数据分析及实践 _Assignment4

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1 实验要求

利用 Assignment3 得到的与 REPEAT 列最相关的 5 个特征作为特征集,根据关联规则算法,挖掘这 5 个特征和 REPEAT 构成的频繁项集和关联规则。注意事项:

- 数据集中与 REPEAT 列直接相关的三个特征在本次实验中仅允许合为一个特征使用 'ST127Q01TA,ST127Q02TA,ST127Q03TA'
- 需要挖掘的频繁项集的最小支持度阈值为 0.6, 最小置信度阈值为 0.15
- 建议使用的关联规则算法: Apriori 或相关改进算法(自行实现)
- 选择的特征可以是数据集里有的,也可以是自己在实验三中构建的特征

2 实验原理

2.1 3σ 准则

 3σ 准则是一个简单的推论,几乎所有的值都在平均值正负三个标准差的范围内,也就是在实验上可以将 99.7% 的机率视为 "几乎一定"。如果数据不服从正态分布,也可以用远离平均值的多少倍标准差来描述(这就使该原理可以适用于不同的业务场景,只是需要根据经验来确定 k, σ 中的 k 值,这个 k 值就可以认为是阈值)。

$$P(|x - \mu| > 3\sigma) \le 0.003$$

其中, μ 是样本的平均值, σ 是样本的标准差。这个公式表示,对于一个正态分布的样本,它的绝对偏差超过 3 倍标准差的概率小于等于 0.003,也就是说,99.7

2.2 提升度

提升度是一种关联规则中的度量,用于衡量两个事件之间的相关性。提升度 越大,表示两个事件之间的相关性越强。提升度的数学原理可以用下面这个公式 表示:

$$lift(A, B) = \frac{P(A, B)}{P(A)P(B)}$$

其中, A 和 B 是两个事件, P(A) 和 P(B) 分别是 A 和 B 的支持度, P(A,B) 是 A 和 B 同时出现的概率。³

2.3 置信度

置信度是指在统计学中描述概率的另一种方式。例如,使用 0.95 的置信水平构建置信区间,则有信心估计值在置信区间指定的上限和下限值之间的次数为 100 次中的 95 次。

2.4 Apriori 算法

Apriori 算法是经典的挖掘频繁项集和关联规则的数据挖掘算法。A priori 在拉丁语中指"来自以前"。当定义问题时,通常会使用先验知识或者假设,这被称作"一个先验"(a priori)。

Apriori 算法的数学原理如下: 首先, 找出所有频繁项集, 然后由频繁项集产生强关联规则。Apriori 算法的核心是利用了频繁项集的性质, 即频繁项集的所有非空子集也一定是频繁的。

以下是 Apriori 算法的伪代码:

```
Algorithm 1: Apriori 算法

Data: 数据集

Result: 频繁项集
initialization;
k = 1;
F_k = \{i|in \in I, \sigma(\{i\}) \ge N \times minsup\};
repeat

\begin{vmatrix} k = k + 1; \\ C_k = \text{apriori-gen}(F_{k-1}) \text{ for } transaction \in T \text{ do} \end{vmatrix}
\begin{vmatrix} C_t = \text{subset}(C_k, t); \\ \text{for } c \in C_t \text{ do} \\ | \sigma(c) = \sigma(c) + 1 \\ | \text{end} \end{vmatrix}
end
F_k = \{c|c \in C_k, \sigma(c) \ge N \times minsup\};
until F_k = \emptyset;
```

3 实验环境

VSCode + Python 3.9.13

4 实验步骤

4.1 数据转换

参考 Assignment3 的特征相关性,首先抽取实验所需要的 5 个特征以及 REPEAT 列,'ST127Q02TA,ST001D01T,GRADE,ISCEDL,OCOD2,REPEAT'。 根据实验要求,只抽取 REPEAT 列值为 1 的数据,丢弃所有缺失数据。

4.1.1 数据去噪

使用 3σ 准则进行去噪。

4.1.2 数据格式转换

为了将原格式数据转换为 **Apriori** 算法的输入数据,将挑选的 5 个特征的 所有不同的取值均作为不同类别的事件,构建一个列为所有不同事件的矩阵 **R**,若 $\mathbf{R}[i][j]$ 非空,则说明在第 i 次记录中,事件 j 发生了。

4.2 寻找频繁项集和关联规则

使用 **Apriori** 算法寻找频繁项集和关联规则,由于 **OCOD2** 中有许多只出现过一次的值,考虑到计算时间复杂度,分别删去出现频率小于 10,小于 50 的值然后计算频繁项集。

4.2.1 Fre > 10

k=1 的频繁项集

ISCEDL_2.0 REPEAT ST127Q02TA_2.0 ST001D01T_9.0 GRADE -1.0

k=2 的频繁项集	
ISCEDL_2.0	REPEAT
${\tt ISCEDL_2.0}$	ST127Q02TA_2.0
REPEAT	ST127Q02TA_2.0
$ISCEDL_2.0$	$ST001D01T_9.0$
$GRADE\1.0$	$ISCEDL_2.0$
ST001D01T_9.0	REPEAT
$GRADE\1.0$	REPEAT
$GRADE\1.0$	$ST001D01T_9.0$

k=3 的频繁项集		
ISCEDL_2.0	REPEAT	ST127Q02TA_2.0
${\tt ISCEDL_2.0}$	ST001D01T_9.0	REPEAT
$GRADE\1.0$	${\tt ISCEDL_2.0}$	REPEAT
$GRADE\1.0$	${\tt ISCEDL_2.0}$	ST001D01T_9.0
$GRADE\1.0$	ST001D01T_9.0	REPEAT

k=4 的频繁项集			
GRADE1.0	ST001D01T_9.0	ISCEDL_2.0	REPEAT

分别以置信度 conf 和置信度 conf+ 提升度 $Lift=\frac{P(Y|X)}{P(Y)}>1$ 计算关联规则,结果见附录。

$4.2.2 ext{ Fre} > 50$

k=1 的频繁项集

ISCEDL_2.0 REPEAT ST127Q02TA_2.0 ST001D01T_9.0 GRADE_-1.0

k=2 的频繁项集	
ISCEDL_2.0	REPEAT
${\tt ISCEDL_2.0}$	ST127Q02TA_2.0
REPEAT	ST127Q02TA_2.0
${\tt ISCEDL_2.0}$	$ST001D01T_9.0$
$GRADE\1.0$	$ISCEDL_2.0$
ST001D01T_9.0	REPEAT
$GRADE\1.0$	REPEAT
$GRADE\1.0$	$ST001D01T_9.0$

k=3 的频繁项集		
ISCEDL_2.0	REPEAT	ST127Q02TA_2.0
${\tt ISCEDL_2.0}$	ST001D01T_9.0	REPEAT
$GRADE\1.0$	${\tt ISCEDL_2.0}$	REPEAT
$GRADE\1.0$	${\tt ISCEDL_2.0}$	ST001D01T_9.0
$GRADE\1.0$	ST001D01T_9.0	REPEAT

k=4 的频繁项集			
GRADE1.0	ST001D01T_9.0	ISCEDL_2.0	REPEAT

分别以置信度 conf 和置信度 conf+ 提升度 $Lift = \frac{P(Y|X)}{P(Y)} > 1$ 计算关联规则,结果见附录。

5 总结

每个特征的大致含义如下:

- REPEAT: 是否留级过
- GRADE: 所在年级是否滞后与同龄人
- ST127Q02TA: 留级的次数
- ST001D01T: 学生年级
- ISCEDL: 学生学段
- OCOD2: 父亲的职业

通过观察频繁项集与关联规则, 发现

- 1. 清洗后的数据中复读的学生均为初中生。
- 2. 九年级的学生与复读具有强相关性
- 3. 九年级的学生大部分只留级过一次。
- 4. 去除低频项的阈值大小与结果几乎无关,父亲职业相对于其他特征对复读 影响较小。

根据分析结果以及现实生活中对上述特征的经验,推测实验结果是合理的。

5.1 探索性分析(附录 6.3)

• 探索对于国家与上述特征的关联规则,除了满足上述规则以外,发现西班牙的学生与留级,并且留级两次强相关。

- 只考虑巴拿马与上述特征的关联规则,除了满足上述规则以外,发现巴拿 马的学生在年级低于同龄人一年时留级过两次,推测留级可能是超前学习 导致的。
- 只考虑墨西哥与上述特征的关联规则,基本满足上述规则
- 值考虑西班牙与上述特征的关联规则,除了满足上述规则以外,发现西班 牙的学生在年级低于同龄人一年时留级过两次,推测留级可能是超前学习 导致的。

6 附录

6.1 Fre > 10 的数据关联规则

6.1.1 只考虑 conf 的关联规则

ISCEDL 2.0-> REPEAT

together support: 1.0, conf: 1.0, lift: 1.0

REPEAT-> ISCEDL 2.0

together support: 1.0, conf: 1.0, lift: 1.0

 $ISCEDL_2.0 -> ST127Q02TA_2.0$

together support: 0.752, conf: 0.752, lift: 1.0

ST127Q02TA 2.0-> ISCEDL 2.0

together support: 0.752, conf: 1.0, lift: 1.0

REPEAT-> ST127Q02TA_2.0

together support: 0.752, conf: 0.752, lift: 1.0

 $ST127Q02TA_2.0-> REPEAT$

together support: 0.752, conf: 1.0, lift: 1.0

ST001D01T 9.0-> ISCEDL 2.0

together support: 0.776, conf: 1.0, lift: 1.0

 $ISCEDL_2.0-> ST001D01T_9.0$

together support: 0.776, conf: 0.776, lift: 1.0

ISCEDL 2.0-> GRADE -1.0

together support: 0.776, conf: 0.776, lift: 1.0

 $GRADE_-1.0->ISCEDL_2.0$

together support: 0.776, conf: 1.0, lift: 1.0

ST001D01T 9.0-> REPEAT

together support: 0.776, conf: 1.0, lift: 1.0

REPEAT-> ST001D01T 9.0

together support: 0.776, conf: 0.776, lift: 1.0

 $GRADE_-1.0-> REPEAT$

together support: 0.776, conf: 1.0, lift: 1.0

REPEAT \rightarrow GRADE -1.0

together support: 0.776, conf: 0.776, lift: 1.0

 $ST001D01T_9.0-> GRADE_-1.0$

together support: 0.776, conf: 1.0, lift: 1.289

 $GRADE_{-1.0} > ST001D01T_{-9.0}$

together support: 0.776, conf: 1.0, lift: 1.289

 $ISCEDL_2.0 \rightarrow REPEAT, ST127Q02TA_2.0$

together support: 0.752, conf: 0.752, lift: 1.0

REPEAT-> ISCEDL $_2.0$, ST127Q02TA $_2.0$

together support: 0.752, conf: 0.752, lift: 1.0

ST127Q02TA_2.0-> ISCEDL_2.0, REPEAT

together support: 0.752, conf: 1.0, lift: 1.0

ST001D01T 9.0-> ISCEDL 2.0, REPEAT

together support: 0.776, conf: 1.0, lift: 1.0

ISCEDL 2.0-> ST001D01T 9.0,REPEAT

together support: 0.776, conf: 0.776, lift: 1.0

REPEAT-> ST001D01T 9.0,ISCEDL 2.0

together support: 0.776, conf: 0.776, lift: 1.0

GRADE -1.0-> ISCEDL 2.0, REPEAT

together support: 0.776, conf: 1.0, lift: 1.0

ISCEDL 2.0-> GRADE -1.0, REPEAT

together support: 0.776, conf: 0.776, lift: 1.0

REPEAT-> ISCEDL 2.0,GRADE -1.0

together support: 0.776, conf: 0.776, lift: 1.0

 $ST001D01T_9.0 -> ISCEDL_2.0, GRADE_-1.0$

together support: 0.776, conf: 1.0, lift: 1.289

ISCEDL_2.0-> ST001D01T_9.0,GRADE_-1.0

together support: 0.776, conf: 0.776, lift: 1.0

GRADE_-1.0-> ST001D01T_9.0,ISCEDL_2.0

together support: 0.776, conf: 1.0, lift: 1.289

GRADE_-1.0-> ST001D01T_9.0,REPEAT

together support: 0.776, conf: 1.0, lift: 1.289

ST001D01T 9.0-> GRADE -1.0, REPEAT

together support: 0.776, conf: 1.0, lift: 1.289

REPEAT-> ST001D01T 9.0,GRADE -1.0

together support: 0.776, conf: 0.776, lift: 1.0

ISCEDL_2.0-> REPEAT,ST001D01T_9.0,GRADE_-1.0

together support: 0.776, conf: 0.776, lift: 1.0

REPEAT-> ST001D01T_9.0,ISCEDL_2.0,GRADE_-1.0

together support: 0.776, conf: 0.776, lift: 1.0

GRADE_-1.0-> ST001D01T__9.0,ISCEDL__2.0,REPEAT

together support: 0.776, conf: 1.0, lift: 1.289

ST001D01T_9.0-> REPEAT, ISCEDL_2.0, GRADE_-1.0

together support: 0.776, conf: 1.0, lift: 1.289

6.1.2 同时考虑 conf 和 Lift 的关联规则

GRADE -1.0 -> ST001D01T 9.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T_{9.0} -> GRADE_{-1.0}$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE -1.0 -> ST001D01T 9.0,ISCEDL 2.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T_9.0 -> GRADE_{-1.0,ISCEDL_{-2.0}}$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE -1.0 -> REPEAT, ST001D01T 9.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T 9.0 \rightarrow REPEAT,GRADE -1.0$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE $-1.0 \rightarrow REPEAT,ST001D01T 9.0,ISCEDL 2.0$

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T 9.0 \rightarrow REPEAT,GRADE -1.0,ISCEDL 2.0$

together support: 0.776, conf: 1.0, lift: 1.289

6.2 Fre > 50 的数据关联规则

6.2.1 只考虑 conf 的关联规则

 $ISCEDL_2.0 \rightarrow REPEAT$

together support: 1.0, conf: 1.0

REPEAT -> ISCEDL_2.0

together support: 1.0, conf: 1.0

 $ISCEDL_2.0 \rightarrow ST127Q02TA_2.0$

together support: 0.752, conf: 0.752

ST127Q02TA 2.0 -> ISCEDL 2.0

together support: 0.752, conf: 1.0

REPEAT \rightarrow ST127Q02TA 2.0

together support: 0.752, conf: 0.752

ST127Q02TA 2.0 -> REPEAT

together support: 0.752, conf: 1.0

ISCEDL $2.0 \rightarrow ST001D01T 9.0$

together support: 0.776, conf: 0.776

 $ST001D01T_9.0 \rightarrow ISCEDL_2.0$

together support: 0.776, conf: 1.0

GRADE $-1.0 \rightarrow ISCEDL 2.0$

together support: 0.776, conf: 1.0

 $ISCEDL_2.0 \rightarrow GRADE_-1.0$

together support: 0.776, conf: 0.776

 $ST001D01T 9.0 \rightarrow REPEAT$

together support: 0.776, conf: 1.0

REPEAT -> ST001D01T 9.0

together support: 0.776, conf: 0.776

GRADE $-1.0 \rightarrow REPEAT$

together support: 0.776, conf: 1.0

REPEAT -> GRADE -1.0

together support: 0.776, conf: 0.776

 $GRADE_-1.0 -> ST001D01T_9.0$

together support: 0.776, conf: 1.0

 $ST001D01T_9.0 -> GRADE_-1.0$

together support: 0.776, conf: 1.0

ISCEDL $2.0 \rightarrow REPEAT,ST127Q02TA$ 2.0

together support: 0.752, conf: 0.752

 $REPEAT \rightarrow ISCEDL_2.0,ST127Q02TA_2.0$

together support: 0.752, conf: 0.752

ST127Q02TA 2.0 -> ISCEDL 2.0, REPEAT

together support: 0.752, conf: 1.0

ISCEDL $2.0 \rightarrow ST001D01T$ 9.0,REPEAT

together support: 0.776, conf: 0.776

ST001D01T $9.0 \rightarrow ISCEDL 2.0, REPEAT$

together support: 0.776, conf: 1.0

REPEAT \rightarrow ISCEDL 2.0,ST001D01T 9.0

together support: 0.776, conf: 0.776

 $GRADE_-1.0 -> ISCEDL_2.0, REPEAT$

together support: 0.776, conf: 1.0

ISCEDL 2.0 -> GRADE -1.0,REPEAT

together support: 0.776, conf: 0.776

 $REPEAT \rightarrow GRADE_-1.0,ISCEDL_2.0$

together support: 0.776, conf: 0.776

GRADE -1.0 -> ISCEDL 2.0,ST001D01T 9.0

together support: 0.776, conf: 1.0

 $ISCEDL_2.0 -> GRADE_{-1.0,ST001D01T_{-9.0}}$

together support: 0.776, conf: 0.776

ST001D01T 9.0 -> GRADE -1.0,ISCEDL 2.0

together support: 0.776, conf: 1.0

 $GRADE_-1.0 -> ST001D01T_9.0,REPEAT$

together support: 0.776, conf: 1.0

 $ST001D01T_9.0 -> GRADE_-1.0, REPEAT$

together support: 0.776, conf: 1.0

REPEAT \rightarrow GRADE -1.0,ST001D01T 9.0

together support: 0.776, conf: 0.776

 $GRADE_-1.0 \rightarrow ISCEDL_2.0,ST001D01T_9.0,REPEAT$

together support: 0.776, conf: 1.0

ST001D01T 9.0 -> GRADE -1.0,ISCEDL 2.0,REPEAT

together support: 0.776, conf: 1.0

ISCEDL_2.0 -> GRADE_-1.0,ST001D01T_9.0,REPEAT

together support: 0.776, conf: 0.776

 $REPEAT -> GRADE_-1.0, ISCEDL_2.0, ST001D01T_9.0$

together support: 0.776, conf: 0.776

6.2.2 同时考虑 conf 和 Lift 的关联规则

GRADE -1.0 -> ST001D01T 9.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T_9.0 -> GRADE_-1.0$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE -1.0 -> ST001D01T 9.0,ISCEDL 2.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T 9.0 \rightarrow GRADE -1.0,ISCEDL 2.0$

together support: 0.776, conf: 1.0, lift: 1.289

 $GRADE_-1.0 \rightarrow REPEAT,ST001D01T_9.0$

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T 9.0 \rightarrow REPEAT,GRADE -1.0$

together support: 0.776, conf: 1.0, lift: 1.289

 $GRADE_-1.0 -> REPEAT,ST001D01T_9.0,ISCEDL_2.0$

together support: 0.776, conf: 1.0, lift: 1.289

ST001D01T 9.0 -> REPEAT, GRADE -1.0, ISCEDL 2.0

together support: 0.776, conf: 1.0, lift: 1.289

6.3 考虑 CNTRYID 的关联规则

6.3.1 全部 CNTRYID-同时考虑 conf 和 Lift 的关联规则

 $ST001D01T_{9.0} -> GRADE_{-1.0}$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE -1.0 -> ST001D01T 9.0

together support: 0.776, conf: 1.0, lift: 1.289

ST127Q02TA 2.0 -> CNTRYID 724.0

together support: 0.67, conf: 0.891, lift: 1.04

 $CNTRYID_724.0 \longrightarrow ST127Q02TA_2.0$

together support: 0.67, conf: 0.782, lift: 1.04

ST001D01T 9.0 -> CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

 $CNTRYID_{724.0} -> ST001D01T_{9.0}$

together support: 0.666, conf: 0.777, lift: 1.002

GRADE $-1.0 \rightarrow \text{CNTRYID} 724.0$

together support: 0.666, conf: 0.858, lift: 1.002

 $CNTRYID_{724.0} \rightarrow GRADE_{-1.0}$

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T 9.0 -> ISCEDL 2.0,GRADE -1.0

together support: 0.776, conf: 1.0, lift: 1.289

GRADE -1.0 -> ST001D01T 9.0,ISCEDL 2.0

together support: 0.776, conf: 1.0, lift: 1.289

 $ST001D01T_9.0 \rightarrow REPEAT,GRADE_{-1.0}$

together support: 0.776, conf: 1.0, lift: 1.289

 $GRADE_-1.0 \rightarrow ST001D01T_9.0,REPEAT$

together support: 0.776, conf: 1.0, lift: 1.289

ST127Q02TA 2.0 -> ISCEDL 2.0, CNTRYID 724.0

together support: 0.67, conf: 0.891, lift: 1.04

CNTRYID_724.0 -> ISCEDL_2.0,ST127Q02TA_2.0

together support: 0.67, conf: 0.782, lift: 1.04

ST127Q02TA 2.0 -> REPEAT, CNTRYID 724.0

together support: 0.67, conf: 0.891, lift: 1.04

 $CNTRYID_{724.0} \rightarrow REPEAT,ST127Q02TA_{2.0}$

together support: 0.67 , conf: 0.782 , lift: 1.04

ST001D01T 9.0 -> ISCEDL 2.0, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

 $CNTRYID_{724.0} -> ST001D01T_{9.0,ISCEDL_{2.0}}$

together support: 0.666, conf: 0.777, lift: 1.002

GRADE -1.0 -> ISCEDL 2.0, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

CNTRYID 724.0 -> ISCEDL 2.0,GRADE -1.0

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T 9.0 -> REPEAT, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

CNTRYID 724.0 -> ST001D01T 9.0, REPEAT

together support: 0.666, conf: 0.777, lift: 1.002

GRADE -1.0 -> REPEAT, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

 $CNTRYID_{724.0} \rightarrow REPEAT,GRADE_{-1.0}$

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T_9.0 -> GRADE_-1.0,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.289

GRADE_-1.0 -> ST001D01T_9.0,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.289

CNTRYID 724.0 -> ST001D01T 9.0,GRADE -1.0

together support: 0.666, conf: 0.777, lift: 1.002

 $ST001D01T_9.0 \rightarrow ISCEDL_2.0, REPEAT, GRADE_-1.0$

together support: 0.776, conf: 1.0, lift: 1.289

GRADE $-1.0 \rightarrow ST001D01T$ 9.0,ISCEDL 2.0,REPEAT

together support: 0.776, conf: 1.0, lift: 1.289

CNTRYID 724.0 -> ISCEDL 2.0, REPEAT, ST127Q02TA 2.0

together support: 0.67, conf: 0.782, lift: 1.04

ST127Q02TA_2.0 -> ISCEDL_2.0,REPEAT,CNTRYID_724.0

together support: 0.67, conf: 0.891, lift: 1.04

CNTRYID 724.0 -> ST001D01T 9.0,ISCEDL 2.0,REPEAT

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T 9.0 -> ISCEDL 2.0, REPEAT, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.002

CNTRYID 724.0 -> ISCEDL 2.0, REPEAT, GRADE -1.0

together support: 0.666, conf: 0.777, lift: 1.002

GRADE_-1.0 -> ISCEDL_2.0,REPEAT,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.002

CNTRYID 724.0 -> ST001D01T 9.0,ISCEDL 2.0,GRADE -1.0

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T 9.0 -> ISCEDL 2.0,GRADE -1.0,CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.289

GRADE_-1.0 -> ST001D01T_9.0,ISCEDL_2.0,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.289

CNTRYID $724.0 \rightarrow ST001D01T$ 9.0,REPEAT,GRADE -1.0

together support: 0.666, conf: 0.777, lift: 1.002

 $ST001D01T_9.0 \rightarrow REPEAT,GRADE_-1.0,CNTRYID$ 724.0

together support: 0.666, conf: 0.858, lift: 1.289

GRADE_-1.0 -> ST001D01T_9.0,REPEAT,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.289

 $CNTRYID_{724.0} -> ST001D01T_{9.0,ISCEDL_{2.0,REPEAT,GRADE_{-1.0}}$

together support: 0.666, conf: 0.777, lift: 1.002

ST001D01T 9.0 -> ISCEDL 2.0, REPEAT, GRADE -1.0, CNTRYID 724.0

together support: 0.666, conf: 0.858, lift: 1.289

GRADE_-1.0 -> ST001D01T_9.0,ISCEDL_2.0,REPEAT,CNTRYID_724.0

together support: 0.666, conf: 0.858, lift: 1.289

6.3.2 CNTRYID591.0-同时考虑 conf 和 Lift 的关联规则

 $ST001D01T_9.0 -> ST127Q02TA_2.0$

together support: 0.612, conf: 0.771, lift: 1.086

ST127Q02TA 2.0 -> ST001D01T 9.0

together support: 0.612, conf: 0.862, lift: 1.086

 $ST127Q02TA_2.0 -> GRADE_-1.0$

together support: 0.612, conf: 0.862, lift: 1.086

 $\label{eq:grade} \text{GRADE_-1.0} -> \text{ST127Q02TA_2.0}$

together support: 0.612, conf: 0.771, lift: 1.086

 $ST001D01T_{9.0} -> GRADE_{-1.0}$

together support: 0.793, conf: 1.0, lift: 1.261

GRADE -1.0 -> ST001D01T 9.0

together support: 0.793, conf: 1.0, lift: 1.261

ST001D01T 9.0 -> ST127Q02TA 2.0,GRADE -1.0

together support: 0.612, conf: 0.771, lift: 1.261

 $ST127Q02TA_2.0 -> ST001D01T_9.0,GRADE_-1.0$

together support: 0.612, conf: 0.862, lift: 1.086

GRADE -1.0 -> ST001D01T 9.0,ST127Q02TA 2.0

together support: 0.612, conf: 0.771, lift: 1.261

 $ST001D01T_9.0 -> ST127Q02TA_2.0,ISCEDL_2.0$

together support: 0.612, conf: 0.771, lift: 1.086

 $ST127Q02TA_2.0 -> ST001D01T_9.0,ISCEDL_2.0$

together support: 0.612, conf: 0.862, lift: 1.086

ST001D01T 9.0 -> ST127Q02TA 2.0,REPEAT

together support: 0.612, conf: 0.771, lift: 1.086

 $ST127Q02TA_2.0 -> ST001D01T_9.0,REPEAT$

together support: 0.612, conf: 0.862, lift: 1.086

 $ST127Q02TA_2.0 \rightarrow GRADE_-1.0,ISCEDL_2.0$

together support: 0.612, conf: 0.862, lift: 1.086

 $GRADE_-1.0 \rightarrow ST127Q02TA_2.0,ISCEDL_2.0$

together support: 0.612, conf: 0.771, lift: 1.086

ST127Q02TA 2.0 -> GRADE -1.0, REPEAT

together support: 0.612, conf: 0.862, lift: 1.086

 $GRADE_-1.0 \longrightarrow ST127Q02TA_2.0,REPEAT$

together support: 0.612, conf: 0.771, lift: 1.086

 $ST001D01T_9.0 \rightarrow GRADE_-1.0,ISCEDL_2.0$

together support: 0.793, conf: 1.0, lift: 1.261

 $\label{eq:grade} \text{GRADE_-1.0} -> \text{ST001D01T_9.0,ISCEDL_2.0}$

together support: 0.793, conf: 1.0, lift: 1.261

 $ST001D01T_9.0 \rightarrow GRADE_{-1.0,REPEAT}$

together support: 0.793, conf: 1.0, lift: 1.261

GRADE -1.0 -> ST001D01T 9.0,REPEAT

together support: 0.793, conf: 1.0, lift: 1.261

ST001D01T 9.0 -> ST127Q02TA 2.0,GRADE -1.0,ISCEDL 2.0

together support: 0.612, conf: 0.771, lift: 1.261

ST127Q02TA 2.0 -> ST001D01T 9.0,GRADE -1.0,ISCEDL 2.0

together support: 0.612, conf: 0.862, lift: 1.086

GRADE -1.0 -> ST001D01T 9.0,ST127Q02TA 2.0,ISCEDL 2.0

together support: 0.612, conf: 0.771, lift: 1.261

ST001D01T 9.0 -> ST127Q02TA 2.0,REPEAT,GRADE -1.0

together support: 0.612, conf: 0.771, lift: 1.261

ST127Q02TA_2.0 -> ST001D01T_9.0,GRADE_-1.0,REPEAT

together support: 0.612, conf: 0.862, lift: 1.086

GRADE_-1.0 -> ST001D01T_9.0,ST127Q02TA_2.0,REPEAT

together support: 0.612, conf: 0.771, lift: 1.261

ST001D01T 9.0 -> ST127Q02TA 2.0, REPEAT, ISCEDL 2.0

together support: 0.612, conf: 0.771, lift: 1.086

 $ST127Q02TA_2.0 -> ST001D01T_9.0, REPEAT, ISCEDL_2.0$

together support: 0.612, conf: 0.862, lift: 1.086

ST127Q02TA 2.0 -> GRADE -1.0, REPEAT, ISCEDL 2.0

together support: 0.612, conf: 0.862, lift: 1.086

GRADE $-1.0 \rightarrow ST127Q02TA$ 2.0, REPEAT, ISCEDL 2.0

together support: 0.612, conf: 0.771, lift: 1.086

 $ST001D01T_9.0 \rightarrow GRADE_{-1.0}$, REPEAT, ISCEDL_2.0

together support: 0.793, conf: 1.0, lift: 1.261

 $\label{eq:grade} GRADE_\text{-}1.0 -> ST001D01T_9.0, REPEAT, ISCEDL_2.0$

together support: 0.793, conf: 1.0, lift: 1.261

ST001D01T_9.0 -> ST127Q02TA_2.0,REPEAT,ISCEDL_2.0,GRADE_-1.0

together support: 0.612, conf: 0.771, lift: 1.261

ST127Q02TA 2.0 -> ST001D01T 9.0,GRADE -1.0,REPEAT,ISCEDL 2.0

together support: 0.612, conf: 0.862, lift: 1.086

GRADE_-1.0 -> ST001D01T_9.0,ST127Q02TA_2.0,REPEAT,ISCEDL_2.0

together support: 0.612, conf: 0.771, lift: 1.261

6.3.3 CNTRYID724.0-同时考虑 conf 和 Lift 的关联规则

 $ST127Q02TA_2.0 -> ST001D01T_9.0$

together support: 0.619, conf: 0.792, lift: 1.018

ST001D01T 9.0 -> ST127Q02TA 2.0

together support: 0.619, conf: 0.797, lift: 1.018

 $ST127Q02TA_2.0 -> GRADE_-1.0$

together support: 0.619, conf: 0.792, lift: 1.018

GRADE -1.0 -> ST127Q02TA 2.0

together support: 0.619, conf: 0.797, lift: 1.018

ST001D01T 9.0 -> GRADE -1.0

together support: 0.777, conf: 1.0, lift: 1.286

 $GRADE_{-1.0} -> ST001D01T_{-9.0}$

together support: 0.777, conf: 1.0, lift: 1.286

ST127Q02TA 2.0 -> ST001D01T 9.0,GRADE -1.0

together support: 0.619, conf: 0.792, lift: 1.018

ST001D01T 9.0 -> ST127Q02TA 2.0,GRADE -1.0

together support: 0.619, conf: 0.797, lift: 1.286

 $GRADE_-1.0 -> ST127Q02TA_2.0,ST001D01T_9.0$

together support: 0.619, conf: 0.797, lift: 1.286

ST127Q02TA_2.0 -> ST001D01T_9.0,ISCEDL_2.0

together support: 0.619, conf: 0.792, lift: 1.018

ST001D01T 9.0 -> ST127Q02TA 2.0,ISCEDL 2.0

together support: 0.619, conf: 0.797, lift: 1.018

 $ST127Q02TA_2.0 -> ST001D01T_9.0,REPEAT$

together support: 0.619, conf: 0.792, lift: 1.018

ST001D01T 9.0 -> ST127Q02TA 2.0,REPEAT

together support: 0.619, conf: 0.797, lift: 1.018

ST127Q02TA 2.0 -> GRADE -1.0,ISCEDL 2.0

together support: 0.619, conf: 0.792, lift: 1.018

GRADE -1.0 -> ST127Q02TA 2.0,ISCEDL 2.0

together support: 0.619, conf: 0.797, lift: 1.018

ST127Q02TA 2.0 -> GRADE -1.0, REPEAT

together support: 0.619, conf: 0.792, lift: 1.018

GRADE $-1.0 \rightarrow ST127Q02TA$ 2.0,REPEAT

together support: 0.619, conf: 0.797, lift: 1.018

ST001D01T 9.0 -> GRADE -1.0,ISCEDL 2.0

together support: 0.777, conf: 1.0, lift: 1.286

 $GRADE_-1.0 -> ST001D01T_9.0,ISCEDL_2.0$

together support: 0.777, conf: 1.0, lift: 1.286

 $ST001D01T 9.0 \rightarrow GRADE -1.0, REPEAT$

together support: 0.777, conf: 1.0, lift: 1.286

 $GRADE_-1.0 \rightarrow ST001D01T_9.0,REPEAT$

together support: 0.777, conf: 1.0, lift: 1.286

ST001D01T 9.0 -> ST127Q02TA 2.0,GRADE -1.0,ISCEDL 2.0

together support: 0.619, conf: 0.797, lift: 1.286

ST127Q02TA 2.0 -> ST001D01T 9.0,ISCEDL 2.0,GRADE -1.0

together support: 0.619, conf: 0.792, lift: 1.018

 $GRADE_-1.0 -> ST127Q02TA_2.0,ST001D01T_9.0,ISCEDL_2.0$

together support: 0.619, conf: 0.797, lift: 1.286

ST001D01T 9.0 -> ST127Q02TA 2.0,GRADE -1.0,REPEAT

together support: 0.619, conf: 0.797, lift: 1.286

ST127Q02TA_2.0 -> ST001D01T_9.0,GRADE_-1.0,REPEAT

together support: 0.619, conf: 0.792, lift: 1.018

 $GRADE_-1.0 -> ST127Q02TA_2.0,ST001D01T_9.0,REPEAT$

together support: 0.619, conf: 0.797, lift: 1.286

 $ST001D01T_9.0 -> ST127Q02TA_2.0,ISCEDL_2.0,REPEAT$

together support: 0.619, conf: 0.797, lift: 1.018

 $ST127Q02TA_2.0 -> ST001D01T_9.0,ISCEDL_2.0,REPEAT$

together support: 0.619, conf: 0.792, lift: 1.018

ST127Q02TA 2.0 -> REPEAT,GRADE -1.0,ISCEDL 2.0

together support: 0.619, conf: 0.792, lift: 1.018

 $GRADE_-1.0 -> ST127Q02TA_2.0,ISCEDL_2.0,REPEAT$

together support: 0.619, conf: 0.797, lift: 1.018

ST001D01T 9.0 -> GRADE -1.0,ISCEDL 2.0,REPEAT

together support: 0.777, conf: 1.0, lift: 1.286

GRADE $-1.0 \rightarrow ST001D01T$ 9.0,ISCEDL 2.0,REPEAT

together support: 0.777, conf: 1.0, lift: 1.286

ST127Q02TA 2.0 -> ST001D01T 9.0,GRADE -1.0,ISCEDL 2.0,REPEAT

together support: 0.619, conf: 0.792, lift: 1.018

GRADE_-1.0 -> ST127Q02TA_2.0,ST001D01T_9.0,ISCEDL_2.0,REPEAT

together support: 0.619, conf: 0.797, lift: 1.286

ST001D01T_9.0 -> ST127Q02TA_2.0,GRADE_-1.0,ISCEDL_2.0,REPEAT

together support: 0.619, conf: 0.797, lift: 1.286

6.3.4 CNTRYID484.0-同时考虑 conf 和 Lift 的关联规则

ST001D01T_9.0 -> GRADE_-1.0 together support: 0.857 , conf: 1.0 , lift: 1.167

GRADE -1.0 -> ST001D01T 9.0

together support: 0.857 , conf: 1.0 , lift: 1.167

 $ST001D01T_9.0 -> GRADE_-1.0,ISCEDL_2.0$

together support: 0.857, conf: 1.0, lift: 1.167

 $GRADE_-1.0 -> ST001D01T_9.0, ISCEDL_2.0$

together support: 0.857, conf: 1.0, lift: 1.167

 $ST001D01T_9.0 \rightarrow GRADE_-1.0,REPEAT$

together support: 0.857, conf: 1.0, lift: 1.167

 $GRADE_-1.0 -> ST001D01T_9.0,REPEAT$

together support: 0.857, conf: 1.0, lift: 1.167

ST001D01T $9.0 \rightarrow GRADE -1.0, REPEAT, ISCEDL 2.0$

together support: 0.857, conf: 1.0, lift: 1.167

GRADE $-1.0 \rightarrow ST001D01T$ 9.0, REPEAT, ISCEDL 2.0

together support: 0.857, conf: 1.0, lift: 1.167

6.3.5 CNTRYID152.0-同时考虑 conf 和 Lift 的关联规则

数据量过少无法产生关联规则。

6.3.6 CNTRYID214.0 -同时考虑 conf 和 Lift 的关联规则

数据量过少无法产生关联规则。