since  $G$  is log-concave,  $\mu_k$  decreases with  $P_k$ . From  $P_k = \mu_k \frac{W}{A_k}$ , we know that there is a unique solution for each optimal price  $P_k$  given the full-information threshold  $v^*(w)$ .

Then, from Lemma 1, we know that there exists a unique solution  $v^*(w)$  to 20 given that the prices are computed through the first-order conditions as in (24). The equilibrium in which shoppers search actively exists and is unique because  $v^*(w)$  exists and is unique.

As Diamond (1971) points out famously, there are always a continuum of equilibria where shoppers do not search and firms charge very high prices, i.e.,  $v^*(w) = -\infty$  and  $P_k = \infty, \forall k$ . ■

### Remarks on Computation of the Full-information Equilibrium:

**Remark 1** (Remark on Computing Steady-State Equilibrium). *The proof of Theorem 1 provides insights on the computational method for the full-information equilibrium.*

1. First guess a  $v^*(w)$
2. Calculate the optimal price distribution given  $v^*(w)$
3. Plug guessed  $v^*(w)$  and derived price distribution into 20 and check if LHS is equal to the given search cost  $\kappa$ .
4. Increases guessed  $v^*(w)$  if LHS is larger than search cost, according to Lemma 1. Vice versa.
5. Loop the procedure 1-4 until the difference between the LHS and the RHS of 20 is smaller than the given tolerance

### Proof of Theorem 2:

*Proof.* Suppose the nominal wage increases from  $w$  to  $w'$ . Notice  $\Delta w = w' - w$  does not need to be small. We guess that all the optimal prices increase proportionally, i.e.,  $p'_k = p_k + \Delta w$ . Then the price distribution  $f(p|w)$  shifts to the right and becomes  $f(p - \Delta w|w')$ . The threshold is determined by,

$$\int \int_{\lambda(v^*(w') + p)}^{\infty} \left( \frac{1}{\lambda} \epsilon - p - v^*(w') \right) g(\epsilon) d\epsilon f(p - \Delta w|w') dp = \kappa \quad (67)$$

Let  $z = p - \Delta w$ . Then we can rewrite the LHS of the above equation,

$$\int \int_{\lambda(v^*(w') + \Delta w + z)}^{\infty} \left( \frac{1}{\lambda} \epsilon - z - (\Delta w + v^*(w')) \right) g(\epsilon) d\epsilon f(z|w') dz = \kappa \quad (68)$$

This implies that  $v^*(w') = v^*(w) - \Delta w$ . According to (24), the elasticity of demand is given by,

$$\begin{aligned} e'_k &= \lambda \frac{g(\lambda(v^*(w') + p'_k))}{1 - G(\lambda(v^*(w') + p'_k))} + 1 \\ &= \lambda \frac{g(\lambda(v^*(w) - \Delta w + p_k + \Delta w))}{1 - G(\lambda(v^*(w) - \Delta w + p_k + \Delta w))} + 1 \\ &= e_k \end{aligned}$$

Since the elasticity of demand does not change, the optimal prices is given by,

$$p'_k = \log\left(\frac{e_k}{e_k - 1}\right) + w' - a_k = p_k + w' - w = p_k + \Delta w \quad (69)$$

Therefore, we verify the guess that the optimal prices increase proportionally with the nominal wage. Based on Theorem 1, the equilibrium is unique. Therefore, the above constructed equilibrium is the only equilibrium when the nominal wage is  $w'$ . ■

**Proof of Proposition 3:** Here, I provide separate proofs for two parts of Proposition 3. I start with the proof of the first part.

**Proof of Part 1.** First, we can rewrite 14 in terms of integrating over the exogenous productivity distribution,

$$\int \int \int_{\lambda(v^*(x) + p^*(a, w))}^{\infty} \left(\frac{1}{\lambda}\epsilon - p^*(a, w) - v^*(x)\right) g(\epsilon) d\epsilon \phi_a(a) dah(w|x) dw = \kappa \quad (70)$$

where  $v^*(x)$  is implicitly determined by the above equation. On the first order, the posterior belief of the nominal wage collapses to a Dirac function at  $E(w|x)$ . Also, combining the shopper's expected price conditional on  $x$  as shown in (??), on the first order, the above equation becomes,

$$\int \int_{\lambda(v^*(x) + \bar{p}_k + \varphi(a)E(\hat{w}|x))}^{\infty} \left(\frac{1}{\lambda}\epsilon - \bar{p}_k - \varphi(a)E(\hat{w}|x) - v^*(x)\right) g(\epsilon) d\epsilon \phi_a(a) da = \kappa \quad (71)$$

Take the total derivative on  $E(\hat{w}|x)$  on both sides,

$$\int \left(\varphi(a) + \frac{dv^*(x)}{dE(\hat{w}|x)}\right) (1 - G(\lambda(v^*(x) + \bar{p}_k + \varphi(a)E(\hat{w}|x)))) \phi_a(a) da = 0$$

On the first order, it can be written as follows,

$$\frac{dv^*(x)}{dE(\hat{w}|x)} = - \int \varphi(a) \bar{\omega}(a) \phi_a(a) da = - \int \varphi_k \bar{\omega}_k dk \quad (72)$$

where  $\bar{\omega}(a)$  is the expenditure share of firms with productivity  $a$  in the full-information equilibrium where  $w = \bar{w}$ . Then, the threshold, on the first order, is given by,

$$v^*(x) = v^*(\bar{w}) - \frac{\partial v^*(x)}{\partial v^*(x)} v^*(x) = v^*(\bar{w}) - \Phi E(\hat{w}|x)$$

Recall  $\hat{p} = \Phi \hat{w}$ . We have the result. ■

**Proof of Part 2 .** First, plug the result in Part 1 into the elasticity of demand in (19), the elasticity becomes,

$$e_k = \lambda \frac{\int X g(\lambda(v^*(\bar{w}) - \Phi E(\hat{w}|x) + p_k)) d\Phi_x(x)}{\int X (1 - G(\lambda(v^*(\bar{w}) - \Phi E(\hat{w}|x) + p_k))) d\Phi_x(x)} + 1 \quad (73)$$

with some abuse of notation,  $\Phi$  is the aggregate total passthrough and  $\Phi_x(x)$  is the cdf of information sets. Let  $y = \lambda \Phi (E(\hat{w}|x) - \bar{E}(\hat{w}))$  and its pdf is  $\phi_y(y)$ , which is a Gaussian distribution with mean zero and standard deviation  $\sigma = \lambda \Phi \theta \sigma_s$ . Further, we denote  $z = \lambda(v^*(w) - \Phi \bar{E}(\hat{w}) + p_k)$ . The elasticity is rewritten as follows,

$$e_k = \lambda \frac{\int X g(z + y) \phi_y(y) dy}{\int X (1 - G(z + y)) \phi_y(y) dy} + 1 \quad (74)$$

It is easy to show that the first-order approximation to the ratio is equivalent to separately approximating numerator and denominator and then combining them. Following this result, we first expand the numerator.

$$g(z + y) = g(z) + g'(z)y + \frac{g''(z)}{2}y^2 + \mathcal{O}(y^3)$$

Substitute this expansion into the integral and also notice that  $X \propto \exp(y + \bar{w})$ ,

$$\begin{aligned} \int \exp(y) g(z + y) \phi_y(y) dy &= \int (1 + y) \left( g(z) + g'(z)y + \frac{g''(z)}{2}y^2 + \mathcal{O}(y^3) \right) \phi_y(y) dy \\ &= g(z) + \int \left( (g'(z) + \frac{g''(z)}{2})y^2 + \mathcal{O}(y^3) \right) \phi_y(y) dy \\ &= g(z) + (g'(z) + \frac{g''(z)}{2})\sigma^2 + \mathcal{O}(\sigma^3) \end{aligned}$$

Therefore,  $\int g(z + y) \phi_y(y) dy \rightarrow g(z)$  on the order of  $\sigma_s^2$ , which is second-order term. Similarly,  $\int (1 - G(z + y)) \phi_y(y) dy \rightarrow 1 - G(z)$  on the order of  $\sigma_s^2$ . On the other hand, the average expectation of nominal wage shock  $\bar{E}(\hat{w})$  approaches zero on the order of  $\sigma_s$ . Therefore, the elasticity, on the first order, is given by,

$$e_k = \lambda \frac{g(z)}{1 - G(z)} + 1 = \lambda \frac{g(\lambda(v^*(w) - \Phi \bar{E}(\hat{w}) + p_k))}{1 - G(\lambda(v^*(w) - \Phi \bar{E}(\hat{w}) + p_k))} + 1 \quad (75)$$

■



**Proof of Lemma 2:**

*Proof.* First, log price is given by,

$$p_k = \log \mu_k + w - a_k$$

Total differentiate on both sides,

$$\hat{p}_k = \frac{\partial \log \mu_k}{\partial p_k} \hat{p}_k + \frac{\partial \log \mu_k}{\partial p} \hat{p} + \hat{w} \quad (76)$$

We further define  $\gamma_k = (1 - \frac{d \log \mu_k}{d p_k} \Big|_{\hat{w}=0})^{-1}$  and  $\xi_k = \frac{d \log \mu_k}{d p} \Big|_{\hat{w}=0} \gamma_k$ . Then, we have,

$$\hat{p}_k = \gamma_k \hat{w} + \xi_k \hat{p} \quad (77)$$

Since  $\hat{p} = \Phi \hat{w}$ , the total passthrough for individual firm satisfies,

$$\varphi_k = \gamma_k + \Phi \xi_k$$

Integrate on both sides,

$$\Phi = \frac{\Gamma}{1 - \Xi}$$

where  $\Gamma = \int \gamma_k \bar{\omega}_k dk$ ,  $\Xi = \int \xi_k \bar{\omega}_k dk$ . ■

**Proof of Theorem 3:** I first prove the “Incompleteness” part of the Theorem. Then I prove an important lemma and finally I prove the comparative statics results.

**Proof of Incompleteness .** First, notice that for any function  $f(w)$ , the first-order approximation to its derivative is,

$$f'(w) = f'(\bar{w}) + f''(\bar{w}) \hat{w} \quad (78)$$

Then,  $f'(w)|_{\hat{w}=0} = f'(\bar{w})$  on the first order. I claim that the approximation gives the same result if we reverse the order of the operations. Let's first take the first-order approximation to  $f(w)$ ,

$$f(w) = f(\bar{w}) + f'(\bar{w}) \hat{w} \quad (79)$$

Then if we take derivative w.r.t.  $\hat{w}$  and then make  $\hat{w} = 0$ , we get the same result.

Now, following this result,  $\frac{\partial e_k}{\partial p_k} \Big|_{\hat{w}=0}$  and  $\frac{\partial e_k}{\partial p} \Big|_{\hat{w}=0}$  can be computed by first first-order approximating  $e_k$  as we did in Proposition 3 and then take derivative to  $\hat{p}_k$  and  $\hat{p}$ . For simplicity, I omit the

argument of the functions, in particular,  $z = z(v^*(\bar{w}) + \bar{p}_k)$  for any function  $z$ . It is straightforward to show that, on the first order,

$$\left. \frac{\partial e_k}{\partial p_k} \right|_{\dot{w}=0} = \lambda^2 \frac{g'(1-G) + g^2}{(1-G)^2} \quad (80)$$

We can derive that  $\gamma_k$  does not depend on  $\theta$ . In addition, we have

$$\left. \frac{\partial e_k}{\partial p} \right|_{\dot{w}=0} = -\theta \lambda^2 \frac{g'(1-G) + g^2}{(1-G)^2} \quad (81)$$

Then, we have  $\frac{\partial \log \mu_k}{\partial p} = -\theta \frac{\partial \log \mu_k}{\partial p_k}$ . According to Lemma 2, we have

$$\xi_k = \theta(1 - \gamma_k) \quad (82)$$

I claim that  $\varphi_k < 1, \forall k$  and notice that to prove it, it is sufficient to prove  $\gamma_k + \xi_k < 1, \forall k$ . We can write out  $\gamma_k + \xi_k$ ,

$$1 - (\gamma_k + \xi_k) = (1 - \gamma_k)(1 - \theta) \quad (83)$$

Since  $-\frac{d \log \mu_k}{dp_k} > 0$ ,  $\gamma_k < 1$ . ■

Before turning to the result on “Composition”, I first prove the following lemma,

**Lemma A-1.** *Let  $\Lambda_k = -\left. \frac{d \log \mu_k}{dp_k} \right|_{\dot{w}=0}$  denote the steady-state markup elasticity. When  $G$  is Gumbel distribution, it has the following property,*

$$\frac{d\Lambda(y)}{dy} < 0$$

In addition,  $\Lambda(y) \rightarrow 0$  as  $y \rightarrow \infty$  and  $\Lambda(y) \rightarrow \infty$  as  $y \rightarrow -\infty$ .

*Proof.* To simplify notation, we denote  $g(y_k) = g(\lambda(v^*(\bar{w}) + \bar{p}_k))$  and  $G(y_k) = G(\lambda(v^*(\bar{w}) + \bar{p}_k))$ . We assume that  $G$  follows standard type-I extreme-value distribution, i.e.,  $G(y) = \exp(\exp(-y))$ ,  $g(y) = \exp(-y - \exp(-y))$ . It also follows that  $\frac{g'}{g} = e^{-y} - 1$ .

First, since  $G$  is log-concave,  $g$  is also log-concave. This implies the following property,

$$\left(\frac{g'}{g}\right)' < 0; \quad \left(\frac{1-G}{g}\right)' < 0$$

Additionally, using  $G$  is Gumbel, we have  $\frac{1-G}{g} \rightarrow 1$  as  $y \rightarrow \infty$  and therefore  $\frac{1-G}{g} > 1$ .

Second, we write out markup elasticity,

$$\Lambda = \frac{\frac{g'}{g} \frac{1-G}{g} + 1}{\frac{1}{\lambda} \frac{1-G}{g} + 1} \quad (84)$$

Then the derivative of markup elasticity w.r.t  $y$  is given by,

$$\begin{aligned}
\frac{d\Lambda(y)}{dy} &= \left(\frac{g'}{g}\right)' \left(\frac{1-G}{g}\right)^2 \frac{1}{\lambda} - \left(\frac{1-G}{g}\right)' \frac{1}{\lambda} + \left(\frac{g' 1-G}{g}\right)' \\
&= -e^{-y} \left(\frac{1-G}{g}\right)^2 \frac{1}{\lambda} + \frac{1}{\lambda} \left(1 + \frac{g' 1-G}{g}\right) + \left(\frac{g' 1-G}{g}\right)' \\
&< -e^{-y} \left(\frac{1-G}{g}\right) \frac{1}{\lambda} + \frac{1}{\lambda} (1 + (e^{-y} - 1) \frac{1-G}{g}) + \left(\frac{g' 1-G}{g}\right)' \\
&= \frac{1}{\lambda} \left(1 - \frac{1-G}{g}\right) + \left(\frac{g' 1-G}{g}\right)'
\end{aligned}$$

The inequality is due to  $\frac{1-G}{g} > 1$ . The first term of the last equation is negative. We need to deal with the second term. Notice that

$$\left(\frac{g' 1-G}{g}\right)' = \left(\frac{g'}{g}\right)' \left(\frac{1-G}{g}\right) + \left(\frac{g'}{g}\right) \left(\frac{1-G}{g}\right)'$$

It is straightforward that when  $y < 0$ ,  $\frac{g'}{g} = e^{-y} - 1 > 0$ . Then,  $\left(\frac{g' 1-G}{g}\right)' < 0$ . We now focus on the case where  $y > 0$ .

$$\begin{aligned}
\left(\frac{g' 1-G}{g}\right)' &= -e^{-y} \frac{1-G}{g} + (1 - e^{-y}) - (1 - e^{-y})^2 \frac{1-G}{g} \\
&< -e^{-y} \frac{1-G}{g} + (1 - e^{-y}) - (1 - e^{-y}) \frac{1-G}{g} \\
&= (1 - e^{-y}) - \frac{1-G}{g} \\
&< 0
\end{aligned}$$

The first inequality is due to  $1 - e^{-y} \in (0, 1)$  when  $y > 0$ . The second inequality is due to  $\frac{1-G}{g} > 1$ .

Combine all together, we have

$$\frac{d\Lambda(y)}{dy} < 0$$

For limit results, first recall  $\frac{1-G}{g} \rightarrow 1$  as  $y \rightarrow \infty$ . Plug into (84), we get  $\Lambda \rightarrow 0$  when  $y \rightarrow \infty$ . Second, since  $\frac{1-G}{g} \rightarrow \infty$  when  $y \rightarrow -\infty$ ,  $\Gamma \approx \lambda g'/g \rightarrow \infty$  since  $g'/g \rightarrow \infty$ . ■

Next, we turn to the result on composition and comparative statics.

**Proof of Composition and MCS.** First, notice that to show  $\varphi_k$  decreases in  $a_k$ , it is sufficient to show that  $\gamma_k$  decreases in  $a_k$  according to (83).

From Lemma 2,  $\gamma_k = (1 + \Lambda_k)^{-1}$ . Since  $\Lambda_k$  decreases in  $P_k$ , it implies  $\gamma_k$  increases in  $P_k$ . Since  $P_k$  decreases in  $a_k$ , it implies  $\gamma_k$  decreases in  $a_k$ .

Next, we prove the comparative statics results. We first consider the comparative statics on  $\kappa$ . From Lemma 1, an increase in the search cost  $\kappa$  implies lower threshold  $v^*(\bar{w})$ . According to Lemma A-1, the steady-state markup elasticity decreases in  $v^*(\bar{w})$ . This implies a uniform decrease in  $\gamma_k$ . As a result,  $\varphi_k$  decreases in  $\kappa$  for any  $k$  according to (83). When  $\kappa \rightarrow 0$ ,  $v^*(\bar{w}) \rightarrow \infty$  and therefore  $\Lambda_k \rightarrow 0$ , resulting in  $\gamma_k \rightarrow 1$  for any  $k$ . This implies  $\varphi_k = 1$  for any  $k$ . When  $\kappa \rightarrow \infty$ ,  $v^*(\bar{w}) \rightarrow -\infty$ , and therefore  $\Lambda_k \rightarrow \infty$ , resulting in  $\gamma_k \rightarrow 0$  for any  $k$ . This implies  $\varphi_k = 0$  for any  $k$ .

Then, we consider the comparative statics on  $\theta$ . An increase in the information friction, which means a decrease in  $\theta$ , induces lower  $\varphi_k$ , according to (83). When  $\theta \rightarrow 0$ ,  $\Phi = \Gamma$  according to Lemma 2. When  $\theta \rightarrow 1$ ,  $\varphi_k = 1$  according to (83). ■

#### **Proof of Proposition 4:**

*Proof.* From (82), and Lemma 2, we have,

$$\hat{p}_k = \gamma_k \hat{w} + (1 - \gamma_k) \theta \hat{w} \quad (85)$$

$$= \gamma_k \hat{w} + (1 - \gamma_k) \bar{E} \hat{w} \quad (86)$$

Aggregate, we have

$$\hat{p} = \Gamma \hat{w} + (1 - \Gamma) \bar{E} \hat{w} \quad (87)$$

The aggregation requires every firm is individually rational, so they know (86). Suppose every shopper believe that firms and other shoppers are rational. Then every shopper believes the above condition holds. Shoppers' average expectation of  $\hat{p}$  satisfies,

$$\bar{E} \hat{p} = \Gamma \bar{E} \hat{w} + (1 - \Gamma) \bar{E}^2 \hat{p} \quad (88)$$

where  $\bar{E}^2[\cdot] = \bar{E}[\bar{E}[\cdot]]$  denotes the second-order belief. Iterating ad infinitum, the change in the actual price index  $\hat{p}$  can be expressed in terms of the higher-order beliefs of the monetary shock  $\hat{w}$ :

$$\hat{p} = \Gamma \sum_{h=0}^{\infty} (1 - \Gamma)^h \bar{E}^h \hat{w} \quad (89)$$

“Iterating ad infinitum” amounts to imposing common knowledge of rationality. The first iteration requires that shoppers know that firms and other shoppers are rational, the second iteration requires that shoppers know that others know they are rational and firms are rational, and so on. ■

**Proof of Proposition 5:**

*Proof.* Since the markup  $\mu_k$  decreases in  $p_k$ , it increases in  $a_k$ . It is easy to show that  $\lim_{a \rightarrow -\infty} e_k = 1 - \lambda \frac{g'}{g} = 1 + \lambda$  and  $\lim_{a \rightarrow \infty} e_k = 1$ . Then,  $\lim_{a \rightarrow -\infty} \mu_k = \frac{\lambda+1}{\lambda}$  and  $\lim_{a \rightarrow \infty} \mu_k = \infty$ .

From Lemma 2,  $\gamma_k = (1 + \Lambda_k)^{-1}$ . Also, we know  $\xi_k = \theta(1 - \gamma_k)$ . Since  $\gamma_k$  decreases in  $a_k$  as shown in the proof of Theorem 3,  $\xi_k$  increases in  $a_k$ . Also, in the limit when  $a \rightarrow \infty$ ,  $p \rightarrow -\infty$ . Then  $\Lambda \rightarrow \infty$  and  $\gamma \rightarrow 0$ ,  $\xi \rightarrow \theta$ . In the opposite limit,  $p \rightarrow \infty$ , and  $\Lambda \rightarrow 0$ , implying  $\gamma \rightarrow 1$  and  $\xi \rightarrow 0$ . ■

**Proof of Proposition 6:**

*Proof.* See Proof of Theorem 3. ■

**Proof of Proposition 7:**

*Proof.* See Proof of Theorem 3. ■

**Proof of Proposition 41:**

*Proof.* In the case of monetary shock, recall the labor supply condition,

$$\hat{p} + \hat{c} = \hat{w} \quad (90)$$

Combine with the definition of the aggregate passthrough,

$$\hat{p} = \frac{\Phi}{1 - \Phi} \hat{c} \quad (91)$$

Plug in the condition in Proposition 4, we have

$$\hat{p} = \frac{\Gamma}{1 - \Gamma} \frac{1}{1 - \theta} \hat{c} \quad (92)$$

In the case of aggregate supply shock, two equations are as follows,

$$\hat{p} + \hat{c} = \hat{w}$$

$$\hat{p} = \Phi(\hat{w} - \hat{a})$$

Substitute  $\hat{w}$ , we achieve  $\hat{p} = \frac{\Phi}{1 - \Phi}(\hat{c} - \hat{a})$ . Again, leveraging Proposition 4, we have the result.

■

## B Proofs and Calibration in Dynamic Model

### Proof of Proposition 9:

*Proof.* We can rewrite worker's problem as:

$$\begin{aligned} \max_{B_t, X_t, L_t} E_0 \sum_{t=0}^{\infty} \beta^t (\log X_t - L_t) \\ \text{s.t. } X_t + B_t = W_t L_t + R_{t-1} B_{t-1} + \Pi_t \end{aligned}$$

It is easy to show that the standard Euler equation holds. Recall we have,

$$\hat{p}_t - \bar{E} \hat{p}_t = \frac{\Gamma}{1 - \Gamma} (\hat{c}_t - \hat{a}_t) \quad (93)$$

Since we assume that households know  $\hat{p}_{t-1}$ , we have:

$$\begin{aligned} (\hat{p}_t - \hat{p}_{t-1}) - (\bar{E} \hat{p}_t - \hat{p}_{t-1}) &= \frac{\Gamma}{1 - \Gamma} (\hat{c}_t - \hat{a}_t) \\ \hat{\pi}_t - \bar{E} \hat{\pi}_t &= \frac{\Gamma}{1 - \Gamma} (\hat{c}_t - \hat{a}_t) \end{aligned}$$

■

**Dynamic Model without Simplifying Assumptions** Now, we get rid of the simplifying assumptions. I only briefly describes the model. Most of the setup is similar to the model laid out in the main text. There is a continuum of shoppers indexed by  $i \in I$ . In the morning, they make consumption-saving and labor supply decisions. In the afternoon, they go shopping with given consumption expenditure that they have allocated to consumption in the morning.

In the morning, the shopper maximizes the following discounted utility:

$$\begin{aligned} \max_{B_{it}, X_{it}, L_{it}} E_0 \sum_{t=0}^{\infty} \beta^t \left( \log \frac{X_{it}}{P_{kt}} + \frac{1}{\lambda} \epsilon_{ikt} - L_{it} \right) \\ \text{s.t. } X_{it} + B_{it} = W_{it} L_{it} + R_{it-1} B_{it-1} + \Pi_{it} \end{aligned}$$

where  $X_{it}$  is the consumption expenditure left for the shopping in the afternoon. Notice that  $W_{it}$  and  $R_{it}$  are shopper-specific and I assume  $w_{it} = w_t + \zeta_{it}$ ,  $i_{it} = i_t + u_{it}$ ,  $\pi_{it} = \pi_t + v_{it}$ , where  $i_t$  is the log-deviation of  $R_t$  following the convention. These shocks  $\zeta_{it}, u_{it}, v_{it}$  are IID across  $i$  and  $t$ , independent of one another, and independent of any other random variable in the economy. Shocks follow normal distribution with their respective variances. They “noise up” the information that each shopper can extract from the available market signals. I assume that shoppers only treat the

current-period price index  $\hat{p}_t$  as their signal to align with the information structure in the main text. In the afternoon, shoppers have the same search problem. The following proposition characterizes the three-equation system,

**Proposition 12.** *The equilibrium dynamics of  $\{\hat{p}_t, c_t, i_t\}$  is described by the following system of equations:*

$$\begin{aligned}\hat{c}_t &= -\sigma \left\{ \sum_{k=1}^{\infty} \beta^{k-1} \bar{E}_t^s [i_{t+k} - \hat{\pi}_{t+k+1}] \right\} + \frac{1-\beta}{\beta} \left\{ \sum_{k=1}^{\infty} \beta^k \bar{E}_t^s [\hat{c}_{t+k}] \right\} \\ \hat{p}_t - \bar{E}_t^s \hat{p}_t &= \frac{\Gamma}{1-\Gamma} (\hat{c}_t - \hat{a}_t) \\ i_t &= \phi_{\pi} \hat{p}_t + \varepsilon_{mt}\end{aligned}$$

where  $\Gamma$  is the aggregate passthrough.

The first equation represents incomplete-information Euler equation. Under incomplete information, households need to form expectations of future aggregate consumption and inflation, which in turn depends on how other households respond to the shock. This forms a dynamic beauty contest game as described in Angeletos and Lian (2018). The second equation presents the Phillips Curve as in the main text. The third equation represents the price-level targeting rule. It guarantees that this system will converge to its steady state as the shock dissipates. Otherwise, if we use the inflation-targeting rule, the price level will never return to its original value.

### Proof of Proposition 10:

*Proof.* The profit of a firm that has  $N$  products indexed by  $j$  is given by,

$$\pi_k = \frac{1}{\rho} \sum_{j=1}^N \int X(1 - G(\lambda(v^*(x) + p_k))) d\Phi_x(x) \frac{1}{P_{jk}} (P_{jk} - \frac{W}{A_{jk}}) (\frac{P_{jk}}{P_k})^{-\sigma} \quad (94)$$

where  $P_k = (\sum_{j=1}^N P_{jk}^{1-\sigma})^{\frac{1}{1-\sigma}}$ . Denote the total expenditure share on firm  $k$  as  $\omega_k = \omega(P_k)$ , then,

$$\pi_k = \frac{1}{\rho} \sum_{j=1}^N \omega(P_k) \frac{1}{P_{jk}} (P_{jk} - \frac{W}{A_{jk}}) (\frac{P_{jk}}{P_k})^{-\sigma} \quad (95)$$

Firm  $k$  will internalize the effect of change in  $P_{jk}$  on overall price index  $P_k$  of the firm. The first-order condition w.r.t.  $P_{jk}$  is given by,

$$P_{jk} = \mu_k \frac{W}{A_{jk}} = \frac{\sigma}{\sigma - 1 - P_k^{-1} \tilde{\pi}_k (e_k - 1 + \sigma - 1)} \frac{W}{A_{jk}} \quad (96)$$

where  $e_k$  is the same as in (19). Notice that the markup is the same across all the products within the firm. Also, we have  $\tilde{\pi}_k = (1 - \mu_k)P_k$ . Plug in the above equation, we have,

$$\mu_k = \frac{e_k}{e_k - 1} \quad (97)$$

The passthrough of productivity shock to a given product  $j$  is proportional to the expenditure share of this product over all products on the market.

$$\gamma_{jk} = \frac{\omega_{jk}}{\omega_k} \gamma_k \quad (98)$$

Therefore, when  $N = 1$ ,  $\gamma_{jk} = \gamma_k$ ; when  $N \rightarrow \infty$ ,  $\gamma_{jk} \rightarrow 0$ . ■

### Proof of Proposition 11:

*Proof.* I generalize the static general equilibrium model to accommodate finite labor supply elasticity.

Due to finite labor supply elasticity, the nominal wage is now endogenously determined by the labor market clearing. The log-linearized labor supply condition for household  $i$  is  $\eta \hat{l}_i = \hat{w}_i - \hat{x}_i$ . Integrate and get aggregate labor supply,

$$\eta \hat{l} = \hat{w} - \hat{x} \quad (99)$$

The resource constraint is  $C = AL$ . However, the average productivity changes after the shock due to demand reallocation cross firms. For instance, after a monetary shock, shoppers search more actively and are more likely to be captured by the high-productivity and low-price firms. The aggregate productivity is given by,

$$\bar{A} = \left[ \frac{\frac{1}{\exp(a)} \frac{1}{\exp(p(a,w))} \omega(a, w) d\Phi_a(a)}{\frac{1}{\exp(p(a,w))} \omega(a, w) d\Phi_a(a)} \right]^{-1} \quad (100)$$

On the first order, the aggregate productivity has two components. One is the shock to the aggregate productivity and another is the allocation-induced productivity change:

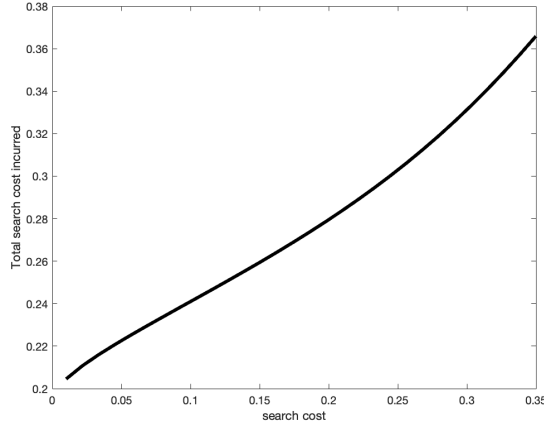
$$\hat{\bar{a}} = \hat{a} + v(\hat{w} - \hat{a})$$

where  $v$  is the first-order effect of change in the nominal wage and aggregate productivity on the aggregate productivity. Therefore, combining resource constraint, we have,

$$\hat{l} = \hat{c} - (\hat{a} + v(\hat{w} - \hat{a})) \quad (101)$$



Figure 7: Total search cost and search cost



*Notes:* The figure plots the total search cost versus the search cost  $\kappa$ .

Combine  $\hat{p} = \Phi(\hat{w} - \hat{a})$  and substitute out  $\hat{w}$ ,

$$\hat{p} = (1 + \eta) \frac{\Phi}{1 + \eta v - \Phi} \left( \hat{c} - \frac{1 + \eta - \eta v}{1 + \eta} \hat{a} \right) \quad (102)$$

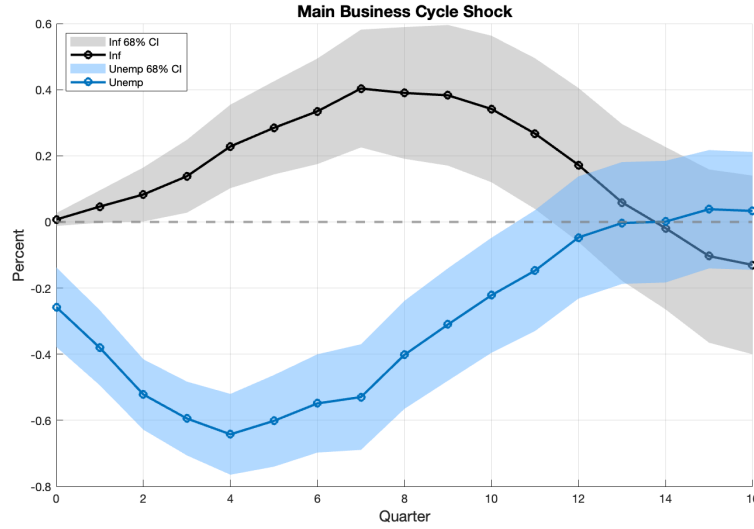
Suppose the effect of demand reallocation is absent, i.e.,  $v = 0$ . Then  $\hat{p} = (1 + \eta) \frac{\Phi}{1 - \Phi} (\hat{c} - \hat{a})$  and the price index response is larger if  $\eta > 0$  because with finite labor elasticity, the real marginal cost increases. Now consider a monetary shock (similarly for a supply shock) with  $v > 0$ . Compared to the  $v = 0$  case, the price index response is smaller because demand reallocation toward high-productivity firms effectively raises aggregate productivity, mitigating the rise in the price index.

■

**Figure 7** — As we see, the total search cost increases with the search cost, even though the average number of searches goes down.

**Figure 8** — I show how inflation and unemployment rate respond to the main business cycle shocks in our sample in Figure 8.

Figure 8: Impulse responses of inflation and Unemployment Rate



*Notes:* The figure plots the impulse responses of unemployment rate and inflation following a main business cycle shock. The sample period is Q3 1979–Q4 2017. The black line represents the impulse responses of inflation and the blue line represents the impulse responses of unemployment rate. The shaded areas are 68% confidence intervals based on heteroskedasticity and autocorrelation robust standard errors and 12 lags. The x-axis denotes months from the shock, starting at 0. The y-axis denotes percent.

## C Empirics on Information Asymmetry

I first show that the main inflation shock exhibits an insignificant negative correlation with inflation in food and drinks. Regressing inflation in food and drinks on the main inflation shocks and four lags of food and drinks inflation over the sample period 1979 Q3 to 2017 Q4 yields a coefficient of -0.12 with a p-value of 0.864. In contrast, using overall inflation instead of food and drinks inflation results in a coefficient of 0.3, which is highly significant. This suggests that the main inflation shocks capture most of the variation in overall inflation but not in the inflation of food and drinks. Therefore, the main inflation shock is not appropriate for our empirical analysis based on NielsenIQ consumer panel.

Now, I show the robust checks if we assume alternative models households use to derive the predicted inflation. Here, I consider the case where households only use 4 lags of inflation in food and drinks to predict inflation. The standard deviation of the unanticipated inflation is 52 bp. The following table shows the result.

Table 5: Non-routine Share of Spending and Unanticipated Inflation

<i>Dep. var.:</i> Non-routine Share	(1)	(2)	(3)	(4)
Unanticipated inflation (F&D)	0.190*** (0.021)		0.181*** (0.021)	0.162*** (0.021)
Unanticipated inflation (overall)		0.075*** (0.017)		
Number of trips			0.033*** (0.002)	-0.028*** (0.003)
Number of distinct stores				0.327*** (0.011)
Observations	2,660,735	2,660,735	2,660,735	2,660,735
Consumer fixed effect	✓	✓	✓	✓
Consumer varying effect	✓	✓	✓	✓

*Notes:* The table reports the estimates in the robustness check. Each observation is at the consumer×quarter level covering from 2006 Q1 to 2019 Q4. The coefficient represents the corresponding change in different measures of search behavior after a standard deviation increase in unanticipated inflation. Consumer fixed and time-varying effects are controlled. Standard errors are clustered at the consumer level. \*Significant at the 10% level; \*\*Significant at the 5% level; \*\*\*Significant at the 1% level.

The table shows that the basic results do not change. The non-routine share of total spending still increases significantly after an unanticipated inflation. After controlling number of trips and number distinct stores, the coefficients only fall a little. The key difference is that now the magnitude of the response is a bit smaller. This can happen when unemployment rates control away some variations that are not related to the change in the search activities.

Now, I consider the case where households use 4 lags of inflation in food and drinks, unemployment rates, 1-year government bond rates. This specification assumes a lot of knowledge about the macro economy households possess. The mean of the residual, measuring the unanticipated inflation, is 2.2 bp, and the standard deviation is 49 bp.

Now the magnitude of responses are much smaller. The 49 bp increase in the unanticipated inflation only triggers 9 bp increase in the non-routine share. It is 2.5 times smaller than our baseline. We should interpret this result as the following. The relatively larger response in the

Table C: Non-routine Share of Spending and Unanticipated Inflation

<i>Dep. var.:</i> Non-routine Share	(1)	(2)	(3)	(4)
Unanticipated inflation (F&D)	0.087*** (0.023)		0.078*** (0.023)	0.057* (0.023)
Unanticipated inflation (overall)		-0.066*** (0.018)		
Number of trips			0.033*** (0.002)	-0.028*** (0.003)
Number of distinct stores				0.328*** (0.011)
Observations	2,660,735	2,660,735	2,660,735	2,660,735
Consumer fixed effect	✓	✓	✓	✓
Consumer varying effect	✓	✓	✓	✓

*Notes:* The table shows the estimates for robustness check. Each observation is at the consumer $\times$ quarter level covering from 2006 Q1 to 2019 Q4. The coefficient represents the corresponding change in different measures of search behavior after a standard deviation increase in unanticipated inflation. Consumer fixed and time-varying effects are controlled. Standard errors are clustered at the consumer level. \*Significant at the 10% level; \*\*Significant at the 5% level; \*\*\*Significant at the 1% level.

baseline result is largely due to the fact that households do not know the government bond rate or the response of the monetary authority. In theory, knowing perfectly the interest rate is sufficient to back out the underlying aggregate shock. However, in reality, households know little about the interest rate as revealed by Michigan survey.