

# Effect of Sample Size on Kernel Deep Neural Network

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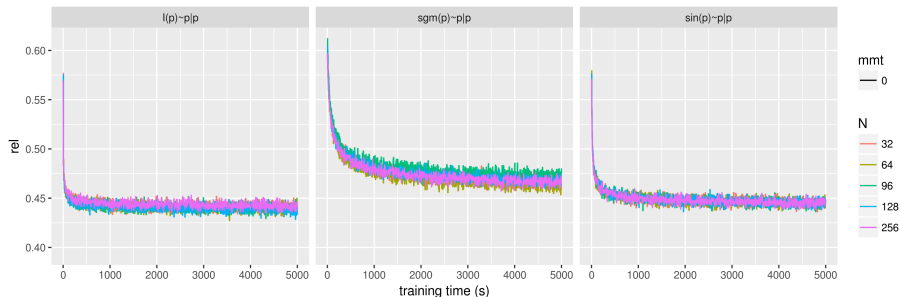
# EXP 01: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

## Simulation Settings:

- $N = \{32, 64, 96, 128, 256\}$
- $P=2000$ ,  $\text{FRQ}=0.50$ ,  $\phi=2.0$
- $\text{link}(h) = \{I, \text{sigmoid}, \sin\}$
- Number of Hidden Units = 96
- True Model:  $y \sim \mathcal{N}(0, X'X + \phi I)$
- Batch Size = 16
- learning rate =  $6.4\text{e-}4$ , Momentum = 0.0
- Reserved Time = 2 hours, Reserved Iteration =  $\infty$
- No random seed.

# EXP 01: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

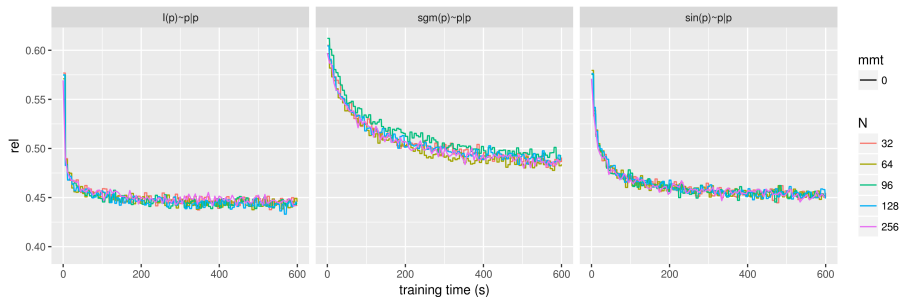
## Performance by Time, till finish:



- y-axis: evaluation error ( $H=256$ ) relative to NULL model.
- no significant performance differentiation between choice of sample sizes.

# EXP 01: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

## Performance by Time, first 10 min:



- y-axis: evaluation error ( $H=256$ ) relative to NULL model.
- no significant performance difference among choices of sample size.

## EXP 01: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

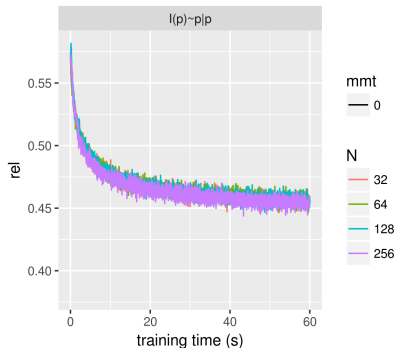
### Evaluation error at Finish:

	N	P	H	frq	ycv	lnk	PHI	bsz	M	err	rep
1	32	2000	256	0.50	p	l	2	16	96	0.92	49
2	64	2000	256	0.50	p	l	2	16	96	0.90	49
3	96	2000	256	0.50	p	l	2	16	96	0.91	50
4	128	2000	256	0.50	p	l	2	16	96	0.90	49
5	256	2000	256	0.50	p	l	2	16	96	0.90	48

- no significant performance difference among choices of sample size;
- smaller batch improves stability.

## EXP 02: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

Performance by Time, first 1 min, finner recording:



- y-axis: evaluation error ( $H=256$ ) relative to NULL model.
- no significantly different performance by varying sample sizes.

## EXP 01: Tied Weight, $h(\text{linear}) \sim \text{linear}|\text{linear}$

**Evaluation error at Finish, finner recording:**

	N	P	H	frq	ycv	lnk	PHI	bsz	M	mu	rep
1	32	2000	256	0.50	p	l	2	16	96	0.92	49
2	64	2000	256	0.50	p	l	2	16	96	0.90	49
3	96	2000	256	0.50	p	l	2	16	96	0.91	50
4	128	2000	256	0.50	p	l	2	16	96	0.90	49
5	256	2000	256	0.50	p	l	2	16	96	0.90	48

- no significant performance difference among choice of sample sizes;



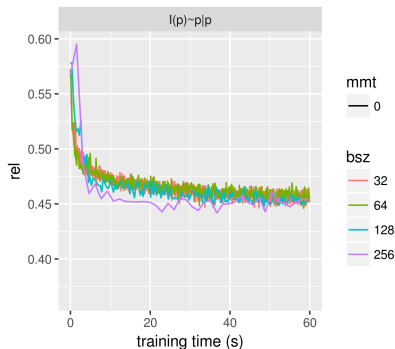
# EXP 01: Tied Weight, $hlinear \sim linear|linear$

## Simulation Settings:

- $N = 256, H=256$
- $P=2000, FRQ=0.50, \phi=2.0$
- $\text{link}(h) = I$
- Number of Hidden Units = 96
- True Model:  $y \sim \mathcal{N}(0, X'X + \phi I)$
- Batch Size =  $\{32, 64, 128, 256\}$
- learning rate =  $\{6.4e-4, 3.2e-4, 1.6e-4, 8.0e-5\}$
- Momentum = 0.0
- Reserved Time = 2 hours, Reserved Iteration =  $\infty$
- No random seed.

# EXP 01: Tied Weight, $hlinear \sim linear|linear$

## Performance by Time, first 1 min:



- y-axis: evaluation error ( $H=256$ ) relative to NULL model
- larger batch may converge better at the beginning.

## EXP 01: Tied Weight, *hlinear* $\sim$ *linear*|*linear*

### Performance at Finish:

	N	P	H	frq	ycv	lnk	PHI	bsz	M	mu	rep
1	256	2000	256	0.50	p	l	2	32	96	0.90	46
2	256	2000	256	0.50	p	l	2	64	96	0.90	42
3	256	2000	256	0.50	p	l	2	128	96	0.93	33
4	256	2000	256	0.50	p	l	2	256	96	0.94	31

- large batch is better at the beginning (1 min), but worse at finishing (2 hours).
- larger batch is unstable, a new simulation is ongoing.

- by varying sample size, the evaluation error after converging seems no difference.