

1. (a) **Solution:**

The number of users should be a poisson distribution which is

$X \sim Poi(\lambda)$ where $\lambda = 5.5$

The probability that more than 7 users will sign-up for the social networking site in the next minute is

$$P(E) = 1 - P(E^c) = 1 - P\{X \leq 7\} = 1 - \sum_{i=0}^7 \frac{e^{-5.5} 5.5^i}{i!}$$

Answer:

We can also use normal distribution to approximate the probability

$$P\{X > 7\} = 1 - \Phi\left(\frac{7-5.5}{\sqrt{5.5}}\right) = 1 - 0.7389 = 0.2611$$

(b) **Answer:**

The probability that more than 13 users will sign-up for the social networking site in the next 2 minute is

$$P\{X > 13\} = 1 - P\{X \leq 13\} = 1 - \Phi\left(\frac{13-5.5 \times 2}{\sqrt{5.5 \times 2}}\right) = 1 - 0.7257 = 0.2743$$

(c) **Answer:**

The probability that more than 15 users will sign-up for the social networking site in the next 3 minute is

$$P\{X > 15\} = 1 - P\{X \leq 15\} = 1 - \Phi\left(\frac{15-5.5 \times 3}{\sqrt{5.5 \times 3}}\right) = \Phi(0.3693) = 0.6433$$

2.

I found there were some mistake in the question 12.b and updated my answers in the night of 5/3.